

Grain size dependence of hardness and fracture toughness in pure near fully-dense boron carbide ceramics

Bibi Malmal Moshtaghioun^{1,2*}, Diego Gomez-Garcia¹, Arturo Dominguez-Rodriguez¹,
Richard. I. Todd²

¹ Department of Condensed Matter Physics, University of Sevilla, 41012 Sevilla, Spain

² Department of Materials, University of Oxford, OX1 3PH, UK

*Corresponding author: mali_moshtagh@us.es, Department of Condensed-Matter Physics,

University of Seville, P. O. 1065, 41080 Seville, Spain. Phone: 0034954559504, Fax:

0034954612010

Abstract

Room temperature fracture toughness and hardness of spark plasma sintered pure B₄C ceramics with grain sizes ranging from 120 nm to 17 μm have been studied. Vickers indentation and single edge V-notched beam (SEVNB) techniques have been used to measure hardness and fracture toughness, respectively. A critical analysis of the results derived from these two techniques has been carried out and the conditions for proper comparison of the derived results are discussed. The results have shown that hardness follows the Hall-Petch dependence with either grain size or twin spacing when the effect of porosity is corrected for. On the contrary, fracture toughness is found to be essentially grain size independent. The value of this quantity is $\sim 2 \text{ MPa m}^{1/2}$.

Keywords: boron carbide; hardness; fracture toughness; SEVNB test

Introduction

The increasing demand for super-hard ceramic materials is a reality nowadays. This fact implies that a precise characterization of their mechanical properties becomes critical. To this purpose, an accurate analysis of hardness and toughness as well as the wear resistance and their grain size dependence is essential for advanced applications. Boron carbide is a keystone in the world of super-hard ceramics because of the combination of outstanding mechanical properties with other properties like low density, high melting point and high elastic modulus. Most scientists and technologists consider that this ceramic will be of especial interest for many strategic applications [1-4].

In spite of many attractive properties of these super-hard ceramics, their major drawback is their brittle nature, characterized by a low value of the fracture toughness. The determination of this quantity can be carried out through several techniques. One popular choice is the so-called indentation method because specimen preparation is simple, requiring only well-polished surfaces and small specimens and finally it is less time-consuming compared to conventional methods. But up to now a universally agreed standard for indentation fracture toughness determination does not exist and the whole technique can be criticised on various grounds [5]. For instance, there are several theoretical models in the literature relating the surface crack lengths measured after indentation to the indenter load and material parameters and it is not clear which is appropriate or correct. The most commonly observed crack systems produced by Vickers indentations are median-radial cracks or Palmqvist cracks, One of these is often assumed to be the relevant geometry, which may or may not be the case for the material in question [6-10].

The correlation between the indentation fracture toughness and its fracture toughness measured by single edge V-notched beam (SEVNB) test in super-hard ceramics has not been studied yet. In the case of pure boron carbide, a relatively wide range of fracture toughness values has been reported and measured by the indentation method [2,3,11-19]. The values of fracture toughness measured by Lee et al [11] were between 2.75-3.15 MPa.m^{1/2} while the density was between 90-93%. They measured fracture toughness by the Anstis equation, based upon median-radial cracks. Ghosh et al. [12] used the Evans and Charles fracture toughness equation, also assuming median-radial cracks which was concluded to be the crack geometry in their B₄C specimens. They reported values between 2.69-3.00 MPa.m^{1/2} for B₄C specimens with grain sizes of 1.6-2.7 µm and densities of 96-99.2%. Hayun et al [13] estimated the K_c values with two different equations when Palmqvist cracks were observed after subsequent polishing. The K_c values were between 3.9 and 4.9 MPa m^{1/2} for fully dense boron carbide specimens with grain size of 4 µm. Sairam et al [14] used the Anstis methodology for fracture toughness calculations. They demonstrated that near full density B₄C with grain size 2-6 µm exhibits a fracture toughness of 2.8 MPa.m^{1/2} and it increases with decreasing density up to a maximum of 5.8 MPa.m^{1/2} corresponding to 91% dense boron carbide. Moshtaghioun et al [15,16] showed the same tendency in fracture toughness values obtained by the Anstis equation. They reported apparent fracture toughness values as high as 4.81 MPa.m^{1/2} for sub-micrometric B₄C with a density of 90.3% while the fracture toughness decreases to values in-between 3-3.65 MPa.m^{1/2} for nearly fully-dense sub-micrometric B₄C specimens (with grain size of 300-800 nm) dropping to 1.88-2.10 MPa.m^{1/2} for fully dense B₄C specimens with grain size of 25-50 µm. Ji et al [17] demonstrated that B₄C ceramics with relatively high density (99.7%) and average grain size of 2.36 µm exhibit Vickers hardness of 37.8 GPa and fracture toughness of 4.7 MPa.m^{1/2} measured

based on radial-median cracks. As for nano-B₄C's, Reddy et al [18] measured toughness values between 3.6-4.7 MPa.m^{1/2} by means of the Laugier equation assuming the Palmqvist crack geometry in samples with a relative density of 92.8% and grain size in the interval 40-150 nm. The value of fracture toughness reported by Moshtaghioun et al [19] for nano-B₄C specimens with density of 94.6-97.5% and grain size of 100-180 nm obtained by the Anstis equation was in the range of 4.12-4.61 MPa.m^{1/2}. According to these studies, the presence of porosity in boron carbide ceramics seems to play an important role in determining the hardness and apparent fracture toughness [14-19], making it difficult to elucidate the grain size dependence of these quantities. It is also well-known that indentation induces amorphization of B₄C [12,15]. The size and shape of the amorphized zone as well as the amorphization intensity beneath a Vickers indentation have been evaluated by Subhash et al. [20] and the damage evolution implies the initiation and formation of radial cracking from the amorphized zone. The amorphization during indentation can affect hardness and apparent fracture toughness as well [20].

In this work, the effects of grain size and porosity (density) on the hardness and fracture toughness were investigated. To this end, a set of boron carbide specimens from micrometric to nanometric grain sizes were prepared and SEVNB fracture toughness tests were performed to measure fracture toughness values in order to evaluate the reported results of this quantity by indentation method while Vickers indentation was used for measuring the hardness.

Experimental procedure

Three available boron carbide powders with average particle size around 500 nm, 220 nm and 40 nm (Grade HD20, H. C. Starck, Germany and Tekna Plasma System Inc., Canada) were used

as the starting materials. The powder was consolidated under vacuum in a SPS device (Dr. Sinter 515S, Kanagawa, Japan), using a cylindrical graphite die with an inner diameter equal to 15 mm. A pressure of 75 MPa was applied upon heating and released at the end of the holding time. In all cases the heating rate was 100 °C/min. During the sintering process, the temperature was measured by an optical pyrometer, which was focused on a bare hole in the middle part of the graphite die. Table1 lists the specific SPS variables used and more details on processing and sample preparation are reported elsewhere [15,16,19].

The relative density of the sintered samples was measured by the Archimedes method, using distilled water as the immersion liquid. Microstructural analysis was performed on both fractured and polished surfaces by scanning electron microscopy (HITACHI S5200, University of Seville, Spain). The grain size was determined from the SEM pictures. The grain diameter was defined as that of the equivalent circle from image analysis. The polished surfaces were electro-chemically etched with a solution of 1% KOH.

Hardness (H) was measured by Vickers indentation on polished surfaces using a hardness tester (Struers A/S, DK-2750 Bullerup, Denmark) with indentation loads of respectively 4.91, 9.81 and 19.6 N and loading time 10 s.

Fracture toughness was measured by SEVNB method tested in four-point bending configuration.

For fracture toughness determinations by SEVNB fracture toughness tests, as-cut beams were ground to beams with dimensions of 13mm×2mm×2.5 mm. The ratio between the notch depths and specimen thickness were between 0.2 and 0.3. The notches were sharpened by means of razor blades with a purpose-built sawing mechanism using diamond paste grades down to 1 µm so that the tip radii of the notches were less than ~10µm. The fracture toughness was measured in a four-point bending configuration, using a crosshead loading rate of 5 N/min and inner and

outer spans of 5.8 and 10 mm, respectively. The tests were performed on a universal testing machine (Dension-Mayes, UK). For estimating the fracture toughness, the following relation was used [21]:

$$K_{C(s)} = \frac{P_f (L_o - L_i)}{BW^{3/2}} \frac{3\alpha^{1/2}}{2(1-\alpha)^{3/2}} f(\alpha) \quad (1)$$

$$f(\alpha) = 1.9887 - 1.326\alpha - \frac{\alpha(1-\alpha)(3.49 - 0.68\alpha + 1.35\alpha^2)}{(1+\alpha)^2} \quad (2)$$

where P_f , L_o , L_i , B and W are the experimentally measured fracture load, outer span, inner span, specimen width, and specimen depth, respectively. The pre-crack size (notch depth), a , enters the equation through α , where $\alpha = a/W$. The reported values are the average of at least five independent measurements.

Results and discussion

Table 1 lists the processing conditions, densities and average grain sizes of the different B_4C ceramics studied in this work with the standard deviation, and Fig. 1 shows SEM micrographs of all of them. It can be seen in Fig. 1a that sample 1 which is SPS-ed at 1800 °C has a coarse microstructure with average grain size of 17.2 μm . The presence of microtwins observed by SEM is a well-known feature in boron carbide ceramics [15,16,19]. In contrast, lower SPS temperatures are increasingly effective in retaining fine-grained microstructures (Fig. 1b-d). Sub-micrometric boron carbide specimens with average grain size of 688 nm and 370 nm were obtained at 1700 °C from two different B_4C powders. Moreover for all these three specimens, the relative densities were > 98% and there were only a few isolated pores in the microstructures (Fig. 1a-c). In the case of nano- B_4C , a lower sintering temperature of 1600 °C was required to

retain the nanostructured character. In addition, two-step SPS was performed to eliminate boron impurities and improve the sinterability [19]. In this condition, nano- B_4C specimens with an average grain size of 120 nm were obtained. Interconnected pores were present in microstructure (Fig. 1d) and the relative density was only 95%.

The experimental results of hardness for each indentation load of 4.91, 9.81 and 19.6 N which are named as HV0.5, HV1 and HV2 are shown in Table 1, as well as the values of fracture toughness determined through SEVNB tests. Figure 2 displays the experimental hardness versus the applied indentation load. The results show a mild “indentation size effect” in which the apparent hardness increases with decreasing load [22, 23]. However, the difference between the highest and lowest values for each material is only $\sim 10\%$.

The hardness also varies with grain size as seen in Fig. 3, which shows the results of experimental hardness (black circle points) versus the inverse square root of the grain diameter determined by indentation test at the highest load value (19.6 N: HV2). The experimental hardness increases when grain size reduces from micrometric to sub-micrometric in the near-full density specimens 1 and 2. This is the expected Hall-Petch (H-P) behaviour: $H = H_0 + kD^{-1/2}$ [24]. The finest grained specimens (370 nm and 120 nm) then show an apparent softening behaviour. Reduction in hardness with grain size in nanomaterials is sometimes attributed to an inherent “inverse Hall-Petch” behaviour, particularly in nanograined metals [25,26]. This is usually for grain sizes of less than 50 nm [25,26], however, and some ceramics have been found to exhibit no such departure from the usual Hall-Petch behaviour down to grain sizes as fine as 28 nm [27]

whereas even the finest grain size here was 120 nm. The most obvious explanation for the present observations is therefore the lower density of the finest grained materials.

In order to clarify the hardness behaviour with grain size, correction for porosity has been carried out, based on minimum solid area models [28,29] in which the hardness $H \sim \exp(-bP)$, where P is the volume fraction of porosity and b is an empirical constant [28-30]. For carbides, values for b of ~5-8 are common [28] and these correspond to various packing geometries of solid spheres in minimum solid area models [28]. In our case, $b=7$ gives the best fitting to a Hall-Petch dependence as displayed in Fig. 3 (blue diamond points) (values of $b \sim 6$ or $b \sim 8$ are also reasonable). The **true** hardness according to this model is listed in Table 2. Assuming the validity of this correction, hardness in boron carbide follows the classical Hall-Petch behaviour. In this fitting regression factors is $r = 0.98$, $H_{0D} (D \rightarrow \infty)$ is equal to 30.23 GPa and k is 105 GPa $\mu\text{m}^{1/2}$.

It is quite interesting that the same hardness tendency is extracted if the twin spacing is considered rather than the grain size. As shown in Fig. 4, the strong activation of twins is a well-known feature in boron carbide because of its low stacking fault energy [31-34]. The average twin spacings for all boron carbide specimens measured by TEM images are listed in Table 2. Fig. 5 shows The **true** hardness **of HV2** versus the reciprocal square root of the twin spacing. This dependency is consistent with the role of twins as a strong obstacle for dislocation motion [35] and it has been invoked to account for the high-temperature B_4C creep response [34,36]. The twins act as strong barriers for dislocation glide thus reducing the effective grain size of the specimens. In fact, Gutierrez-Urrutia et al. [35], claim that the Hall-Petch relationship should be substituted by the so-called dynamical Hall-Petch, which is merely the same mathematical

equation in which the grain size has been replaced by the twin spacing. The fitting in Fig. 5 with dynamical H-P has regression factors of $r = 0.90$ while $H_{0t} (t \rightarrow \infty)$ is equal to 30.38 GPa and k_t is $24 \text{ GPa } \mu\text{m}^{1/2}$.

As for the fracture toughness, a quite different behaviour was observed. The results (Table 1) show an apparent increase of toughness when the grain size goes down to the nanometric range. In order to study possible evidence of toughening with the grain size, SEM micrographs of the fracture surfaces of the SEVNB tests were examined as shown in Fig. 6. For B_4C ceramics with grain sizes of $17.2 \mu\text{m}$, 688 nm and 340 nm , the fracture surfaces look very flat demonstrating an essentially transgranular fracture mode with occasional intergranular cracks (Fig. 6a-c). There is also some evidence of side cracks which are indicated by red arrows in Fig. 6a-c, also observed in Fig. 1(a) (see arrow). A similar picture is seen for the nano- B_4C specimens with a grain size of 120 nm except that the interconnected pores shown in Fig. 1(d) can be observed (Fig. 6d, blue arrows). There is no evidence of significant toughening mechanisms such as crack deflection, bridging etc. with this finest grain size suggesting that the higher raw toughness value in Table 1 may be an artifact of the testing method.

Artificially high toughness values can arise with notched beam testing when the defects from which crack growth initiates at the notch root are comparable in dimension or smaller than the notch root radius [37,38]. This is the case for the finest grained specimens investigated here. The largest flaws corresponding to the interconnected pores in specimen 4 (Fig. 6d), for example, are about $2 \mu\text{m}$ in length, which is significantly smaller than the notch root radius of $10 \mu\text{m}$. Damani et al. [37,38] have shown that the effect of the blunt notch in these cases can be corrected for by

considering the initiating defect as a short surface crack loaded by the stress field of the relatively blunt notch. This leads to the following expression for the true fracture toughness K_c [37, 38]:

$$K_c = K_{exp} \tanh\left(2Y \sqrt{\frac{\delta a}{\rho}}\right) \quad (3)$$

where K_{exp} is the apparent experimental toughness obtained using eqs (1) and (2), Y is a geometric constant with value between $2/\pi$ and 1.12, ρ is the tip radius of the notch and δa is the initiating defect size. The lower value of Y corresponds to a semicircular initiating flaw at the notch root, whilst 1.12 corresponds to a straight crack along the length of the root. For closely spaced flaws, the correct value is probably between these extremes which can therefore be regarded as upper and lower bounds on the corrected toughness. The size of the biggest flaws were estimated from micrographs and used to calculate upper and lower bounds for K_c using eq. (3) as shown in Table 2. The correction is very small for the largest grained material (1) which had correspondingly large defects, greater in dimension than the notch root, and confirms that $K_c \approx 2.0 \text{ MPa m}^{1/2}$ for this ceramic. The upper bound values for the other specimens show that any grain size dependence is much smaller than indicated by the raw results, with the corrected toughness increasing by only about 35% from 2.0 to 2.7 $\text{MPa m}^{1/2}$ while the grain size reduces by more than 2 orders of magnitude from 17 μm to 0.12 μm . The near constancy of the lower bound values coupled with the transgranular fracture mode and lack of evidence for toughening mechanisms noted above suggests that the toughness of all specimens is in fact close to 2 $\text{MPa m}^{1/2}$, independent of grain size.

This toughness level is lower than many reported values in the literature, particularly those from indentation methods, as described in the Introduction [11-19]. This confirms that the indentation

method is not a good way of measuring toughness in boron carbide. The correlation between fracture surface analysis and toughness values shown here suggests that SEVNB is a suitable measurement method providing suitable correction for notch tip radius is made in fine grained specimens.

Conclusions

Hardness and fracture toughness have been measured by means of Vickers indentation and single edge V-notched beam (SEVNB) plus four points bending test techniques, respectively, in a set of specimens with grain sizes covering two orders of magnitude. The effect of grain size on hardness is analyzed after correction for the residual porosity. Theoretical hardness adjusted based on minimum solid area models to eliminate the effect of porosity is found to follow a classical Hall-Petch law with increment of 31 to 40 GP versus either grain size (17-0.12 μm) or twin spacing (290-6 nm). On the contrary, fracture toughness seems to be grain size independent with a value of $\approx 2 \text{ MPa m}^{1/2}$ when the grain size reduces from 17 μm to 120 nm. This fact is consistent with the transgranular nature of crack growth.

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Figure captions

Fig. 1. Representative SEM micrographs of the polished surface of the B₄C ceramics prepared by SPS at 75 MPa with heating ramp of 100 °C/min with: (a) B₄C powders with average particle size of 220nm and SPS-ed at 1800 °C for 3 min, (b) B₄C powders with average particle size of 500 nm and SPS-ed at 1700 °C for 3 min, (c) B₄C powders with average particle size of 220nm and SPS-ed at 1700 °C for 3 min and (d) nano- B₄C powders with average particle size of 40 nm and SPS-ed at 1200 °C for 10 min plus 1600 °C for 1 min.

Fig. 2. **Experimental hardness** as a function of the applied indentation load for B₄C ceramics with different grain size: ■ symbol denotes n-B₄C with grain size of 120 nm, ▲ symbol denotes sub-B₄C with grain size of 370 nm, ▼ symbol denotes sub-B₄C with grain size of 688 nm and ● symbol denotes B₄C with grain size of 17.2 μm. The error bars represent the standard deviation from all the ten indentations measurement.

Fig. 3 **Experimental hardness** measured by the indentation load of **HV2** as a function of inverse square root of the grain diameter (● points). **True** hardness versus inverse square root of the grain diameter (◆ points) as commented in the main text.

Fig. 4. TEM micrographs: (a) B₄C with grain size of 17.2 μm, (b) sub-B₄C with grain size of 688 nm and (c) n-B₄C with grain size of 120 nm. Twins are important feature in all TEM micrographs.

Fig. 5. **True** hardness measured by the indentation load of **HV2** as a function of inverse square root of the twin spacing (◆ points) as commented in the main text.

Fig. 6. SEM micrographs of the fracture surfaces of the broken B₄C ceramics after SEVNB plus four-point bending test: (a) micro-B₄C with grain size of 17.2 μm, (b) sub-B₄C with grain size of 688 nm, (c) sub-B₄C with grain size of 370 nm and (d) nano-B₄C with grain size of 120 nm.

Table caption

Table 1. Processing conditions, microstructural features, and room-temperature mechanical properties.

Table 2. True hardness values removing the influence of porosity and adjusted fracture toughness values considering defect size.