

The long and winding road to understanding organismal construction: Reply to comments on “From genotypes to organisms: State-of-the-art and perspectives of a cornerstone in evolutionary dynamics”

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1 The series of comments [1–4] on our review on the map between genotypes,
2 phenotypes, and eventually organisms [5] are gratifying in that they are exactly
3 the discussion we hoped our review would engender. As a snapshot of the state
4 of the field at a moment in time, it is missing the new contributions that have
5 already come after it —only partly amended through this reply—, but we hope
6 it may provide a citation portal to find such developments forward in time.

7 Understanding how a viable organism unfolds from the engagement of ge-
8 nomic sequence information in a suitable, but often variable, environment is a
9 daunting challenge, and one that we will not see solved in the near future. The
10 different aspects that need to be considered in the process are too many to be
11 enumerated; even if an exhaustive list could be provided, the quantitative effect
12 of each variable in the construction of the functional organism —an effect that is
13 expected to vary with the specifics of each unfolding—, would remain largely un-
14 known. In our review [5] we highlighted some aspects of the problem, focusing on
15 commonalities that emerge from studies of (mainly) genotype-phenotype (GP)
16 maps and pointing out unavoidable limitations of broader analyses, such as the
17 impossibility to explore the whole of genotype spaces, the inherent stochastic-
18 ity of the evolutionary process (which calls for statistical-mechanical approaches
19 and limits its long-term predictability), or important epistemological difficulties
20 to characterize a complete genotype-to-organism map.

21 In four comments to our review [1–4], further aspects of the problem are
22 pointed out, and the discussion is enriched by different viewpoints and the addi-
23 tion of related open questions. Certainly, GP models have been instrumental to
24 clarify important evolutionary features, such as the compatibility between high
25 robustness and evolvability [2]. The existence of universal or quasi-universal prop-
26 erties of GP maps, regardless of the model under study, suggests that only major
27 features are essential in biologically acceptable GP maps [6]: these might be
28 summarized in the ability to navigate genotype spaces without losing functional-
29 ity, which is a condition for innovation to be possible. All GP maps of interest
30 fulfill this constraint, even if they differ in the details [3] and even when some of
31 them yield a minute fraction of genotypes mapping onto functional phenotypes
32 [4].

33 Nitash and Adami [4] call attention to the relevance of measuring the informa-
34 tion content of sequences to complement analyses of genotype spaces structure.
35 This is closely related to the concept of sequence entropy —the logarithm of the
36 number of sequences yielding a phenotype—, which we describe in detail using

37 a statistical mechanical framework of phenotypic evolution in the weak mutation
38 regime (section 5.5 in [5]). As an example, Nitash and Adami investigate the set
39 of the smallest self-replicators in the digital life system Avida [7] and show that an
40 information-theoretic analysis reveals details about the robustness of replicators
41 and its relationship with the sign of epistasis in their genotypes.

42 McCandlish [3] argues that the biophysical characteristics of specific systems
43 play a role in evolutionary dynamics. The formation of GU pairs in RNA permits
44 transitions between GC, GU and AU pairings, but changes from GC to CG, for
45 instance, require rare double mutations. Therefore, neutral sets for RNA sec-
46 ondary structure consist *a priori* of many disconnected components depending
47 on the choice for each base pair [3]. A question in this respect, however, is
48 whether such disconnected components are equally abundant and, more impor-
49 tantly, whether disconnection implies lack of evolvability. Firstly, the components
50 of the neutral network for a given RNA secondary structure differ in size when
51 folding energy is taken into account [8, 9]. Indirect studies suggest that the
52 largest among such components could become progressively dominant as the
53 length of RNA sequences increases (see [6] and references therein). Second,
54 fragmentation due to lack of percolation only holds for small components, a
55 relevant observation when it comes to ensuring navigability of genotype spaces.

56 Another property of the RNA sequence-to-secondary structure map is that
57 single mutations can cause large rearrangements, leading to punctuated pat-
58 terns of adaptation [10]. Still, phenotypic stasis followed by sudden changes
59 is not exclusive of adaptive changes in RNA secondary structure, since it has
60 been empirically observed, e.g., in antigenic changes in viral populations [11].
61 It can be argued that any GP map that breaks the genotype space in a set
62 of disjoint genotype networks for different phenotypes will by definition display
63 sudden phenotypic transitions [12]. Actually, the fixation of a fitter phenotype
64 in a population is in general an exponentially fast process compared with the
65 search for new phenotypes, and the comparison between these two broadly dif-
66 ferent time scales can be described as punctuated equilibrium-like: sudden major
67 changes interrupt prolonged stasis, over the relevant time scales, regardless of
68 the mutational mechanism considered and the definition of phenotype.

69 As argued by McCandlish [3], the biophysical characteristics of particular
70 evolutionary systems are important and do have an explanatory power. Also,
71 system-specific and universal properties of GP maps can simultaneously hold:
72 phenotypic bias is a universal property, but which phenotypes have high pheno-
73 typic frequencies is set by the biophysics of the system (e.g. number of stacks [13]
74 and base pairs [6] in RNA, contact traces [14] in proteins). System-specific fea-

75 tures also yield important clues to understand how a variety of GP maps achieve
76 robustness and evolvability. In two-letter alphabets, for example, neutral net-
77 works are small and disconnected [15], seriously compromising navigability. This
78 situation is analogous to the phenomenon of quenched disorder at large popu-
79 lation sizes occurring in the weak mutation regime [16]. This is also the case
80 of systems with highly compressed information, as the smallest self-replicators in
81 Avida [4]. However, navigability (and evolvability) can be restored if information
82 becomes redundant in the genotype, if additional levels are added on top of the
83 basic sequence-structure map [17], or if the population size is reduced allowing
84 genetic drift to traverse local fitness valleys [16].

85 While the vast majority of RNA sequences stably fold into a minimum-free-
86 energy secondary structure, functional phenotypes are extremely rare in other GP
87 maps, as toyLIFE [18], regulatory gene networks [19] or metabolic reaction net-
88 works [20]. These systems display sufficient redundancy, but navigability relies on
89 the existence of non-trivial correlations between genotypes: meaningful function
90 clusters in the space of possible genotypes, and can be maintained while alterna-
91 tive phenotypes are explored—often through a variety of mutational mechanisms.
92 When it comes to adaptation, nature uses multiple other tricks that are rarely
93 considered in GP map studies, such as molecular mimicry [21], protein moon-
94 lighting [22] or enzyme promiscuity [23]. Inclusion of these forms of phenotypic
95 redundancy and functional flexibility explicitly turn the GP map into a many-to-
96 many relationship, and may significantly modify its topology. Our knowledge on
97 the large-scale structure induced by generic GP maps is very limited, and future
98 progress critically depends on our ability to extract model-independent features
99 relevant in evolutionary and adaptive dynamics. In this respect, synthetic sys-
100 tems, such as Avida [7] or Dawkins' biomorphs [24], can provide important clues
101 on the nature of universal features in evolving systems, and serve as examples
102 of alternative solutions that differ in the details but coincide in essential mecha-
103 nisms.

104 GP maps are limited to specific aspects of the development process, un-
105 avoidably leaving a large gap between the molecular phenotypes in many models
106 and the properties of whole cells or organisms [25]. The next crucial level to
107 integrate in the overall description is the map from genotype to fitness (GF).
108 Though the GF map does not always require an explicit definition of phenotype,
109 the connection between phenotype and fitness, when possible, becomes essential
110 for predictions of evolution by natural selection, as de Visser points out [1]. The
111 connection between genotype and fitness has been explored in our review [5],
112 aware as we are of the non-trivial role played by phenotypic bias and GP maps in

113 evolutionary dynamics (e.g. in speciation [26]). Basic organismal body plans, for
114 instance, are conserved over many millions of years through stabilizing selection,
115 and yet the underlying gene regulation and genetic makeup between species can
116 dramatically diverge —this is known as developmental system drift. Similarly, as
117 also discussed in [5], basic protein folds are under strong stabilising selection and
118 highly conserved: simple models of GP maps suffice to explain the observation
119 of the marginal stability of proteins [25, 27].

120 This nonetheless, various other possibilities have to be considered to complete
121 the GF relationship, unavoidably complicating the description. Fitness is diffi-
122 cult to quantify due to its dependence on exogenous and endogenous variation.
123 Fitness can be only defined in a specific environment, since the adaptive value
124 of a phenotype (or a genotype) depends on the conditions under which it has to
125 function: experiments with viral populations nicely illustrate this dependence by
126 showing how the value of mutations depends on the infected host [28]. Actually,
127 a strict separation between phenotype and fitness is in general not possible. The
128 ability of a genotype to produce different phenotypes when exposed to different
129 environments (phenotypic plasticity) causes an intimate, environment-mediated
130 relationship between genotype, phenotype, and fitness: RNA sequences, for ex-
131 ample, yield a simple case because they fold into different secondary structures
132 depending on temperature [29], pH or the molecular context. The scenario be-
133 comes more complex when we consider that organisms themselves interact with
134 the environment in non-trivial ways. Organism-environment interactions alter the
135 fitness landscape through short-term (e.g. metabolic [30]) and long-term (as in
136 an extended phenotype [31] and niche construction) modifications of expressed
137 phenotypes that in turn affect both fitness and the environmental conditions
138 [25]. Such feedback loops between phenotype and environment might lead to
139 non-commutativity of mutations [32] (the fitness landscape in the neighborhood
140 of a given genotype depends on the evolutionary history [33]), turning evolution-
141 ary pathways highly dependent on contingent events.

142 Can the (quasi-)universal features of GP maps be extrapolated to GF maps?
143 This is a relevant question raised by de Visser [1], who suggests future research
144 avenues: the development of fitness models of phenotypes (possibly including
145 feedback loops from the metabolic activity of the organism, to begin with) and
146 the exploration of how GP maps change under environmental variation. Efforts
147 in these two directions exist but have not yet been conceptually integrated to
148 the degree that multiple GP models have. Some instances of feedback between
149 the molecular environment and the unfolded (functional) genotypes have been
150 addressed in our review [5] when we discuss GP maps as evolving objects. Such

151 an evolution is the result of self-organization in evolving populations, where rel-
152 evant biological functions themselves (equivalent to a GF map) emerge from
153 intra-specific interactions in an RNA molecular quasispecies [34, 35]. Few other
154 models have addressed the evolution of the GP map in a complex, cellular-like
155 environment under a fixed fitness function [36]. Adaptation in variable fitness
156 landscapes has been investigated through the introduction of seascares [37], for
157 example, though the inability of static fitness landscapes to capture environmen-
158 tal changes already worried Wright himself [38]. Despite its relevance, this latter
159 question has received limited attention so far.

160 Recent work [39] on genotype to phenotype to fitness maps has demonstrated
161 that the nonlinear relationships between these different levels can interact in sur-
162 prising ways, reducing, for example, the amount of reciprocal sign epistasis, that
163 normally frustrates adaptive dynamics. For transcription factor landscapes, these
164 interactions lead to an important enhancement of the likelihood that low- and
165 intermediate-affinity binding sites fix in a population, over and above the *arrival*
166 *of the frequent* effect [40] that enhances the likelihood that such phenotypes
167 appear as potential variation in the first place.

168 More generally, it has recently been argued [41] that explicitly including the
169 phenotype as an intermediate step between genotype and fitness, and therefore
170 implicitly including a number of key organizational properties of the mapping
171 from genotypes to phenotypes – such as large neutral networks, neutral correla-
172 tions (or high mutational robustness) that facilitate neutral exploration and high
173 dimensions—greatly increases the number of accessible paths with monotonically
174 increasing fitness or navigability, in associated fitness landscapes, even under a
175 worst-case scenario of random fitness assignment to the phenotypes.

176 Such enhanced navigability may help explain the remarkably tight correlation
177 between the frequency with which RNA secondary structures are found in nature,
178 and the frequency with which they arise as potential variation [42]. Of course
179 at the level of individual phenotypes, fitness matters greatly, but at the level of
180 distributions (such as the probability of obtaining a certain coarse-grained shape)
181 the fitness effects apparently wash out in this system.

182 A similar strong sculpting by the GP map has been observed for the dis-
183 tribution of protein cluster topologies from the Protein Data bank, providing a
184 non-adaptive explanation for the strong preference for symmetry observed in na-
185 ture [43]. Of course fitness effects play an important role in all these systems,
186 but nature can only fix those phenotypes that appear in the first place.

187 Arguments based on the coding theorem from algorithmic information the-
188 ory [44] suggest that, under some mild assumptions, GP maps should be gener-

189 ically biased with an exponential drop in the size of neutral sets with linear
190 increases in the descriptive (Kolmogorov) complexity of the phenotype [43].
191 One of the really interesting open questions is whether the strong bias towards
192 simple phenotypes leads to phenotypes that are also favored by natural selection.
193 One potential property to investigate is higher-than-average robustness exhib-
194 ited by these preferred phenotypes. This property will in turn, make it easier to
195 accumulate other functions, and so may facilitate the emergence of modularity,
196 making evolution more evolvable.

197 In a scenario that seems to become increasingly complex, it is important to
198 come back to the relevant question: Do we need to know all details of GF maps
199 to predict (even if in a probabilistic way) the evolutionary dynamics of popu-
200 lations? Manhart and Bonhoeffer [2] provide an important clue by noting that
201 recent investigation of some phenotype-fitness maps reveals a low dimensionality
202 (of order 10) of fitness-relevant phenotypes [45, 46], supporting the hypothesis
203 advanced in [47] that phenotypic variation falls within low-dimensional spaces.
204 This is an encouraging possibility, though the point is whether the properties of
205 phenotype to fitness maps can be generalized across environmental conditions,
206 erasing possible idiosyncratic dependencies of fitness on environments and, even-
207 tually, rendering fitness landscapes a useful tool to predict evolutionary dynamics
208 [2].

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