

Research



**Cite this article:** Johnson PJ, Noonan MJ, Kitchener AC, Harrington LA, Newman C, Macdonald DW. 2017 Rensching cats and dogs: feeding ecology and fecundity trends explain variation in the allometry of sexual size dimorphism. *R. Soc. open sci.* **4**: 170453. <http://dx.doi.org/10.1098/rsos.170453>

Received: 15 May 2017

Accepted: 1 June 2017

**Subject Category:**

Biology (whole organism)

**Subject Areas:**

ecology/evolution

**Keywords:**

dimorphism, Felidae, Canidae, allometry, resource dispersion, diet

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Electronic supplementary material is available online at <https://dx.doi.org/10.6084/m9.figshare.c.3804838>.

# Rensching cats and dogs: feeding ecology and fecundity trends explain variation in the allometry of sexual size dimorphism

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The tendency for sexual size dimorphism (SSD) to increase with body mass in taxa where males are larger, and to decrease when females are larger, is known as Rensch's rule. In mammals, where the trend occurs, it is believed to be the result of a competitive advantage for larger males, while female mass is constrained by the energetics of reproduction. Here, we examine the allometry of SSD within the Felidae and Canidae, demonstrating distinctly different patterns: in felids, there is positive allometric scaling, while there is no trend in canids. We hypothesize that feeding ecology, via its effect on female spacing patterns, is responsible for the difference; larger male mass may be advantageous only where females are dispersed such that males can defend access to them. This is supported by the observation that felids are predominately solitary, and all are obligate carnivores. Similarly, carnivorous canids are more sexually dimorphic than insectivores and omnivores, but carnivory does not contribute to a Rensch effect as dietary variation occurs across the mass spectrum. The observed inter-familial differences are also consistent with reduced constraints on female mass in the canids, where litter size increases with body mass, versus no observable allometry in the felids.

# 1. Background

Dimorphism in secondary sexual characteristics—those not directly involved with reproduction—has long attracted the attention of biologists (e.g. [1–3]). Darwin [4] was among the first to speculate on its causes, coining the term ‘sexual selection’ to describe the general tendency of males to compete for females, and its phenotypic consequences. He remarked that: ‘The law of battle for the possession of the female appears to prevail throughout the whole great class of mammals’. Intersexual difference in size (sexual size dimorphism, henceforth SSD) is a conspicuous and widespread form of dimorphism. Male-biased mass dimorphism is predominant in mammals, where sexual selection has come to be regarded as the most likely explanation for its origin [5].

Most mammals have a predominantly polygynous mating system, where sexual selection is thought to drive the observed association with SSD. In primates, monogamous species are consistently less dimorphic than polygynous species [6]. Similarly, in ruminants, species with harem-based mating systems are more dimorphic than those with territorial, polygynous and monogamous mating systems [7]. Soulsbury *et al.* [8] observed that SSD was higher in mammals with greater variation in the reproductive success of males, a measure of the degree of sexual selection. Lukas & Clutton-Brock [9] showed that mating system and SSD were linked, with male-biased SSD being more common in species where females are solitary and with their ranges overlapping compared with socially monogamous species. Reduced SSD in domestic sheep and goats compared with their wild ancestors has been attributed at least partly to the reduced importance of male combat [10].

The maintenance of male-biased SSD by sexual selection has been implicated in explaining an allometric pattern known as ‘Rensch’s rule’. This rule states that, within a lineage, SSD is positively correlated with mean body mass (hyperallometry) in taxa where males are larger, and negatively correlated (hypoallometry) where females are larger (Rensch 1950 cited by Abouheif & Fairbairn [11]). Rensch’s rule holds for a variety of taxa (e.g. [11–15]), but is by no means universal, and the conditions required for its expression in mammal lineages are not completely understood. For instance, while the Rensch effect holds for Mammalia as a whole, when individual groups are considered only primates [16], bovids (antelopes), cervids (deer) and macropodids (kangaroos) have shown significant Rensch allometry [15]. Conversely, for carnivorans as a whole, no Rensch effect has been observed [11,13], but this may have masked heterogeneity among families. Indeed, Webb & Freckleton [17] commented on the sensitivity of Rensch’s rule to the taxonomic level investigated. Explorations of individual carnivoran families, however, are few.

In this study, we explore patterns of SSD in canids and felids, two families of Carnivora with species spanning a wide mass spectrum and differing in their dietary and socio-ecological patterns, and therefore promising for further exploration of influences on SSD. Sexual selection, although important [5], does not provide a complete explanation for patterns of SSD—it is also necessary to explain what controls female mass [14]. Indeed, the presence of the Rensch effect among breeds of domestic dog, *Canis familiaris*, shows that sexual selection cannot be the sole cause. Domestic dogs have been artificially bred for smaller mass from a common ancestor close to the wolf (*Canis lupus*) that was markedly dimorphic. A Rensch effect has been hypothesized to arise because female mass is constrained by a minimum neonate mass, so that males get smaller faster than females under selection for small mass, such that the smaller breeds are least dimorphic [18]. Where larger male mass is selected in natural populations, correlated selection for larger females will also occur due to genetic linkage [3,12,19]. But if fecundity decreases with increasing mass among female mammal species [14], a counter pressure for small female mass may reinforce a positive Rensch effect within taxa. While litter size does tend to decline with body mass in mammals as a whole [20], variation among mammalian taxa may account for some absences of a Rensch effect. In this respect, there is also a reproductive advantage for greater female mass (e.g. [21,22]). In wild canids, for example, larger species have larger litter sizes [23]—which also leads to the expectation of no Rensch effect, as has been observed in domestic canids [18].

Resource ecology is also likely to be a complicating factor: Ralls [24] speculated that the quality and dispersion of food resources could oppose polygyny by influencing the dispersion of females and therefore how individuals organize their intra- and inter-sexual territories. Any configuration of resources preventing males from defending access to females might therefore be expected to militate against a tendency for sexual dimorphism, and hence the Rensch effect. The analysis of Lukas & Clutton-Brock [9] provided some support for this; transition from the mammalian ancestral (polygynous) state to social monogamy was associated with a lower population density of individuals (adjusting for body mass); they speculated this occurred with increased competition among females, and lower female population densities. In these circumstances, it might not be possible for a male to defend more than

one female, and the benefits of larger male mass would therefore tend to be lost [9]. Recent observations on mustelids and their close relatives, where a negative Rensch allometry was observed [25], support the idea that resource ecology is influential in determining whether or not a Rensch effect is observed. The explanation offered by those authors was that the smaller species tend to be wholly carnivorous, a diet hypothesized to result in a spatial configuration of females that enables males to defend access to them [26,27], which did not occur for diets with different dispersal characteristics (i.e. herbivory, insectivory and omnivory [25]).

Here, we use phylogenetically controlled analyses to explore patterns in diet, socio-ecology and fecundity relating to SSD in wild canids and felids. Felids are all obligate carnivores, and while it may be an over-simplification to allude to a 'typical felid social system' [28], most are solitary. Canids, by contrast, vary considerably in feeding ecology, but monogamy is dominant. Previous studies have found no evidence for a Rensch effect in canids [29] and an inconclusive pattern in felids [30]. The study of Bideau & Martinez [29] did not investigate the effect of diet. We explore how body mass and diet type are related to sexual dimorphism *per se* and to the Rensch effect in these families. We also explore how that part of fecundity indexed by litter size changes with body mass in these groups, as the overall positive Rensch effect in mammals has been said to be based in part on reproductive constraint on female mass.

## 2. Material and methods

The data on sexual dimorphism were obtained from the monographs on wild canids and felids by Macdonald & Loveridge [31] and Macdonald & Sillero-Zubiri [32], respectively, and augmented as detailed in the electronic supplementary material. Data concerning diet and social system were taken from the life-history dataset used by Noonan *et al.* [33]. Diet and social system were treated as categorical predictors in statistical models. Diet with levels: 'carnivorous', 'omnivorous' and 'insectivorous', and social class with levels: '1', 'Solitary'; '2', 'Pairs'; '3', 'Groups'; '4', 'Social'. Because, social classes '1' and '3' were scarce, these were aggregated with '2' and '4', respectively. Social class and diet data were used only for canids, the felids being dominated by solitary systems and carnivorous diets.

For consistency with previous studies, we quantified SSD as the ratio of mean male to mean female masses [11]. Following [12,13], we regressed  $\log_e$  male mass (the dependent variable in our models) against  $\log_e$  female mass. We tested our null hypothesis of no allometric trend using the slope of this regression; slopes of greater than 1.0 are consistent with conventional positive Rensch allometry, and where slope confidence intervals do not include zero, the  $H_0$  of no effect is rejected at the 0.05 level. We used a model 1 regression; model 1 and model 2 solutions converge as the correlation between male mass and female mass approaches 1.0 [17]. The correlation was 0.994 for felids and 0.996 for canids. For canids, we treated diet and social class as categorical predictors in our models, with SSD used as the response. We also tested if body mass was related to diet for canids, aggregating non-carnivores in the same class to avoid sparse classes, and with female mass as the response.

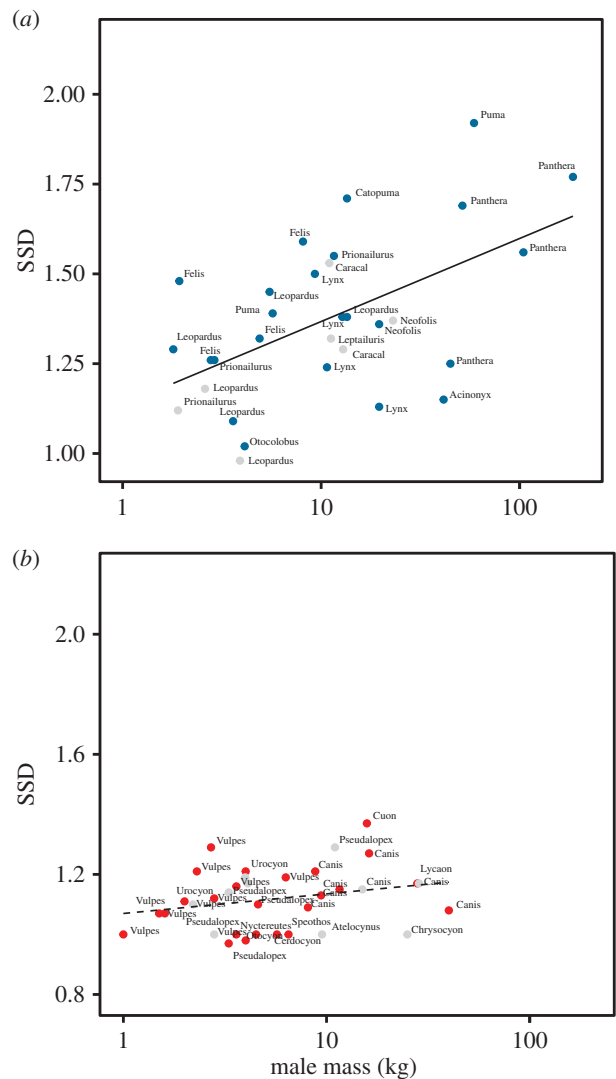
We used the R (CRAN) 'MCMCglmm' package [34] to control for phylogenetic dependencies. Phylogenetic relationships for the Felidae were taken from a recent consensus phylogeny of the Carnivora [35]. For the Canidae, however, we took relationships from Lindblad-Toh *et al.* [36] because its tree was better resolved and included more species. The programme derives parameter estimates using a Bayesian framework; uninformative, inverse gamma priors were applied, as in [33]. The number of model iterations, thinning interval and burn-in period were determined using diagnostic tests in the R package 'coda' [37], and convergence was confirmed using the Geweke diagnostic [38].

## 3. Results

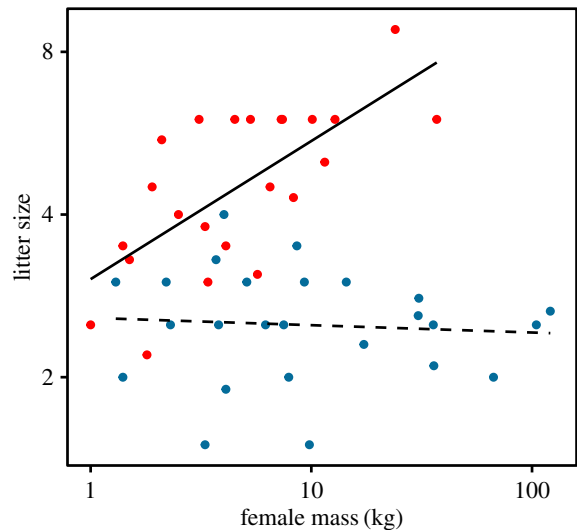
In felids, the MCMCglmm slope of male mass versus female mass (log scale) was 1.07 (CI 1.01–1.12), indicating a slope significantly greater than 1.0 and a conventional positive Rensch trend (figure 1a). In canids, the slope was close to 1.0, and there was no evidence for a Rensch effect (figure 1b, 0.99, CI 0.95–1.06).

Litter size scaled positively with body mass in canids (figure 2, slope = 0.29, CI 0.13–0.45, pMCMC = 0.002). The slope was lower for carnivorous canids alone (0.10, CI –0.06 to 0.30). There was no trend for felids (figure 2, slope = 0.02, CI –0.09 to 0.13, pMCMC = 0.68).

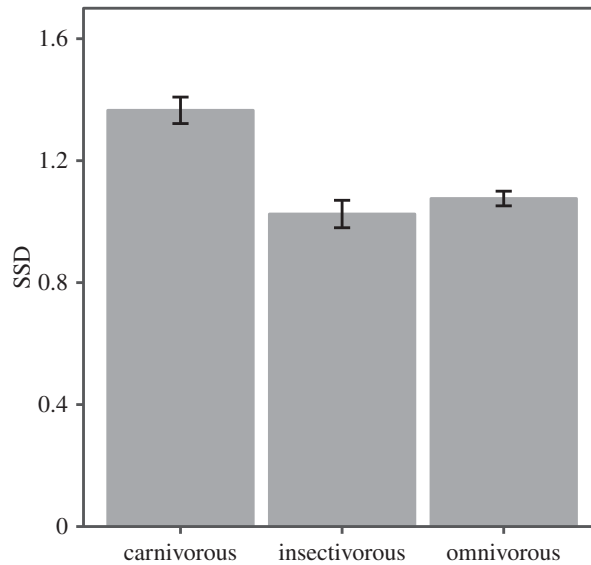
Carnivorous canid species were more sexually dimorphic than other dietary categories combined (figure 3, difference = 0.07, CI –0.009 to 0.14, pMCMC = 0.07) and were also larger (difference = 6.47, CI 0.5 – 12.5, pMCMC = 0.03). There was no evidence for a Rensch effect in this subgroup (slope = 0.95, CI



**Figure 1.** Sexual dimorphism and female mass in (a) felids and (b) canids. (Species plotted as grey points do not appear in the phylogeny.)



**Figure 2.** Litter size and female mass in felids (blue points) and canids.



**Figure 3.** Sexual dimorphism and dietary class in canids (means with CI).

0.87–1.04,  $N = 10$  species), or any evidence that canid social system was related to sexual dimorphism (difference =  $-0.03$ , CI  $-0.16$  to  $0.08$ ,  $p\text{MCMC} = 0.60$ ).

## 4. Discussion

Here, we demonstrate a positive Rensch effect among wild felids, which has not previously been shown, and confirm the absence of the effect in canids. We also demonstrate a link between SSD and diet—the most carnivorous canids were more dimorphic, and were also larger. The effect of size and diet on SSD is therefore difficult to disentangle. We note that a previous study [30], reporting no Rensch effect in felids after phylogenetic correction, used different biomass values and also included a number of subspecies, which may have influenced the authors' conclusions. Increasing litter size with body mass in canids, bearing in mind that this is not a complete measure of fecundity [20], suggests no constraint attributable to this part of fecundity for this group; indeed, it suggests the opposite effect, that larger mass is favoured. Carnivorous canid species also followed this overall pattern, which clearly militates against the expression of a Rensch effect in this group.

While felids and canids are not very closely related, and we cannot exclude the possibility that confounding variables are correlated with the observed effects, these observations support the idea that the presence of a Rensch effect in carnivorans may arise at least in part as a result of diet affecting sexual selection. We observe here that the trend in musteloids for SSD to be associated with carnivory [25] is mirrored among canids: the most sexually dimorphic canids are also the most carnivorous (figure 3). This does not scale with body mass (figure 1) because the species with SSD below 1.1 span the range of body masses in the group. These are almost all omnivores and insectivores; only one (with  $\text{SSD} < 1.1$ ), the bush dog (*Speothos venaticus*), is principally carnivorous. The difference between felids and canids may also result from the tendency for canids to exploit large prey by forming groups rather than by evolving larger individual body mass, which is the felid pattern; the scaling of body mass with prey mass is much looser in canids [28]. Group-hunting species at the upper end of the mass spectrum, conspicuously African wild dogs (*Lycan pictus*) and grey wolves (*C. lupus*), have relatively low SSD (figure 2). This tendency was also observed in musteloids, where, the social otters, for example, have low SSD [25].

For a link between diet and sexual dimorphism to be part of a general explanation for the expression of Rensch's rule in Carnivora, it would be necessary to explain how a carnivorous diet frequently allows males to compete for access to females, and therefore, for there to be an advantage of larger body mass. The evidence for this is as yet indirect and incomplete. For felids, accounts of the social systems of species are often fragmentary and awaiting elucidation by molecular work [28]. While patterns of overlap of both male and female home ranges vary, male ranges are generally substantially larger than those of females (table 5.2 in [28]). This is comparable to the mammalian ancestral system where females are sedentary and males are 'roaming' [9]. Under this system, we would expect male mass to be selected for. Lukas &

Clutton-Brock [9] provide some evidence that shifts from this system to social monogamy are associated with resource effects; the ancestral system may tend to give way to social monogamy and lower sexual dimorphism when the diet is of lower nutritional quality. Our observation that carnivorous canids are more dimorphic than omnivores and insectivores is consistent with this, though we did not find any evidence that social system was consistently related to sexual dimorphism. Resource effects may be more complicated; patchiness and predictability may form an important part of the explanation for patterns in sexual dimorphism but are not easily measured in nature.

## 5. Conclusion

While the Felidae follow a positive Rensch allometry, exhibiting greater SSD among larger species, the Canidae show no significant trend. We attribute these differences to variation in feeding ecology, where the dispersion of resources for omnivorous and insectivorous species precludes mating systems where defending access to multiple females is a viable male strategy [25,27]. This is supported by the observation that felids are predominately solitary, and all are obligate carnivores. Similarly, carnivorous canids are more sexually dimorphic than insectivores and omnivores, but carnivory does not contribute to a Rensch effect as dietary variation occurs across the mass spectrum. The observed inter-familial differences are also consistent with reduced constraints on female mass in the canids, where litter size increases with body mass, versus no observable allometry in the felids. We conclude that diet and resource dispersion can promote social and mating systems that undermine the advantage of large male size, by reducing the extent to which contest competition contributes to male reproductive success.

**Data accessibility.** The data used in these analyses are provided as the electronic supplementary material.

**Authors' contributions.** P.J.J. and M.J.N. contributed equally to this work and performed the analyses. All authors contributed to writing. P.J.J. conceived the study. A.C.K., C.N., L.A.H., M.J.N. and D.W.M. contributed to study concepts and interpretation. M.J.N. collected these data. L.A.H. and A.C.K. contributed to data collection.

**Competing interests.** We declare we have no competing interests.

**Funding.** M.J.N. was supported by the Rhodes Trust, an NSERC postgraduate scholarship and a Smithsonian Institution CGPS grant to J. M. Calabrese. We gratefully acknowledge the support of a grant from the PTES to D.W.M.

**Acknowledgements.** We acknowledge useful input from two anonymous reviewers.

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