

1 **Operationalizing the net negative carbon economy**

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12 **The remaining carbon budget for limiting global warming to 1.5°C will likely be exhausted**
13 **within this decade^{1,2}. Carbon debt³ generated thereafter will need to be compensated by**
14 **net negative emissions⁴. However, economic policy instruments to guarantee potentially**
15 **very costly net carbon-dioxide removal (CDR) have not yet been devised. Here, we**
16 **propose novel intertemporal instruments to provide the basis for widely applied carbon**
17 **taxes and emission trading systems to finance a net negative carbon economy⁵. We**
18 **investigate an idealized market approach to incentivize repayment of previously accrued**
19 **carbon debt by establishing emitters' responsibility for net carbon removal through**
20 **'Carbon Removal Obligations' (CROs). Inherent risks, such as the default risk of carbon**
21 **debtors, are addressed by pricing atmospheric CO₂ storage through interest on carbon**
22 **debt. In contrast to the prevailing literature on emission pathways, we find that interest**
23 **payments for CROs induce substantially more ambitious near-term decarbonization**
24 **complemented by earlier and less aggressive deployment of CDR. We conclude that CROs**
25 **will need to become an integral part of the global climate policy mix if we are to ensure**
26 **the viability of ambitious climate targets and an equitable distribution of mitigation**
27 **efforts across generations.**

28

29 **Introduction**

30 Delivering on the many national and corporate net-zero emission pledges will likely require
31 gross removal of atmospheric CO₂ on top of conventional emission reductions^{6,7}. To achieve
32 the Paris Agreement, global gross CO₂ removals will need to exceed gross residual
33 emissions^{4,8} beyond mid-century^{1,9}. The resultant net negative emissions compensate
34 carbon debt³ accrued by CO₂ emissions overshooting the remaining carbon budget^{10,11}.
35 Carbon debt is projected to amount to roughly the equivalent of nine years of global pre-
36 COVID emissions according to the IPCC's 1.5°C 'middle of the road' scenario P3/S2¹
37 (Extended Data Table 1). Such large-scale deployment of carbon-dioxide removal (CDR) is
38 controversial mainly for the implied economic and technological risks¹²⁻¹⁶ and
39 environmental impacts^{17,18}; and because reliance on CDR in mitigation scenarios often goes
40 hand-in-hand with a substantial shift of the mitigation burden to future generations¹⁹.
41 Here we would like to point to a fundamental economic problem associated with the
42 existing climate mitigation scenario assessments, aiming to inform international climate
43 negotiations. Existing economic policy instruments for emission control are inadequate to
44 incentivize a global transformation towards a net negative carbon economy without
45 imposing excessive fiscal burden from 2050 onwards: Currently envisaged carbon tax
46 schemes would turn into public subsidies under net negative emissions with potentially
47 prohibitive fiscal implications⁵. Emission trading schemes (ETS), on the other hand, are
48 presently designed to handle positive emission caps only. Negative emissions are merely
49 treated as offsets, implying that CO₂ emissions from one point in time cannot be
50 compensated by an equivalent quantity of negative emissions at another point in time, as
51 required by most mitigation scenarios. Crucially, we observe that pricing the depletion of
52 the remaining carbon budget is fundamentally different to pricing overshoot emissions after
53 the budget's depletion, which has profound implications for the consistent earmarking of
54 accrued revenues from a price on CO₂.

55 We argue that establishing emitters' responsibility for carbon debt is a prerequisite to
56 ensuring viable net negative carbon futures. Carbon debt could therefore be treated similar
57 to financial debt including interest payments on physical liabilities, or 'Carbon Removal
58 Obligations' (CROs), to internalize the inherent risks. Based on this idealized global carbon
59 policy proposal motivated by the IPCC's mitigation scenarios, our numerical results address

60 the shortcomings of the existing climate mitigation literature²⁰. Despite the conceptual
61 character of this study, we establish profound implications for national carbon policy, which
62 is strongly influenced by the IPCC's global mitigation pathways in many high-emitting
63 countries²¹.

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65 **Carbon pricing for net negative emissions**

66 Integrated Assessment Models (IAMs) provide global carbon price paths serving as a proxy
67 for a wider range of cost-effective climate policy options to achieve specified greenhouse
68 gas (GHG) mitigation goals (ref⁹). Such carbon prices typically increase exponentially with
69 the interest rate as a consequence of the Hotelling rule, which defines the intertemporally
70 optimal extraction schedule and price of a non-renewable resource^{22,23}, such as the carbon
71 budget. If understood as a global common, revenues generated from pricing its depletion
72 should consistently add to public budgets, for instance to compensate for the associated
73 welfare impacts which may be unfairly distributed across society. However, in scenarios
74 where the carbon budget is overshot and subsequently replenished, the budget can no
75 longer be regarded as a non-renewable resource. In this case, the Hotelling rule lends itself
76 to an 'intertemporal interpretation' for carbon policy: Revenues from carbon pricing after
77 the budget's depletion can be invested at the market interest rate to finance net carbon
78 removal later in the century. Because marginal abatement costs increase at the market
79 interest rate, this calculation is exact under perfect foresight conditions, as assumed in most
80 IAMs, if the retained funds purchase net negative emissions at marginal costs later on.
81 Because emitters pay for future net CDR through the carbon price, this intertemporal
82 interpretation is compatible with the Polluter Pays Principle. The resultant intertemporal
83 financial transfer thereby addresses concerns of intergenerational equity because public
84 budgets in the near-term no longer spuriously benefit from pricing an already-depleted
85 resource, whilst future generations thereafter are forced to replenish the carbon budget
86 through other sources, such as income, sales or payroll taxes. According to the 'conventional
87 interpretation', revenues from carbon pricing are merely treated as contemporaneous
88 additions to public budgets, with no clear earmarking of accrued funds. Crucially, since both
89 approaches are simply interpretations of the same underlying carbon price paths, emitters
90 also pay the discounted future costs of net emission removal in case of the conventional

91 interpretation. However, in the absence of consistent earmarking, the financial viability of
92 net CDR in the second half of the 21st century is highly doubtful (ref⁵), and intergenerational
93 equity remains unaccounted for.

94 To operationalize a future net negative carbon economy, carbon tax revenues could be
95 partially retained and transferred over generations to finance net CDR in the style of a
96 nuclear decommissioning trust fund or a sovereign wealth fund. The value of such a global
97 net carbon removal fund is potentially enormous, yet in the range of comparable funds,
98 peaking at roughly 100% of global GDP in the median of SSP scenarios compatible with
99 RCP1.9²⁴ (Figure 1). For comparison, Norway's large sovereign wealth fund has passed 250%
100 of national GDP²⁵. Given this order of magnitude, intermediate investment portfolios could
101 be a game changer to lift CDR out of the pilot phase even before payout of the fund.
102 However, protecting financial resources from diversion for other purposes as political
103 environments change, or as public finances get stressed, will surely be extremely
104 challenging. For instance, sovereign borrowing to cushion the impacts of the COVID-19
105 pandemic meant that by the end of 2020 OECD governments' debt-to-GDP ratio had
106 increased by about 13.4 percentage points²⁶. Severe crises in the future might induce
107 considerable pressure for governments to appropriate savings originally reserved for net
108 CDR.

109 The success of a net CDR fund also depends on the appropriate choice of several inherently
110 uncertain parameters, including future abatement costs. If costs and other socio-economic
111 parameters are not estimated in line with the precautionary principle, or if regulators are
112 reluctant to adequately reflect future carbon removal in near-term price instruments,
113 insufficient financial resources would be collected as observed for nuclear
114 decommissioning²⁷. Because carbon debt and associated risks would be mutualized by a net
115 CDR fund, missing financial resources would need to be replenished by public budgets.

116

117 **Dynamic emission trading**

118 Emission trading with fully liberalized banking and borrowing of allowances can be regarded
119 as a response to these concerns. Decentralized decision making and price determination in a
120 competitive market is believed to improve efficiency by leveraging the ability of carbon
121 markets to determine cost-effective time paths of mitigation²⁸. In an idealized global

122 scheme, the remaining carbon budget would be distributed over time resulting in positive
123 emission caps for consecutive auctioning periods. Emitters would decide in each period
124 what fraction of their CO₂ emissions to compensate by allowances and how much carbon
125 debt to generate for compensation by future allowances – or future CDR in the absence of a
126 positive emission cap. Effectively, emitters generating carbon debt would remain liable for
127 the timing and delivery of net negative emissions (Figure 2) and can therefore balance
128 present against future abatement based on individual expectations, such as those
129 concerning technological breakthrough. Stranded assets can be avoided by harmonizing
130 abatement investments with natural renewal cycles of capital; and fluctuations in the
131 business cycle can be addressed. Fixed price schedules under a carbon tax imply lower costs
132 for hedging risks related to the long-run costs of negative emissions and low-carbon
133 investments. However, increased intertemporal flexibility in emission trading stabilizes
134 prices – which reflect discounted future marginal abatement costs – compared to currently
135 implemented ETS with no intertemporal trade of allowances^{29,30}. At least in principle, this
136 ETS arrangement allows emitters to develop optimal investments over longer time horizons,
137 increasing the dynamic efficiency of emission trading. While emission caps can be overshoot,
138 the quantity of cumulative emissions remains exactly controlled under an ETS with
139 intertemporal trade of carbon debt, which is, more generally, the main advantage of cap-
140 and-trade schemes over carbon taxes. If caps no longer directly control emission reductions,
141 they can be set to equitably distribute ETS revenues over time. However, as the carbon
142 budget diminishes rapidly – the 1.5°C compatible budget is projected to become depleted
143 roughly within the next 10 years (ref¹) – the importance of carbon debt management
144 increasingly outweighs the requirement of an adequate temporal distribution of the
145 remaining carbon budget.

146 Privately managed carbon debt within an ETS also has considerable drawbacks: the
147 enforcement of carbon debt, assessment of creditworthiness of emitters, the potential for
148 speculation on future softening of emission targets and subsequent deferral of mitigation
149 (*time inconsistency*) – which is stronger the lower the solvency of emitters (*adverse*
150 *selection*) – and the resultant incentive to lobby for cancellation of carbon debt (*moral*
151 *hazard*) are crucial obstacles that explain why such intertemporal mechanisms are severely
152 restricted in currently implemented ETS (ref²⁸). Moreover, intertemporal trade of carbon

153 debt by means of forward and futures markets trading negative emissions over potentially
154 long periods at a fixed price is perceived as infeasible, given the deep uncertainty in the
155 parameters guiding a large-scale CDR rollout³¹.

156 **Carbon Removal Obligations**

157 Intertemporal emission trading would necessarily come at the cost of considerable
158 regulation to address these drawbacks. We argue, however, that practices from the financial
159 industry and monetary policy could be leveraged to reduce risks and adaptively balance
160 potentially competing interests of economic development and climate mitigation by treating
161 carbon debt in a similar fashion as a financial debt obligation, and thereby invoking an
162 interest on carbon debt. Economic growth, aggregate demand for carbon debt and
163 individual financial ratings of debtors would define a general base rate, individual markups,
164 term structures and debt maturities. To assure its physical conservation and exert control
165 over its aggregate level, carbon debt would initially be issued at the base rate by managing
166 authorities, e.g., Central Banks, towards which commercial banks would be held liable in
167 case of insolvent debtors. Commercial banks, or their equivalents, would issue debt to
168 emitters and, assisted by rating agencies, assess and hedge their insolvency risk by
169 determining individual markups on the base rate. Carbon debt would enter firms' balance
170 sheets as physical liability in tonnes CO₂ – a Carbon Removal Obligation, for which interest
171 payments would be due (Extended Data Figure 7a). This chain of legal liabilities across layers
172 of public and private actors reduces the moral hazard that governments would ultimately
173 pick up the bill for net emission removal, and limit issuance of CROs to debtors reluctant to
174 fulfill (interest) obligations. Individual interest markups would also balance the market's
175 push for adverse selection and incentivize a debt transfer from agents losing ground under
176 stringent climate policy to low-risk agents; or lead to more near-term abatement (see
177 Results) if risks are deemed non-insurable. The rate controls carbon price volatility
178 (Extended Data Figure 1) and therefore directly impacts on price-risk costs of scheduled
179 abatement investments. More generally, interest and debt maturities would need to reflect
180 the speculative nature of CDR, leading to short – but potentially renewable – repayment
181 terms and elevated rates in the near-term.

182 For intertemporal emission trading to work efficiently, for instance to reduce issues of time
183 inconsistency and price volatility, emission caps would need to be credibly announced as

184 early as possible. By consequence, regulators would lose the flexibility of adapting caps as
185 new knowledge concerning the Earth system becomes available. In an idealized global
186 scheme emission caps need to reflect exactly the remaining carbon budget. Budget
187 uncertainties related to issuing of carbon debt, like those of permafrost thaw following a
188 temperature overshoot², could be hedged by collecting risk funds through base rate
189 payments and by incentivizing more ambitious emission reductions to minimize the risk of
190 climate feedbacks (see Results). Such uncertainties should remain manageable by risk
191 reserves, allowing for the budget to be replenished by drawing on risk funds rather than
192 requiring a downwards correction of scheduled emissions caps. In the best case,
193 uncertainties and base rates would decrease over time as updated carbon budget estimates
194 converge to a value within the expected range of the previously announced budget.
195 However, new findings might realistically also lead to exceeding the capabilities of risk
196 management, requiring a combined effort of future generations to counter potentially
197 abrupt climate change. Management of physical risks therefore remains limited to what is
198 presently perceivable and realistically quantifiable.

199 *Box 1: Hypothetical implementation of a CRO-ETS in the European Union (EU) and beyond.*

The EU's total carbon debt amounts to 22.5 Gt CO₂ already by 2050, or roughly 7 years³² of present CO₂ emissions*, according to the 1.5°C-compatible mitigation scenarios LIFE and TECH from the European Commission (COM)³³. In line with the Union's net zero GHG target for 2050, CO₂ emissions must turn net negative already by 2043³⁴. Despite the lack of any adequate mechanism to do so, sectors currently covered by the EU-ETS will therefore need to deliver 50Mt CO₂eq net GHG removal by 2050 in the more ambitious 1.5-TECH scenario. CDR volumes are expected to grow after 2050 in line with the economy-wide net negative GHG emissions objective already enshrined in the EU Climate Law. Beyond 2050, negative caps in the EU-ETS³⁵ will require significant public funding, which is likely to obstruct the implementation of ambitious net-CO₂ removal targets. With CROs in place, overburdening of public budgets can be avoided.

We envision the following scenario: With the revision for Phase IV of the EU-ETS initiated in 2021, the linear reduction factor of emission caps is brought in line with the COM's long-term cumulative net-CO₂ 'target' of 26 Gt CO₂** while the scheme is gradually extended to full sectoral coverage. The implied increase of the reduction factor is balanced by a simultaneous phase-in of CROs, and carbon debt management is added to the European Central Bank's (ECB) portfolio. The ECB issues debt to commercial banks at a base rate, which in turn issue debt to firms participating in the EU-ETS charging individual markups depending on firms' financial ratings. To be able to repay the ECB despite defaulting debtors, banks would have to develop their own CDR portfolios. The resultant increase of CDR supply and expertise in assessing carbon debt risks induces development of a wider variety of CRO-products, with different maturities. For securing the long-term supply with fossil fuels in hard-to-transition sectors, like long-haul aviation and shipping^{36,37}, large energy firms would be incentivized to develop CDR for counterbalancing residual emissions³⁸. Alternatively, accrued carbon debt would be transferred to other agents, such as wealthy – potentially non-EU – tech firms, with presumably low credit risk and a proclivity for mitigation technology³⁹. For CDR suppliers^{40,41} CROs are the basis of a business case, and because negative emissions do not have to be delivered immediately, CROs simultaneously act like loans to finance development.

It may be that global implementation of a CRO-ETS under the UNFCCC, as conceptualized in this article, is not realistic for the time being. However, given the potential opportunities for the financial sector and CDR investors, as well as the implications for public finance, non-EU countries with ambitious climate

targets and (pilot-) ETS schemes, like China, Japan, South Korea, Quebec or California⁴², would likely be under pressure to liberalize intertemporal trade of carbon debt, and thereby establish responsibility for overshoot emissions. The EU-wide rollout would therefore be followed by attempts to actively influence regulation globally (e.g., via ‘regulatory export’⁴³) and subsequent linkage with other national and regional schemes⁴⁴.

**All numbers provided here include the United Kingdom (UK) and emissions from land use, land use change and forestry (LULUCF). Carbon debt for compensation in the 2050-2100 period is determined by subtracting the 2018-2100 budget from the higher 2018-2050 budget. Budgets are average values from the 1.5-TECH and LIFE scenarios. Annual emissions in 2018 amount to 3.14 Gt CO₂⁴⁵.*

***2018-2100 period; 1.5-TECH and LIFE scenarios combined, including net removals.*

200

201 **Climate mitigation under carbon debt**

202 In IAMs abatement costs are discounted at the market interest rate, implying a cost
203 advantage for abatement in the distant future vis-à-vis near-term decarbonization in net
204 present value terms. The interest rate is therefore a key driver of carbon debt accrual in
205 IAMs^{46,47}. This ‘discounting effect’ is balanced by imposing interest on carbon debt. Longer
206 CRO maturities imply lower net present costs for CDR. Simultaneously carbon debt interest
207 is paid over a longer period, compensating for these gains. When the market rate of interest
208 and the carbon debt interest rate (r_d) coincide, the gains from discounting are balanced
209 exactly, as we analytically show in the Methods. In Figure 3 we illustrate the sensitivity of
210 2°C-compatible global mitigation pathways to interest on carbon debt, with rates constant
211 over the 2020-2100 period ranging from $r_d = 0$ to $r_d = 0.08$. For each rate, 13 scenarios are
212 computed based on different SSPs and IAMs used to calibrate the marginal abatement cost
213 (MAC) curves of our model (Extended Data Table 2).

214 To illustrate by comparison, only the two extreme cases, $r_d = 0$ and $r_d = 0.08$, are depicted in
215 panels a-d of Figure 3. Crucially, when $r_d = 0.08$, the cumulative emission target is achieved
216 without accrual of carbon debt in the median path, implying that emissions remain at the
217 net zero level once achieved. This is accomplished by contemporaneous compensation of
218 residual CO₂ from fossil fuels and industry (‘FFI’) with negative emissions from bioenergy
219 with carbon capture and storage (‘BECCS’) and land use change. Complete decarbonization
220 of FFI emissions is, however, not cost-effective due to the high marginal costs of emission
221 reductions from hard-to-abate sectors. Remarkably, net negative emissions of individual
222 scenarios in panel a turn back to zero before 2100, thereby minimizing the “problem of
223 phasedown”⁴⁸. With reduced reliance on net negative emissions marginal costs are higher in

224 the near-term due to the more rapid reduction of FFI emissions and ramp-up of BECCS, but
225 significantly lower in 2100 (panel b). Panel e shows a reduction of total carbon debt D as r_d is
226 gradually increased. Carbon debt risks are therefore greatly reduced at a moderate cost
227 increase of below 12.5% in more than 75% of scenarios where $r_d > 0.02$.

228 A similar analysis is performed for the 1.5°C global warming target; however, direct air
229 capture and storage (DACS) is added to the mitigation technology mix, represented by 6
230 different DACS-specific MAC curves with low, medium and high costs as well as low and
231 high-capacity limits. This results in a set of 78 scenarios for each rate r_d . Not surprisingly, the
232 higher the potential for DACS to be deployed, the larger the level of D , when $r_d = 0$. By
233 contrast, when interest is invoked, this discounting effect is reversed and scenarios with
234 large-capacity low-cost DACS simultaneously exhibit the lowest levels of D , see Extended
235 Data Figure 2. The pathways in Figure 4 show baseline (panels a and b) and reduced D
236 (panels c and d) scenarios for those scenarios that achieve at least a 30% reduction of D
237 compared to their associated baselines. See Extended Data Figures 3-5 for 5%, 15% and
238 45%, respectively. For illustration, we interpret the CRO-ETS baseline scenarios, where $r_d =$
239 0, as conventional ETS scenarios because both schemes are theoretically equivalent in terms
240 of the resultant emission profiles while they imply a qualitatively different timing of financial
241 flows.

242 Despite the earlier ramp-up of DACS in panel c, causing emissions to turn net zero around
243 2050, an emission overshoot appears to be inevitable if warming is to be limited to 1.5°C.
244 Remaining net negative emissions might cause problems of phasedown in 2100, unless CRO
245 maturities are further extended to allow for a smooth transition towards net-zero; or more
246 net negative emissions are needed to stabilize the climate in the 22nd century⁴⁹. Hence,
247 median D equals to roughly 7 years of 2019 global net emissions in panel c. Yet, the role of
248 CDR changes considerably: without considering risks, CDR seems to justify late-century
249 compensation of carbon debt. In this case median D is equivalent to about 11 years of 2019
250 global net emissions, with compensation starting roughly 10 years later in panel a. However,
251 when risks are accounted for by imposing interest, CDR supports a rapid decrease of net
252 emissions by balancing residual emissions. Controversially, the availability of cheap and
253 large-scale CDR options, like DACS, is key in 1.5°C scenarios with reduced reliance on carbon
254 debt accrual. As illustrated by the pie-charts in panel d, the share of high capacity DACS

255 scenarios among feasible scenarios with respect to the 30% reduction requirement grows to
256 81% (50% in the underlying set) and the share of low cost DACS scenarios to 54% (33% in
257 the underlying set). Should CDR not become readily available as asserted in IAMs⁵⁰⁻⁵², this
258 would be reflected in an elevated carbon debt interest rate, incentivizing emission
259 reductions provided by other sources, such as replacement of fossil with renewable energy
260 sources in hard-to-abate sectors – even if this leads to much higher costs.

261

262 **Impact on financial flows in time**

263 Figure 4, moreover, illustrates the distribution of annual mitigation cost shares, including
264 investments in emission reductions and negative emissions (red and yellow shades) and the
265 financial flows associated with ETS allowances and interest for CROs (blue shades). The
266 share of abatement costs for emission reductions ('ABM') and negative emissions ('RES' and
267 'NNE') incurred in the near- versus the long-term increases with larger levels of r_d ; compare
268 Figure 4d to Extended Data Figures 3d-5d. Here, CROs with interest induce a more equitable
269 temporal distribution of these cost items, in sum peaking at 2.4% in panel d compared to
270 4.5% of GDP in panel b. This is partly because the CRO-ETS requires carbon debtors to
271 reserve financial resources early in the century, and such funds earn interest until they are
272 spent for net negative emissions ('NNE', yellow). By contrast, NNE expenditures in panel b
273 are incurred at the time of net carbon removal and would need to be funded by public
274 sources in the absence of intertemporal financial transfers. Note that here we show average
275 abatement costs. If marginal costs are paid by incentivizing net CDR on a market, public
276 expenditures are much higher; see for comparison Figure 1. Pricing overshoot emissions
277 under a conventional ETS, moreover, implies much larger revenues ('ETS', light blue) than
278 under the CRO-ETS, where emission caps reflect exactly the remaining carbon budget.
279 Median total discounted abatement costs, excluding ETS costs and interest costs ('INT'),
280 increase from 1.6% to 2.0% of GDP when interest is invoked within the CRO-ETS. Median
281 interest costs in these scenarios are substantial, peaking at above 1.3% of GDP, and 0.4% to
282 1.5% in the Extended Data Figures 3-5. These numbers are, however, highly uncertain and
283 will need to be determined considering the viability and scalability of near-term CDR options
284 and other emission reduction technologies.

285 Enlarging IAM CDR-portfolios to reduce technological risks and environmental impacts
286 would likely lead to further burdening of future generations in scenarios if CDR remains
287 primarily a motivation for reducing net present costs by accrual of carbon debt. This is
288 especially problematic if such results trickle down via the IPCC and international climate
289 negotiations into national target setting because no viable mechanisms for carbon debt
290 repayment have entered the policy debate at the moment. Simultaneously, mitigation
291 pathways with reduced carbon debt heavily rely on CDR, requiring that risks be
292 appropriately managed. Similar pathways result from lowering the market interest rate in
293 IAMs (ref⁴⁶) or from adequately setting intermediate climate targets or constraints on net
294 emissions (ref²⁰). However, such measures would individually not resolve the more
295 profound issue of finance of net negative emissions discussed here.

296 **Conclusion**

297 In view of the rapid depletion of the global carbon budget CROs appear indispensable for
298 any robust climate mitigation framework. While emitters under a combined tax-fund system
299 pay upfront for net carbon removal, debtors in a CRO-ETS individually manage their financial
300 resources. The implied flexibility for emitters also bears the largest drawback of
301 intertemporal emission trading, if public bailout of carbon debtors becomes necessary. To
302 minimize such risks ‘conservation of carbon debt’ needs to take top priority by controlling
303 the total amount of carbon debt and by establishing liability across several layers of actors.
304 Risk management under a CRO-ETS relies on imposing interest on carbon debt. For higher
305 and risk adjusted carbon debt interest rates, net negative emission investments no longer
306 benefit from net present cost gains when mitigation is deferred to the distant future. By
307 implication, CDR under a CRO-ETS will need to prove its viability vis-à-vis conventional
308 emission reduction options already in the near-term. This will promote bottom-up CDR
309 market development with the attendant benefits of price discovery, earlier technological
310 learning, testing of scalability and identification of socio-environmental co-benefits and
311 hazards, and ultimately, eliminating the uncertainties surrounding CDR.

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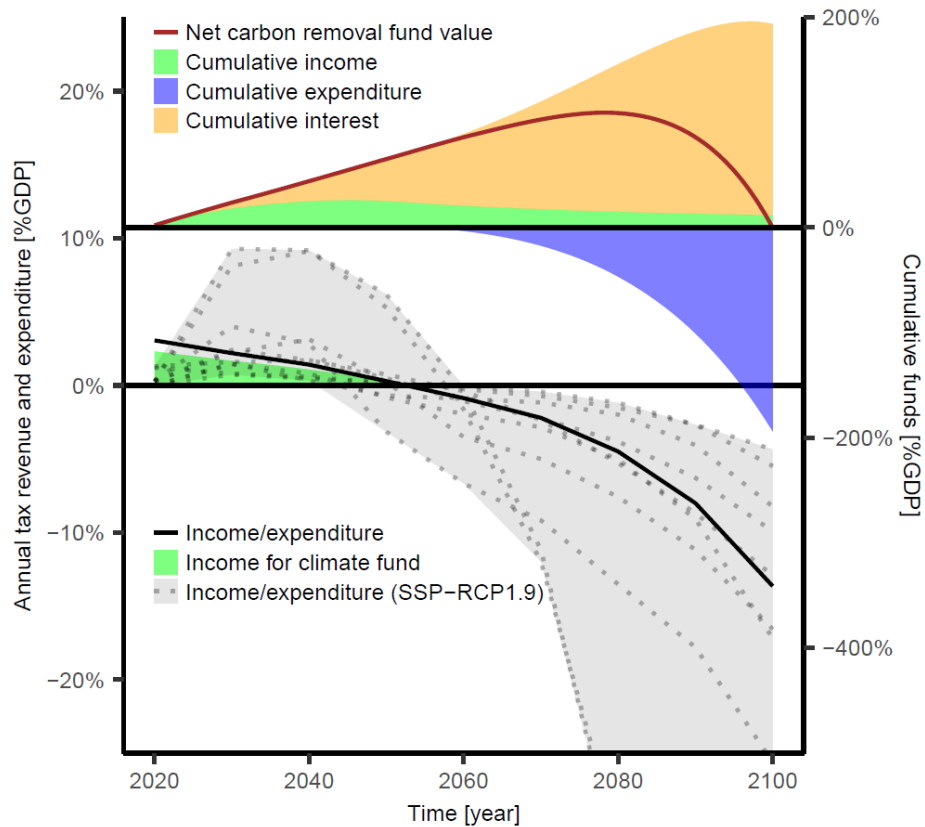
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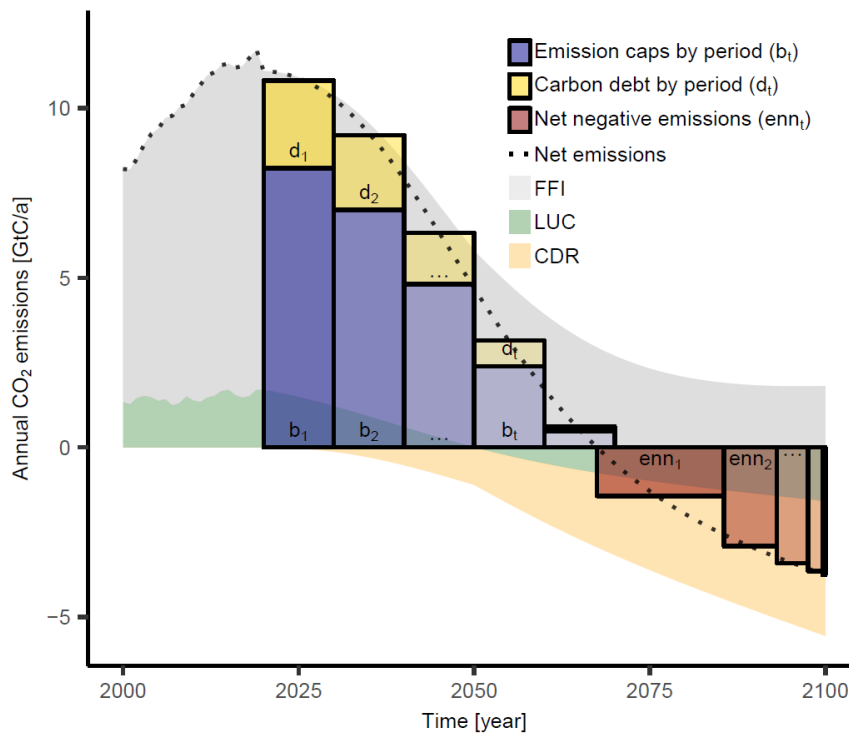
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416 **Figures**

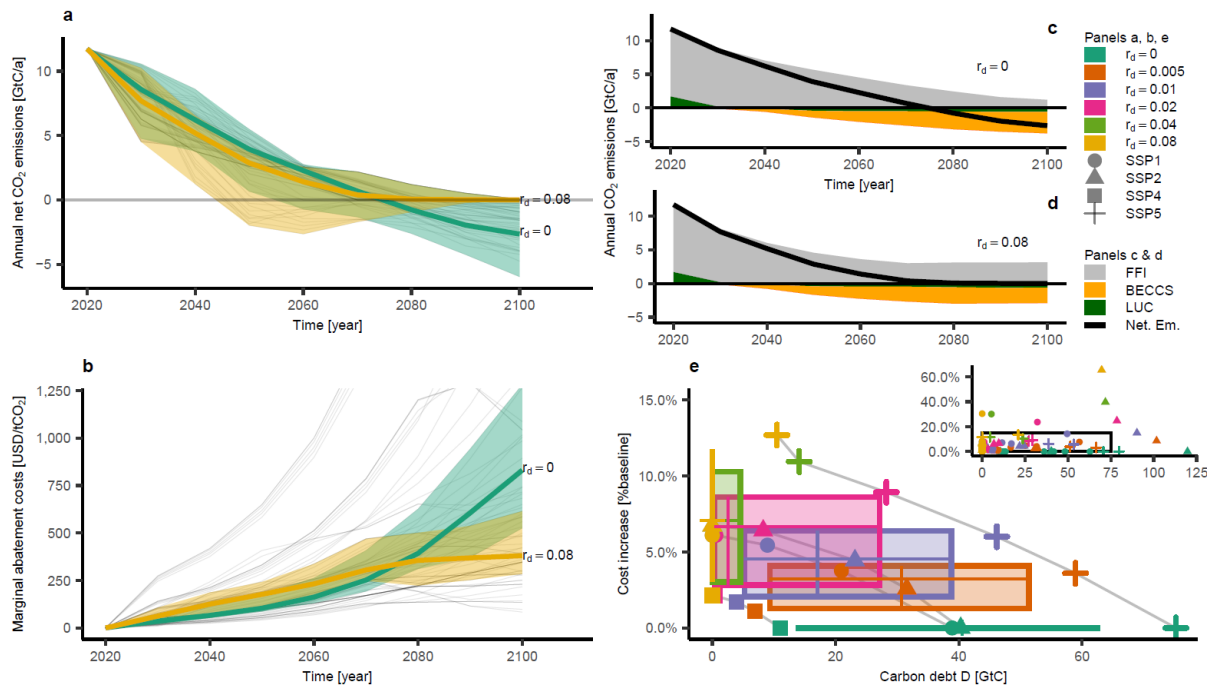


417 **Figure 1: Idealized global tax scheme with net carbon removal fund.** Lower figure (left hand side axis): Public income and
 418 expenditure from a tax on net emissions expressed as GDP percentage. Hotelling-compatible (exponential) carbon prices
 419 from SSP-RCP1.9 scenarios are multiplied by net emissions and divided by GDP (grey dashed lines). An idealized
 420 income/expenditure curve (black solid line) was derived from these scenarios using a strictly exponential median carbon
 421 price, median net emissions and GDP. Instead of reserving 100% of tax revenues after depletion of the carbon budget, we
 422 assert that a fraction $\phi = 0.76$ of revenues are earmarked for net carbon removal, however, already from 2020 onwards. This
 423 share of income (green area) would need to be accrued into a net carbon removal fund invested at the market rate of interest
 424 to account for later expenditure when net emissions turn negative. See Methods for a definition of ϕ . **Upper figure (right**
 425 **hand side axis):** Cumulative payments into the net carbon removal fund (green) and interest (orange) in theory pay exactly
 426 for cumulative tax expenditure (blue), such that the fund's net value (brown solid line) gets exhausted as the warming target
 427 is achieved in 2100.
 428



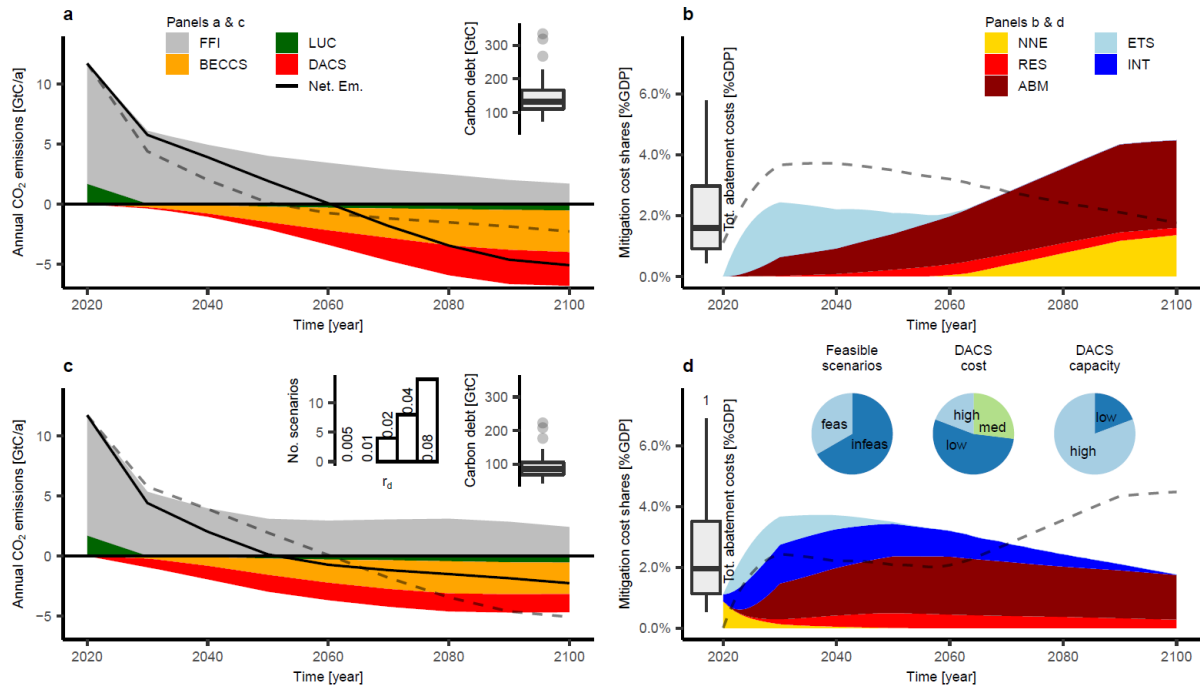
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Figure 2: Idealized emission trading system (ETS) with intertemporal trade of carbon debt. Illustrative 2°C pathway with gross carbon emissions from fossil fuels and industry (FFI), land use change (LUC), and non-specified sources of carbon-dioxide removal (CDR) including the schematic architecture of idealized global intertemporal emission trading. ETS emission caps b_t are obtained by distributing the carbon budget in tranches over consecutive periods. The amount by which emission caps b_t are exceeded by net emissions is conceptualized as ‘carbon debt’ (d_t). In this idealized illustration, d_t is compensated later by corresponding net negative emissions (enn_t) such that $d_t = -enn_t$. In a conventional ETS emission caps would be set to $b_t + d_t$, and enn_t would have to be incentivized by public subsidies. Historical emissions are from ref⁵³.



438
 439 **Figure 3: 2°C (RCP2.6) mitigation scenarios for a range of interest rates on carbon debt.** Panel a: Net CO₂ emissions of all
 440 scenarios with $r_d = 0$ (turquoise) and $r_d = 0.08$ (yellow), including geometric median paths (bold solid lines) and min to max
 441 ranges (shaded areas). Panel b: Marginal abatement costs of scenarios with $r_d = 0$ (turquoise) and $r_d = 0.08$ (yellow). Bold
 442 solid lines indicate geometric medians, shaded areas indicate 25-75% interquartile ranges. Panels c ($r_d = 0$) and d ($r_d = 0.08$):
 443 Geometric median net emissions as in panel a, including gross emissions from fossil fuels and industry (FFI), bioenergy with
 444 carbon capture and storage (BECCS) and land use change (LUC). Panel e: Total discounted abatement costs (net present
 445 value, including interest costs) expressed as percentage cost increase compared to the baseline ($r_d = 0$) are shown as function
 446 of total carbon debt D . The boxes indicate 25-75% interquartile ranges around median values of costs and D . Symbols linked
 447 by grey solid lines indicate medians grouped by SSPs. The entire dataset is shown in the upper-right corner, where each
 448 scenario is reflected by a symbol, grouped by SSPs (symbol type) and r_d (color).

449



450
 451 **Figure 4: 1.5°C (RCP1.9) pathways under a conventional ETS (panels a and b) compared to a CRO-ETS (panels c and d).**
 452 **Panels a and c:** Geometric median net emissions (solid line) and gross emissions from fossil fuels and industry (FFI), bioenergy
 453 with carbon capture and storage (BECCS), land use change (LUC) and direct air capture and storage (DACs). Net emissions
 454 from panel a are also displayed in panel c (dashed line) and vice-versa. Total carbon debt D is shown as box-and-whiskers
 455 plot. Boxes indicate the 25-75% interquartile range around median values (bold line), whiskers indicate min to max ranges,
 456 points mark the outliers. **Panels b and d:** Annual mitigation costs as GDP percentage, including the share of average
 457 abatement costs attributed to emission reductions (ABM), to compensation of residual emissions by CDR (RES) and to net
 458 negative emissions (NNE) as well as expenditures for allowances (ETS) and interest costs (INT). Total mitigation costs (i.e.,
 459 ABM+RES+NNE+ETS+INT) from panel d are also displayed in panel b (dashed line) and vice-versa. Box-and-whiskers plots
 460 show total discounted abatement costs (i.e., ABM+RES+NNE) as GDP percentage, the number above the chart indicates out-
 461 of-range outliers. Pie charts in panel d summarize properties of the underlying set of scenarios (see Methods). The
 462 distribution of r_d in CRO-ETS scenarios is depicted in panel c.

463

464

465 **Methods**

467 **Basic analytical setup**

468 Emission reductions induced by a CRO-ETS are quantified using a Hotelling-type
470 optimization problem (see ref⁴⁶ for an analytical solution of the model). A global social
471 planner is tasked to implement emission reductions at minimum costs to meet a cumulative
472 emission target, i.e., the remaining carbon budget B , by $T=2100$ ($t_0=2020$). Exogenously
473 given baseline emissions E_{base} i.e., future emission paths based on ‘business-as-usual’
474 climate policy assumptions, are reduced by a fraction a to obtain net emissions e :

$$475 \quad e(t) = E_{base}(t) * (1 - a(t)). \quad [1]$$

476 Total abatement costs c_{tot} are discounted at the market interest rate r to obtain the net
477 present value of total abatement costs, which is minimized:

$$478 \quad \min_{a(t), c_{tot}(t, a(t))} \int_{t_0}^T c_{tot}(t, a(t)) * \exp(-r * (t - t_0)) dt, \quad [2]$$

479 subject to:

$$\int_{t_0}^T e(t) dt = B. \quad [3]$$

480 Integrating over marginal abatement costs $MAC(a)$ gives the cost per ton CO₂ for an
481 instantaneous emission reduction of a compared to the baseline. Consequently, total
482 abatement costs c_{tot} are defined as:

$$c_{tot}(t, a(t)) = E_{base}(t) * \int_0^{a(t)} MAC(t, \tilde{a}) d\tilde{a}. \quad [4]$$

483 Assume that under an idealized CRO-ETS a constant fraction $1-\phi$ of net positive emissions
484 e_{NP} is equivalent to a (continuous) emission cap b , i.e., the amount of conventional emission
485 allowances issued over time, and $\phi < 1$ of e_{NP} equals carbon debt d , i.e., the quantity of
486 CROs issued. Then ϕ is defined as the ratio of cumulative net negative emissions e_{NN} to
487 cumulative net positive emissions e_{NP} :

488

$$\Phi = \frac{\int_{t_0}^T e_{NN}(t) dt}{\int_{t_0}^T e_{NP}(t) dt}, \quad [5]$$

489 and net negative emissions and net positive emissions equal the negative and positive parts
490 of net emissions ($e_{NP}, e_{NN} > 0$)

491

$$e_{NN}(t) = \begin{cases} -e(t), & e(t) < 0 \\ 0, & e(t) \geq 0 \end{cases}, \quad [6]$$

492

$$e_{NP}(t) = \begin{cases} e(t), & e(t) > 0 \\ 0, & e(t) \leq 0 \end{cases}. \quad [7]$$

493

494 Carbon debt d and the continuous emission cap b are defined as:

495

$$d(t) = \Phi * e_{NP}(t), \quad b(t) = (1 - \Phi) * e_{NP}(t), \quad [8]$$

496

497 and total carbon debt D is obtained by integration over the planning horizon T (see [5] and
498 [8]):

$$D = \int_{t_0}^T d(t) dt = \int_{t_0}^T e_{NN}(t) dt. \quad [9]$$

499 Consequently, we can write ϕ as:

$$\Phi = \frac{D}{B + D}. \quad [10]$$

500 By implication, a fraction ϕ of cumulative net positive emissions overshoots B and thereby
501 generates D , and a fraction $1 - \phi$ depletes the budget B .

502 Instead of exogenously imposing ETS emission caps, ϕ allows us to endogenously compute
503 caps b and carbon debt d to conceptualize the intertemporal allocation of carbon debt such
504 that debt is solely compensated by net negative emissions e_{NN} . Based on that we can
505 compute a 'physical repayment term' T_R linking the timing of net positive to net negative
506 emissions (see [12]). CROs in this idealized ETS therefore represent a long-term
507 intertemporal net transaction for financing net negative emissions. This aggregate can be
508 regarded as a proxy for a multitude of smaller carbon debt transfers over shorter
509 timeframes possible in real ETS implementations where CROs can be compensated by
510 (gross) carbon removal, issuance of new CROs or allowances at a later point in time.

511 Average abatement costs are obtained from total abatement costs by dividing by the abated
512 quantity of CO₂:

$$c_{avg}(t, a(t)) = \frac{c_{tot}(t, a(t))}{a(t) * E_{base}(t)}. \quad [11]$$

513
514 Next, we introduce interest payments which are due for carbon debt d over the repayment
515 term $t \rightarrow t+T_R(t)$, i.e., from issuance of the CRO until its retirement (see Extended Data
516 Figure 11b-e). T_R is implicitly defined as:

$$\int_{t_0}^t d(\tau) d\tau = \int_{t_0}^{t+T_R(t)} e_{NN}(\tau) d\tau, \quad [12]$$

518 and instantaneous interest payments are obtained by multiplication of the quantity of CO₂
519 for which CROs have been issued ($d = \phi * e_{NP}$) and the average abatement costs, c_{avg} , the
520 moment of retirement of the CRO, $t+T_R(t)$, with the interest rate on carbon debt r_d :

$$i_{inst}(t) = d(t) * c_{avg}(t + T_R(t), a(t + T_R(t))) * r_d. \quad [13]$$

522
523 Integrating and discounting instantaneous interest payments over the repayment term T_R
524 gives the total net present interest costs at t for carbon debt $d(t)$:

$$i_{tot}(t) = i_{inst}(t) * \int_t^{t+T_R(t)} \exp(-r * (\tau - t_0)) d\tau. \quad [14]$$

525 Now we add interest costs to the standard objective function [2] to obtain the optimization
526 problem for a CRO-ETS:

$$\min_{a(t), c_{tot}(t, a(t)), i_{tot}(t)} \int_{t_0}^T (c_{tot}(t, a(t)) * \exp(-r * (t - t_0)) + i_{tot}(t)) dt. \quad [15]$$

528
529 **Mitigation cost discounting**

530 If we set $r = r_d$, the objective function can be written as (see [S13](#)):

531

$$\min_{a(t), e_{NP}(t), d(t), c_{avg}(t, a(t))} \int_{t_0}^T \left(d(t) * c_{avg}(t + T_R(t), a(t + T_R(t))) \right. \\ \left. + (E_{base}(t) - e_{NP}(t)) * c_{avg}(t, a(t)) \right) * \exp(-r * (t - t_0)) dt. \quad [16]$$

532 Crucially, instead of pricing e_{NN} , carbon debt d is now paid for the moment it is created,
533 however, at the average (undiscounted) future costs during removal at $t+T_R$, which is due to
534 our definition of interest costs in [13]. This is because when $r = r_d$ interest payments exactly
535 compensate the cost reduction in net present value terms from discounting. The second
536 term, $E_{base}(t) - e_{NP}(t)$ equals emission reductions in the net positive / net zero domain. These
537 reductions can be achieved by a mix of CDR, low carbon- and zero carbon technologies,
538 however CDR is deployed only to offset contemporaneous emissions and not to recapture
539 CO₂ released earlier.

540 Intuitively, r_d therefore controls to what extent cost discounting becomes a driver for
541 accruing carbon debt. If r_d equals the market interest rate future costs c_{avg} at $t+T_R$, driven by
542 technological learning and the aggregate demand for abatement a in $t+T_R$ determine
543 whether the carbon debt route (d) proves competitive vis-à-vis instantaneous emission
544 reductions ($E_{base} - e_{NP}$). However, if d is reduced, e_{NP} needs to be reduced simultaneously to
545 meet the emission target (less carbon debt leads to higher demand for near-term emission
546 reductions, thus an increase of near-term marginal costs). Because near-term emission
547 reductions potentially include CDR, technological and socio-environmental learning
548 associated with CDR is induced earlier, leading to a reduction of uncertainty, which is key for
549 operating in the net negative domain later in the century. In this article we provide some
550 intuition about the dynamic effects of invoking an interest on carbon debt, but do not
551 determine optimal risk-reducing rates, which could – but do not necessarily need to –
552 coincide with market interest rates. We expect, however, under circumstances where
553 physical and financial risks associated with carbon debt are managed by appropriately
554 setting an interest rate on carbon debt, that r_d is driven by the market interest rate: In our
555 model, an increase in the market interest rate induces deferral of mitigation due to
556 discounting, leading to higher quantities of D , thereby also to an increase of risks, and finally
557 the necessity to correct r_d upwards to account for the increased risks.

558

559

560 **Assessing the value of carbon debt**

561 Note that net present cost gains from discounting are only cancelled exactly if the market
562 interest rate is invoked on abatement costs at $t+T_R$. Costs are known in our model, but
563 potentially impossible to determine in the context of real emission control policy. Therefore,
564 given their liability for issued debt, managing authorities and financial institutions need to
565 estimate the financial value of carbon debt as basis for interest payments and CRO
566 maturities. The incentive to correctly value debt has a societal benefit of gradually reducing
567 uncertainty with respect to CDR and other technologies relied on at large scales in
568 mitigation scenarios. Importantly, by prudently valuing debt, issuing bodies assure the
569 quality of price signals on carbon markets, instead of relying on the carbon price to value
570 debt. In fact, carbon prices on its own are insufficient benchmarks for valuing debt. For
571 instance, large demand for carbon debt would lead to a lower carbon price if this were not
572 balanced by an increase of r_d , which in turn would lead to an undervaluation of risks.

573

574 **Supply and demand of CROs**

575 Supply of allowances under a pure ETS is completely inelastic, whereas supply in a tax
576 system is infinitely elastic. By contrast, the supply of CROs (adding to the supply of
577 allowances) is finitely elastic. Generally, the supply curve is increasing because the larger the
578 demand for CROs, the more abatement is required in the future, making future abatement
579 and thus CROs more expensive. Because total discounted interest costs (i_{tot}) are reflected in
580 the supply curve, by valuing carbon debt and setting the rate r_d accordingly, debt issuing
581 bodies can partly control its slope. The slope, however, determines the level of price
582 volatility, e.g., resulting from a demand shock, as depicted in Extended Data Figure 1. By
583 implication, price volatility is largest in a pure ETS, and zero in a tax system. By increasing
584 interest costs in a CRO-ETS, the potential for volatile prices increases, and vice versa. On the
585 other hand, net emissions are fixed in an idealized ETS, and subject to demand fluctuations
586 in a tax system. In a CRO-ETS the cumulative quantity of net emissions is fixed, however,
587 only if default risks are adequately managed.

588

589

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591

592

593 **Numerical solution of the model**

594 The model used to solve the CRO optimization problem [15] is based on marginal
595 abatement cost curves (MACCs, see [4]) derived from scenarios reported in the SSP
596 scenario database^{24,54}. MACCs are derived for each IAM and Shared Socioeconomic Pathway
597 (SSP) by combining and fitting a curve to carbon prices from different Representative
598 Concentration Pathways (RCPs) in each time step. For instance, a MACC in 2040 for a
599 specific IAM/SSP configuration is composed of the carbon prices reported for RCP1.9-
600 RCP6.0. The set of parameters of each IAM/SSP configuration of our model is therefore
601 composed of net emissions from the baseline scenario (E_{base}), the interest rate r (derived
602 from the slope of log carbon prices), the carbon budget B derived from the sum of net
603 emissions compatible with specific climate targets and 8 MACCs for the period from 2030 to
604 2100, i.e., one per decade. We fix abatement rates a during optimization where no MACCs
605 could be derived because reported prices p_i are (close to) zero over the whole range of a_i ,
606 i.e., in 2020 for all configurations; for IMAGE/SSP2 in 2030; for IMAGE/SSP3 in 2030 and
607 2040; for IMAGE/SSP5 in 2030. Where abatement is fixed, costs are set to zero. Moreover,
608 for the 1.5°C and 2°C case studies carbon budgets were corrected using historical emission
609 data⁵³ (scenarios reported in the SSP database start in 2005 or 2010 and were exceeded by
610 estimated net emissions in the past decades). Baseline emissions in 2020 were replaced by
611 the projection for 2019 in ref⁵³.

612 We fit the inverse of the generalized logistic function⁵⁵ to log prices p_i as reported in the SSP
613 database. Abatement rates a_i are computed by subtracting net emissions in a scenario with
614 climate target from net emissions in the baseline scenario and dividing by the baseline. The
615 index i denotes different RCPs within the same IAM/SSP configuration and the same year
616 (see [SI2.1](#) for the cost curves of all IAM/SSP configurations):

617

$$\ln(p_i) = P + \frac{1}{k} * \ln\left(\frac{1}{v} * \left(\left(\frac{L - A}{a_i - A}\right)^v - 1\right)\right). \quad [17]$$

618 MAC are therefore a power law defined on the interval $\{a \in \mathbb{R} | L < a < A\}$:

619

$$MAC(a_i) = b * \left(\frac{1}{v} * \left(\left(\frac{L - A}{a_i - A}\right)^v - 1\right)\right)^c, \quad [18]$$

620 where $b = \exp(P)$ and $c = \frac{1}{k}$. An interpretation of the parameters is provided in Extended
621 Data Figure 8a. $L \approx 0$ (subject to model fitting) and $A = \max(a_i) + \varepsilon$ (such that a can become
622 $\max(a_i)$ without $MAC(a)$ becoming *inf*), i.e., A is set to the maximum abatement (plus $\varepsilon =$
623 0.01) observed in each decade for each IAM/SSP configuration because this level cannot be
624 exceeded. For numerical reasons, however, a is also constrained by A during optimization
625 such that $a < A$.

626 In most IAMs carbon prices are either imposed exogenously as driver of mitigation (e.g., in
627 the recursive dynamic models AIM/CGE or GCAM4) or prices are derived after optimization
628 from Lagrange multipliers of emission caps (e.g., in the intertemporal optimization models
629 MESSAGE-GLOBIOM, WITCH-GLOBIOM or REMIND-MAgPIE). In these cases carbon prices
630 typically increase exponentially with the interest rate, as explained by the Hotelling-rule^{22,23}.
631 In heavily constrained detailed process-based IAMs, intertemporally optimal carbon prices
632 are a good proxy of marginal costs, however, they do not necessarily reflect MACs exactly in
633 each point of time, as a consequence of growth constraints or caps on total deployment
634 levels of specific mitigation technologies. This is also the case here because we limit $a < A$
635 with an additional constraint and we fix a where no MACCs could be derived, implying that
636 MAC and carbon prices (derived from the Lagrange multiplier of the budget constraint [3])
637 don't necessarily coincide.

638 We compare MAC and carbon prices from our model with carbon prices as reported for the
639 individual scenarios in the SSP database for all models, SSPs and RCPs (see [SI2.2](#)). Reported
640 carbon prices in the database for AIM/CGE do not follow an exact exponential curve
641 because these prices reflect marginal costs from the SSP1 scenario which was initially
642 constrained by emission caps to obtain the climate target. Then prices were manually scaled
643 and imposed on other SSP scenarios to achieve the respective climate targets⁵⁶. Therefore,
644 AIM/CGE prices are better replicated by our model's MAC than by carbon prices. The same
645 is true for the IMAGE framework, which contains simulation as well as optimization
646 components and does not report Hotelling-type carbon prices.

647 Furthermore, we show abatement costs for all SSPs, IAMs and RCPs computed with our
648 model (see [SI2.3](#)). Because abatement costs are not explicitly reported in the database, we
649 compare costs from our model with close proxies, i.e., GDP loss and consumption loss in SSP
650 scenarios. For GCAM4 and IMAGE GDP loss and consumption loss are either not reported or

651 losses are close to zero. For GCAM4 we therefore added abatement costs for some
652 scenarios as reported in the supplementary information of ref⁵⁷, which are well replicated
653 by our model. No comparable data could be retrieved for the IMAGE model. For the other
654 IAMs our model's abatement costs mainly coincide with consumption loss. Net CO₂
655 emissions are also compared for all SSPs, IAMs and RCPs (see [SI2.4](#)).
656 Abatement rates a cannot exceed A , hence only IAM/SSP configurations with RCP1.9 data
657 are used for our 2°C case studies because more ambitious mitigation under a CRO-ETS
658 requires our model to partly operate in the 1.5°C abatement domain to achieve 2°C.
659 Therefore, 13 IAM/SSP parameter sets of our model are used for the case studies: AIM/CGE
660 (SSP1 and SSP2), GCAM4 (SSP1, SSP2 and SSP5), IMAGE (SSP1), MESSAGE-GLOBIOM (SSP1
661 and SSP2), REMIND-MAGPIE (SSP1 and SSP2 and SSP5), WITCH-GLOBIOM (SSP1 and SSP4);
662 i.e. 6 parameter sets for SSP1, 4 for SSP2, 1 for SSP4 and 2 for SSP5 (see Extended Data
663 Table 2). All 2°C scenarios are shown graphically in SI1.1 and numerically in SI1.2.

664

665 **Scenarios for direct air capture and storage**

666 For our 1.5°C (RCP1.9) case study, additional sources of abatement are required to assess
667 compatible pathways of more ambitious mitigation than suggested by RCP1.9 scenarios. We
668 therefore add direct air capture and storage (DACs) to the mitigation portfolio, however, we
669 treat this technology in a stylized manner as completely stand-alone and independent of
670 other abatement technologies (e.g., the energy needs for DACs are assumed to be met by
671 additional local renewable sources which do not interfere with the ramp-up of renewable
672 energy as part of conventional abatement). DACs is less controversial than bioenergy with
673 carbon capture and storage (BECCS) with respect to land use and has potentially limited
674 environmental impacts compared to other large scale CDR options¹⁶, making it more
675 independently scalable. However, capital and energy requirements are uncertain and
676 potentially enormous. Costs range between 20 and 1000 USD/tCO₂^{16,18,58-60}, and potentials
677 for CDR range from 0.5-5 GtCO₂/a in 2050 to 15-40 GtCO₂/a in 2100¹⁸, however, these
678 potentials are mainly constrained by cost considerations rather than biophysical limits⁶¹.
679 Here we derive 6 idealized MACCs for DACs covering 3 cost ranges and 2 maximum
680 abatement rates (see Extended Data Figure 8b). Instead of modifying the MACCs derived
681 from SSP scenarios to account for DACs, we add a_{DACs} to

682 [1]:

683

$$e(t) = E_{base}(t) * (1 - a(t) - a_{DACs}(t)). \quad [19]$$

684

685 and change total costs in [4] to:

686

$$c_{tot}(t, a(t)) = E_{base}(t) * \left(\int_0^{a(t)} MAC(t, \tilde{a}) d\tilde{a} + \int_0^{a_{DACs}(t)} MAC_{DACs}(\bar{a}) d\bar{a} \right). \quad [20]$$

687

688 Moreover, marginal abatement costs are always required to be equal:

689

$$MAC(t, a(t)) = MAC_{DACs}(a_{DACs}(t)). \quad [21]$$

690

691 To obtain a detailed technology downscaling of sources and sinks of CO₂ (fossil fuels and
692 industry, including residual emissions from carbon capture and storage; BECCS and land use
693 emissions) we interpolate linearly between the closest abatement levels reported in the SSP
694 database, i.e., $a_i < a < a_{i+1}$ (again, i denotes different RCPs withing the same IAM/SSP
695 configuration and the same year) and add DACs after the interpolation.

696

697 **1.5°C scenarios for Figure 4**

698 For Figure 4 the set of all 468 scenarios (13 IAM/SSP parameter sets, 6 rates r_d and 6 DACs
699 parameters sets) is filtered for scenarios achieving at least a 30% reduction of D compared
700 their baselines, i.e., where $r_d = 0$. For scenarios depicted in Extended Data Figures 3-5 this
701 reduction of D needs to be at least 5%, 15% and 45%, respectively. From scenarios with
702 different rates r_d but otherwise identical parameters, only the lowest rate is kept, resulting
703 in a potential set of 78 scenarios, of which 26 are feasible regarding the 30% carbon debt
704 reduction requirement in Figure 4. Hence, in panels c and d geometric median pathways of
705 26 scenarios where $r_d > 0$ are compared to the associated 26 baselines in panels a and b
706 where $r_d = 0$. Baselines are interpreted as ‘conventional ETS’ scenarios, which are in terms of
707 emission paths equivalent to CRO-ETS scenarios with $r_d = 0$. All underlying scenarios are
708 shown graphically in SI1.3 and numerically in SI1.4., abatement and interest costs are
709 illustrated in Extended Data Figure 6 for all scenarios.

710 **A note on technological learning**

711 Technological learning in most IAMs is either exogenous, i.e., purely time dependent, or
712 induced by learning-by-doing, which is strongly backed by empirical evidence. However,
713 learning is best perceived as a complex interplay between R&D, learning-by-doing and
714 different types of spillovers⁶², which only few models attempt to fully address. The MACCs
715 derived here from SSP scenario results reflect learning rates in the IAMs used to generate
716 these scenarios, resulting in typically decreasing marginal costs over time for similar
717 abatement rates. Therefore, learning in our model is exogenous (purely time dependent),
718 which is one of the main caveats of this model, because fixed learning rates over time imply
719 an incentive to wait until abatement becomes cheaper. More ambitious near-term
720 mitigation under a CRO-ETS, however, would likely lead to earlier cost reductions than
721 reflected in the model. Due to the complexity of learning and the simplicity of our model we
722 disregard DACS related technological change.

723

724 **Software and solver**

725 The model is solved using the CONOPT solver in GAMS v26.1. CONOPT is based on the
726 Generalized Reduced Gradient (GRG) algorithm, one of the most robust and commonly
727 applied methods for solving models with highly nonlinear objective functions or
728 constraints⁶³.

729

730 **Data availability**

731 All data generated or analyzed during this study are included in this published article and its
732 supplementary information files.

733

734 **Code availability**

735 The source code of the numerical model used for generating the data used in this study is
736 available at <https://github.com/jobednar/CROmodel>.

737 The numerical model was calibrated using scenarios from the SSP scenario database hosted
738 by IIASA and available at <https://tntcat.iiasa.ac.at/SspDb/>.

739

740

741 **References (Methods)**

742

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762

763 **Statements**

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769

770 **Author Contribution**

771 Michael Obersteiner, Fabian Wagner, Marcus Thomson and Johannes Bednar have equally
772 contributed to identifying the knowledge gaps and main ideas of this article, as well as
773 sharpening the field of interest. Johannes Bednar acted as lead author and was primarily
774 involved in formalizing and quantifying the ideas of the article, as well as in drafting of the
775 main article and development of analytical and numerical methods. Jim Hall and Michael
776 Obersteiner have supervised the development of the article from the first draft throughout
777 the review process. Jim Hall, Oliver Geden, Myles Allen, Fabian Wagner and Marcus
778 Thomson contributed to the work's framing, conception and design, as well as to the
779 interpretation of results. Artem Baklanov provided quality control of methods and result
780 presentation and contributed the mathematical proof of the equations derived in the
781 methods section. Oliver Geden contributed by significantly improving the article's policy
782 relevance, for instance by developing the EU implementation scenario. All authors were
783 equally involved in the revision process and have approved the submitted version of the
784 article.

785

786 **Competing interest declaration**

787 The authors declare no competing interests.

788

789 **Additional information**

790 This article contains supplementary information.

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795 Extended Data Legends

796 **Extended Data Table 1 | Net and gross emission removal in illustrative pathways from the IPCC's Special Report on global warming of**
797 **1.5°C**

798 Net and gross emission removal including bioenergy with carbon capture and storage (BECCS) and Agriculture, Forestry and Other Land Use
799 (AFOLU). To compute emission removal in term of years of current emissions we used a net emission value of 11.73 GtC in 2019. Data were
800 retrieved from the scenario database hosted by IIASA and available at: <https://data.ene.iiasa.ac.at/iamic-1.5c-explorer>.

801 **Extended Data Table 2 | Combinations of models and SSPs used to calibrate the model in this study**

803 13 combinations of models and SSPs for which RCP1.9 results are available in the SSP scenario database. The RCP2.6 scenarios presented in
804 the Results are composed of these 13 configurations of our model combined with six rates of interest on carbon debt ($r_d = 0, 0.005, 0.1, 0.2, 0.4,$
805 0.8), resulting in 78 scenarios. The RCP1.9 scenarios are composed of the same 78 model configurations combined with 6 marginal abatement
806 cost curves for direct air capture and storage resulting in 468 scenarios.

807 **Extended Data Figure 1 | Schematic supply of emission allowances and Carbon Removal Obligations (CROs) at a fixed point in time.** The
808 supply of allowances is completely inelastic (emission cap), whereas the supply elasticity of CROs is determined by discounted future abatement
809 costs, which increase as the demand for CROs increases, as well as interest costs, which can be controlled by managing authorities and financial
810 institutions (dashed blue CRO supply curves). If CROs are traded on a market, they clear at the same price as allowances and thereby reduce the
811 price of allowances. The larger the elasticity of the CRO supply curve, the lower the potential for price volatility (red arrows), as, e.g., induced by a
812 demand shock (dashed orange line). The sum of allowances and CROs issued equals net emissions. Abated emissions equal the difference
813 between baseline emissions (green) and net emissions and are comprised of emission reductions and/or carbon removal.
814

815 **Extended Data Figure 2 | 1.5°C (RCP1.9) scenarios abatement costs and carbon debt for six different marginal abatement cost (MAC)**
816 **curves of direct air capture and storage (DACs) and interest rates on carbon debt $r_d = 0$ and $r_d = 0.08$.** For a definition of D refer to the
817 Methods; abatement costs are discounted and expressed as GDP percentage. Abatement costs are exclusive of interest costs. For each rate r_d ,
818 78 scenarios as for the RCP2.6 analysis times 6 DACS parameters) are grouped by DACS costs (low to high, i.e. "LoCost", "MedCost",
819 "HiCost") and DACS capacity limits (10% and 30% of baseline emissions, i.e. "LoCap" and "HiCap"). **Panels a & b:** Median abatement costs as
820 function of median carbon debt D for $r_d = 0$ (panel a) and $r_d = 0.08$ (panel b). For $r_d = 0$ we observe an inverse relation between the level of carbon
821 debt and abatement costs; and the capacity limit is a stronger determinant of abatement costs than DACS deployment costs. This "discounting
822 effect" is reversed when $r_d = 0.08$ and high levels of D are penalized. In this case, lower abatement costs are realized by lower carbon debt (and
823 vice versa). For both rates r_d "LoCost_HiCap" DACS scenarios are characterized by the lowest abatement costs, however, at very different levels
824 of D . When interest is invoked DACS deployments costs become an increasingly important determinant of total abatement costs. **Panels c & d:**
825 **Distribution of total carbon debt D (panel c) and abatement costs (panel d) for the median values shown in panels a & b.** Boxes indicate
826 the 25-75% interquartile ranges around medians (bold solid line), whiskers indicate min to max ranges, black dots mark outliers.

827 **Extended Data Figure 3 | 1.5°C (RCP1.9) pathways under a conventional ETS (panels a and b) compared to a CRO-ETS (panels c and d).**
828 The underlying set of scenarios was filtered for those scenarios that achieve at least a 5% reduction of total carbon debt compared to their
829 baselines (see Methods). **Panels a and c:** Geometric median net emissions (solid line) and gross emissions from fossil fuels and industry (FFI),
830 bioenergy with carbon capture and storage (BECCS), land use change (LUC) and direct air capture and storage (DACs). Net emissions from
831 panel a are also displayed in panel c (dashed line) and vice-versa. Total carbon debt D is shown as box-and-whiskers plot. Boxes indicate the 25-
832 75% interquartile range around median values (bold line), whiskers indicate min to max ranges, points mark the outliers. **Panels b and d:** Annual
833 mitigation costs as GDP percentage, including the share of average abatement costs attributed to emission reductions (ABM), to compensation of
834 residual emissions by CDR (RES) and to net negative emissions (NNE) as well as expenditures for allowances (ETS) and interest costs (INT).
835 Total mitigation costs (i.e., ABM+RES+NNE+ETS+INT) from panel d are also displayed in panel b (dashed line) and vice-versa. Box-and-
836 whiskers plots show total discounted abatement costs (i.e., ABM+RES+NNE) as GDP percentage, the number above the chart indicates out-of-
837 range outliers. Pie charts in panel d summarize properties of the underlying set of scenarios (see Methods). The distribution of r_d in CRO-ETS
838 scenarios is depicted in panel c.

839 **Extended Data Figure 4 | 1.5°C (RCP1.9) pathways under a conventional ETS (panels a and b) compared to a CRO-ETS (panels c and d).**
840 The underlying set of scenarios was filtered for those scenarios that achieve at least a 15% reduction of total carbon debt compared to their
841 baselines (see Methods). **Panels a and c:** Geometric median net emissions (solid line) and gross emissions from fossil fuels and industry (FFI),
842 bioenergy with carbon capture and storage (BECCS), land use change (LUC) and direct air capture and storage (DACs). Net emissions from
843 panel a are also displayed in panel c (dashed line) and vice-versa. Total carbon debt D is shown as box-and-whiskers plot. Boxes indicate the 25-
844 75% interquartile range around median values (bold line), whiskers indicate min to max ranges, points mark the outliers. **Panels b and d:** Annual
845 mitigation costs as GDP percentage, including the share of average abatement costs attributed to emission reductions (ABM), to compensation of
846 residual emissions by CDR (RES) and to net negative emissions (NNE) as well as expenditures for allowances (ETS) and interest costs (INT).
847 Total mitigation costs (i.e., ABM+RES+NNE+ETS+INT) from panel d are also displayed in panel b (dashed line) and vice-versa. Box-and-
848 whiskers plots show total discounted abatement costs (i.e., ABM+RES+NNE) as GDP percentage, the number above the chart indicates out-of-
849 range outliers. Pie charts in panel d summarize properties of the underlying set of scenarios (see Methods). The distribution of r_d in CRO-ETS
850 scenarios is depicted in panel c.

851 **Extended Data Figure 5 | 1.5°C (RCP1.9) pathways under a conventional ETS (panels a and b) compared to a CRO-ETS (panels c and d).**
852 The underlying set of scenarios was filtered for those scenarios that achieve at least a 45% reduction of total carbon debt compared to their
853 baselines (see Methods). **Panels a and c:** Geometric median net emissions (solid line) and gross emissions from fossil fuels and industry (FFI),
854 bioenergy with carbon capture and storage (BECCS), land use change (LUC) and direct air capture and storage (DACs). Net emissions from
855 panel a are also displayed in panel c (dashed line) and vice-versa. Total carbon debt D is shown as box-and-whiskers plot. Boxes indicate the 25-
856 75% interquartile range around median values (bold line), whiskers indicate min to max ranges, points mark the outliers. **Panels b and d:** Annual
857 mitigation costs as GDP percentage, including the share of average abatement costs attributed to emission reductions (ABM), to compensation of
858 residual emissions by CDR (RES) and to net negative emissions (NNE) as well as expenditures for allowances (ETS) and interest costs (INT).
859 Total mitigation costs (i.e., ABM+RES+NNE+ETS+INT) from panel d are also displayed in panel b (dashed line) and vice-versa. Box-and-
860 whiskers plots show total discounted abatement costs (i.e., ABM+RES+NNE) as GDP percentage, the number above the chart indicates out-of-
861 range outliers. Pie charts in panel d summarize properties of the underlying set of scenarios (see Methods). The distribution of r_d in CRO-ETS
862 scenarios is depicted in panel c.

863 **Extended Data Figure 6 | 1.5°C (RCP1.9) scenarios' abatement costs (panel a) and interest costs (panel b) as function of percentage carbon**
864 **debt reduction compared to the baseline scenario, i.e., where $r_d = 0$, for all 468 RCP1.9 scenarios, grouped by the carbon debt interest rate (r_d) and**
865 **cost and capacity parameters of direct air capture and storage (DACs). DACS cost parameters range from low to high, i.e., "LoCost", "MedCost",**

866 "HiCost"; capacity limits include 10% and 30% of baseline emissions, i.e., "LoCap" and "HiCap". **Panel a:** Total discounted abatement costs
867 excluding interest costs (i.e., ABM + RES + NNE as in Figure 4 and Extended Data Figure 7-9). **Panel b:** Total discounted interest costs (i.e. INT
868 as in Figure 4 and Extended Data Figures 7-9).

869 **Extended Data Figure 7 | Schematic overview and illustrative repayment terms of RCP1.9 scenarios. Panel a:** Schematic overview of the
870 CRO-ETS. The physical overshoot of a cumulative emission target, potentially amplified by outgassing of CO₂ from the Earth's stocks, subsequently
871 necessitates carbon sequestration for returning to the target. For accrued carbon debt CROs are issued, obliging emitters to compensate for a
872 tonne of CO₂ before a specified maturity, e.g., by physically removing atmospheric CO₂ or by acquiring an adequate quantity of allowances in the
873 future. Similar to financial debt, CROs require debtors to pay interest to hedge physical and financial risks associated with carbon debt. Three ear-
874 marked financial resources are created under a CRO-ETS (1) Revenues from auctioning allowances are recycled into the economy to the benefit
875 of society. (2) Revenues from interest on carbon debt are targeted at managing risks, i.e., by enabling additional carbon sequestration when Earth
876 system risks (e.g., permafrost thaw) and financial risks (e.g., default risk of debtors) materialize. (3) Funds for repayment of carbon debt are
877 individually managed by debtors. **Panels b-e:** Repayment term function $T_R(t)$ for the scenarios illustrated in Extended Data Figure 7 (panel b),
878 Extended Data Figure 8 (panel c), Figure 4 (panel d) and Extended Data Figure 9 (panel e). Interest on carbon debt r_d reflects the mean values of
879 the distributions shown in panel c of these figures. Bold lines indicate geometric median repayment-terms derived from scenarios presented in these
880 figures. $T_R(t)$ maps the timing of carbon debt accrual to the time of its compensation; see Methods. For instance, in panel c carbon debt accrued in
881 2020 is compensated approximately 40 years later in scenarios with interest ($r_d=0.058$, yellow lines) and roughly 50 years later in scenarios where
882 $r_d=0$ (turquoise lines). As r_d is increased, the net zero year moves closer, implying that carbon debt in 2020 is compensated earlier, while in general
883 T_R extends over longer periods. The increasingly flat net negative emissions profile (when r_d is increased) implies that T_R increases more rapidly in
884 the beginning than when $r_d=0$ because cumulative carbon debt at t grows faster than cumulative net negative emissions at $t+T_R(t)$. The point of
885 inflection indicates where cumulative carbon debt begins to grow more slowly than cumulative net negative emissions compensating that carbon
886 debt. For instance, in panel d (yellow line) cumulative carbon debt from 2030 onwards grows at a slower pace than cumulative net negative
887 emissions approximately 63 years later.

888 **Extended Data Figure 8 | Marginal abatement cost curves. Panel a:** The functional form of marginal abatement costs, $MAC(a) = b * \left(\frac{1}{v} * \left(\left(\frac{L-A}{a-A} \right)^v - 1 \right) \right)^c$, is derived from the inverse generalized logistic function. It is relatively flexible with respect to replicating a wide range of MAC
889 curves derived from the SSP database. Here $A=1$ and $L=0$ are upper and lower asymptotes along the y-axis. Crucially, $MAC(a=A) = inf$, therefore
890 A is a maximum abatement rate built into the MAC curve. b defines the y-position of the pivot point. The x-position of the pivot point is determined
891 by v , and for $v=1$ it is exactly the middle of the interval (L, A) , $\frac{L+A}{2}$. c defines the level of rotation with respect to the pivot point. **Panel b:** Six stylized
892 MAC curves for direct air capture and storage (DACS) covering the literature range for costs from 20 to 1000 USD/tCO₂ (orange area). Low-cost
893 MACCs (dotted lines) start at approximately 50 USD/tCO₂ and reach 1000 USD/tCO₂ at abatement rates $a_{DACS} = 0.07$ (low capacity, blue line) and
894 $a_{DACS} = 0.27$ (high capacity, red line) equivalent to approximately 3 and 12 GtCO₂/a at current emission levels, respectively. Medium cost MAC
895 curves (dashed lines) start at 250 USD/tCO₂ and reach 1000 USD/tCO₂ at $a_{DACS} = 0.05$ (low capacity, blue line) and $a_{DACS} = 0.22$ (high capacity,
896 red line), i.e. roughly 2 and 10 GtCO₂/a at current emission levels, respectively. High cost MAC curves (solid lines) start at approximately 500
897 USD/tCO₂ and reach 1000 USD/tCO₂ at $a_{DACS} = 0.03$ (low capacity, blue line) and $a_{DACS} = 0.12$ (high capacity, red line), amounting to roughly 1 and
898 5 GtCO₂/a at current emission levels, respectively.
899

900