

Research Paper

Unlocking planetesimal magnetic field histories: A refined, versatile model for thermal evolution and dynamo generation

Hannah R. Sanderson ^{a,*}, James F.J. Bryson ^a, Claire I.O. Nichols ^a, Christopher J. Davies ^b

^a Department of Earth Sciences, University of Oxford, South Parks Road, Oxford, OX1 3AN, UK

^b School of Earth and Environment, University of Leeds, Leeds, LS2 9JT, UK

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ABSTRACT

The thermal and magnetic histories of planetesimals provide unique insights into the formation and evolution of Earth's building blocks. These histories can be gleaned from meteorites by using numerical models to translate measured properties into planetesimal behaviour. In this paper, we present a new 1D planetesimal thermal evolution and dynamo generation model. This magnetic field generation model is the first of a differentiated, mantled planetesimal that includes both mantle convection and sub-eutectic core solidification. We have improved fundamental aspects of mantle heat transport by including a more detailed viscosity model and stagnant lid convection parametrisations consistent with internal heating. We have also added radiogenic heating from ⁶⁰Fe in the metallic Fe-FeS core. Additionally, we implement a combined thermal and compositional buoyancy flux, as well as the latest magnetic field scaling laws to predict magnetic field strengths during the planetesimal's thermal evolution until core solidification is complete. We illustrate the consequences of our model changes with an example run for a 500 km radius planetesimal. These effects include more rapid erosion of core thermal stratification and longer duration of mantle convection compared to previous studies. The additional buoyancy from core solidification has a marginal effect on dynamo strength, but for some initial core sulfur contents it can prevent cessation of the dynamo when mantle convection ends. Our model can be used to investigate the effects of individual parameters on dynamo generation and constrain properties of specific meteorite parent bodies. Combined, these updates mean this model can predict the most reliable and complete magnetic field history for a planetesimal to date, so is a valuable tool for deciphering planetesimal behaviour from meteorite properties.

1. Introduction

Magnetic field generation in rocky bodies depends on conditions in their interiors, such as the extent of differentiation, and the vigour of core and mantle convection. Planetesimals were small, rocky bodies, which accreted in the first few million years (Ma) after Solar System formation and formed the building blocks of the terrestrial planets. Some planetesimals survive today as asteroids, and meteorites are the fragments of them that reach the Earth. Magnetisations recorded in meteorites can provide key insights into the evolution of planetesimals, as well as processes in the protoplanetary disk. Planetesimal thermal evolution and magnetic field generation models are crucial for interpreting these remanences in terms of processes in these bodies and in the solar nebula that generated these fields.

In order to generate a magnetic field by dynamo action, a rocky body must have a partially molten, metallic core, that is in vigorous motion. Core flow can be driven by thermal or compositional convection, or a combination of the two, or by mechanical forcing. However,

the latter is thought not to be relevant for planetesimals (Dodds et al., 2021). Thermal convection is driven by temperature-induced density differences and requires that the heat flux across the core-mantle boundary (CMB) is superadiabatic. Compositional convection is driven by chemically-induced density differences resulting from core solidification. For example, at the present day the Earth's magnetic field is driven by partitioning of buoyant, incompatible light elements from the solidifying inner core into the liquid outer core, which rise and drive convection in the liquid outer core (Braginsky, 1963; Gubbins, 1977; Nimmo, 2007). A record of past internally generated magnetic fields on a planetesimal tells us that this body met the requirements for thermal (e.g. Wang et al., 2017) and/or compositional (e.g. Maurel et al., 2021) dynamo generation at some point in its history.

Chondritic and achondritic meteorites from the inner and outer Solar System have had their paleomagnetic remanences measured (e.g. Carporzen et al., 2011; Courneade et al., 2015; Wang et al., 2017; Weiss

* Corresponding author.

E-mail address: hannah.sanderson@earth.ox.ac.uk (H.R. Sanderson).

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et al., 2017). Some of these measurements relate to bulk rocks (e.g. Carporzen et al., 2011), while others are measurements of individual phases, such as dusty olivines in chondrules (e.g. Tarduno et al., 2012; Fu et al., 2014) or cloudy zones in metal-rich meteorites (e.g. Nichols et al., 2021; Maurel et al., 2021). These measurements combined with numerical modelling provide evidence that differentiated (e.g. Fu et al., 2012) and partially differentiated bodies (e.g. Elkins-Tanton et al., 2011; Bryson et al., 2019b) generated magnetic fields. If a paleomagnetic remanence can be dated, numerical models can be used to predict a range of parent body sizes and properties that generate a magnetic field at the identified time (e.g. Bryson et al., 2019b). If a remanence cannot be dated, numerical models can be used to estimate the age at which the magnetisation was acquired (e.g. Tarduno et al., 2012; Bryson et al., 2015; Nichols et al., 2021).

Some meteorites have been interpreted to record magnetisations from the nebula field, which threaded the entire protoplanetary disk until 4–5 Ma after CAI formation (Wang et al., 2017). The nebula field affected stellar accretion from the protoplanetary disk (Wardle, 2007; Weiss et al., 2021) and may have influenced disk structure (Hu et al., 2019). Paleomagnetic records of the nebula field can help us understand disk lifetime (Wang et al., 2017; Borlina et al., 2022), structure and strength of the disk field (Cournede et al., 2015; Borlina et al., 2021; Bryson et al., 2023), movement of solids within the disk (Bryson et al., 2020a,b), and stellar accretion rate (Weiss et al., 2021). Randomly oriented paleomagnetic directions between individual chondrules (Fu et al., 2014, 2020; Borlina et al., 2021) can provide evidence these chondrule remanences are pre-accretionary, and therefore must have acquired a nebula field record prior to planetesimal accretion. In contrast, ancient, bulk paleomagnetic remanences require planetesimal dynamo generation models to help determine whether these remanences were imparted by dynamo or nebula fields (e.g. Cournede et al., 2015; Maurel and Gattacceca, 2024).

There have been several previous models of dynamo generation in planetesimals (Elkins-Tanton et al., 2011; Sterenborg and Crowley, 2012; Bryson et al., 2019a; Dodds et al., 2021). Each model iteration included a new degree of complexity, such as parametrised mantle convection (Sterenborg and Crowley, 2012), multi-stage accretion (Bryson et al., 2019a), gradual accretion (Dodds et al., 2021), or core thermal stratification (Dodds et al., 2021). These models have predicted the range of planetesimal sizes that can generate a dynamo (e.g. >340 km Bryson et al., 2019a) and the timing and duration of the dynamo (4–30 Ma after CAI formation and 5–25 Ma depending on size, Dodds et al., 2021). Additionally, these models have been used to constrain the properties of meteorite parent bodies, including the CV chondrites, H chondrites, and angrites (Bryson et al., 2019a; Dodds et al., 2021). Other numerical models have been developed that focus purely on dynamo generation by core solidification and compositional convection. These models either have a fixed entropy dissipation in the core (Nimmo, 2009) or focus on the IVA iron meteorites so have no mantle (Scheinberg et al., 2016; Neufeld et al., 2019). Here, we present our refined planetesimal thermal evolution and dynamo generation model, which can be used to understand the controls on planetesimal dynamo generation and recover meteorite parent body properties.

While each previous model added new behaviour, some fundamental aspects of mantle heat transport have remained unchanged between models and are reconsidered here. Magnetic field generation requires rapid core cooling (superadiabatic CMB heat flux) or core solidification, for which heat must be moved from the core to the mantle. Therefore, the timing of magnetic field generation is intrinsically linked to mantle cooling. Unlike previous models, our chosen mantle convection scaling laws are suitable for a body with internal heating and surface and basal heat fluxes and have been benchmarked against 2D numerical simulations (Deschamps and Vilella, 2021; Thiriet et al., 2019). Mantle convection depends strongly on viscosity, so we have refined the viscosity law from previous models. Our chosen mantle convection

scaling laws also respond consistently to changes to viscosity parameters, which enables a full investigation of the effects of viscosity on dynamo generation. Moreover, our criterion for the cessation of mantle convection ensures smooth and more physically realistic behaviour in the CMB heat flux and the mantle temperature profiles when the mantle becomes fully conductive. In the core, we have also included heating from radiogenic ^{60}Fe , which may increase the core temperature and the heat flux into the mantle at early times.

Alongside mantle convection and variable viscosity, we also consider sub-eutectic core solidification. Modelling dynamo generation from planetesimal core solidification is challenging, because there are multiple possible mechanisms of core solidification including: growth of stable or unstable iron dendrites; iron snow (Scheinberg et al., 2016); or viscous delamination of solid iron from the CMB (Neufeld et al., 2019). Due to the uncertainty in solidification mechanism, some models only studied early thermal dynamos until the end of mantle convection (Sterenborg and Crowley, 2012; Dodds et al., 2021) or used the time taken for eutectic core solidification as a proxy for when a compositional dynamo could be generated even though eutectic solidification cannot drive a compositional dynamo (Bryson et al., 2019a). Also, Bryson et al. (2019a) used different magnetic field scaling laws for thermal compared to compositional dynamos and were not able to accommodate both mechanisms driving core flow simultaneously. Models that have included sub-eutectic core solidification either focus on unmantled planetesimals (Scheinberg et al., 2016; Neufeld et al., 2019) or neglect mantle convection in the early thermal history of the body (Nichols et al., 2021). Here, we have developed a model for magnetic field generation by sub-eutectic core solidification, which also considers the relative contribution of both thermal and compositional buoyancy to magnetic field generation during core solidification.

In this paper, we describe our refined, 1D, spherically symmetric thermal evolution model in Section 2. We show the results of an example run and discuss the effects of our model changes in Section 3. We justify our assumptions about accretion and differentiation, the mantle melting, and core solidification in Sections 4–6, respectively. Future applications of the model and areas for further refinement are addressed in Section 7, and we conclude in Section 8.

2. Thermal evolution model

2.1. Overview

The key stages in planetesimal thermal evolution are shown in Fig. 1. After accretion, the planetesimal will heat up due to the decay of radiogenic ^{26}Al ($t_{1/2} = 0.717$ Ma, Neumann et al., 2012). If accreted sufficiently early (within 1.5–2.5 Ma, Neumann et al., 2012; Monnereau et al., 2023), the planetesimal reaches a high enough temperature that it can melt and differentiate, forming a core and mantle. During differentiation ^{26}Al partitions into the mantle, while radiogenic ^{60}Fe ($t_{1/2} = 2.62$ Ma, Ruedas, 2017) partitions into the core. These two isotopes then heat the mantle and the core, respectively, and the mantle becomes unstable to convection. The adiabatic gradient is small in planetesimals due to their small size, so we neglect the core adiabat in our core convection criterion and when determining the direction of heat flow across the CMB. If the mantle becomes hotter than the core (e.g. due to strong internal heating and low surface heat flux) the core is heated by the mantle from above and becomes thermally stratified at shallow depths (Dodds et al., 2021). Once the mantle is cooler than the core, the core also begins to cool. Since the CMB heat flux, F_{CMB} , is positive, core convection begins. If the magnetic Reynolds number, Re_m , is greater than a critical value this convection can lead to the onset of the dynamo. As the mantle cools, it becomes more viscous and mantle convection ceases and heat in the mantle is transported by conduction. Initially, the cessation of mantle convection decreases

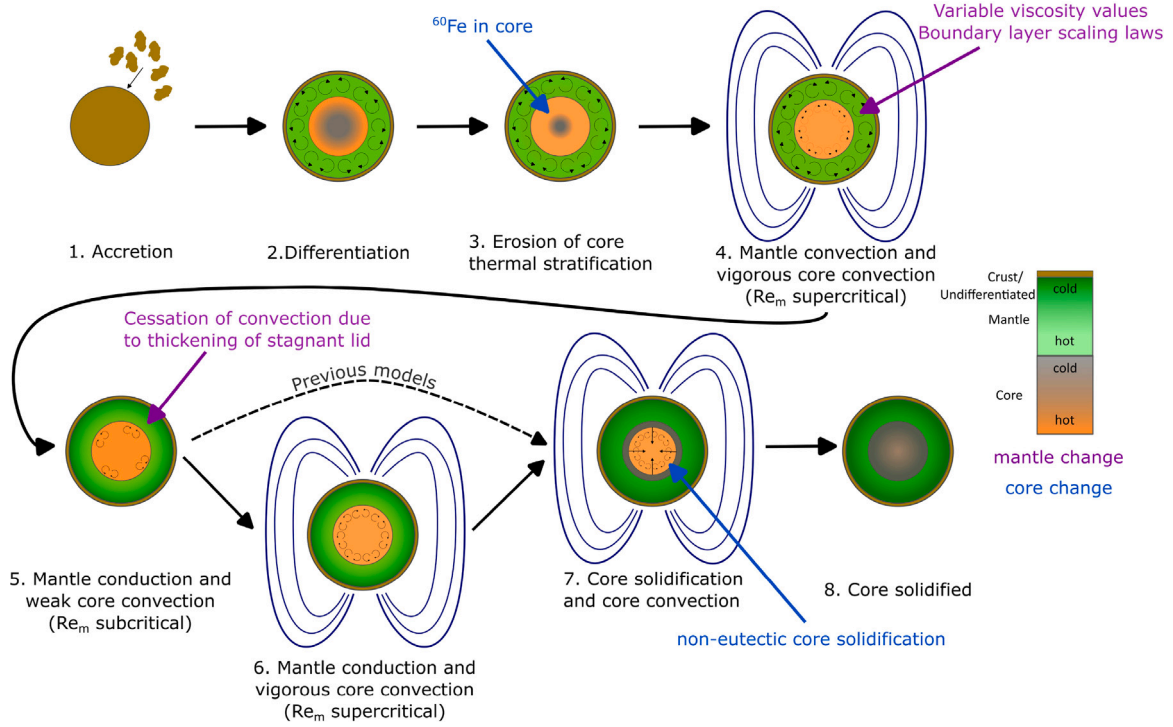


Fig. 1. Schematic depicting the stages in our planetesimal thermal evolution. Blue (core) and purple (mantle) labels highlight significant refinements adopted in our model compared to Sterenberg and Crowley (2012), Bryson et al. (2019a) and Dodds et al. (2021). Previous models only considered magnetic field generation after the end of mantle convection via core solidification (stage 7). However, our model allows for the possibility of two epochs of magnetic field generation prior to core solidification. Magnetic field generation can occur in stages 4, 6, and 7 if the magnetic Reynolds number exceeds a critical value. For low initial core sulfur contents, the core can start solidifying before the cessation of mantle convection and there may not be a pause in dynamo generation (stage 5). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

F_{CMB} and can lead to a subcritical Re_m and the cessation of the dynamo. Later, during mantle conduction, if F_{CMB} increases sufficiently, Re_m can become supercritical again and the dynamo can restart. Once the core cools below its liquidus, core solidification begins. This provides an additional buoyancy source for the core dynamo due to the ejection of light elements (e.g. carbon, sulfur) and can lead to a second period (or extend the first/second period) of dynamo generation. Dynamo generation is no longer possible once the core is fully solidified.

We describe our 1D, spherically symmetric model in detail in the following sections. We begin with our mantle viscosity model, then explain each stage in the thermal evolution and finish with magnetic field generation and the numerical implementation. Model assumptions are discussed in Sections 4–6.

2.2. Mantle viscosity

Mantle viscosity varies over many orders of magnitude during a planetesimal's thermal evolution, due to variations in mantle temperature and melt fraction, and has a large impact on mantle cooling. It controls mantle boundary layer thicknesses during convection and the transition from mantle convection to conduction, which affects CMB heat flux and dynamo generation. In this model, we define a four-piece viscosity law to capture changing rheological behaviour with temperature, and ensure the viscosity law and convection parametrisations are self-consistent and can be fully adjusted to reflect uncertainties in viscosity parameters.

The temperature dependence of mantle viscosity is defined piecewise with five control variables (Fig. 2): critical melt fraction, ϕ_c , Arrhenius slope, β , melt weakening exponent, α_n , reference viscosity

at the solidus, η_0 , and liquid viscosity, η_l :

$$\eta = \begin{cases} \eta_0 \exp(-\beta(T - T_{m,s})) & T \leq T_{m,s} \\ \eta_0 \exp\left(-\left(\beta + \frac{\alpha_n}{T_{m,l} - T_{m,s}}\right)(T - T_{m,s})\right) & T_{m,s} < T \leq T_{\phi_c} \\ \eta_C 10^{\frac{\Delta\eta}{w}(T - T_{\phi_c})} & T_{\phi_c} < T < T_{\phi_c} + w \\ \eta_l \left(\frac{\phi - \phi_c}{1 - \phi_c}\right)^{-2.5(1 - \phi_c)} & T_{\phi_c} + w \leq T \end{cases} \quad (1)$$

Here $T_{m,s}$ and $T_{m,l}$ are the mantle solidus and liquidus temperatures, respectively, T_{ϕ_c} is the temperature at ϕ_c and $\eta_C = \eta(T_{\phi_c})$ is the viscosity at ϕ_c , which is calculated using Eq. (1b). The melt fraction, ϕ is calculated assuming a linear liquidus approximation: $\phi = \frac{T - T_{m,s}}{T_{m,l} - T_{m,s}}$.

We do not specify a mantle composition and assume the same silicate solidus, $T_{m,s} = 1400$ K, and liquidus, $T_{m,l} = 1800$ K, values as Bryson et al. (2019a) and Dodds et al. (2021) (see Section 5.1). The mantle solidus and liquidus are pressure-independent constants, because the pressure variation in planetesimal mantles is small (<50 MPa).

Below the solidus, the viscosity has an Arrhenius temperature dependence (Eq. (1a)). This dependence is modelled using the Frank-Kamenetskii approximation at a reference temperature, T_{ref} , and reference viscosity, η_0 , $\frac{E}{RT} \approx \frac{E(T - T_{\text{ref}})}{R_g T_{\text{ref}}^2} = \beta(T - T_{m,s})$, where E is the activation energy, $R_g = 8.31 \text{ J K}^{-1} \text{ mol}^{-1}$ is the gas constant, and the mantle solidus is taken as the reference temperature (Frank-Kamenetskii, 1969). Above the solidus, but below the critical melt fraction, this kinetic Arrhenius dependence has an additional melt weakening dependence $\alpha_n \phi = \alpha_n \frac{T - T_{m,s}}{T_{m,l} - T_{m,s}}$ (Eq. (1b)). There is a sharp drop in viscosity at ϕ_c , because melt surrounds any remaining solid phases and the material disaggregates. Above ϕ_c , viscosity is described by the Krieger-Dougherty relation (Faroughi and Huber, 2015; Sturtz et al., 2022)

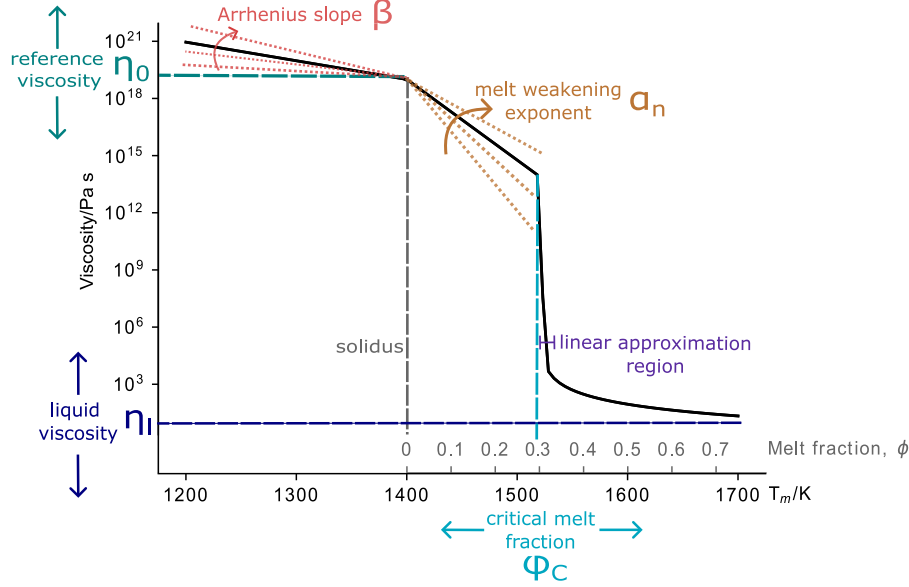


Fig. 2. Variation of mantle viscosity with temperature (solid black line) for $\eta_0 = 10^{19}$ Pa s, $\phi_C = 0.3$, $\beta = 0.0225$ K $^{-1}$, $\alpha_n = 30$, and $\eta_l = 10$ Pa s. The effect of varying each parameter is shown by the coloured arrows and lines. The grey, upper ticks on the horizontal axis indicates the equivalent melt fraction for temperatures above the solidus for mantle solidus and liquidus temperatures of 1400 K and 1800 K, respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

(Eq. (1d)), which tends to a constant liquid viscosity as the melt fraction approaches unity.

Eq. (1c) is an approximation using $\frac{d\log_{10}\eta}{dT} = \frac{\Delta\eta}{w}$ to ensure numerical stability at the rapid drop in viscosity at ϕ_C . w is the width of the region covered by this approximation, and is set to 5 K to minimise the approximated region, but ensure numerical stability. $\Delta\eta = \log_{10}(\eta(T_{\phi_C} + w)) - \log_{10}(\eta(T_{\phi_C}))$ is the logarithmic difference in the viscosity at ϕ_C , determined by Eq. (1b), and the viscosity at $T_{\phi_C} + w$, determined by Eq. (1d).

The Arrhenius temperature dependence (Eq. (1a)) determines the viscous temperature scale, $\frac{\Delta T}{T_{\text{rh}}}$, which determines the fraction of the temperature difference across the convecting region that will control convection (Michaut and Neufeld, 2022; Davaille and Jaupart, 1993)

$$f_{\text{rh}} = -\frac{d\eta(T_m)/dT}{\eta(T_m)} \Delta T. \quad (2)$$

In this definition, T_m is the temperature of the convecting region (the mantle) and ΔT is the temperature difference between the interior and the boundary (for the mantle $\Delta T = T_m - T_s$).

Compared to the three piece model of Bryson et al. (2019a), this model has an order of magnitude narrower region approximated for numerical stability, w , and applies the Krieger-Dougherty relation to viscosity beyond ϕ_C rather than assuming a constant value. Unlike the tanh approximation employed by Dodds et al. (2021), it captures the change in slope at the solidus, has a steeper gradient in viscosity at ϕ_C , and can be adjusted using physically meaningful parameters.

2.3. Accretion

Our model begins with instantaneous accretion of an undifferentiated mixture of silicates and Fe–FeS at 200 K at a specified time, t_{acc} , after CAI formation. The planetesimal surface temperature is fixed at an equilibrium temperature of 200 K throughout the simulation, because the range of planetesimal surface heat fluxes is small enough that its effect on the equilibrium surface temperature is negligible (<10 K; Dodds et al., 2021). At the planetesimal centre, $\frac{\partial T}{\partial r} \Big|_{r=0} = 0$ throughout the simulation.

2.4. Before differentiation

After accretion, the planetesimal heats up due to decay of radiogenic ^{26}Al and ^{60}Fe . Heat is initially transported through the body by conduction

$$\rho_{\text{ch}} c_{p,\text{ch,eff}} \frac{\partial T}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(k_{\text{ch}} r^2 \frac{\partial T}{\partial r} \right) + \rho_{\text{ch}} H, \quad (3)$$

where ρ is the density, c_p is the specific heat capacity, T is the temperature, r is the radius, t is the time, and k is the thermal conductivity. The subscript ch denotes the values for the undifferentiated, chondritic material. The undifferentiated planetesimal is assumed to have the same thermal properties as the silicate mantle (e.g. Elkins-Tanton et al., 2011; Bryson et al., 2019a) except for the density which uses the bulk density of the planetesimal. Compaction and sintering of the planetesimal prior to differentiation are neglected and a constant thermal diffusivity is used throughout, because these processes only affect the planetesimal as it initially heats up from 200 K to 700 K (Yomogida and Matsui, 1984) and have a minimal effect on the overall thermal evolution. H is the radiogenic heating power per unit mass

$$H = H_{\text{Al},0} f_{26\text{Al}} 0.01 X_{\text{Al}} e^{-\frac{\ln(2)t}{t_{1/2,\text{Al}}}} + H_{\text{Fe},0} f_{60\text{Fe}} 0.01 X_{\text{Fe}} e^{-\frac{\ln(2)t}{t_{1/2,\text{Fe}}}}, \quad (4)$$

where $H_{i,0}$ is the heating power per unit mass of isotope i at the time of CAI formation, f_i is the radiogenic isotope abundance as a ratio to its most common stable isotope, X_i is the elemental abundance in wt% in the accreting material, and $t_{1/2,i}$ is the radiogenic isotope half life. The values chosen for each parameter are summarised in Table 1. Melting of metal and silicate as the planetesimal heats up is accounted for using a modified specific heat capacity (adapted from Merk et al., 2002; Dodds et al., 2021, for a mixture of metal and silicate).

$$c_{p,\text{ch,eff}} = \begin{cases} c_{p,\text{ch}} & T < T_{\text{c},\text{s}} \text{ \& } T < T_{\text{m},\text{s}} \\ c_{p,\text{ch}} \left(1 + \frac{0.01 X_{\text{Fe}} L_{\text{c}}}{c_{p,\text{ch}} (T_{\text{c},\text{l}} - T_{\text{c},\text{s}})} \right) & T_{\text{c},\text{s}} < T < T_{\text{c},\text{l}} \text{ \& } T < T_{\text{m},\text{s}} \\ c_{p,\text{ch}} \left(1 + \frac{0.01 X_{\text{Fe}} L_{\text{c}}}{c_{p,\text{ch}} (T_{\text{c},\text{l}} - T_{\text{c},\text{s}})} + \frac{0.01 X_{\text{Si}} L_{\text{m}}}{c_{p,\text{ch}} (T_{\text{m},\text{l}} - T_{\text{m},\text{s}})} \right) & T_{\text{c},\text{s}} < T < T_{\text{c},\text{l}} \text{ \& } T_{\text{m},\text{s}} < T < T_{\text{m},\text{l}} \\ c_{p,\text{ch}} \left(1 + \frac{0.01 X_{\text{Si}} L_{\text{m}}}{c_{p,\text{ch}} (T_{\text{m},\text{l}} - T_{\text{m},\text{s}})} \right) & T_{\text{c},\text{l}} > T \text{ \& } T_{\text{m},\text{s}} < T < T_{\text{m},\text{l}} \end{cases} \quad (5)$$

Table 1

All fixed parameters used in the model and their references. Blank reference indicates the value is chosen in this work. The choice of viscosity parameters is justified in Section 2.2.

Symbol	Meaning	Value	Reference
Whole body parameters			
T_s	Surface temperature	200 K	^a Bryson et al. (2019a)
Ω	Rotational frequency of planetesimal	$1.75 \times 10^{-4} \text{ s}^{-1}$	^a Bryson et al. (2019a)
Undifferentiated material parameters			
ρ_{ch}	Density	$(\rho_m(R^3 - r_c^3) + \rho_c r_c^3)/R^3 \text{ kg m}^{-3}$	
$c_{p,\text{ch}}$	Specific heat capacity	$c_{p,m}$	Elkins-Tanton et al. (2011) Bryson et al. (2019a)
α_{ch}	Thermal expansivity	α_m	Elkins-Tanton et al. (2011) Bryson et al. (2019a)
k_{ch}	Thermal conductivity	$k_m = \kappa_m \rho_m c_{p,m}$	Elkins-Tanton et al. (2011) Bryson et al. (2019a)
Mantle parameters			
ρ_m	Density	3000 kg m^{-3}	Elkins-Tanton et al. (2011)
$c_{p,m}$	Specific heat capacity	800 $\text{J kg}^{-1} \text{ K}^{-1}$	Ghosh and McSweeney (1999)
L_m	Latent heat of fusion	$400 \times 10^3 \text{ J kg}^{-1}$	^a Ghosh and McSweeney (1998)
$T_{m,l}$	Liquidus	1800 K	Dodds et al. (2021)
$T_{m,s}$	Solidus	1400 K	Dodds et al. (2021)
α_m	Thermal expansivity	$4 \times 10^{-5} \text{ K}^{-1}$	^a Nimmo and Stevenson (2000)
κ_m	Thermal diffusivity	$9 \times 10^{-7} \text{ m}^2 \text{ s}^{-1}$	Dodds et al. (2021)
Ra_c	Critical Rayleigh number for isoviscous convection	1000	Schubert et al. (2001)
Viscosity parameters			
ϕ_C	Critical melt fraction	0.3	Scott and Kohlstedt (2006)
β	Arrhenius slope	0.0225 K^{-1}	$E = 366 \text{ kJ mol}^{-1}$, $T_{\text{ref}} = 1600 \text{ K}$ Hirth and Kohlstedt (2003)
α_n	Melt weakening exponent	30	Hirth and Kohlstedt (2003)
η_0	Reference viscosity	10^{19} Pa s	Lichtenberg et al. (2019b)
η_l	Liquid viscosity	10 Pa s	Giordano et al. (2008)
Core parameters			
$\rho_{\text{Fe},s}$	Solid iron density	7800 kg m^{-3}	Bryson et al. (2015)
$c_{p,c}$	Specific heat capacity	850 $\text{J kg}^{-1} \text{ K}^{-1}$	^a Bartels and Grove (1991)
L_c	Latent heat of fusion of core	$270 \times 10^3 \text{ J kg}^{-1}$	^a Ghosh and McSweeney (1998)
$T_{c,s}$	Fe–FeS solidus	1260 K	Buono and Walker (2011)
$X_{s,\text{eut}}$	Eutectic sulfur content	33 wt%	Buono and Walker (2011), $R = 300 \text{ km}$
α_c	Thermal expansivity	$9.2 \times 10^{-5} \text{ K}^{-1}$	^a Nimmo (2009)
k_c	Thermal conductivity	30 $\text{W m}^{-1} \text{ K}^{-1}$	^a Opeil et al. (2010)
η_c	Viscosity	0.01 Pa s	^a de Wijs et al. (1998)
λ	Magnetic diffusivity	$1.3 \text{ m}^2 \text{ s}^{-1}$	^a Weiss et al. (2010)
f_{ohm}	Fraction of energy flux dissipated ohmically	1	Christensen (2009)
c_u	Convective velocity constant	1.31	Aubert et al. (2009)
c_b	Magnetic field strength constant	0.23	Davies et al. (2022)
Radiogenic heating parameters			
$H_{\text{Al},0}$	Heating power of ^{26}Al at $t = 0$ Ma after CAI formation.	0.355 W kg^{-1}	^a Castillo-Rogez et al. (2009)
$f_{^{26}\text{Al}}$	$^{26}\text{Al}/^{27}\text{Al}$	5×10^{-5}	^a MacPherson et al. (1995)
X_{Al}	wt% Al in accreting material	1.4 wt%	^a Doyle et al. (2015)
$t_{1/2,\text{Al}}$	^{26}Al half life	0.717 Ma	^a Neumann et al. (2012)
$H_{\text{Fe},0}$	Heating power of ^{60}Fe at $t = 0$ Ma after CAI formation.	0.0366 W kg^{-1}	Ruedas (2017)
X_{Fe}	wt% Fe in accreting material	22.4 wt%	Lodders (2021)
$t_{1/2,\text{Fe}}$	^{60}Fe half life	2.62 Ma	Ruedas (2017)

^a References denote the that they were used in Dodds et al. (2021), but the original reference has been given here.

Here X_{Fe} and X_{Si} are the Fe–FeS and silicate fraction in wt% in the accreted material, L_c and L_m are the latent heats of fusion of Fe–FeS and silicate, $T_{c,l}$ and $T_{m,l}$ are the Fe–FeS and silicate liquidus, and $T_{c,s}$ and $T_{m,s}$ are the Fe–FeS and silicate solidus. The Fe–FeS and silicate melt fractions are both calculated using the linear liquidus approximation. The sulfur content of the Fe–FeS system is set as an input parameter. For planetesimals with eutectic Fe–FeS compositions, the temperature is held fixed once the planetesimal temperature reaches the Fe–FeS solidus, until all the Fe–FeS is melted. In this scenario, the time evolution of the Fe–FeS melt fraction, ϕ_{Fe} , is calculated by replacing the term on the left hand side of Eq. (3) by $\rho_{\text{ch}} X_{\text{Fe}} L_{\text{Fe}} \frac{\partial \phi_{\text{Fe}}}{\partial t}$ where $\rho_{\text{ch}} X_{\text{Fe}}$ is the density of Fe–FeS in the undifferentiated material.

Solid-state stagnant lid convection (Section 2.5.2) could begin prior to differentiation, as the body heats up. In this mode of convection, the stagnant lid is a conductive, immobile boundary layer at the surface

of the planetesimal with a thickness δ_0 (Eq. (7)) and the interior beneath the lid convects (Fig. 3). The interior is assumed to be isothermal, because pressure variation in the planetesimal is small enough for the adiabatic temperature gradient to be neglected. The interior temperature, T_i , evolves according to

$$\rho_{\text{ch}} c_{p,\text{ch}} V_i \frac{\partial T_i}{\partial t} = -F_{\text{lid}} A_{\text{lid}} + \rho_{\text{ch}} V_i H, \quad (6)$$

where $F_{\text{lid}} = -k_{\text{ch}} \frac{dT}{dr} \Big|_{r=R-\delta_0}$, V_i is the volume of the interior, and A_{lid}

is the surface area of the base of the stagnant lid (Solomatov, 1995). The stagnant lid continues to transport heat following Eq. (3), assuming equal abundances of radiogenic elements in the interior and the lid, and decreases in thickness as the planetesimal heats up. If eutectic Fe–FeS melting occurs while the planetesimal is convecting, the left hand side of Eq. (6) is replaced by $\rho_{\text{ch}} X_{\text{Fe}} L_{\text{Fe}} \frac{\partial \phi_{\text{Fe}}}{\partial t}$. We assume solid-state stagnant

lid convection can occur if δ_0 is less than 99% of the planetesimal radius, R .

Once the silicate melt fraction, ϕ , reaches the critical melt fraction, ϕ_c , there is a steep drop in the silicate viscosity and differentiation proceeds via rain-out, where the more dense, molten Fe–FeS settles through the less dense, low-viscosity silicate via Stokes settling. This process is rapid (10^4 years for mm size droplets, see S5) and can be approximated as instantaneous. Differentiation via percolation prior to $\phi = \phi_c$ is neglected due to the uncertainties in the timescales for this process (see Section 4 and Section S5). Due to the small internal pressure gradient, the body is almost isothermal and, for simplicity, the entire planetesimal is assumed to differentiate at the same time. Our model assumes all Fe–FeS is fully molten before differentiation and that the core is initially liquid. In order to satisfy this assumption, the liquidus temperature for the initial core sulfur content of the Fe–FeS must be less than or equal to the temperature of ϕ_c . This limits the range of initial core sulfur contents (see Section 4.4.1).

At the point of differentiation, the body is assumed to instantly form an Fe–FeS core, with a radius half that of the body, $r_c = \frac{R}{2}$, with an overlying silicate mantle (Fig. 3). The core and the mantle are isothermal at the temperature of the critical melt fraction, T_{ϕ_c} . All iron is assumed to partition into the core and all aluminium is assumed to stay in the mantle. This increases the concentration of ^{26}Al in the mantle and ^{60}Fe in the core compared to initial conditions. The initial core sulfur content, $X_{S,0}$, is set by an input parameter and is the same as the sulfur content in Fe–FeS in the undifferentiated planetesimal.

2.5. After differentiation

2.5.1. Crust

The presence of a crust is simplified to the fixed surface temperature boundary condition. Only the surface node does not become hot enough to differentiate. Therefore, the thickness of any porous regolith is below the resolution of this model and has been neglected (Section 4.2).

2.5.2. Mantle

The mantle transports heat either via conduction or stagnant lid convection. In stagnant lid convection, the mantle is assumed to have an isothermal, convecting interior with a conductive boundary layer ('stagnant lid') below the surface and another above the CMB (Fig. 3). In our adopted parametrisation, the stagnant lid thickness includes the thin mobile boundary layer at the base of the lid (see section S1.2.2). We assume an empirically determined expression for stagnant lid thickness, δ_0 , for a system with internal heating, heat flux at the top and bottom boundaries, temperature-dependent viscosity, and free-slip boundary conditions (Deschamps and Vilella, 2021)

$$\delta_0 = a_{lid}(R - r_c)f_{rh}^{1.21} Ra^{-0.27}, \quad (7)$$

where a_{lid} is an empirically determined constant (0.633 for $Ur < 1$ and 0.667 for $Ur > 1$). Here Ur is the Urey ratio, which is the ratio of the power of internal heating, Q_H , to the power of cooling from the surface, Q_S ,

$$Ur = \frac{Q_H}{Q_S} = \frac{\rho_m V_m H_{Al}}{F_s A_s}, \quad (8)$$

where V_m is the volume of the mantle, F_s and A_s are the surface heat flux and surface area, respectively. In Eq. (7), the Rayleigh number, Ra , is calculated using the interior mantle temperature

$$Ra = \frac{\rho_m \alpha_m g(R) \Delta T (R - r_c)^3}{\kappa_m \eta}. \quad (9)$$

Here α_m , ρ_m , and κ_m are the thermal expansivity, density, and diffusivity of the mantle respectively, $\Delta T = T_m - T_s$ is the difference between the interior convective temperature, T_m , and the surface temperature T_s , $g(R)$ is the gravitational field strength at radius $r = R$, and the viscosity is calculated for the convecting interior temperature $\eta = \eta(T_m)$. In this

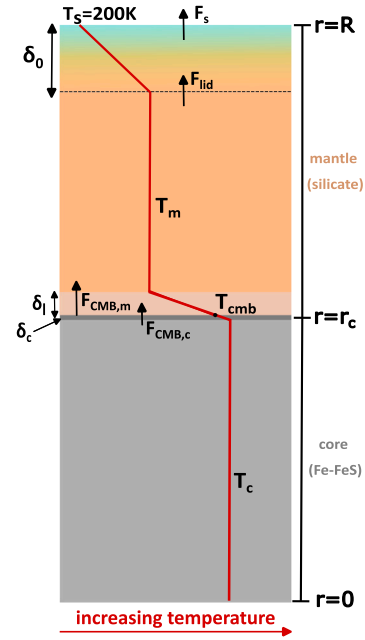


Fig. 3. Schematic depicting our model setup for a convecting silicate mantle and a convecting Fe–FeS core. The core and mantle are two coupled reservoirs. The crust is approximated by the fixed surface temperature, $T_s = 200\text{ K}$. The red line is the temperature profile in the planetesimal and temperature increases to the right. In this diagram, the mantle is convecting in the stagnant lid regime: the interior is isothermal and there are conductive boundary layers at the CMB, δ_l , and the surface, δ_0 . The black dashed line denotes the base of the stagnant lid. The core has a thermal boundary layer at the CMB, δ_c . When the mantle and core are conductive, there is a temperature gradient throughout each layer instead. The balance of CMB heat fluxes ($F_{CMB,m} = F_{CMB,c}$) is used to calculate the CMB temperature T_{CMB} . The meaning of the symbols is given in Sections 2.5.2 and 2.5.3. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

model, we adopt the middle value of silicate diffusivity, $9 \times 10^{-7} \text{ m}^2 \text{ s}^{-1}$, used in previous work (6, 9 and $12 \times 10^{-7} \text{ m}^2 \text{ s}^{-1}$, Bryson et al., 2019a), which corresponds to an ordinary chondrite composition. Eq. (7) was derived neglecting melt weakening, therefore $f_{rh} = -\frac{d\eta(T_m)/dT}{-\eta(T_m)} \Delta T = \beta(T_m - T_s)$ based on the first piece of the viscosity law (Eq. (1a)).

The thickness of the CMB boundary layer at the base of the mantle, δ_l , is difficult to parametrise because it could be affected by downwelling material from the upper boundary layer interfering with its thermal structure (Thiriet et al., 2019). δ_l has been approximated in previous planetesimal models in two ways. First, δ_l has been assumed to be equal thickness to the mobile layer in the stagnant lid at the surface (Bryson et al., 2019a). Second, δ_l has been calculated with the same parametrisation for lid thickness as the top boundary layer, but using $\Delta T = T_{CMB} - T_m$ rather than $\Delta T = T_m - T_s$ (Dodds et al., 2021). We have chosen to implement the CMB boundary layer scaling following Eq. (13) in Thiriet et al. (2019), which has been benchmarked against 2D and 3D mantle convection simulations

$$\delta_l = (R - \delta_0 - r_c) \left(\frac{Ra_{bl,crit}}{Ra_{bl}} \right)^{\frac{1}{3}}. \quad (10)$$

Here Ra_{bl} is the Rayleigh number in the boundary layer and $Ra_{bl,crit}$ is the boundary layer critical Rayleigh number. Using equations 14 and 16 in Thiriet et al. (2019) to substitute for Ra_{bl} and $Ra_{bl,crit}$ gives

$$\delta_l = 0.65(R - r_c)^{0.21} \left(\frac{\eta(T_{bl})}{(T_{CMB} - T_m)g_c} \right)^{\frac{1}{3}} \left(\frac{\eta(T_m)}{(T_m - T_s)g(R)} \right)^{-0.07} \times \left(\frac{\kappa_m}{\alpha_m \rho_m} \right)^{0.26}, \quad (11)$$

where T_{CMB} is the CMB temperature, and g_c is the gravitational field strength at the CMB. The temperature profile through the lower boundary layer is conductive and the temperature in the midpoint of the layer, $T_{bl} = \frac{T_m + T_{\text{CMB}}}{2}$, is used to calculate Ra_{bl} . These boundary layer thicknesses control the heat flux from the CMB into the mantle during convection, $F_{\text{CMB,m}}^{\text{conv}}$

$$F_{\text{CMB,m}}^{\text{conv}} = \frac{-k_m(T_m - T_{\text{CMB}})}{\delta_l} \quad (12)$$

and to the surface, F_s

$$F_s = \frac{-k_m(T_s - T_m)}{\delta_0}. \quad (13)$$

Altogether, the thermal evolution of the convecting portion of the mantle is given by

$$\rho_m c_{p,\text{eff}} V_m \frac{\partial T_m}{\partial t} = -F_{\text{lid}} A_{\text{lid}} + F_{\text{CMB,m}}^{\text{conv}} A_{\text{CMB}} + \rho_m V_m H_{\text{Al}}. \quad (14)$$

Here, V_m is the volume of the convecting region; the silicate modified specific heat capacity, $c_{p,\text{eff}}$, is calculated at T_m ; A_{lid} and A_{CMB} are the surface areas at the base of the stagnant lid and CMB, respectively; and $F_{\text{lid}} = -k \frac{dT}{dr} \Big|_{r=R-\delta_0}$. The silicate modified specific heat capacity, $c_{p,\text{eff}}$, accounts for melting and solidification of silicate.

$$c_{p,\text{eff}} = \begin{cases} c_{p,m} & T_m < T_{m,s} \\ c_{p,m} \left(1 + \frac{L}{c_{p,m}(T_{m,l} - T_{m,s})} \right) & T_{m,s} < T_m < T_{m,l}. \end{cases} \quad (15)$$

Due to efficient heat loss by convection in the model, the mantle is never hotter than its liquidus temperature.

Heat is transported by conduction in the stagnant lid and the CMB boundary layer. As the mantle cools, both these layers thicken until the combined boundary layer thickness equal the thickness of the mantle, i.e., $\delta_0 + \delta_l = (R - r_c)$. From this point, mantle convection ceases and the entire mantle cools conductively, such that the thermal evolution is dictated by

$$\rho_m c_{p,\text{eff}} \frac{\partial T}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(k_m r^2 \frac{\partial T}{\partial r} \right) + \rho_m H_{\text{Al}}. \quad (16)$$

In the conductive regime, the heat flux across the CMB into the mantle is given by

$$F_{\text{CMB,m}}^{\text{cond}} = -k_m \frac{dT}{dr} \Big|_{r=r_c^+} = -k_m \frac{T_{\text{CMB}+1}^m - T_{\text{CMB}}}{\Delta r}, \quad (17)$$

where $T_{\text{CMB}+1}^m$ and r_c^+ are the temperature and radius one node above the CMB, respectively, and Δr is the length of one grid cell in the simulation. T_{CMB} is determined by balancing the heat fluxes across the CMB ($F_{\text{CMB,m}} = F_{\text{CMB,c}}$).

2.5.3. Core

The thermal evolution of the core is coupled to the mantle by F_{CMB} . Due to the low pressure in planetesimal cores, the adiabatic temperature gradient is negligible ($T(r = r_c) = 0.995T(r = 0)$ for a 250 km core). Therefore, we assume the core is isothermal when convecting and that the criteria for core convection is $F_{\text{CMB}} > 0$. At the beginning of the thermal evolution, the core and mantle are isothermal. If the abundance of ^{60}Fe in the core is low, the mantle experiences stronger radiogenic heating (from ^{26}Al) than the core. This increases the mantle temperature relative to the core and heat flows from the mantle to the core ($F_{\text{CMB}} < 0$). The top of the core becomes thermally stratified, which inhibits core convection. While the core is thermally stratified, heat is transferred conductively as described by

$$\rho_c c_{p,c} \frac{\partial T}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(k_c r^2 \frac{\partial T}{\partial r} \right) + \rho_m H_{\text{Fe}}, \quad (18)$$

where $c_{p,c}$ is core specific heat capacity, ρ_c is core density, k_c is core thermal conductivity, and

$H_{\text{Fe}} = H_{\text{Fe},0} f_{^{60}\text{Fe}} 0.01 X_{\text{Fe}} e^{-\frac{t}{t_{1/2, \text{Fe}}}}$ is heating from ^{60}Fe . An effective specific heat capacity is not used because the core begins molten and

core solidification causes core convection so is treated separately (see Section 2.5.4). The boundary conditions are a fixed CMB temperature using the temperature determined at the previous timestep (which is a reasonable approximation given the small timestep) and no temperature gradient at the centre of the body, i.e., $\frac{dT}{dr} \Big|_{r=0} = 0$. The conductive heat flux from the core to the CMB is given by

$$F_{\text{CMB,c}}^{\text{cond}} = -k_c \frac{dT}{dr} \Big|_{r=r_c^-} = -k_c \frac{T_{\text{CMB}} - T_{\text{CMB}-1}^c}{\Delta r}, \quad (19)$$

where $T_{\text{CMB}-1}^c$ and r_c^- are the temperature and radius one node below the CMB, respectively. Once the CMB temperature is below the core temperature, either due to mantle cooling or core heating by ^{60}Fe , the top of the core begins to cool ($F_{\text{CMB}} > 0$) and thermal stratification begins to erode (Fig. 4). Positive F_{CMB} leads to the onset of convection in the upper portion of the core that is hotter than the CMB. As such, we assume this material convectively mixes down to the level of neutral buoyancy (the depth where core temperature is equal to the CMB temperature), d_{conv} . This forms an isothermal convecting layer, with temperature T_c , above a conductive region. This convective mixing continues until core thermal stratification is removed and the entire core is isothermal and convecting.

The temperature of the convecting portion of the core evolves according to

$$\rho_c c_{p,c} V_{\text{conv}} \frac{\partial T_c}{\partial t} = -F_{\text{CMB,c}}^{\text{conv}} A_{\text{CMB}} + \rho_c V_{\text{conv}} H_{\text{Fe}} + 4\pi R_{\text{conv}}^2 F_{R_{\text{conv}}}, \quad (20)$$

where $R_{\text{conv}} = r_c - d_{\text{conv}}$, V_{conv} is the volume of the convecting portion of the core, and $A_{\text{CMB}} = 4\pi r_c^2$ is the CMB surface area (Dodds et al., 2021). While thermal stratification is being eroded, there is a heat flux into the convecting region from the conductive core beneath, $F_{R_{\text{conv}}} = -k_c \frac{\partial T}{\partial r} \Big|_{r=R_{\text{conv}}}$, and the final term in Eq. (20) is non-zero. When the core is convecting, a boundary layer, δ_c , forms at the top of the core. Although core rotation has a known effect on the convective boundary layer scaling law (Cheng et al., 2015), the combined effect of rotation, magnetic field generation and spherical geometry on heat transfer is unclear. Therefore, for simplicity, we assume the thickness of this boundary layer can be described by the non-rotating scaling (Schubert et al., 2001; Dodds et al., 2021)

$$\delta_c = \left(\frac{\kappa_c \eta_c Ra_{c,iso}}{\rho_c \alpha_c g_c (T_c - T_{\text{CMB}})} \right)^{\frac{1}{3}}, \quad (21)$$

where η_c and κ_c are the viscosity and thermal diffusivity of the core, respectively, and $Ra_{c,iso} = 1000$ (Schubert et al., 2001) is the critical Rayleigh number for isoviscous convection. The corresponding CMB heat flux is given by

$$F_{\text{CMB,c}}^{\text{conv}} = -k_c \frac{T_{\text{CMB}} - T_c}{\delta_c}. \quad (22)$$

2.5.4. Core solidification

Planetesimal CMBs are at lower pressures compared to Earth, so are likely to solidify inwards (Williams, 2009; Dodds et al., 2025). The mechanism of this inward solidification and its implications for dynamo generation are still being investigated, but could include formation of iron snow (Rückriemen et al., 2015; Davies and Pommier, 2018) formation of dendrites (Scheinberg et al., 2016) or viscous delamination of solid iron from the CMB (Neufeld et al., 2019). Previous models for mantled planetesimals that incorporate convection either ended before core solidification (Elkins-Tanton et al., 2011; Sterenberg and Crowley, 2012; Dodds et al., 2021) or used eutectic core solidification to estimate the time period over which a compositional dynamo could be possible (Bryson et al., 2019a). To avoid the specificity of a particular core solidification model, we have chosen to use a parametrised model that captures two key changes in an inward solidifying core that will affect dynamo generation: (i) the decrease of convective lengthscale; (ii) the increase in sulfur content of the bulk liquid, assuming perfect

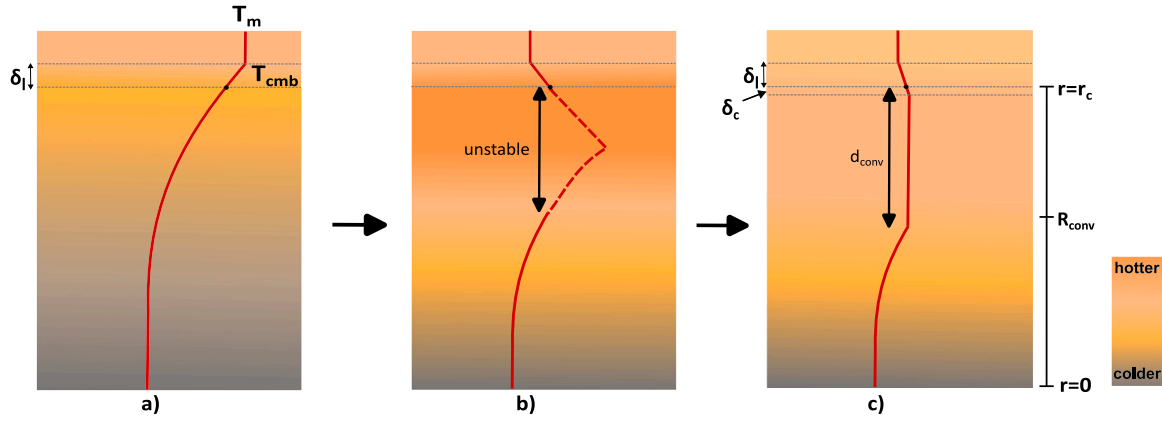


Fig. 4. Schematic of the erosion of core thermal stratification by convective mixing of the unstable layer at the top of the core. The red lines indicate temperature profiles and temperature increases to the right. The dashed red line indicates the portion of the core that is unstable to convection. The top of the figure is the base of the convecting mantle above the CMB boundary layer in the mantle, δ_i , and CMB boundary layer in the core, δ_c . Time proceeds from left to right (a–c). Dashed lines indicate the mantle and core CMB boundary layers. The core CMB boundary layer (lower dashed layer) is only present when the core is convecting. Core thermal stratification is eroded either by mantle cooling (shifts the mantle temperature profile to the left relative to that of the core) or heating by ^{60}Fe in the core (shifts the core temperature profile to the right relative to the mantle). All symbols are defined in Section 2.5.3. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

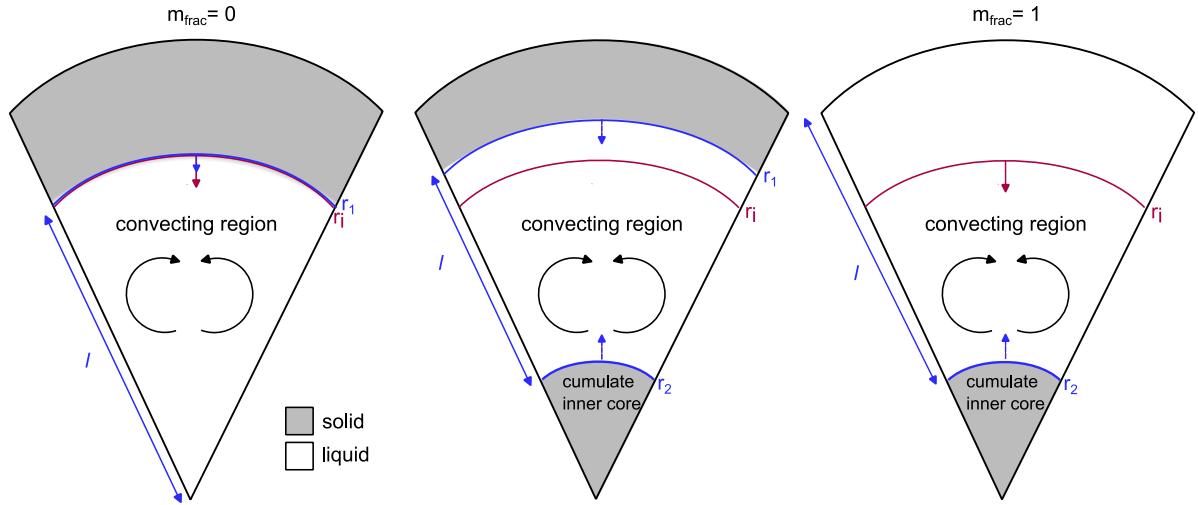


Fig. 5. Schematic showing the geometry for core solidification. The amount of solidifying material is parametrised by r_i (magenta line) and the lengthscale for convection is given by $l = r_1 - r_2$. To account for the uncertainty in the mechanism of planetesimal core solidification we consider two endmember geometries (the middle scenario in the figure also depicts an intermediate geometry). In one endmember, $m_{\text{frac}} = 0$, the stable, solid portion of the core grows from the CMB inwards. In the other endmember, $m_{\text{frac}} = 1$, all solidified iron falls without remelting and forms a cumulate inner core. For $m_{\text{frac}} = 0$, the convective lengthscale decreases the slowest as the core solidifies, and for $m_{\text{frac}} = 1$, the convective lengthscale decreases the fastest. Due to the uncertainty in the mechanism for planetesimal core solidification, we do not prescribe how convection is driven in each scenario and just focus on the change in lengthscale. In both endmembers, the solid fraction in the solidified region is assumed to be 100%. For more details and discussion see Sections 2.5.4 and 6.1.

partitioning of sulfur into the liquid (Goldstein et al., 2009). This enables us to calculate a core solidification timescale and magnetic field strengths during sub-eutectic core solidification.

Core solidification is parametrised by a time-varying, inward moving boundary r_i , $\frac{dr_i}{dt} < 0$. The total material solidified is given by $M_{\text{solid}} = \frac{4}{3}\pi\rho_c(r_c^3 - r_i^3)$. This solidified material can decrease the convective lengthscale of the core either due to formation of a solidified layer at the top of the core and/or due to the formation of a solid cumulate inner core formed by solidified material falling from r_i without remelting to the centre of the core (Scheinberg et al., 2016; Neufeld et al., 2019). To capture both of these possibilities, we vary the proportion of total solidified mass in the innermost core for a given time and r_i , M_{ic} , using a constant input parameter, $m_{\text{frac}} = \frac{M_{\text{ic}}}{M_{\text{solid}}}$ (see Fig. 5). Using $f = \frac{r_i}{r_c}$ and conservation of mass, the resulting radii of the base of the solidified outer shell, r_1 , and the solid innermost core, r_2 , are given by

$$r_1 = r_c(m_{\text{frac}}(1 - f^3) + f^3)^{\frac{1}{3}}, \quad (23)$$

and

$$r_2 = r_c m_{\text{frac}}^{\frac{1}{3}} (1 - f^3)^{\frac{1}{3}}. \quad (24)$$

We show results for the two endmembers to explore the plausible range of geometric lengthscales: solidified outer layer only, $m_{\text{frac}} = 0$; and solid inner core only, $m_{\text{frac}} = 1$. Current dynamo theories suggest the convective lengthscale is some fixed fraction of this geometric lengthscale (Davidson, 2013; Aubert et al., 2017), but in this model we assume these lengthscales are the same (see Section 6.1). Our model assumes the solidified portions of the core are completely solid and not a mushy layer, because self-consistently calculating a solid fraction is overly complex given the uncertainties in core material properties (see Section 6.2).

The onset of solidification occurs when the temperature at the top of the core drops beneath the liquidus. Because compositional convection in the core will efficiently homogenise the temperature in the liquid

core, the thermal conductivity of the solid portion is high, and the adiabatic gradient is minimal, the entire core is assumed to be isothermal at temperature T_c during solidification. During solidification, the heat flux across the CMB is balanced by secular cooling, radiogenic heating, and release of latent heat. Energy released due to changes in gravitational potential during solidification has a negligible effect on the time of core solidification (see Section S3.1) and contributions due to planetary contraction are also negligible. The resulting thermal evolution of the core is expressed as

$$F_{\text{CMB}} A_{\text{CMB}} = M_c H_{\text{Fe}} - M_c c_{p,c} \frac{dT_c}{dt} - 4\pi r_i^2 \rho_c L_c \frac{dr_i}{dt}, \quad (25)$$

where L_c is the latent heat from solidification of iron and M_c is the total mass of the core (Nimmo, 2007). For an isothermal solidifying core, the rate of change of inner core boundary is given by

$$\frac{dr_i}{dt} = - \frac{1}{\rho_c g_c \frac{dT_{c,l}}{dP}} \frac{dT_c}{dt}, \quad (26)$$

which is adapted to account for inward solidification and no core adiabat (Gubbins et al., 2003; Nimmo, 2009; Davies and Pommier, 2018). The sign of the pressure gradient of the liquidus, $\frac{dT_{c,l}}{dP}$, determines whether $\frac{dr_i}{dt}$ is positive (outward solidification) or negative (inward solidification). As the core solidifies, we assume as an upper limit that sulfur partitions completely into the liquid portion of the core (Goldstein et al., 2009; Nichols et al., 2021), is homogeneously distributed, and this partitioning has a negligible effect on the total volume of the core. This enriches the liquid inner core relative to the initial sulfur content, $X_{S,0}$ according to (Nichols et al., 2021)

$$X_S = \frac{r_c^3}{r_i^3} X_{S,0} = \frac{1}{f^3} X_{S,0}. \quad (27)$$

Once the core sulfur content reaches the eutectic (33 wt% S), the remaining liquid inner core will solidify as FeS. During eutectic solidification, there is no temperature change ($T_c = 1260$ K) and the fraction of core solidified is determined by the removal of latent heat, as given by

$$\frac{dr_i}{dt} = - \frac{F_{\text{CMB}} A_{\text{CMB}} - M_c H}{4\pi r_i^2 L_c \rho_c}. \quad (28)$$

Once the whole core has solidified ($r_i < 0.001$) the model run ends.

This model uses the Fe–FeS liquidus from Buono and Walker (2011), which depends on pressure and bulk sulfur content,

$$T_{c,l}(X_{S,mol}, P) = A(P)X_{S,mol}^4 + B(P)X_{S,mol}^3 + C(P)X_{S,mol}^2 + D(P)X_{S,mol} + E(P), \quad (29)$$

where the pressure, P , is in GPa and $X_{S,mol} = \frac{X_S}{100 - X_S} \frac{M_{r,Fe}}{M_{r,S}}$ is the mole fraction of FeS in the core, $M_{r,i}$ are the molar masses of sulfur (32.07 amu) and iron (55.84 amu), respectively, and X_S is the core sulfur content in wt%. The pressure dependent coefficients are given by (Buono and Walker, 2011)

$$\begin{aligned} A &= -2.4724P^4 + 28.025P^3 + 9.1404P^2 + 581.71P + 3394.8, \\ B &= 1.7978P^4 - 6.7881P^3 - 197.69P^2 - 271.69P - 8219.5, \\ C &= -0.1702P^4 - 9.3959P^3 + 163.53P^2 - 319.35P + 5698.6, \\ D &= -0.2308P^4 + 7.1P^3 - 64.118P^2 + 105.98P - 1621.9, \\ E &= 0.2302P^4 - 5.3688P^3 + 38.124P^2 - 46.681P + 1813.8. \end{aligned} \quad (30)$$

This expression for the Fe–FeS liquidus is valid for sub-eutectic sulfur concentrations and pressures < 10 GPa. The pressure at a radius r in the core (assuming an incompressible core and mantle) is given by

$$P_c = \frac{2\pi G}{3} \left[r_c^2 (\rho_c^2 - \rho_m^2) + R^2 \rho_m^2 + 2\rho_m (\rho_c - \rho_m) r_c^2 \left(1 - \frac{r_c}{R} \right) \right]. \quad (31)$$

For a $\mathcal{O}(100)$ km radius body, the difference in pressure between the centre and the CMB is $\mathcal{O}(10^{-3})$ GPa; therefore, the central pressure is always used in the expression for the liquidus. The sulfur content used

to calculate the liquidus and pressure gradient of the liquidus is updated as the core solidifies.

2.6. Magnetic field generation

2.6.1. Magnetic Reynolds number

The magnetic Reynolds number, Re_m , determines whether flow in a planetesimal core is vigorous enough to generate a magnetic field. This dimensionless number characterises the balance between magnetic induction and diffusion in the fluid and is given by

$$Re_m = \frac{ul}{\lambda}, \quad (32)$$

where u and l are the characteristic velocity and lengthscale of the flow and $\lambda = 1.3 \text{ m}^2 \text{ s}^{-1}$ (Weiss et al., 2010) is the magnetic diffusivity. If Re_m is greater than a critical value, a magnetic field can be generated. The minimum analytical critical value is 10 and numerical dynamo simulations suggest a critical value between 40–100 (Christensen and Aubert, 2006). To account for this uncertainty, we calculate three sets of dynamo onset and cessation times with critical Re_m values of 10, 40, and 100. λ depends on pressure, temperature and composition, but the appropriate value for a given set of conditions is uncertain (Pozzo et al., 2013; Konôpková et al., 2016; Tassin et al., 2021). In addition, measurements are limited to Earth-like conditions, i.e., much higher pressures and temperatures than in planetesimals. Therefore, we take λ to be a constant between simulations and uncertainties in this parameter are considered by adopting multiple critical Re_m values. l is assumed to be the length over which convection can occur, $l = r_i - R_{\text{conv}}$, which accounts for the possible existence of a stratified layer. In this model, we use the numerical scaling from Aubert et al. (2009) for the characteristic velocity, u ,

$$u = c_u p^{0.42} \Omega l. \quad (33)$$

$c_u = 1.31$ is a constant (Aubert et al., 2009), Ω is the rotation rate of the planetesimal, and p is the convective power per unit volume. To enable comparison with previous work, we adopt a nominal rotation period of 10 h ($\Omega = 1.7 \times 10^{-4} \text{ s}^{-1}$), which is a typical value for rotation periods of asteroids at the present day (Bryson et al., 2019a; Dodds et al., 2021). We use this characteristic velocity scaling law because it is not singular in the absence of an inner core so can be applied to inward solidification where a solid inner core is not present. Additionally, this law has been shown to agree with subsequent analytical derivations of dynamo scaling laws (Davidson, 2013). This also aligns with the work of Christensen (2015) who used this scaling law when determining the dimensional magnetic field strength of Ganymede.

2.6.2. Magnetic field strength

We have determined that the Magnetic-Archimedean-Coriolis (MAC) force balance dominates in planetesimal cores (Table S1). For a core in MAC force balance, the magnetic dipole field at the CMB can be estimated as

$$B_{\text{CMB}}^{\text{dip}} = c_B f_{\text{ohm}}^{\frac{1}{2}} p^{0.31} (\rho_c \mu_0)^{\frac{1}{2}} \Omega l. \quad (34)$$

Here $f_{\text{ohm}} = 1$ (Christensen, 2009) is the fraction of energy dissipated ohmically in the core, $\mu_0 = 4\pi \times 10^{-7} \text{ NA}^{-2}$ is the vacuum permeability and $c_B = 0.23$ is the median value of the scaling constant for CMB dipole field strength across the simulations assessed in Davies et al. (2022). The field strength decays from the CMB to the surface according to $B_{\text{surf}} = \left(\frac{r_c}{R} \right)^3 B_{\text{CMB}}^{\text{dip}}$. The exponents of the scaling law agree within error of the field strength scaling in Aubert et al. (2009), so this is consistent with the chosen characteristic velocity scaling. Additionally, the MAC force balance has been shown to best fit a large range of simulations of the geodynamo (Davies et al., 2022) and scaling analysis suggests planetesimal dynamos are in a similar regime (see Table S1).

2.6.3. Convective power and buoyancy flux

The scaling laws for both u and B require a convective power per unit volume, p . This can be calculated using $p = \gamma Ra_Q$, where $\gamma = 3/5$ (Equation 18 in Aubert et al., 2009, for no inner shell and $f_i = 0$). Ra_Q is the flux based Rayleigh number given by

$$Ra_Q = \frac{g(r_i)Q_b}{4\pi\rho_c\Omega^3l^4}, \quad (35)$$

for a gravitational acceleration at the top of the convecting region, $g(r_i)$, and buoyancy flux, Q_b . The buoyancy flux combines the two possible contributions: thermal and compositional. Adapting from Buffett et al. (1996) (see Appendix A) for an inwardly solidifying core with $\frac{dr_i}{dt} < 0$, the buoyancy flux at the liquid inner core boundary r_i is given by

$$Q_b = 4\pi r_i^2 \left[\frac{\alpha_c k_c}{c_{p,c}} \left(-\frac{dT}{dr} \right)_{r_i} - \frac{\alpha_c g(r_i)}{c_{p,c}} T(r_i) \right] - \left(\Delta\rho + \frac{\alpha_c \rho_c L_c}{c_{p,c}} \right) \frac{dr_i}{dt}, \quad (36)$$

where α_c is the core thermal expansivity. The first term in this equation represents the thermal buoyancy contribution from the superadiabatic heat flux at the upper boundary of the convecting region (i.e., the heat flux available to drive convection), assuming all the heat is advected by the flow. Although we have neglected the adiabatic gradient in the temperature structure of the convecting core, we retain the adiabatic heat flux in the expression for the buoyancy flux for consistency with previous literature (e.g. Lister, 2003; Rückriemen et al., 2015; Dodds et al., 2021). In our simulations, Re_m becomes subcritical before the CMB heat flux becomes subadiabatic and the adiabatic gradient is an order of magnitude smaller than the CMB heat flux when Re_m is supercritical. Therefore, including the adiabatic gradient will have minimal effect on the timings of dynamo generation.

The second term in Eq. (36) is the compositional density difference and the latent heat release from the solidifying core. $\Delta\rho = \rho_{Fe,s} - \rho_l(X_s)$ is the density difference between the solidified iron $\rho_{Fe,s} = 7800 \text{ kg m}^{-3}$ (Bryson et al., 2015) and the liquid inner core, ρ_l , which is calculated using the relationship from (Morard et al., 2018)

$$\rho_l = (-3108X_{S,at}^2 - 5176X_{S,at} + 6950)(1 + \alpha_c(1900 - 1600)), \quad (37)$$

where $X_{S,at} = \left(1 + \frac{1-0.01X_s}{0.01X_s} \frac{M_{r,s}}{M_{r,Fe}}\right)^{-1}$ is atom % S and the core is assumed to only contain Fe and FeS. In Eq. (37), the term in the first parentheses is the density from Morard et al. (2018) and the term in the second parentheses corrects for the fact the expression from Morard et al. (2018) was derived for ambient pressure at a temperature of 1900 K, whereas peak core temperatures are ~ 1600 K in our model. The change in core density due to core cooling below 1600 K to the eutectic (a further 3% difference in density) was neglected in order to simplify the model. Although we explore geometries for two possible endmembers for core solidification (Fig. 5), we use the same density difference for both, because it is the correct order of magnitude and $\Delta\rho$ is raised to a fractional power in both Eqs. (33) and (34).

Prior to core solidification, Eqs. (35) and (36) are evaluated at the CMB ($r_i = r_c$) and the second term in Eq. (36) is zero. As the core solidifies inwards, these equations are evaluated at the liquid inner core boundary, r_i , which is the boundary of the convecting region. Once the eutectic composition is reached, the second term in Eq. (36) is no longer calculated, because a compositional density difference is no longer generated by solidification. Combining thermal and compositional buoyancy flux contributions enables both drivers of convection to be considered simultaneously at all timesteps.

2.7. Numerical implementation

Our model is 1D and spherically symmetric. The one spatial dimension is radius, r , which runs from $r = 0$ at the centre of the planetesimal to $r = R$ at the surface. The model is run on a grid with

fixed node spacing of $\Delta r = 500 \text{ m}$ following Bryson et al. (2019a) with the first node at the centre of the planetesimal and the last at the surface. The temperature change of convecting regions was calculated using the forward Euler method. The temperature in the conductive portion was calculated using matrix methods with a forward in time, centred in space (FTCS) stencil (see S6). The core conductive timescale, $\tau_{c,cond} = \frac{(R_c)^2}{\kappa_c}$, is a factor of ten shorter than the mantle conductive timescale. Therefore, the timestep was fixed to $dt = 0.075\tau_{c,cond}$ in order to resolve conduction in the core and mantle and ensure stability of the FTCS scheme, which is stable for $dt \leq \frac{(R_c)^2}{2\kappa_c}$. To test the gridsize and timestep, four simulations were run for a 300 km body: one using the model gridsize and timestep; one for half the gridsize; one for two thirds the timestep; and one for one third the timestep. The results of the model were independent of the choice of timestep and gridsize (Section S6.1).

2.8. Parameter values

The list of parameters used in the model are given in Table 1. The viscosity parameters are poorly constrained: the values here are the median value in a wide range (explored in more detail in Sanderson et al., 2024). The range of possible initial core sulfur contents, $X_{S,0}$, primordial $^{60}\text{Fe}/^{56}\text{Fe}$, planetesimal radii, and accretion times are shown in Table 2. The maximum $X_{S,0}$ is assumed to be the eutectic composition and the minimum $X_{S,0}$ is based on the highest liquidus temperature for which all the Fe–FeS will be molten before differentiation for $\phi_C = 0.3$ and $R = 300 \text{ km}$. The eutectic sulfur content varies with pressure and was estimated as 33 wt% by finding the intersection of the liquidus with the eutectic temperature of 1260 K (Buono and Walker, 2011) for a 300 km radius planetesimal. Due to its presumed low concentration, previous studies have neglected radiogenic heating from ^{60}Fe . However, recent studies suggest the primordial $^{60}\text{Fe}/^{56}\text{Fe}$ could be as high as 6×10^{-7} (Cook et al., 2021). To incorporate this possible range, we adopt values from 0 to 6×10^{-7} . The minimum planetesimal radius is based on the lower limit for compositional dynamo generation (Nimmo, 2009), while the upper limit is approximately the radius of Ceres (470 km Russell et al., 2016), the largest asteroid surviving today. Planetesimal accretion times affect the strength of radiogenic heating and must be within 2.5 Ma after CAI formation for there to be sufficient ^{26}Al for full planetesimal differentiation (Neumann et al., 2012). Accretion earlier than 1.1 Ma after CAI formation reconciles best with our choice to neglect silicate melt migration (Monnereau et al., 2023, see Section 4).

3. Example run

Results of an example run for a 500 km body that accreted 0.8 Ma after CAI formation with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$ and $X_{S,0} = 29.85 \text{ wt\%}$ are shown in Figs. 6–9. The planetesimal radius and accretion time were chosen to enable comparison with the instantaneous accretion model (Case 1) from Dodds et al. (2021). The $X_{S,0}$ value is the median value for the range of $X_{S,0}$ that can be used in our model. Following a similar argument, we chose to use $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$ to produce a representative simulation. This ^{60}Fe value is higher than that used in previous models ($^{60}\text{Fe}/^{56}\text{Fe} = 0$; Bryson et al., 2019a; Dodds et al., 2021), but is on the lower end of recently measured primordial $^{60}\text{Fe}/^{56}\text{Fe}$ values, which range from 10^{-8} to 6×10^{-7} (Cook et al., 2021). All fixed parameters are given in Table 1.

The thermal profile for this 500 km radius planetesimal is shown in Fig. 6. The planetesimal reaches its critical melt fraction, ϕ_C , and differentiates at 1520 K, 1.2 Ma after CAI formation¹ (0.4 Ma after accretion). Once the planetesimal differentiates, the combined stagnant

¹ The time resolution of this description is limited by the frequency at which model output is saved. Output is saved every 0.01 Ma prior to differentiation and every 0.1 Ma after differentiation. All times given are representative of the

Table 2

Computational parameters and variable parameters for model runs. The choice of variable parameters is explained in Section 2.8. Accretion times are discussed further in Section 4.

Symbol	Meaning	Value	Reference (if relevant)
Computational parameters			
Δr	Cell spacing	500 m	Bryson et al. (2019a)
dt	Timestep	$0.075 \frac{(\Delta r)^2}{\kappa_c}$ s	
Variable parameters			
R	Planetesimal radius	100–500 km	
$X_{s,0}$	Initial core sulfur content	26.7–33 wt%	
$f_{^{60}\text{Fe}}$	$^{60}\text{Fe}/^{56}\text{Fe}$	$0-6 \times 10^{-7}$	Dodds et al. (2021) Cook et al. (2021)
t_{acc}	Accretion time	<2.5 Ma after CAI formation	Neumann et al. (2012)

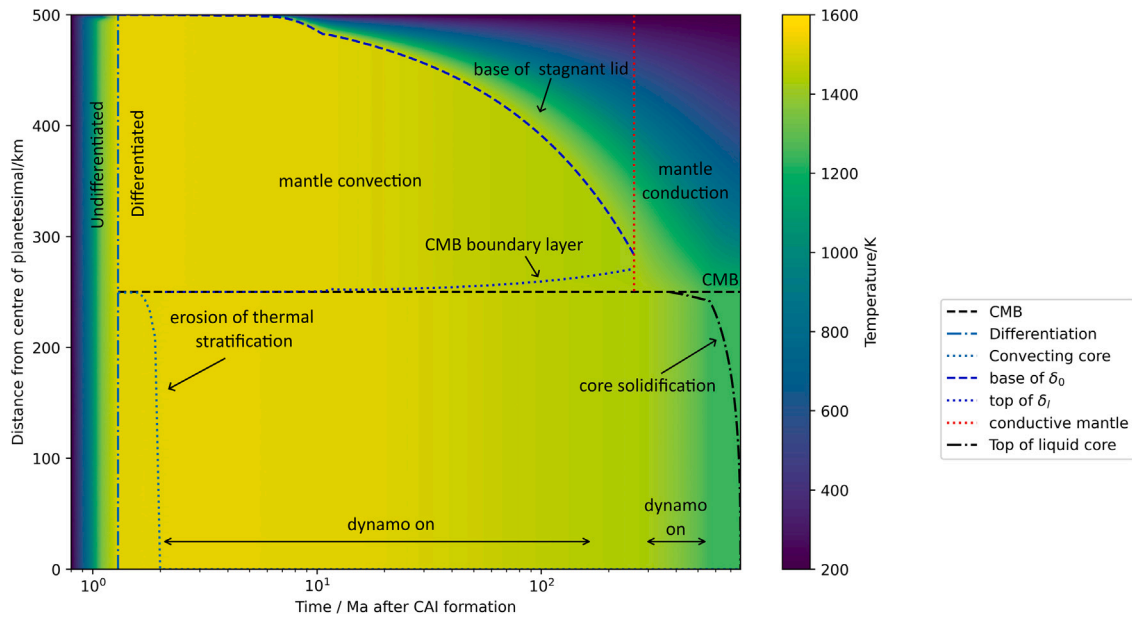


Fig. 6. Annotated thermal profile for a 500 km planetesimal accreted at 0.8 Ma after CAI formation with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$ and $X_{s,0} = 29.85$ wt%. Prior to differentiation, the body heats up due to radiogenic heating by ^{26}Al . After differentiation, core thermal stratification is eroded rapidly due to heating by ^{60}Fe . The stagnant lid and CMB boundary layer thicken until the two boundary layers meet and convection ceases, which terminates the dynamo. The temperature gradient at the CMB steepens following the cessation of convection and the dynamo restarts prior to the onset of core solidification. The black horizontal arrows indicate the period of dynamo activity, their vertical position is arbitrary.

lid and CMB boundary layer thickness is less than the mantle thickness and the whole mantle convects. The mantle reaches a peak mantle temperature of 1525 K within 0.1 Ma of differentiation. At these early times, radiogenic heating from ^{26}Al is so strong that the dominant controls on mantle temperature are surface heat flux, F_S , and radiogenic heat flux, F_{rad} (see Fig. 7, middle panel). When the mantle melt fraction is at or above ϕ_C , there is a negative feedback between these two heat fluxes, because the planetesimal loses heat very efficiently. An increase in mantle temperature, due to high F_{rad} , causes the stagnant lid to thin, which in turn increases F_S , causing the mantle temperature to decrease. This results in a mantle peak temperature close to $T_{\phi_C} = 1520$ K and very thin stagnant lid (~100–700 m) and CMB boundary layers (~100 m) at early times. This feedback plays a role until 3.8 Ma after CAI formation (Fig. 7). From 1.2–1.7 Ma after CAI formation the mantle is hotter than the core due to the faster decay of ^{26}Al in the mantle compared to ^{60}Fe in the core. From 1.7–2.0 Ma after CAI formation, core thermal stratification is eroded as radiogenic heating from ^{60}Fe increases the core temperature (Fig. 7, top panel). Once core

thermal stratification has been eroded, the core begins to convect. Re_m is immediately supercritical, so magnetic field generation begins 2.0 Ma after CAI formation. At 4.3 Ma after CAI formation, the temperature at the top of the mantle drops below T_{ϕ_C} and the stagnant lid begins to thicken. At 13 Ma after CAI formation, the temperature at the base of the mantle drops below T_{ϕ_C} and the CMB boundary layer begins to thicken. As the stagnant lid and CMB boundary layer thicken, F_{CMB} decreases and the first epoch of magnetic field generation ends ~170 Ma after CAI formation. At ~260 Ma after CAI formation, the combined CMB boundary layer and stagnant lid thickness reaches the thickness of the mantle, so mantle convection stops (Fig. 6). Immediately after the cessation of mantle convection, there is a shallower temperature gradient across the portion of the mantle that was the CMB boundary layer compared to the portion of the mantle that was the stagnant lid (Figure S11). As a single conductive gradient is established throughout the whole mantle, the conductive temperature gradient at the CMB increases and the temperature gradient near the surface decreases. As a result, F_{CMB} increases and the dynamo restarts at ~280 Ma after CAI formation. Core solidification starts at ~370 Ma, which provides an additional source of buoyancy for dynamo generation. As solidification proceeds the liquid core sulfur content increases and the core reaches the FeS eutectic at ~550 Ma. This reduces the buoyancy to drive the

approximate time for these processes. Therefore times are given to a precision of 0.1 Ma from 1–10 Ma, 1 Ma for 10–100 Ma and 10 Ma for >100 Ma.

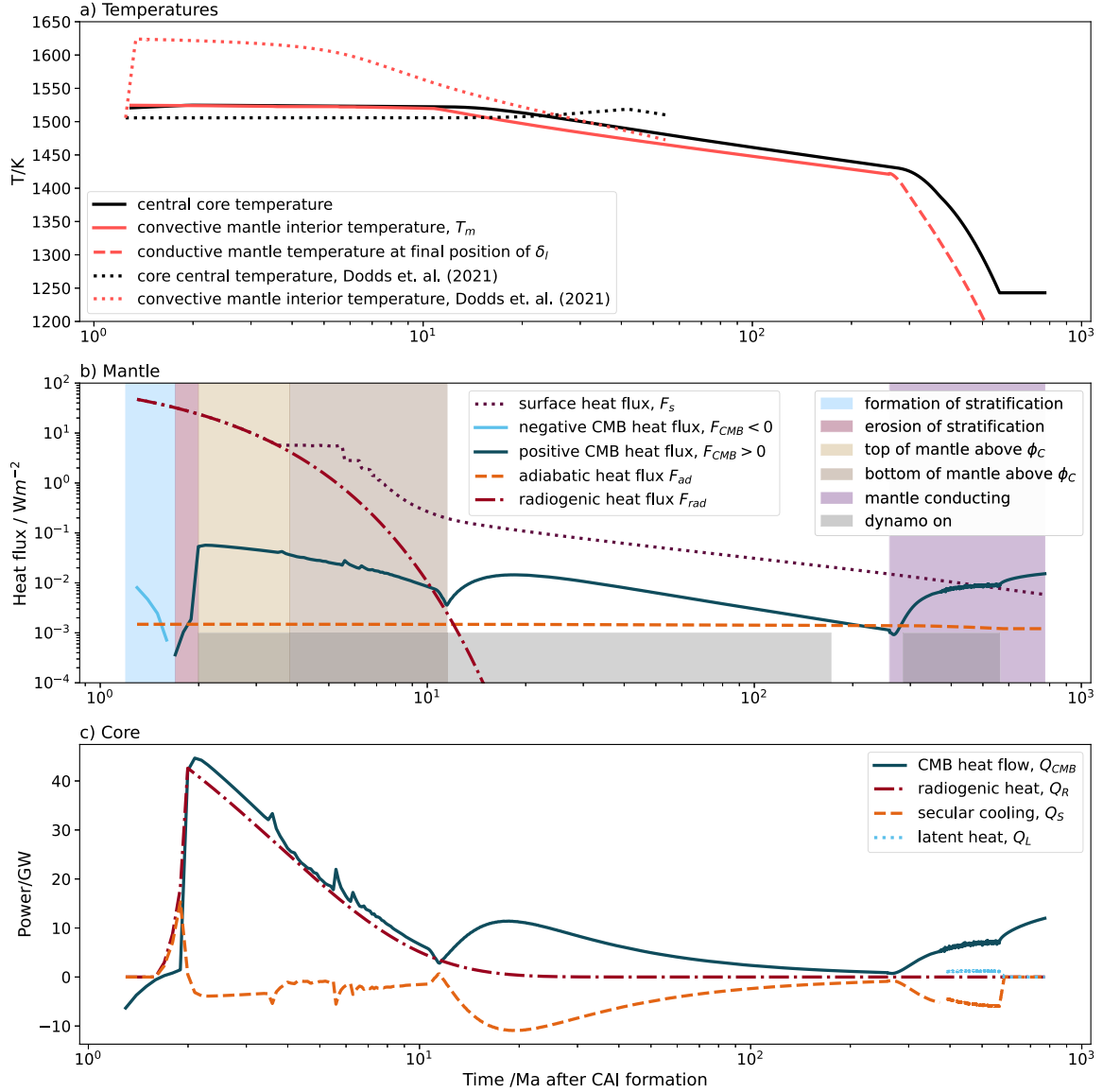


Fig. 7. Temperatures (a) and mantle heat fluxes (b) and core power sources (c) for the same parameters as Fig. 6: 500 km planetesimal accreted at 0.8 Ma after CAI formation with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$ and $X_{\text{S},0} = 29.85 \text{ wt\%}$. In the upper panel, after the cessation of convection, the mantle temperature evolution at the position of the final mantle height of the CMB boundary layer is shown by the red, dashed line. For comparison, the central core temperature and convecting mantle temperature from Dodds et al. (2021) are shown by the dotted lines. The Dodds et al. (2021) temperature evolution is shorter, because their model ended after the cessation of mantle convection ($\sim 50 \text{ Ma}$ in their model). In the middle panel, at the beginning of the thermal evolution, F_{CMB} is negative, because the mantle heats up faster than the core (blue box). The absolute value of F_{CMB} has been plotted for these times (light blue line). Before 3.8 Ma after CAI formation, the surface heat flux, F_s , matches the radiogenic heat flux, F_{rad} , because the top of the mantle is above the critical melt fraction and there is a negative feedback loop between mantle temperature and stagnant lid thickness (yellow-brown box). The downward spike in F_{CMB} at 13 Ma after CAI formation is due to the rapid thickening of the CMB boundary layer when the base of the mantle drops below the critical melt fraction. The horizontal plateaus and vertical drops in F_s and spikes in F_{CMB} prior to 13 Ma is a model artefact due to the discretisation of the stagnant lid, and we expect smooth curves in reality. The CMB heat flux, F_{CMB} , decreases with time and the dynamo turns off just before the cessation of convection due to the thickening of the CMB boundary layer. In the lower panel, the latent heat contribution only appears once the core begins solidifying. The latent heat release and secular cooling during core solidification are shown as a rolling average over 200 timesteps (20 Ma) to remove oscillations due to the discrete nature of the model. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

dynamo, causing Re_m to become subcritical and the dynamo shuts off. The core solidifies completely by $\sim 770 \text{ Ma}$.

3.1. Inclusion of ^{60}Fe

Previous models neglected the role of radiogenic heating by ^{60}Fe in the core because it only led to a $\sim 10 \text{ K}$ difference in peak core temperature over the lifetime of the planetesimal (Henke et al., 2013).

Although this temperature difference is small compared to the overall core temperature, it is significant compared to the temperature difference across the CMB ($\sim 1 - 5 \text{ K}$). Radiogenic heating by ^{60}Fe is therefore important at early times in the thermal evolution. Indeed, radiogenic heating from ^{60}Fe can increase the core temperature above the temperature at the base of the mantle, causing the core's thermal stratification to be removed far more rapidly (see Table 3) than in previous models (Dodds et al., 2021). As a result, the inclusion of ^{60}Fe can lead to an earlier onset of dynamo generation (by $\sim 4 \text{ Ma}$ compared

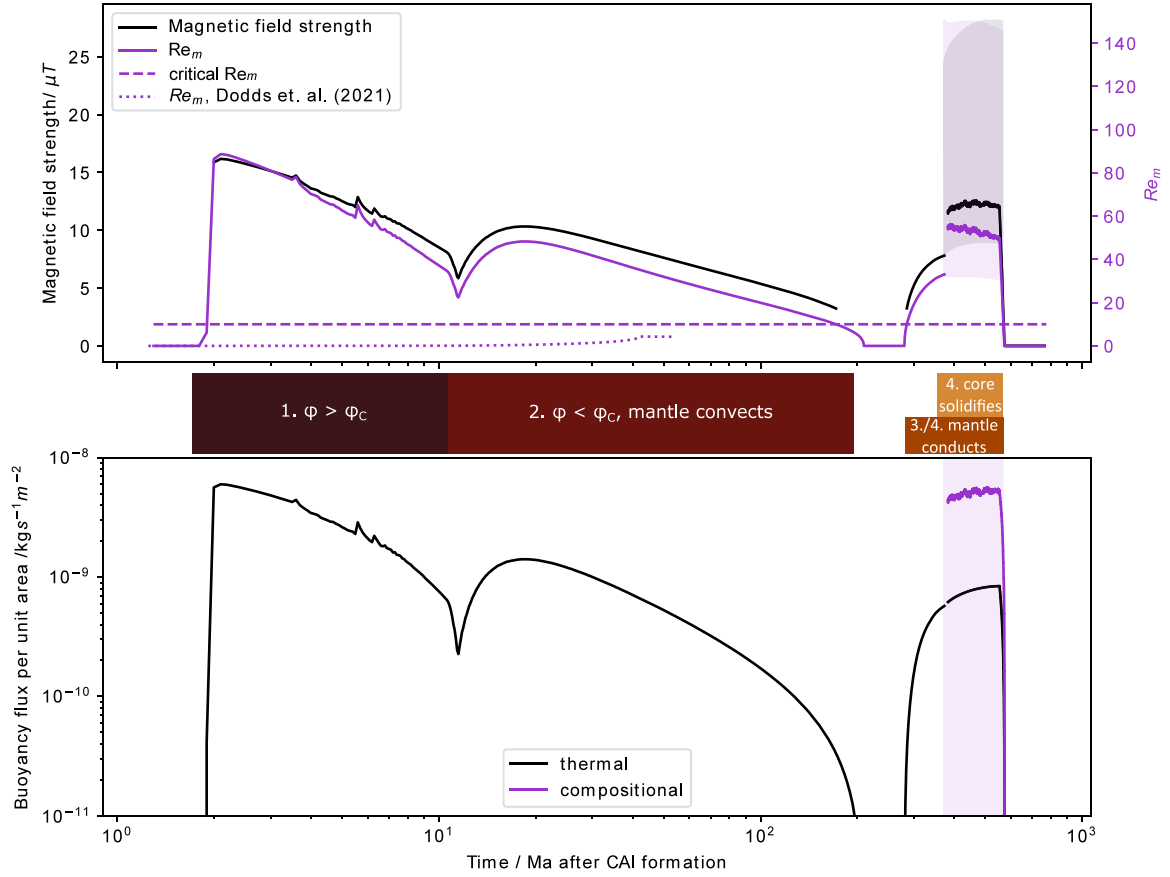


Fig. 8. Predicted dipole magnetic field strength at the surface of the planetesimal and magnetic Reynolds number, Re_m , (upper panel) and buoyancy flux per unit area (lower panel) as a function of time for a 500 km planetesimal accreted at 0.8 Ma after CAI formation with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$, $m_{\text{frac}} = 1$ and $X_{\text{S},0} = 29.85 \text{ wt\%}$. In the upper panel, the purple, horizontal dashed line is a critical Re_m of 10 and the dotted, purple line is the Re_m from Dodds et al. (2021). The longevity of core thermal stratification in Dodds et al. (2021) prevented their Re_m from becoming supercritical. The spikes in the traces prior to 13 Ma are model artefacts due to the discretisation of the stagnant lid. Due to the discrete nature of latent heat release in the model, the magnetic field strength and Re_m oscillate during core solidification. This oscillating output is shown by the faded grey and purple traces, and the rolling average over 200 output steps (20 Ma) is shown in bold. The small gap between the purely thermally driven dynamo and the average values for the thermo-compositional dynamo is due to the lag in the rolling average. The thermal (first term in square brackets in Eq. (36)) and compositional (second term in square brackets in Eq. (36)) buoyancy fluxes are shown in the lower panel. Again, the model compositional buoyancy flux (faded purple) and rolling average buoyancy flux (bright purple) are shown. Time is plotted logarithmically to make the early trends in magnetic field generation with time visible. The downward spike in magnetic field strength in the first epoch of dynamo generation occurs when the mantle cools sufficiently for its melt fraction, ϕ , to drop below the critical melt fraction, ϕ_c . The dynamo stops when mantle convection ceases and restarts prior to the onset of core solidification once the conductive temperature gradient at the CMB has steepened sufficiently. Core solidification very slightly increases magnetic field strength and Re_m . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

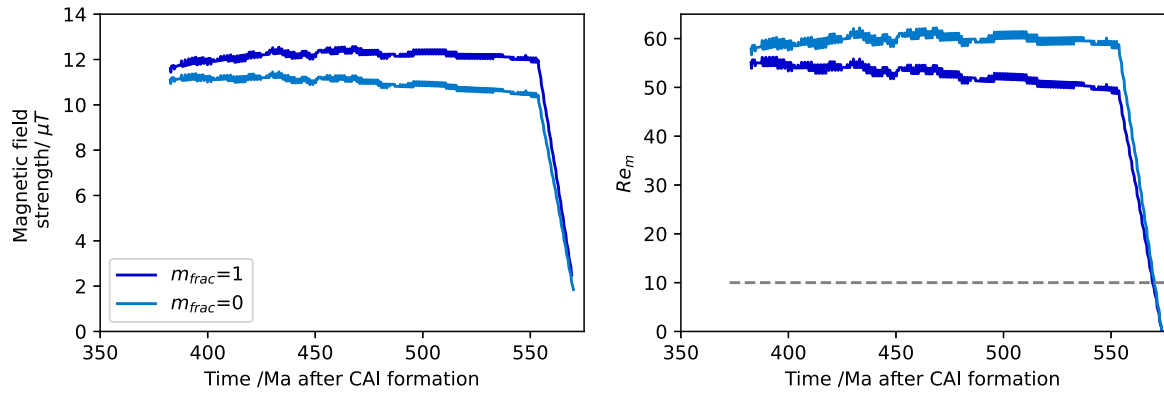


Fig. 9. Magnetic field strength (left panel) and magnetic Reynolds number, Re_m , (right panel) for the two core solidification endmembers: no solidified material falls to the centre and no passive inner core forms, $m_{\text{frac}} = 0$ (dark blue line); and all solidified material falls to the centre to form a passively growing inner core, $m_{\text{frac}} = 1$ (light blue line). The lines indicate a rolling average over 20 Ma. Magnetic field strength is slightly increased and Re_m is slightly decreased in the presence of a passively growing inner core, but the difference between the two endmembers is minimal. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 3

Differences between key aspects of planetesimal thermal evolution between our model and previous models, and a reason for each difference. Our model run is for a 500 km radius planetesimal accreted at 0.8 Ma after CAI formation with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$. The Case 1 run from Dodds et al. (2021) (a) is used for comparison. Dynamo generation is compared with both Case 1 from Dodds et al. (2021) and the single accretion event model from Bryson et al. (2019a) (b), because thermal stratification prevented dynamo generation in Dodds et al. (2021). A model run for a 400 km radius planetesimal accreted at 0.5 Ma after CAI formation was used to compare with the Bryson et al. (2019a) model. All times are Ma after CAI formation and are given to a precision of 0.1 Ma from 1–10 Ma, 1 Ma for 10–100 Ma and 10 Ma for >100 Ma. ϕ_c is the critical melt fraction.

	Our model	Previous model	Reference	Reason
Peak mantle temperature/K	1525 at 1.2 Ma	1620 at 1.2 Ma	a	New viscosity model, lower ϕ_c
Mantle hotter than the core until/Ma	1.7	9	a	Inclusion of ^{60}Fe
Core thermal stratification eroded/Ma	2.0	40	a	Inclusion of ^{60}Fe
End of mantle convection/Ma	260	56	a	Mantle convection model
First dynamo onset/Ma	2.0	–	a	Inclusion of ^{60}Fe
	1.4	5.4	b	
First dynamo cessation/Ma	170	–	a	Mantle convection model
	150	17	b	

to Bryson et al., 2019a) or an early epoch of dynamo generation that was not observed for an instantaneously accreting body in the model presented by Dodds et al. (2021). Because it will cause more heat to be produced, the effect of ^{60}Fe on dynamo timing and strength will be even more significant for the upper estimates of primordial $^{60}\text{Fe}/^{56}\text{Fe}$.

3.2. Mantle convection criterion

Mantle convection and the first epoch of dynamo generation lasts an order of magnitude longer in our model than previous models (Table 3) due to our chosen criteria for the cessation of mantle convection. In previous models, solid-state convection immediately ceased when the Rayleigh number dropped below the critical Rayleigh number, Ra_c , for the first time (Sternberg and Crowley, 2012; Bryson et al., 2019a; Dodds et al., 2021). This previous cessation criterion resulted in mantle convection ceasing early, at a time when the CMB boundary layer was too thin and the temperature profile near the base of the mantle was isothermal (the mantle adiabatic gradient is negligible). This isothermal profile resulted in a pause in cooling at the CMB until conductive cooling from the top of the mantle reached the CMB. We have mitigated this artefact in our model by assuming the cessation of convection occurs when the combined stagnant lid and CMB boundary layer thickness equals the mantle thickness. This better represents the gradual cessation of convection, because the convecting domain gradually shrinks in size until the entire domain is conductive (Fig. 6). This criterion has been used to calculate cessation of convection by many planetary thermal evolution studies (e.g. Grott et al., 2011; Morschhauser et al., 2011) and predicts similar thermal evolutions to equivalent 2D and 3D numerical simulations (Tosi et al., 2013). We assume a conductive profile in the CMB boundary layer, such that upon the cessation of mantle convection there is already a conductive temperature gradient at the base of the mantle. This ensures there is mantle and core cooling via conduction the moment convection ceases. The gradual thickening of the CMB boundary layer is reflected in the slow decrease in F_{CMB} and dynamo field strength in Figs. 7 and 8 and lack of spike in F_{CMB} at cessation of convection compared to Bryson et al. (2019a). The conductive gradient in the CMB boundary layer enables a second epoch of dynamo generation to begin before the onset of core solidification, because the conductive temperature gradient at the CMB is large enough to produce supercritical Re_m .

3.3. Magnetic field generation with time

Planetesimal magnetic field generation can be split into four regimes (Fig. 8). In Regime 1, radiogenic heating from ^{60}Fe is strong and the mantle is above ϕ_c , such that the CMB boundary layer is thin and F_{CMB} is high. The peak magnetic field strength (16 μT for our example run) for the whole thermal evolution is reached at the onset of dynamo generation, when the temperature gradient across the CMB is largest due to heating by ^{60}Fe . Magnetic field strength decreases

as the CMB boundary layer thickens (see Figs. 6 and 8). Regime 1 ends ~ 13 Ma after CAI formation when the temperature at the base of the mantle drops below T_{ϕ_c} . There is a downward spike in magnetic field strength at this time, because the CMB boundary layer thickness increases rapidly (see Figure S2) and the same temperature difference is accommodated across a larger distance, which decreases F_{CMB} . At the beginning of Regime 2, as the mantle continues to cool, the core-mantle temperature difference initially increases more rapidly than the CMB boundary layer thickness, which temporarily increases F_{CMB} and the magnetic field strength. F_{CMB} and magnetic field strength then decline as the CMB boundary layer thickening outweighs the change in core-mantle temperature difference. Regime 3 occurs after the mantle has stopped convecting. The conductive temperature gradient at the CMB steepens (Figure S11), which increases F_{CMB} enough to restart the dynamo. Magnetic field strength increases with time up to 8 μT , because the temperature gradient in the deep mantle increases as the mantle cools. Once core solidification begins this provides an additional source of buoyancy to drive the dynamo (Regime 4) and the field strength is approximately constant at 13 μT until the core reaches the eutectic composition. Once the core reaches this composition there is insufficient buoyancy flux to drive the dynamo.

The field strengths and transition times between these regimes will change with chosen planetesimal parameters. For lower core sulfur contents, core solidification will start earlier and the compositionally driven regime (Regime 4) may overlap with preceding regimes (Fig. 10). Smaller planetesimals will cool more quickly, so will have a compressed magnetic field generation history. The transition between Regimes 1 and 2 is partially due to the jump in viscosity. These two regimes may become one with a smooth decrease in field strength with time if viscosity parametrisations are improved in the future.

3.3.1. Compositional vs. thermal dynamos

In our model, the primary difference between compositional and thermal dynamos is the release of gravitational potential energy in the liquid region of the core, which increases the buoyancy flux to drive the dynamo. As a result, thermo-compositional dynamos generate stronger magnetic fields than thermal dynamos at the same point in planetesimal thermal evolution (orange/grey vs. yellow lines in Fig. 10). For a 500 km body at the thermo-compositional field strength peak, the magnetic field is 1.7 times stronger than the thermal dynamo alone at the same period of dynamo generation and the compositional buoyancy flux is ~ 6 times higher than the thermal buoyancy flux (Fig. 8). However, the absolute difference in magnetic field strength between mechanisms (~ 7 μT) would require small measurement uncertainties to be detected in the paleomagnetic record and would be degenerate with the time the magnetisation was recorded. For instance, in Regime 3, both field strengths decrease with time so a later generated thermo-compositional field could have the same strength as a thermally

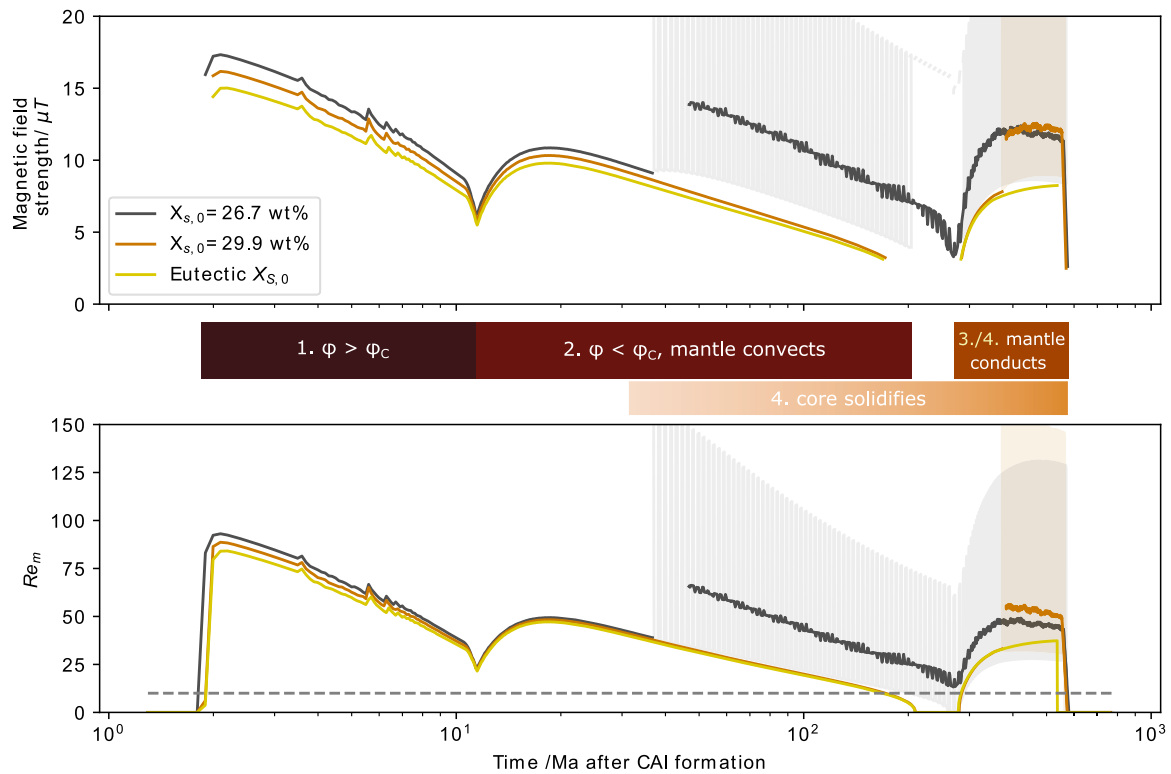


Fig. 10. Magnetic field strength and Re_m with time for 500 km planetesimals with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$ and initial core sulfur contents, $X_{S,0}$, from 26.7–33 wt%. Due to the discrete nature of the model, the magnetic field strength and Re_m oscillate during core solidification. This oscillating output is shown by the faded traces and the rolling average over 200 output steps (20 Ma) is shown in bold. The small gap between the purely thermally driven dynamo and the average values for the thermo-compositional dynamo is due to the lag in the rolling average. The dynamo generation regimes are the same as in Fig. 8. As $X_{S,0}$ decreases, the core liquidus temperature increases and the onset of core solidification moves to earlier times. Compositional buoyancy leads to up to a 70% increase in magnetic field strength. Core solidification is not required to produce a second epoch of dynamo generation. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

generated one earlier in the same regime. The timing of the different magnetic field regimes is also strongly affected by planetesimal size (Sanderson et al., 2024).

Although the onset of core solidification may not have a resolvable effect on field strength, it can have a strong effect on the timing of dynamo generation. For $X_{S,0} = 26.7$ wt%, the increase in buoyancy flux due to core solidification is enough to prevent cessation of the dynamo when mantle convection ceases and there is no gap in dynamo generation.

Our model now predicts the first epoch (epoch denotes a continuous period of dynamo generation compared to regimes, which demarcate the different mantle/core states during dynamo generation) of thermal dynamo generation can last up to 170 Ma after CAI formation for 500 km radius planetesimals (Fig. 8). The dynamo restarts in 500 km radius planetesimals with $X_{S,0} = 29.85$ wt% and 33 wt% at ~280 Ma after CAI formation prior to the onset of core solidification (Fig. 10). As such, core solidification is not required for a second epoch of dynamo generation. Core solidification does not prolong the life of the dynamo, but strengthens the resulting magnetic field and narrows the gap between generation epochs. The restart of the dynamo prior to core solidification predicted by our model suggests that core solidification may not be required to explain younger magnetic remanences (e.g. Nichols et al., 2021; Maurel et al., 2021, >65 Ma after CAI formation based on current evidence). This could resolve the problem of finding an inward solidification mechanism which can drive compositional convection rather than stably stratifying the core (Dodds et al., 2025), because the later meteorite paleomagnetic remanences could have been generated by a purely thermal dynamo.

3.3.2. Magnetic field strengths

The magnetic field generation scaling laws we use enable us to predict both Re_m and dipolar, surface magnetic field strengths for the entire planetesimal thermal evolution. These magnetic field strengths can be compared to the paleomagnetic record to determine a range of possible parameters for a given meteorite parent body (see Sanderson et al., 2024). We have determined that a MAC scaling law for magnetic field strength is appropriate for planetesimal cores (Table S1). Previous planetesimal thermal evolution models were uncertain which core force balance and scaling law was appropriate for planetesimals, so did not predict magnetic field strengths (Bryson et al., 2019a; Dodds et al., 2021) or used multiple scaling laws (Sternberg and Crowley, 2012). Additionally, we have developed a parametrised model for inward core solidification, which enables us to calculate a combined thermal and compositional buoyancy flux (Eq. (36)) and use the same convective velocity and magnetic field scaling laws before and during core solidification. This means a full internally-generated magnetic field history for a given planetesimal can be predicted without having to assume a single buoyancy source at a given time. This is important for trying to understand time-resolved magnetic field generation records for a specific body, such as the Main Group pallasites (Tarduno et al., 2012; Bryson et al., 2015; Nichols et al., 2021) and the IIE irons (Maurel et al., 2021), for which magnetic field strengths were previously predicted only during outward solidification with a conductive mantle.

4. Accretion and differentiation assumptions

4.1. Accretion timescale and partial differentiation

We do not consider the effects of gradual accretion, because there are a range of possible accretion growth laws (Neumann et al., 2012)

and the most appropriate law for planetesimals may depend on the initial conditions of dynamical simulations (Weidenschilling, 2019). Prolonged accretion over $\mathcal{O}(0.1 \text{ Ma})$ could erode core thermal stratification by the later addition of cool material to the top of the core, which can bring forward the onset of the dynamo relative to the instantaneous accretion case (Dodds et al., 2021). However, our model includes heating by ^{60}Fe in the core, which can rapidly remove thermal stratification and will counter the effect of prolonged accretion on core thermal structure.

Accretion over even longer timescales ($\mathcal{O}(1 \text{ Ma})$) following an exponential accretion law can lead to partial differentiation, smaller planetesimal cores, and weaker dynamos (Dodds et al., 2021). Partial differentiation could be included in the model in the future by adding regolith with lower conductivity to the top of the planetesimal and introducing a variable ratio of core to planetesimal radii, $\frac{r_c}{R}$. This could lead to a weaker dynamo with shorter duration for a given planetesimal radius compared to the results in this paper due to reduced core and mantle size. These extensions will be important for applying the model to partially differentiated bodies that preserve a thick chondritic layer and have been proposed to have generated a magnetic field, such as the CV and H chondrites (Elkins-Tanton et al., 2011; Bryson et al., 2019b).

4.2. Compaction, sintering and regolith

Our model does not include variations in planetesimal thermal conductivity between accretion and differentiation due to compaction and sintering. The planetesimal sinters at 700 K (Yomogida and Matsui, 1984) and rapidly reaches the thermal properties assumed in this model. For a 500 km planetesimal the inner 496 km is below 700 K only for the first 0.12 Ma after accretion and the last node sinters 0.5 Ma after accretion, so a lower thermal conductivity prior to sintering has a negligible effect on heat transport over the 10–500 Ma timescales for dynamo generation. We have neglected any unsintered regolith because this layer is so thin ($<500 \text{ m}$). This may result in a very slight over-estimate of the surface heat flux and planetesimal cooling rate.

4.3. Water

Following other models of differentiated planetesimals (Neumann et al., 2018; Sturtz et al., 2022; Monnereau et al., 2023), our model does not include the thermal effects of water prior to differentiation. We adopted this approach because radiogenic heating is strong enough that the thermal contributions of melting ice, hydrating, and dehydrating silicates has a minimal effect on the differentiation time. Additionally, the early accreted planetesimals considered here rapidly reach temperatures above the silicate dehydration temperature (1223 K, Lichtenberg et al., 2019a), and after differentiation planetesimals retain very little water (Peterson et al., 2023; Newcombe et al., 2023).

4.4. Differentiation mechanism

Our model for differentiation must enable planetesimals to form a core in which a dynamo can be generated. In order for the planetesimal to differentiate, the material which will form the core, assumed to be Fe–FeS, must be able to move to the centre of the body. There are at least two possible differentiation mechanisms: percolation, where Fe–FeS melt, which has a lower solidus than silicates, moves along grain boundaries in a solid, silicate matrix; and rain-out, where more dense molten Fe–FeS falls through less dense silicate melt to the planetesimal centre. Percolation requires an interconnected network of melt. Metal melts have large dihedral angles (110° , Néri et al., 2020) and need high volume fractions to form this interconnected network (up to 20%–25%, Néri et al., 2020). These high volume fractions would require high planetesimal metal contents, which would result in unrealistically large core radii. Only 12.5 vol% metal is required to form a core that has a radius that is 50% the radius of the planetesimal (Dodds et al., 2021)

and cores predicted to form from chondritic compositions have core radii that are 30%–50% of the planetesimal radius (Bercovici et al., 2022). However, the need for an inter-connected network of metal for percolation could be removed by shear deformation due to solid-state convection (Rushmer et al., 2000), crack formation (Keil and Wilson, 1993) or silicate melting (Wilson et al., 2008).

Estimates of the percolation velocity, assuming Darcy flow, are linearly dependent on the permeability of the planetesimal matrix, for which model values vary by six orders of magnitude from 10^{-8} m^2 (Fu and Elkins-Tanton, 2014) to 10^{-14} m^2 (Neumann et al., 2012). As a result, the time taken to differentiate via this mechanism is very uncertain ($\mathcal{O}(10^{-10^6})$ years, see Section S5.1). Differentiation via rain out occurs rapidly in comparison to a model timestep, $\mathcal{O}(10^2)$ years for 1 mm radius droplets, once $\phi = \phi_C$ (i.e., once the silicate portion of the body has a liquid viscosity). Therefore, in this model we adopt differentiation via rain out when $\phi = \phi_C$, because the mechanics are simpler and any Fe–FeS that has not already reached the centre via percolation will move there rapidly once $\phi = \phi_C$.

4.4.1. Minimum core sulfur content

Our model assumes differentiation occurs at the critical melt fraction and that the core of the planetesimal is completely molten at the point of differentiation, which limits the range of initial core sulfur contents we can model. For the core material to be completely molten at differentiation requires the differentiation temperature to be greater than or equal to the Fe–FeS liquidus. The liquidus temperature is a function of core sulfur content and core pressure (Eq. (29)), while the differentiation temperature is assumed to be equal to the temperature of ϕ_C , which depends on the mantle solidus (Section 5.1) and the choice of ϕ_C . Experiments (0.2, Scott and Kohlstedt, 2006) and previous planetesimal thermal evolution models (0.5, e.g. Bryson et al., 2019a) provide a possible range of ϕ_C .

Previous studies of planetesimal dynamo generation were not limited in their value of $X_{S,0}$, because they used the linear liquidus approximation (Neufeld et al., 2019; Nichols et al., 2021), which has lower liquidus temperatures for $X_{S,0}$ in the range 0–10 wt% compared to the Buono and Walker (2011) liquidus (Figure S5). Prior studies of planetesimal differentiation via percolation predicted differentiation of sulfur-poor bodies, because they only considered heat transfer via conduction not convection, which allows for higher maximum planetesimal temperatures (Neumann et al., 2012).

For the mantle solidus used in this model (1400 K), the minimum $X_{S,0}$ varies from 22.2–28.3 wt% (Fig. 11), which is higher than the sulfur contents in iron meteorites (0–17 wt% Kruijer et al., 2014). If the mantle solidus in the model is raised to 1473 K (Fu and Elkins-Tanton, 2014), the minimum $X_{S,0}$ varies from 6.9–25.9 wt% S (Fig. 11). However, it is unclear if this is the most appropriate solidus value and the lower values in this range require extremal values of planetesimal size (500 km) and critical melt fraction (0.5). Planetesimals could have initially been sulfur rich and lost their sulfur by later processes, such as immiscible fluid separation in the core (e.g. Bercovici et al., 2022) or volatile loss (e.g. Hirschmann et al., 2021). Bodies differentiating from CI, CM, LL, CO, CV, and CK chondritic starting compositions are predicted to have $X_S \geq 22\%$ (Bercovici et al., 2022), which is in line with the minimum $X_{S,0}$ in the model. Further research is needed to constrain the mantle solidus and critical melt fraction and to explore these additional processes occurring during or immediately after differentiation.

As a first estimate, sulfur poor bodies would have an earlier onset and longer duration of compositional convection than those modelled here, because the core liquidus temperature is higher and more core solidification is required before the bulk liquid core sulfur content reaches the eutectic. In addition, decreasing $X_{S,0}$ lowers the density difference between the solidified iron and the bulk liquid core, which could decrease buoyancy flux and magnetic field strength at the beginning of core solidification.

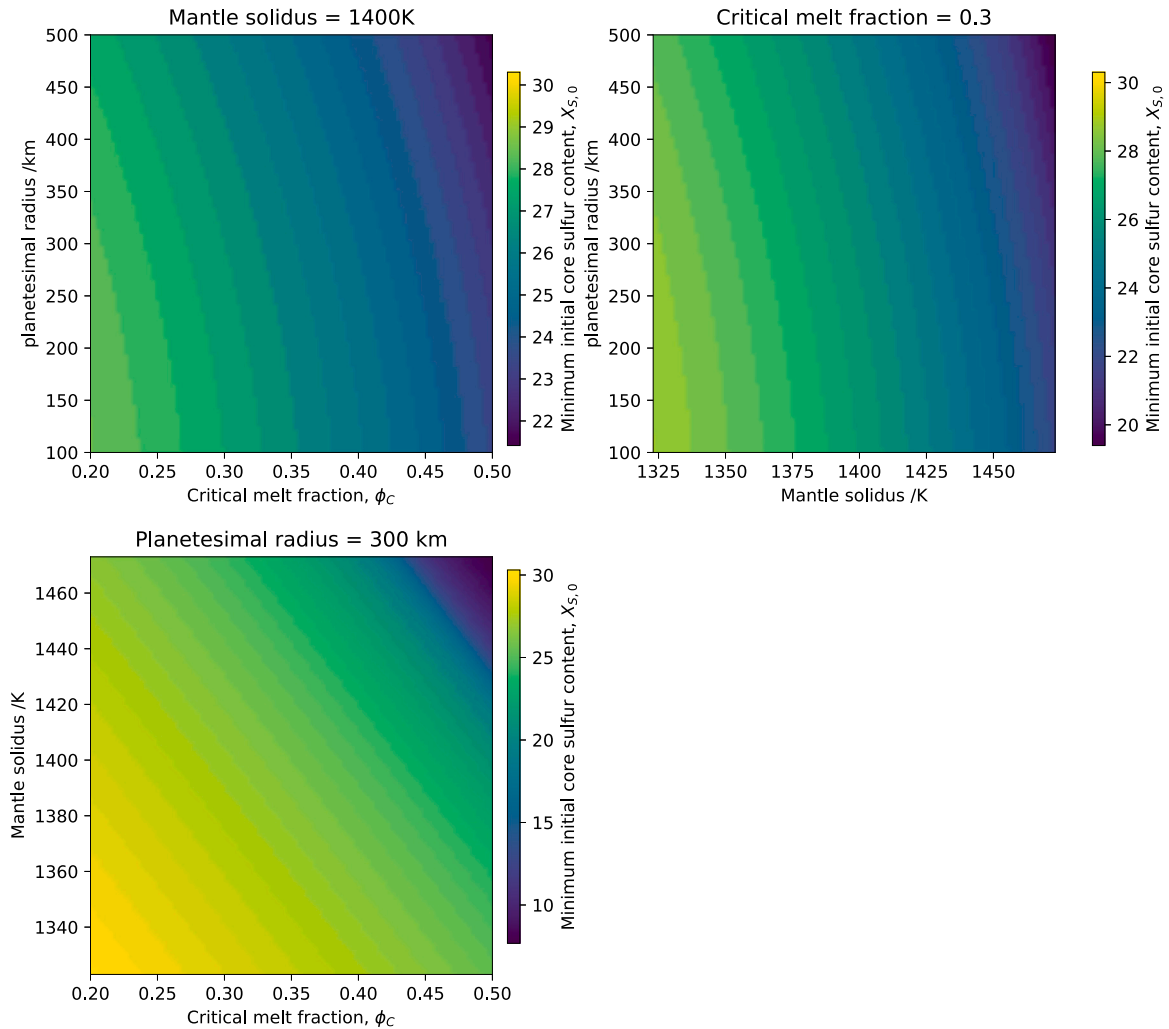


Fig. 11. Minimum initial core sulfur content, $X_{S,0}$, in our model as a function of: planetesimal radius, which controls core pressure (top left, top right); critical melt fraction, which controls the temperature at differentiation (top left, bottom left); and mantle solidus, which controls the temperature at differentiation (top right, bottom left). The lowest radii, lowest critical melt fractions and lowest mantle solidus temperatures have the highest minimum $X_{S,0}$. The minimum and maximum values on the colour scale vary between subplots, in order to highlight the effect of each parameter. Variations in mantle solidus temperature combined with variations in critical melt fraction produce the largest spread in $X_{S,0}$. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

5. Mantle assumptions

5.1. Silicate solidus and liquidus

The silicate solidus, $T_{m,s}$, and liquidus, $T_{m,l}$, depend on pressure and composition (Hirschmann, 2000). Meteorite melting experiments suggest the silicate solidus lies between 1323–1423 K and the liquidus is ~ 400 K hotter than the solidus (Agee et al., 1995; McCoy et al., 1999). Previous planetesimal models have used values for the mantle solidus between 1400–1473 K (Hevey and Sanders, 2006; Elkins-Tanton et al., 2011; Fu and Elkins-Tanton, 2014; Kaminski et al., 2020; Bryson et al., 2019a; Dodds et al., 2021) based on differing degrees of rounding of these experimental results in $^{\circ}\text{C}$. For consistency with the studies of Bryson et al. (2019a) and Dodds et al. (2021), we have chosen to use a mantle solidus and liquidus of 1400 K and 1800 K, respectively.

Increasing the silicate solidus and liquidus temperature increases the temperature of the critical melt fraction and peak planetesimal temperature. Increasing the silicate solidus has little effect on thermal dynamo generation (Fig. 12), but will delay compositional dynamo generation, because a higher silicate solidus temperature requires more

cooling before the core reaches the Fe–FeS liquidus, for the same initial core sulfur content. Decreasing the silicate solidus can bring forward the onset of core solidification, for a given initial core sulfur content, to before the cessation of mantle convection. In this scenario, the additional buoyancy provided by core solidification could power the dynamo when mantle convection ceases and prevent a gap in dynamo generation. The choice of mantle solidus will determine the range of $X_{S,0}$ over which early onset of core solidification is possible.

5.2. Silicate melt migration

Silicate melt migration could lead to formation of high silicate melt fraction layers rather than global planetesimal (pre-differentiation) or mantle (post-differentiation) melting due to the preferential partitioning of ^{26}Al into melt (e.g. Neumann et al., 2014). Melt migration is significant if the timescale for percolation of silicate melt through the solid matrix is shorter than the timescale for radiogenic heating (Lichtenberg et al., 2019b; Monnereau et al., 2023). However, the timescale for melt migration varies by seven orders of magnitude between studies (Moskovitz and Gaidos, 2011; Neumann et al., 2012;

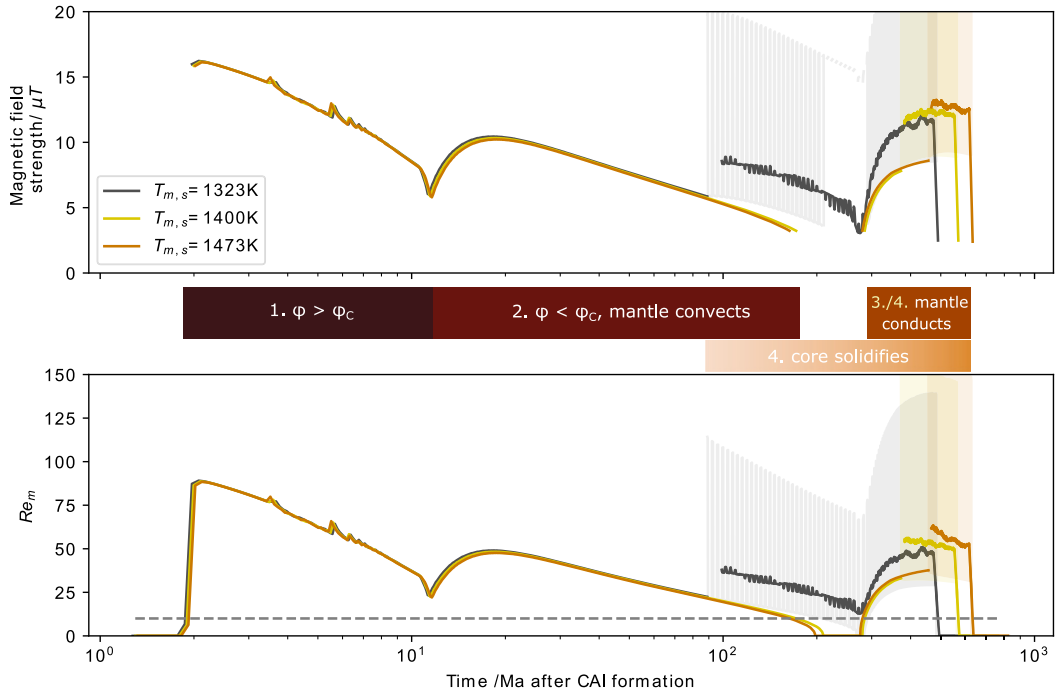


Fig. 12. Magnetic field strength and Re_m with time for 500 km planetesimals with $^{60}\text{Fe}/^{56}\text{Fe} = 10^{-8}$, $X_{\text{S},0} = 29.85$ wt% and three different mantle solidus temperatures. In all scenarios, the mantle liquidus temperature is 400 K above the solidus temperature. Due to the discrete nature of the model, the magnetic field strength and Re_m oscillate during core solidification. This oscillating output is shown by the faded traces and the rolling average over 200 output steps (20 Ma) is shown in bold. The spikes in F_{CMB} prior to 13 Ma is due to the discretisation of the stagnant lid. The small gap between the purely thermally driven dynamo and the average values for the thermo-compositional dynamo is due to the lag in the rolling average. The dynamo generation regimes are the same as in Fig. 8. Mantle solidus temperatures do not affect thermal dynamo generation, but lower solidus temperatures bring forward the onset and completion of core solidification, because less cooling is required to reach the core liquidus. This earlier onset of core solidification can provide additional buoyancy and prevent a gap in dynamo generation at the cessation of convection.

Monnereau et al., 2023) due to different assumptions about silicate grain growth and matrix permeability. Therefore, the importance of melt migration in planetesimal differentiation is heavily debated. An additional limitation of these studies of melt migration is that they do not include the possibility of solid-state convection below the critical melt fraction, which may chemically and thermally homogenise the mantle.

Due to the uncertainties in melt migration timescale, we have neglected melt migration in this model. For bodies that accrete <1.1 Ma after CAI formation, the radiogenic heating timescale is short enough to neglect melt migration (Monnereau et al., 2023). For bodies accreting after 1.1 Ma after CAI formation, but early enough to differentiate fully (i.e., <2.5 Ma after CAI formation, Neumann et al., 2012), our model may still be appropriate if solid-state convection can homogenise temperature variations resulting from melt migration. If melt migration can create temperature inhomogeneity in later accreting bodies after differentiation, our model may overestimate the extent of silicate melting at the base of the mantle. The effects of temperature heterogeneity on F_{CMB} and the dynamo are unclear, because the mantle temperature will be lower, but the conductive region will be larger (whole mantle rather than thin CMB boundary layer) compared to our model.

5.3. Compositional homogeneity

We do not specify a mantle composition and assume the mantle is compositionally homogeneous. A compositionally distinct, cumulate layer could form at the base of the mantle when it is convecting above the critical melt fraction (Sturtz et al., 2022). This could thicken the conductive boundary layer at the base of the mantle, decreasing F_{CMB} and reducing dynamo strength. However, formation of this cumulate is very sensitive to crystal size and also depends on mantle

composition (Sturtz et al., 2022). Because these parameters are uncertain, it is unclear how widespread cumulate formation will be among planetesimals and we have not included it in our model.

6. Core solidification model

In order to calculate a full planetesimal thermal history, we had to balance detail in our core solidification model with ease of implementation. Since there is such large uncertainty in the mechanism of core solidification, we did not want to adopt an unreasonable level of specificity in our core solidification model. We chose to focus on two key changes to dynamo generation that will result from core solidification: decrease in convective lengthscale; and change in density difference due to changing composition of bulk liquid core during solidification. The assumptions within our core solidification model are discussed below.

6.1. Convective lengthscale

For a planetesimal core solidifying inwards, either a stably stratified, partially solid layer may remain at shallow depths in the core, (e.g. iron snow Rückriemen et al., 2015; Davies and Pommier, 2018) or a portion of material may delaminate and fall to the centre of the planetesimal forming a passively growing inner core (e.g. Scheinberg et al., 2016; Neufeld et al., 2019). The m_{frac} parameter allows us to adjust our model between these two endmembers: no passively growing inner core ($m_{\text{frac}} = 0$); and all material immediately falling to the centre to form an inner core ($m_{\text{frac}} = 1$). This gives us a first estimate to the effect of core solidification for the most ($m_{\text{frac}} = 1$) and least ($m_{\text{frac}} = 0$) rapid changes in geometric lengthscale. In reality, the convective lengthscale is some fraction of the geometric lengthscale (Davidson, 2013; Aubert et al., 2017), which could increase the magnetic field strength and decrease Re_m (Figure S12). However, the value of this

fraction for planetesimal cores is uncertain, so we approximate the convective lengthscale as equal to the geometric lengthscale. This may overestimate dynamo duration and underestimate magnetic field strength. The endmember with the passively growing inner core was used in Figs. 8 and 10, because this is the minimum estimate of geometric lengthscale and will give a minimum estimate of Re_m . Core solidification with a passively growing inner core has a slightly stronger magnetic field strength and lower Re_m than core solidification where solid without an inner core (Fig. 9). However, magnetic field strength and Re_m both scale weakly with convective lengthscale (see Figure S3), so these changes are minimal.

For both scenarios, the amount of material solidified is parametrised by the inward motion of a solidification front, r_i , and the buoyancy flux is calculated at this position. For $m_{\text{frac}} = 0$, the radius of the base of the solidified outer layer, r_1 is equal to the position of the solidification front ($r_1 = r_i$). For $m_{\text{frac}} = 1$, there is no outer shell ($r_1 = r_c$) and all the material is at the centre. In this case, r_i differs from r_1 by a maximum of 6% (Figure S4) before the core reaches the eutectic. Therefore, evaluating the buoyancy flux at r_i rather than r_c for $m_{\text{frac}} = 1$ introduces a minimal effect.

6.2. Density difference

During core solidification, the density difference between the solidified, pure iron phase and the Fe-FeS liquid drives convection. The density difference between the solid and liquid varies as the core solidifies and the sulfur content of the liquid core increases. The adiabatic gradient in planetesimal cores is probably too shallow for solidified iron to remelt as it falls towards the centre of the planetesimal (Dodds et al., 2025). Therefore, we assume the bulk liquid core becomes more sulfur rich as the core solidifies and the driving density difference is between solidified iron and the bulk Fe-FeS liquid. Assuming perfect partitioning of sulfur into the liquid portion of the core (Goldstein et al., 2009) may overestimate the density difference available to drive the dynamo. We use the same density difference formalism in both solidification endmembers, because this estimate is the correct order of magnitude for the density difference even if it may differ between solidification modes.

Our variable density difference is up to seven times larger than in previous models (see Figure S6) which assumed a constant fractional density difference ($\frac{\Delta\rho}{\rho_c}$ of 5% based on Earth values, e.g. Nimmo, 2007; Bryson et al., 2015, 2019a; Nichols et al., 2021). This previous value underestimated the density difference due to the higher pressure and lower core sulfur content in the Earth's core compared to planetesimal cores. Our variable density difference increases the density difference available to drive a dynamo.

Our model does not consider the density difference resulting from super-eutectic core solidification as a mechanism for driving the dynamo. This is for two reasons. First, there is minimal evidence for super-eutectic planetesimal cores in the meteorite record. For instance, there are no iron meteorites with super-eutectic compositions (Hilton et al., 2022) and only parent bodies formed from CM chondrite and CI chondrite compositions potentially could have formed super-eutectic cores (Bercovici et al., 2022). Second, the density and liquidus of super-eutectic Fe-FeS is very poorly constrained (Rückriemen et al., 2018). As a result, it is unclear whether crystallisation of super-eutectic Fe-FeS can drive a compositional dynamo.

6.3. Comparison with iron snow

The $m_{\text{frac}} = 0$ endmember is an approximation to iron snow solidification, and uses a simplified description of the energetics and solid fraction in the snow zone. The full energetics of the iron snow system is complex (Rückriemen et al., 2015; Davies and Pommier, 2018) and the dynamics of iron snow solidification, including nucleation and bursts of solidification (Huguet et al., 2023), are still poorly understood and

difficult to incorporate into a numerical model. Our simplified model aims to capture the key aspects of this complicated solidification mechanism for dynamo generation. Additionally, our simplifications enable easy transition between core solidification endmembers using a single parameter, m_{frac} .

One key approximation in our model compared to the iron snow system is the treatment of the solid fraction in the snow layer. In a full iron snow model, stable stratification is formed at the top of the core by a slurry layer, with a very low, almost constant solid fraction (Davies and Pommier, 2018), whereas in our model this stable stratification is formed by a layer of pure, solid iron. This solid iron layer still captures the decrease in the lengthscale of convection with the downward growth of the snow layer.

Another key approximation in our model is in the energetics; specifically, the treatment of gravitational potential energy in the solid and the release of latent heat for driving the dynamo. Since our snow layer is a pure solid, we neglect release of gravitational potential energy in the snow zone and only consider release of gravitational potential energy in the liquid portion of the core, when calculating the buoyancy flux (Eq. (36)). Neglecting the gravitational potential energy release in the snow region is reasonable, because gravitational potential energy release in the liquid dominates (Davies and Pommier, 2018). Energetically, this is the same as the growth of a solid inner core, but adapted for inward core solidification (Gubbins et al., 2003; Nimmo, 2007). Our model includes the release of latent heat due to core solidification, but not absorption of latent heat by remelting of falling snow. In an iron snow system, these two latent heat contributions almost balance (Davies and Pommier, 2018), so could be neglected altogether. However, the adiabatic gradient in planetesimal cores may not be steep enough for iron snow to remelt (Dodds et al., 2025). Therefore, we have omitted latent heat absorption during remelting but included latent heat release during solidification. This enables a single parameter, m_{frac} , to capture variation between core solidification endmembers. The contribution of latent heat release during solidification is an order of magnitude smaller than the other contributions to core energetics during solidification (Fig. 7), so including it has a minimal effect on core solidification.

7. Outlook

Our model includes several physical and chemical features that have been neglected or simplified in previous models. For instance, our planetesimal thermal evolution model is the first to model sub-eutectic core solidification of a mantled planetesimal that also includes mantle convection. Calculating a unified buoyancy flux also enables us to use the same scaling laws for Re_m and magnetic field strength throughout the thermal evolution, and allows thermal and compositional convection to occur simultaneously. Additionally, radiogenic heating from ^{60}Fe has been added to the core thermal structure. We also chose to adjust the mantle convection parametrisation to model the gradual cessation of convection and boundary layer thicknesses applicable to systems with surface cooling and internal heating. We have implemented more physically realistic values in the mantle viscosity function and added extra pieces to the viscosity function to capture the full range of viscosity behaviour as a function of temperature. The stagnant lid scaling laws have also been implemented, such that they respond to changes in mantle viscosity. This will enable future studies to choose viscosity parameters that are most applicable for a planetesimal of a given size and composition. The other parameters in the model are fully adjustable, which enables future studies of the effects of a given parameter as well as application to specific meteorite parent bodies to enable interpretation of the meteorite paleomagnetic record. In a separate study, we systematically vary mantle viscosity, primordial $^{60}\text{Fe}/^{56}\text{Fe}$, initial core sulfur content and planetesimal size to gain a deeper understanding of these parameters on dynamo generation

and the implications of our model for the meteorite paleomagnetic record (Sanderson et al., 2024).

There are two key refinements that could be made to the model. First, the mechanism of planetesimal differentiation and initial core sulfur contents must be reconciled. Whether planetesimal cores can either form with initially low sulfur contents or lose their sulfur later, and the consequences of these factors for the onset of core solidification and dynamo generation, require further study. Second, possible mechanisms of inward core solidification in mantled planetesimals, and the implications of this on dynamo generation, should be explored in more detail. Additional improvements to the model could be made by including partial differentiation and crust formation.

8. Conclusions

Planetesimals formed during the first few Ma after Solar System formation and many were accreted into the terrestrial planets. Thermal evolution and dynamo generation models can provide insight into the interior structures and thermal histories of these planetesimals. However, previous models have focused on either early or late epochs of dynamo generation, limiting their ability to predict a complete magnetic field history. Our model focuses on the description of mantle convection and the parametrisation for sub-eutectic core solidification to provide a unified, more versatile model for planetesimal thermal evolution and dynamo generation. Specific enhancements include:

- Radiogenic heating from ^{60}Fe in the core.
- A mantle viscosity model that is self-consistent with the mantle convection parametrisation and can be adjusted to investigate the effect of mantle viscosity.
- Stagnant lid and CMB boundary layer parametrisations consistent with boundary heat fluxes and internal heating.
- Cessation of convection when the combined stagnant lid and CMB boundary layer thickness is greater than the mantle thickness.
- A parametrised model for sub-eutectic core solidification with a unified thermal and compositional buoyancy flux to drive magnetic field generation.
- Calculation of magnetic field strength during epochs of dynamo generation.

The key results of these changes implemented in our model are demonstrated by an example of the magnetic history generated for a 500 km radius planetesimal. Compared to previous models we find that:

- Core thermal stratification is eroded more rapidly.
- Mantle convection and the first epoch of dynamo generation lasts longer.
- Core solidification marginally increases dipole field strength, but exerts a much stronger control on dynamo duration by providing an additional buoyancy source after the cessation of mantle convection.
- The second epoch of dynamo generation is not triggered by core solidification.

Our model can predict a complete magnetic field generation history for a planetesimal with magnetic field strengths for both compositional and thermal dynamos. It therefore has the potential to serve as a powerful tool for understanding the general controls on planetesimal dynamo generation, as well as recovering constraints on the properties of meteorite parent bodies from their paleomagnetic records.

CRediT authorship contribution statement

Hannah R. Sanderson: Writing – original draft, Software, Methodology, Conceptualization. **James F.J. Bryson:** Conceptualization, Writing - Review & Editing, Supervision. **Claire I.O. Nichols:** Conceptualization, Writing - Review & Editing, Supervision. **Christopher J. Davies:** Writing – review & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The code for this model is available at this <https://zenodo.org/records/12771396> repository, as are the parameter files required for the example runs in this paper.

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Appendix A. Derivation of core buoyancy flux equation

From equations A8 and A14 in Buffett et al. (1996), an approximation for the dissipation in the core is

$$\Phi = \frac{\alpha_c Q_{\text{CMB}}^*}{c_{p,c}} [\psi(r_c) - \bar{\psi}] + 4\pi r_i^2 \frac{dr_i}{dt} \left(\Delta\rho + \frac{\alpha_c \rho_c L_c}{c_{p,c}} \right) [\bar{\psi} - \psi(r_i)], \quad (38)$$

where $Q_{\text{CMB}}^* = Q_{\text{CMB}} - Q_{ad}$ is the difference between the total CMB heat flux and adiabatic flux; ψ is the gravitational potential evaluated at the CMB or solidification front, $r = r_i$; and $\bar{\psi}$ is the mass-averaged gravitational potential in the liquid portion of the core. During core solidification, the region above the solidification front is solid and does not contribute entropy to drive the dynamo. Therefore, we calculate the first term in Eq. (38) at the top of the liquid inner core (dynamo region), $r = r_i$. Before core solidification, $r_i = r_c$. This simplifies the change in gravitational potential and the dissipation in the core becomes

$$\Phi = (F_T + F_c) \Delta\psi = \left[\frac{\alpha_c Q_{r_i}^*}{c_{p,c}} - 4\pi r_i^2 \frac{dr_i}{dt} \left(\Delta\rho + \frac{\alpha_c \rho_c L_c}{c_{p,c}} \right) \right] (\psi(r_i) - \bar{\psi}), \quad (39)$$

where $Q_{r_i}^* = Q_{r_i} - Q_{ad}$ is the superadiabatic heat flux at the boundary between the solid outer and liquid inner core and F_T and F_c are the thermal and compositional buoyancy fluxes, respectively (Rückriemen et al., 2015). The combined buoyancy flux, $Q_b = F_T + F_c$ is inside Eq. (39). Using $Q_{r_i}^* = 4\pi r_i^2 (F_{r_i} - F_{ad}) = (-k_c \frac{dT}{dr} \Big|_{r_i} - \frac{\alpha_c g(r_i) k_c}{c_{p,c}} T(r_i))$ gives

$$Q_b = 4\pi r_i^2 \left[\frac{\alpha_c k_c}{c_{p,c}} \left(-\frac{dT}{dr} \Big|_{r_i} - \frac{\alpha_c g(r_i)}{c_{p,c}} T(r_i) \right) - \left(\frac{\alpha_c \rho_c L_c}{c_{p,c}} + \Delta\rho \right) \frac{dr_i}{dt} \right]. \quad (40)$$

Eq. (38) neglects compositional diffusion and assumes compositional fluxes are mixed evenly into the liquid portion of the core rather than assuming the combination of compositional fluxes and entropy are evenly mixed (Lister, 2003). This well-mixed approximation means the latent heat released at the upper boundary of the dynamo generation region during core solidification can contribute entropy to drive the dynamo. This introduces the same amount of error as the Boussinesq approximation (Lister, 2003), so for our model this approximation is acceptable.

For a constant density core and a solidified outer layer only ($m_{\text{frac}} = 0$), the flux-based Rayleigh number approximation to the convective power used by our model is equivalent to calculating the convective

power directly. The convective power, p , is related to the Ohmic dissipation, Φ , by

$$p = \frac{\Phi}{\rho_c \Omega^3 I^2 V}, \quad (41)$$

where V is the volume of the convecting region (Aubert et al., 2009). For a constant density core $\psi(r_i) = \frac{r_i g_i}{2}$ and $\tilde{\psi} = \frac{3r_i g_i}{10}$ (denoting the outer convecting boundary by r_i rather than r_o and setting the radius of the inner convecting boundary to 0 in Equation 16 in Aubert et al., 2009). Combining the expressions for $\psi(r_i)$ and $\tilde{\psi}$ with Eq. (39),

$$\Phi = \frac{Q_b r_i g_i}{5}. \quad (42)$$

Substituting Eq. (42), the volume of the convecting core and $r_i = l$ into Eq. (41) gives

$$\begin{aligned} p &= \frac{g_i r_i Q_b}{5 \rho \Omega^3 r_i^2 V} \\ &= \frac{3}{5} \frac{g_i Q_b}{4 \pi \rho \Omega^3 I^4} = \gamma Ra_Q, \end{aligned} \quad (43)$$

which is equivalent to Eq. (36).

Appendix B. Supplementary data

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.icarus.2024.116323>.

References

- Agee, C.B., Li, J., Shannon, M.C., Circone, S., 1995. Pressure-temperature phase diagram for the Allende meteorite. *J. Geophys. Res. Solid Earth* 100 (B9), 17725–17740. <https://doi.org/10.1029/95JB00049>.
- Aubert, J., Gastine, T., Fournier, A., 2017. Spherical convective dynamos in the rapidly rotating asymptotic regime. *J. Fluid Mech.* 813, 558–593. <https://doi.org/10.1017/jfm.2016.789>.
- Aubert, J., Labrosse, S., Poitou, C., 2009. Modelling the palaeo-evolution of the geodynamo. *Geophys. J. Int.* 179 (3), 1414–1428. <https://doi.org/10.1111/j.1365-246X.2009.04361.x/3/179-3-1414-FIG012.JPEG>.
- Bartels, K.S., Grove, T.L., 1991. High pressure experiments on magnesian eucrite compositions: constraints on magmatic processes in the eucrite parent body. *Proc. Lunar Planet. Sci.* 21, 351–365.
- Bercovici, H.L., Elkins-Tanton, L.T., O'Rourke, J.G., Schaefer, L., 2022. The effects of bulk composition on planetesimal core sulfur content and size. *Icarus* 380, 114976. <https://doi.org/10.1016/j.icarus.2022.114976>.
- Borlina, C.S., Weiss, B.P., Bryson, J.F.J., Armitage, P.J., 2022. Lifetime of the outer solar system nebula from carbonaceous chondrites. *J. Geophys. Res. Planets* 127 (7), e2021JE007139. <https://doi.org/10.1029/2021JE007139>.
- Borlina, C.S., Weiss, B.P., Bryson, J.F.J., Bai, X.-N., Lima, E.A., Chatterjee, N., Mansbach, E.N., 2021. Paleomagnetic evidence for a disk substructure in the early solar system. *Sci. Adv.* 7 (42), eabj6928. <https://doi.org/10.1126/sciadv.abj6928>.
- Braginsky, S.I., 1963. Structure of the f layer and reasons for convection in the Earth's core. *Sov. Phys. Dokl.* 149, 8–10.
- Bryson, J.F., Neufeld, J.A., Nimmo, F., 2019a. Constraints on asteroid magnetic field evolution and the radii of meteorite parent bodies from thermal modelling. *Earth Planet. Sci. Lett.* 521, 68–78. <https://doi.org/10.1016/j.epsl.2019.05.046>.
- Bryson, J.F., Nichols, C.I., Herrero-Albillos, J., Kronast, F., Kasama, T., Alimadadi, H., Van Der Laan, G., Nimmo, F., Harrison, R.J., 2015. Long-lived magnetism from solidification-driven convection on the pallasite parent body. *Nature* 517 (7535), 472–475. <https://doi.org/10.1038/nature14114>.
- Bryson, J.F.J., Nichols, C.I.O., Mac Niocaill, C., 2023. A unified intensity of the magnetic field in the protoplanetary disk from the Winchcombe meteorite. *Meteorit. Planet. Sci.* n/a (n/a), 1–22. <https://doi.org/10.1111/maps.14079>.
- Bryson, J.F.J., Weiss, B.P., Biersteker, J.B., King, A.J., Russell, S.S., 2020a. Constraints on the distances and timescales of solid migration in the early solar system from meteorite magnetism. *Astrophys. J.* 896 (2), 103. <https://doi.org/10.3847/1538-4357/ab91ab>.
- Bryson, J.F.J., Weiss, B.P., Getzin, B., Abrahams, J.N.H., Nimmo, F., Scholl, A., 2019b. Paleomagnetic evidence for a partially differentiated ordinary chondrite parent asteroid. *J. Geophys. Res. Planets* 124 (7), 1880–1898. <https://doi.org/10.1029/2019JE005951>.
- Bryson, J.F.J., Weiss, B.P., Lima, E.A., Gattacceca, J., Cassata, W.S., 2020b. Evidence for asteroid scattering and distal solar system solids from meteorite paleomagnetism. *Astrophys. J.* 892 (2), 126. <https://doi.org/10.3847/1538-4357/ab7cd4>.
- Buffett, B.A., Huppert, H.E., Lister, J.R., Woods, A.W., 1996. On the thermal evolution of the Earth's core. *J. Geophys. Res. Solid Earth* 101 (B4), 7989–8006. <https://doi.org/10.1029/95JB03539>.
- Buono, A.S., Walker, D., 2011. The Fe-rich liquidus in the Fe–FeS system from 1 bar to 10 GPa. *Geochim. Cosmochim. Acta* 75 (8), 2072–2087. <https://doi.org/10.1016/j.gca.2011.01.030>.
- Carporzen, L., Weiss, B.P., Elkins-Tanton, L.T., Shuster, D.L., Ebel, D., Gattacceca, J., 2011. Magnetic evidence for a partially differentiated carbonaceous chondrite parent body. *Proc. Natl. Acad. Sci.* 108 (16), 6386–6389. <https://doi.org/10.1073/pnas.1017165108>.
- Castillo-Rogez, J., Johnson, T.V., Lee, M.H., Turner, N.J., Matson, D.L., Lunine, J., 2009. 26Al decay: Heat production and a revised age for Iapetus. *Icarus* 204 (2), 658–662. <https://doi.org/10.1016/j.icarus.2009.07.025>.
- Cheng, J.S., Stellmach, S., Ribeiro, A., Grannan, A., King, E.M., Aurnou, J.M., 2015. Laboratory-numerical models of rapidly rotating convection in planetary cores. *Geophys. J. Int.* 201 (1), 1–17. <https://doi.org/10.1093/gji/ggu480>.
- Christensen, U.R., 2009. Dynamo scaling laws and applications to the planets. *Space Sci. Rev.* 152 (1), 565–590. <https://doi.org/10.1007/S11214-009-9553-2>.
- Christensen, U.R., 2015. Iron snow dynamo models for Ganymede. *Icarus* 247, 248–259. <https://doi.org/10.1016/j.icarus.2014.10.024>.
- Christensen, U.R., Aubert, J., 2006. Scaling properties of convection-driven dynamos in rotating spherical shells and application to planetary magnetic fields. *Geophys. J. Int.* 166 (1), 97–114. <https://doi.org/10.1111/j.1365-246X.2006.03009.x>.
- Cook, D.L., Meyer, B.S., Schönbächler, M., 2021. Iron and nickel isotopes in IID and IVB iron meteorites: Evidence for admixture of an SN II component and implications for the initial abundance of 60Fe. *Astrophys. J.* 917 (2), 59. <https://doi.org/10.3847/1538-4357/ac0add>.
- Cournede, C., Gattacceca, J., Gounelle, M., Rochette, P., Weiss, B.P., Zanda, B., 2015. An early solar system magnetic field recorded in CM chondrites. *Earth Planet. Sci. Lett.* 410, 62–74. <https://doi.org/10.1016/j.epsl.2014.11.019>.
- Davaille, A., Jaupart, C., 1993. Transient high-Rayleigh-number thermal convection with large viscosity variations. *J. Fluid Mech.* 253, 141–166. <https://doi.org/10.1017/S0022112093001740>.
- Davidson, P.A., 2013. Scaling laws for planetary dynamos. *Geophys. J. Int.* 195 (1), 67–74. <https://doi.org/10.1093/gji/ggt167>.
- Davies, C.J., Bono, R.K., Meduri, D.G., Aubert, J., Greenwood, S., Biggin, A.J., 2022. Dynamo constraints on the long-term evolution of Earth's magnetic field strength. *Geophys. J. Int.* 228 (1), 316–336. <https://doi.org/10.1093/gji/ggab342>.
- Davies, C.J., Pommier, A., 2018. Iron snow in the Martian core? *Earth Planet. Sci. Lett.* 481, 189–200. <https://doi.org/10.1016/j.epsl.2017.10.026>.
- de Wijs, G.A., Kresse, G., Vočadlo, L., Dobson, D., Alfè, D., Gillan, M.J., Price, G.D., 1998. The viscosity of liquid iron at the physical conditions of the Earth's core. *Nature* 392 (6678), 805–807. <https://doi.org/10.1038/33905>.
- Deschamps, F., Vilella, K., 2021. Scaling laws for mixed-heated stagnant-lid convection and application to Europa. *J. Geophys. Res. Planets* 126 (10), e2021JE006963. <https://doi.org/10.1029/2021JE006963>.
- Dodds, K.H., Bryson, J.F., Neufeld, J.A., Harrison, R.J., 2021. The thermal evolution of planetesimals during accretion and differentiation: Consequences for dynamo generation by thermally-driven convection. *J. Geophys. Res. Planets* 126 (3), <https://doi.org/10.1029/2020JE006704>.
- Dodds, K.H., Bryson, J.F.J., Neufeld, J.A., Harrison, R.J., 2025. The direction of core solidification in asteroids: Implications for dynamo generation. *Icarus* 425, 116319. <https://www.sciencedirect.com/science/article/pii/S0019103524003798>.
- Doyle, P.M., Jogo, K., Nagashima, K., Krot, A.N., Wakita, S., Ciesla, F.J., Hutcheon, I.D., 2015. Early aqueous activity on the ordinary and carbonaceous chondrite parent bodies recorded by fayalite. *Nature Commun.* 6 (1), 7444. <https://doi.org/10.1038/ncomms8444>.
- Elkins-Tanton, L.T., Weiss, B.P., Zuber, M.T., 2011. Chondrites as samples of differentiated planetesimals. *Earth Planet. Sci. Lett.* 305 (1), 1–10. <https://doi.org/10.1016/j.epsl.2011.03.010>.
- Faroughi, S.A., Huber, C., 2015. A generalized equation for rheology of emulsions and suspensions of deformable particles subjected to simple shear at low Reynolds number. *Rheol. Acta* 54 (2), 85–108. <https://doi.org/10.1007/s00397-014-0825-8>.
- Frank-Kamenetskii, D., 1969. *Diffusion and Heat Exchange in Chemical Kinetics*. Plenum Press, New York, (translation by JP Appleton).
- Fu, R.R., Elkins-Tanton, L.T., 2014. The fate of magmas in planetesimals and the retention of primitive chondritic crusts. *Earth Planet. Sci. Lett.* 390, 128–137. <https://doi.org/10.1016/j.epsl.2013.12.047>.
- Fu, R.R., Kehayias, P., Weiss, B.P., Schrader, D.L., Bai, X.-N., Simon, J.B., 2020. Weak magnetic fields in the outer solar nebula recorded in CR chondrites. *J. Geophys. Res. Planets* 125 (5), e2019JE006260. <https://doi.org/10.1029/2019JE006260>.
- Fu, R.R., Weiss, B.P., Lima, E.A., Harrison, R.J., Bai, X.-N., Desch, S.J., Ebel, D.S., Suavet, C., Wang, H., Glenn, D., Le Sage, D., Kasama, T., Walsworth, R.L., Kuan, A.T., 2014. Solar nebula magnetic fields recorded in the Semarkona meteorite. *Science* 346 (6213), 1089–1092. <https://doi.org/10.1126/science.1258022>.
- Fu, R.R., Weiss, B.P., Shuster, D.L., Gattacceca, J., Grove, T.L., Suavet, C., Lima, E.A., Li, L., Kuan, A.T., 2012. An ancient core dynamo in asteroid Vesta. *Science* 338 (6104), 238–241. <https://doi.org/10.1126/science.1225648>.
- Ghosh, A., McSweeney, H.Y., 1998. A thermal model for the differentiation of asteroid 4 Vesta, based on radiogenic heating. *Icarus* 134 (2), 187–206. <https://doi.org/10.1006/icar.1998.5956>.

- Ghosh, A., McSween, H.Y., 1999. Temperature dependence of specific heat capacity and its effect on asteroid thermal models. *Meteorit. Planet. Sci.* 34 (1), 121–127. <http://dx.doi.org/10.1111/j.1945-5100.1999.tb01737.x>.
- Giordano, D., Russell, J.K., Dingwell, D.B., 2008. Viscosity of magmatic liquids: A model. *Earth Planet. Sci. Lett.* 271 (1), 123–134. <http://dx.doi.org/10.1016/j.epsl.2008.03.038>.
- Goldstein, J.I., Scott, E.R.D., Chabot, N.L., 2009. Iron meteorites: Crystallization, thermal history, parent bodies, and origin. *Geochemistry* 69 (4), 293–325. <http://dx.doi.org/10.1016/j.chemer.2009.01.002>.
- Grott, M., Breuer, D., Laneuville, M., 2011. Thermo-chemical evolution and global contraction of mercury. *Earth Planet. Sci. Lett.* 307 (1), 135–146. <http://dx.doi.org/10.1016/j.epsl.2011.04.040>.
- Gubbins, D., 1977. Energetics of the Earth's core. *J. Geophys.* 43 (1), 453–464.
- Gubbins, D., Alfè, D., Masters, G., Price, G.D., Gillan, M.J., 2003. Can the Earth's dynamo run on heat alone? *Geophys. J. Int.* 155 (2), 609–622. <http://dx.doi.org/10.1046/j.1365-246X.2003.02064.x>.
- Henke, S., Gail, H.P., Tieloff, M., Schwarz, W.H., 2013. Thermal evolution model for the chondritic asteroid-instantaneous formation versus protracted accretion. *Icarus* 226 (1), 212–228. <http://dx.doi.org/10.1016/j.icarus.2013.05.034>.
- Hevey, P.J., Sanders, I.S., 2006. A model for planetesimal meltdown by 26Al and its implications for meteorite parent bodies. *Meteorit. Planet. Sci.* 41 (1), 95–106. <http://dx.doi.org/10.1111/j.1945-5100.2006.tb00195.x>.
- Hilton, C.D., Ash, R.D., Walker, R.J., 2022. Chemical characteristics of iron meteorite parent bodies. *Geochim. Cosmochim. Acta* 318, 112–125. <http://dx.doi.org/10.1016/j.gca.2021.11.035>.
- Hirschmann, M.M., 2000. Mantle solidus: Experimental constraints and the effects of peridotite composition. *Geochim. Geophys. Geosyst.* 1 (10), <http://dx.doi.org/10.1029/2000GC000070>.
- Hirschmann, M.M., Bergin, E.A., Blake, G.A., Ciesla, F.J., Li, J., 2021. Early volatile depletion on planetesimals inferred from C–S systematics of iron meteorite parent bodies. *Proc. Natl. Acad. Sci.* 118 (13), e2026779118. <http://dx.doi.org/10.1073/pnas.2026779118>.
- Hirth, G., Kohlstedt, D., 2003. Rheology of the upper mantle and the mantle wedge: A view from the experimentalists. In: *Inside the Subduction Factory*. In: *Geophysical Monograph Series*, vol. 138, American Geophysical Union, pp. 83–105. <http://dx.doi.org/10.1029/138GM06>.
- Hu, X., Zhu, Z., Okuzumi, S., Bai, X.-N., Wang, L., Tomida, K., Stone, J.M., 2019. Nonideal MHD simulation of HL tau disk: Formation of rings. *Astrophys. J.* 885 (1), 36. <http://dx.doi.org/10.3847/1538-4357/ab44cb>.
- Huguet, L., Le Bars, M., Deguen, R., 2023. A laboratory model for iron snow in planetary cores. *Geophys. Res. Lett.* 50 (24), e2023GL105697. <http://dx.doi.org/10.1029/2023GL105697>.
- Kaminski, E., Limare, A., Kenda, B., Chausson, M., 2020. Early accretion of planetesimals unraveled by the thermal evolution of the parent bodies of magmatic iron meteorites. *Earth Planet. Sci. Lett.* 548, 116469. <http://dx.doi.org/10.1016/j.epsl.2020.116469>.
- Keil, K., Wilson, L., 1993. Explosive volcanism and the compositions of cores of differentiated asteroids. *Earth Planet. Sci. Lett.* 117 (1), 111–124. [http://dx.doi.org/10.1016/0012-821X\(93\)90121-O](http://dx.doi.org/10.1016/0012-821X(93)90121-O).
- Konôpková, Z., McWilliams, R.S., Gómez-Pérez, N., Goncharov, A.F., 2016. Direct measurement of thermal conductivity in solid iron at planetary core conditions. *Nature* 534 (7605), 99–101. <http://dx.doi.org/10.1038/nature18009>.
- Kruijer, T.S., Touboul, M., Fischer-Gödde, M., Bermingham, K.R., Walker, R.J., Kleine, T., 2014. Protracted core formation and rapid accretion of protoplanets. *Science* 344 (6188), 1150–1154. <http://dx.doi.org/10.1126/science.1251766>.
- Lichtenberg, T., Golabek, G.J., Burn, R., Meyer, M.R., Alibert, Y., Gerya, T.V., Mordasini, C., 2019a. A water budget dichotomy of rocky protoplanets from 26Al-heating. *Nat. Astron.* 3 (4), 307–313. <http://dx.doi.org/10.1038/s41550-018-0688-5>.
- Lichtenberg, T., Keller, T., Katz, R.F., Golabek, G.J., Gerya, T.V., 2019b. Magma ascent in planetesimals: Control by grain size. *Earth Planet. Sci. Lett.* 507, 154–165. <http://dx.doi.org/10.1016/j.epsl.2018.11.034>.
- Lister, J.R., 2003. Expressions for the dissipation driven by convection in the Earth's core. *Phys. Earth Planet. Inter.* 140 (1), 145–158. <http://dx.doi.org/10.1016/j.pepi.2003.07.007>.
- Lodders, K., 2021. Relative atomic solar system abundances, mass fractions, and atomic masses of the elements and their isotopes, composition of the solar photosphere, and compositions of the major chondritic meteorite groups. *Space Sci. Rev.* 217 (3), 44. <http://dx.doi.org/10.1007/s11214-021-00825-8>.
- MacPherson, G.J., Davis, A.M., Zinner, E.K., 1995. The distribution of aluminum-26 in the early solar system—a reappraisal. *Meteoritics* 30 (4), 365–386. <http://dx.doi.org/10.1111/j.1945-5100.1995.tb01141.x>.
- Maurel, C., Bryson, J.F.J., Shah, J., Chopdekar, R.V., T. Elkins-Tanton, L., A. Raymond, C., Weiss, B.P., 2021. A long-lived planetesimal dynamo powered by core crystallization. *Geophys. Res. Lett.* 48 (6), e2020GL091917. <http://dx.doi.org/10.1029/2020GL091917>.
- Maurel, C., Gattacceca, J., 2024. A 4,565-My-old record of the solar nebula field. *Proc. Natl. Acad. Sci.* 121 (12), e2312802121. <http://dx.doi.org/10.1073/pnas.2312802121>.
- McCoy, T.J., Dickinson, T.L., Lofgren, G.E., 1999. Partial melting of the Indarch (EH4) meteorite: A textural, chemical, and phase relations view of melting and melt migration. *Meteorit. Planet. Sci.* 34 (5), 735–746. <http://dx.doi.org/10.1111/j.1945-5100.1999.tb01386.x>.
- Merk, R., Breuer, D., Spohn, T., 2002. Numerical modeling of 26Al-induced radioactive melting of asteroids considering accretion. *Icarus* 159 (1), 183–191. <http://dx.doi.org/10.1006/icar.2002.6872>.
- Michaut, C., Neufeld, J.A., 2022. Formation of the lunar primary crust from a long-lived slushy magma ocean. *Geophys. Res. Lett.* 49 (2), e2021GL095408. <http://dx.doi.org/10.1029/2021GL095408>.
- Monnereau, M., Guignard, J., Néri, A., Toplis, M.J., Quitté, G., 2023. Differentiation time scales of small rocky bodies. *Icarus* 390, 115294. <http://dx.doi.org/10.1016/j.icarus.2022.115294>.
- Morard, G., Bouchet, J., Rivoldini, A., Antonangeli, D., Roberge, M., Boulard, E., Denoed, A., Mezouar, M., 2018. Liquid properties in the Fe-FeS system under moderate pressure: Tool box to model small planetary cores. *Am. Mineral.* 103 (11), 1770–1779. <http://dx.doi.org/10.2138/am-2018-6405>.
- Morschhauser, A., Grott, M., Breuer, D., 2011. Crustal recycling, mantle dehydration, and the thermal evolution of Mars. *Icarus* 212 (2), 541–558. <http://dx.doi.org/10.1016/j.icarus.2010.12.028>.
- Moskovitz, N., Gaidos, E., 2011. Differentiation of planetesimals and the thermal consequences of melt migration. *Meteorit. Planet. Sci.* 46 (6), 903–918. <http://dx.doi.org/10.1111/j.1945-5100.2011.01201.x>.
- Néri, A., Guignard, J., Monnereau, M., Bystricky, M., Perrillat, J.-P., Andrault, D., King, A., Guignot, N., Tenaillon, C., Duployer, B., Toplis, M.J., Quitté, G., 2020. Reevaluation of metal interconnectivity in a partially molten silicate matrix using 3D microtomography. *Phys. Earth Planet. Inter.* 308, 106571. <http://dx.doi.org/10.1016/j.pepi.2020.106571>.
- Neufeld, J.A., Bryson, J.F., Nimmo, F., 2019. The top-down solidification of iron asteroids driving dynamo evolution. *J. Geophys. Res. Planets* 124 (5), 1331–1356. <http://dx.doi.org/10.1029/2018JE005900>.
- Neumann, W., Breuer, D., Spohn, T., 2012. Differentiation and core formation in accreting planetesimals. *Astron. Astrophys.* 543, A141. <http://dx.doi.org/10.1051/0004-6361/201219157>.
- Neumann, W., Breuer, D., Spohn, T., 2014. Differentiation of Vesta: Implications for a shallow magma ocean. *Earth Planet. Sci. Lett.* 395, 267–280. <http://dx.doi.org/10.1016/j.epsl.2014.03.033>.
- Neumann, W., Henke, S., Breuer, D., Gail, H.-P., Schwarz, W.H., Tieloff, M., Hopp, J., Spohn, T., 2018. Modeling the evolution of the parent body of acapulcoites and lodranites: A case study for partially differentiated asteroids. *Icarus* 311, 146–169. <http://dx.doi.org/10.1016/j.icarus.2018.03.024>.
- Newcombe, M.E., Nielsen, S.G., Peterson, L.D., Wang, J., Alexander, C.M.O., Sarafian, A.R., Shimizu, K., Nittler, L.R., Irving, A.J., 2023. Degassing of early-formed planetesimals restricted water delivery to Earth. *Nature* 615 (7954), 854–857. <http://dx.doi.org/10.1038/s41586-023-05721-5>.
- Nichols, C.I., Bryson, J.F., Cottrell, R.D., Fu, R.R., Harrison, R.J., Herrero-Albillos, J., Kronast, F., Tarduno, J.A., Weiss, B.P., 2021. A time-resolved paleomagnetic record of main group pallasites: Evidence for a large-cored, thin-mantled parent body. *J. Geophys. Res. Planets* 126 (7), e2021JE006900. <http://dx.doi.org/10.1029/2021JE006900>.
- Nimmo, F., 2007. *Energetics of the core*. In: *Treatise on Geophysics*, first ed. vol. 8, Elsevier, Amsterdam ; Boston, pp. 33–62.
- Nimmo, F., 2009. Energetics of asteroid dynamos and the role of compositional convection. *Geophys. Res. Lett.* 36 (10), <http://dx.doi.org/10.1029/2009GL013797>.
- Nimmo, F., Stevenson, D.J., 2000. Influence of early plate tectonics on the thermal evolution and magnetic field of Mars. *J. Geophys. Res. Planets* 105 (E5), 11969–11979. <http://dx.doi.org/10.1029/1999JE001216>.
- Opeil, C.P., Consolmagno, G.J., Britt, D.T., 2010. The thermal conductivity of meteorites: New measurements and analysis. *Icarus* 208 (1), 449–454. <http://dx.doi.org/10.1016/j.icarus.2010.01.021>.
- Peterson, L.D., Newcombe, M.E., Alexander, C.M.O., Wang, J., Klein, F., Bekaert, D.V., Nielsen, S.G., 2023. The H content of aubrites: An evaluation of bulk versus in situ methods for quantifying water in meteorites. *Earth Planet. Sci. Lett.* 620, 118341. <http://dx.doi.org/10.1016/j.epsl.2023.118341>.
- Pozzo, M., Davies, C., Gubbins, D., Alfè, D., 2013. Transport properties for liquid silicon-oxygen-iron mixtures at Earth's core conditions. *Phys. Rev. B* 87 (1), 014110. <http://dx.doi.org/10.1103/PhysRevB.87.014110>.
- Rückriemen, T., Breuer, D., Spohn, T., 2015. The Fe snow regime in Ganymede's core: A deep-seated dynamo below a stable snow zone. *J. Geophys. Res. Planets* 120 (6), 1095–1118. <http://dx.doi.org/10.1002/2014JE004781>.
- Rückriemen, T., Breuer, D., Spohn, T., 2018. Top-down freezing in a Fe-FeS core and Ganymede's present-day magnetic field. *Icarus* 307, 172–196. <http://dx.doi.org/10.1016/j.icarus.2018.02.021>.
- Ruedas, T., 2017. Radioactive heat production of six geologically important nuclides. *Geochim. Geophys. Geosyst.* 18 (9), 3530–3541. <http://dx.doi.org/10.1002/2017GC006997>.
- Rushmer, T., Minarik, W.G., Taylor, G.J., 2000. Physical processes of core formation. In: *Canup, R.M., Righter, K. (Eds.), Origin of the Earth and Moon*. University of Arizona Press, pp. 227–244. <http://dx.doi.org/10.2307/j.ctv1v7zdrp.19>.

- Russell, C.T., Raymond, C.A., Ammannito, E., Buczkowski, D.L., De Sanctis, M.C., Hiesinger, H., Jaumann, R., Konopliv, A.S., McSween, H.Y., Nathues, A., Park, R.S., Pieters, C.M., Prettyman, T.H., McCord, T.B., McFadden, L.A., Mottola, S., Zuber, M.T., Joy, S.P., Polanskey, C., Rayman, M.D., Castillo-Rogez, J.C., Chi, P.J., Combe, J.P., Ermakov, A., Fu, R.R., Hoffmann, M., Jia, Y.D., King, S.D., Lawrence, D.J., Li, J.-Y., Marchi, S., Preusker, F., Roatsch, T., Ruesch, O., Schenk, P., Villarreal, M.N., Yamashita, N., 2016. Dawn arrives at Ceres: Exploration of a small, volatile-rich world. *Science* 353 (6303), 1008–1010. <http://dx.doi.org/10.1126/science.aaf4219>.
- Sanderson, H.R., Bryson, J.F.J., Nichols, C.I.O., 2024. Early and elongated epochs of planetesimal dynamo generation. <http://dx.doi.org/10.48550/arXiv.2405.05147>.
- Scheinberg, A., Elkins-Tanton, L.T., Schubert, G., Bercovici, D., 2016. Core solidification and dynamo evolution in a mantle-stripped planetesimal. *J. Geophys. Res. Planets* 121 (1), 2–20. <http://dx.doi.org/10.1002/2015JE004843>.
- Schubert, G., Turcotte, D.L., Olson, P., 2001. *Mantle Convection in the Earth and Planets*. Cambridge University Press, Cambridge, UNITED KINGDOM.
- Scott, T., Kohlstedt, D.L., 2006. The effect of large melt fraction on the deformation behavior of peridotite. *Earth Planet. Sci. Lett.* 246 (3–4), 177–187. <http://dx.doi.org/10.1016/J.EPSL.2006.04.027>.
- Solomatov, V.S., 1995. Scaling of temperature-and stress-dependent viscosity convection. *Phys. Fluids* 7, 266. <http://dx.doi.org/10.1063/1.868624>.
- Sterenborg, M.G., Crowley, J.W., 2012. Thermal evolution of early solar system planetesimals and the possibility of sustained dynamos. *Phys. Earth Planet. Inter.* <http://dx.doi.org/10.1016/j.pepi.2012.10.006>.
- Sturtz, C., Limare, A., Tait, S., Kaminski, É., 2022. Birth and decline of magma oceans in planetesimals: 2. Structure and thermal history of early accreted small planetary bodies. *J. Geophys. Res. Planets* 127 (12), e2021JE007020. <http://dx.doi.org/10.1029/2021JE007020>.
- Tarduno, J.A., Cottrell, R.D., Nimmo, F., Hopkins, J., Voronov, J., Erickson, A., Blackman, E., Scott, E.R., McKinley, R., 2012. Evidence for a dynamo in the main group pallasite parent body. *Science* 338 (6109), 939–942. <http://dx.doi.org/10.1126/science.1223932>.
- Tassin, T., Gastine, T., Fournier, A., 2021. Geomagnetic semblance and dipolar–multipolar transition in top-heavy double-diffusive geodynamo models. *Geophys. J. Int.* 226 (3), 1897–1919. <http://dx.doi.org/10.1093/GJI/GGAB161>.
- Thiriet, M., Breuer, D., Michaut, C., Plesa, A.-C., 2019. Scaling laws of convection for cooling planets in a stagnant lid regime. *Phys. Earth Planet. Inter.* 286, 138–153. <http://dx.doi.org/10.1016/j.pepi.2018.11.003>.
- Tosi, N., Grott, M., Plesa, A.-C., Breuer, D., 2013. Thermochemical evolution of Mercury's interior. *J. Geophys. Res. Planets* 118 (12), 2474–2487. <http://dx.doi.org/10.1002/jgre.20168>.
- Wang, H., Weiss, B.P., Bai, X.-N., Downey, B.G., Wang, J., Wang, J., Suavet, C., Fu, R.R., Zucolotto, M.E., 2017. Lifetime of the solar nebula constrained by meteorite paleomagnetism. *Science* 355 (6325), 623–627. <http://dx.doi.org/10.1126/science.aaf5043>.
- Wardle, M., 2007. Magnetic fields in protoplanetary disks. *Astrophys. Space Sci.* 311 (1), 35–45. <http://dx.doi.org/10.1007/s10509-007-9575-8>.
- Weidenschilling, S.J., 2019. Accretion of the asteroids: Implications for their thermal evolution. *Meteorit. Planet. Sci.* 54 (5), 1115–1132. <http://dx.doi.org/10.1111/maps.13270>.
- Weiss, B.P., Bai, X.-N., Fu, R.R., 2021. History of the solar nebula from meteorite paleomagnetism. *Sci. Adv.* 7 (1), eaba5967. <http://dx.doi.org/10.1126/sciadv.aba5967>.
- Weiss, B.P., Gattacceca, J., Stanley, S., Rochette, P., Christensen, U.R., 2010. Paleomagnetic records of meteorites and early planetesimal differentiation. *Space Sci. Rev.* 152 (1), 341–390. <http://dx.doi.org/10.1007/s11214-009-9580-z>.
- Weiss, B.P., Wang, H., Sharp, T.G., Gattacceca, J., Shuster, D.L., Downey, B., Hu, J., Fu, R.R., Kuan, A.T., Suavet, C., Irving, A.J., Wang, J., Wang, J., 2017. A nonmagnetic differentiated early planetary body. *Earth Planet. Sci. Lett.* 468, 119–132. <http://dx.doi.org/10.1016/j.epsl.2017.03.026>.
- Williams, Q., 2009. Bottom-up versus top-down solidification of the cores of small solar system bodies: Constraints on paradoxical cores. *Earth Planet. Sci. Lett.* 284 (3–4), 564–569. <http://dx.doi.org/10.1016/J.EPSL.2009.05.019>.
- Wilson, L., Goodrich, C.A., Van Orman, J.A., 2008. Thermal evolution and physics of melt extraction on the ureilite parent body. *Geochim. Cosmochim. Acta* 72 (24), 6154–6176. <http://dx.doi.org/10.1016/j.gca.2008.09.025>.
- Yomogida, K., Matsui, T., 1984. Multiple parent bodies of ordinary chondrites. *Earth Planet. Sci. Lett.* 68 (1), 34–42. [http://dx.doi.org/10.1016/0012-821X\(84\)90138-9](http://dx.doi.org/10.1016/0012-821X(84)90138-9).