

Scattering analysis of LOFAR pulsar observations

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Accepted 2017 May 9. Received 2017 May 4; in original form 2017 February 14

ABSTRACT

We measure the effects of interstellar scattering on average pulse profiles from 13 radio pulsars with simple pulse shapes. We use data from the LOFAR High Band Antennas, at frequencies between 110 and 190 MHz. We apply a forward fitting technique, and simultaneously determine the intrinsic pulse shape, assuming single Gaussian component profiles. We find that the constant τ , associated with scattering by a single thin screen, has a power-law dependence on frequency $\tau \propto \nu^{-\alpha}$, with indices ranging from $\alpha = 1.50$ to 4.0, despite simplest theoretical models predicting $\alpha = 4.0$ or 4.4. Modelling the screen as an isotropic or extremely anisotropic scatterer, we find anisotropic scattering fits lead to larger power-law indices, often in better agreement with theoretically expected values. We compare the scattering models based on the inferred, frequency-dependent parameters of the intrinsic pulse, and the resulting correction to the dispersion measure (DM). We highlight the cases in which fits of extreme anisotropic scattering are appealing, while stressing that the data do not strictly favour either model for any of the 13 pulsars. The pulsars show anomalous scattering properties that are consistent with finite scattering screens and/or anisotropy, but these data alone do not provide the means for an unambiguous characterization of the screens. We revisit the empirical τ versus DM relation and consider how our results support a frequency dependence of α . Very long baseline interferometry, and observations of the scattering and scintillation properties of these sources at higher frequencies, will provide further evidence.

Key words: scattering – pulsars: general – ISM: structure.

1 INTRODUCTION

Prominent evidence for radio wave scattering comes from observing that average pulsar profiles grow asymmetrically broader at low frequencies (e.g. Löhmer et al. 2001). These observed *scattering tails* represent the power of the pulsar delayed through multipath propagation in the ionized interstellar medium (ISM). The exponential

broadening of the pulse profiles is parametrized by a characteristic scattering time-scale, τ .

From the variety of propagation effects associated with radio waves travelling through the ISM, interstellar scattering is expected to display the strongest frequency (ν) dependence. The strong dependence on frequency is caused by inhomogeneities in the electron density gradients of the ISM along the line of sight to the pulsar (Salpeter 1967; Scheuer 1968).

Different models of the ISM predict different frequency dependencies. Many theoretical models make use of the *thin screen approximation*, by which it is assumed the scattering along the line

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of sight to the pulsar can be approximated by a single-scattering surface approximately mid-way to pulsar, which is infinitely extended transverse to the line of sight and thin along the line of sight (e.g. Williamson 1972). Modelling the inhomogeneities of such a thin screen as a Kolmogorov turbulence in a cold plasma, leads to a dependence of scattering time-scales proportional to $\nu^{-4.4}$ (Lee & Jokipii 1976; Rickett 1977). A more simple approach, by which the scattering is assumed to be isotropic and described by a circularly symmetric Gaussian distribution in scattering angles, leads to a dependence of $\tau \propto \nu^{-4}$ (Cronyn 1970; Lang 1971).

Observations of scatter broadened pulsars have led to measurements of the power-law index α (where $\tau \propto \nu^{-\alpha}$) in agreement with the theoretical models, as well as to deviations of α from 4 or 4.4. Notably Löhmer et al. (2001) found a mean value of $\bar{\alpha} = 3.44 \pm 0.13$ from the scatter broadening measurements of nine pulsars, at frequencies between 600 MHz and 2.7 GHz. The pulsars in the study were selected to have large dispersion measure (DM) values, and as such the authors argue that the low α values could be due to multiple finite scattering screens along the long lines of sights to the sources.

More recently, Lewandowski et al. (2013) measured α values in the range 2.77–4.59 (from 25 sources), and Lewandowski, Kowalińska & Kijak (2015a) published a similar range of 2.61–5.61 (based on 60 sources). In both cases, even lower α values than these were found, but were considered spurious and were subsequently disregarded from the analysis. Their measurements were based on observations with the Giant Meterwave Radio Telescope (GMRT, Pune India) between 325 MHz and 1.2 GHz, and with the 100 m Effelsberg Radiotelescope (2.6–8.35 GHz) as well as published scattering times from the literature.

Additionally, low-frequency scattering and scintillation studies conducted at the Pushchino Radio Astronomy Observatory in Russia, have measured α values below the theoretically expected values (Kuzmin & Losovsky 2007; Smirnova & Shishov 2008). The observatory hosts the Large Phased Array (LPA or BSA) and the DKR-1000 telescope operating at 111.9 MHz and 41, 62.4 and 88.6 MHz, respectively.

Space-ground interferometry, which combined the efforts of the 10-m Space Radio Telescope aboard *RadioAstron*, the Arecibo telescope and the Westerbork Synthesis Radio Telescope, have led to observations with a 220 000 km projected baseline, and unprecedented resolution at metre wavelengths. Studying the scattering towards the nearby pulsar B0950+08 with this interferometer, Smirnova et al. (2014) inferred two independent scattering surfaces along the line of sight, and an α value of 3.00 ± 0.08 .

Flatter τ spectra, i.e. spectra for which $\alpha < 4$, have been reasoned to be due to anomalous scattering mechanisms and geometries. This includes scattering by a finite (truncated) scattering screen (Cordes & Lazio 2001), the impact of an inner cut-off scale (Rickett et al. 2009) and anisotropic scattering mechanisms (Stinebring et al. 2001; Tuntsov, Bignall & Walker 2012). Ionized gas clouds in the ISM, as small as an order of astronomical unit in transverse radius, have been promoted by e.g. Walker (2001) to explain extreme scattering events (ESEs) observed in quasars. ESEs have also been observed in pulsars (e.g. Cognard et al. 1993; Coles et al. 2015) and may be associated with the same ISM structures.

Evidence for anisotropic scattering has especially come from organized patterns in the dynamic spectra of pulsar observations (Gupta, Rickett & Lyne 1994). These patterns translate to parabolic arc features in the secondary (power) spectra, which are considered to be tell-tale signs of anisotropic scattering (Stinebring et al. 2001; Walker et al. 2004).

In a previous paper, we have shown that fitting anisotropically scattered (simulated) data with an isotropic model can lead to α values less than the theoretically predicted value (Geyer & Karastergiou 2016, hereafter GK16). As an extension of Cordes & Lazio (2001), we also showed how non-circular scattering screens at locations off-centred with respect to the direct line of sight, lead to low α values. In our chosen examples, the theoretical setups lead to α values as low as 2.9.

The proposed mechanisms for obtaining smaller α values have certainly led to an improved understanding of correlations between ISM structure and pulsar scattering, but the detailed structure of the ISM and the physical interpretation (e.g. the distribution and size of anomalous scattering clouds) remain unclear. It also remains to be investigated to what extent observations promote an evolution of α with frequency.

Low-frequency data sets, due to the strong expected dependence of scatter broadening on frequency, are ideal for investigating scattering effects and ISM structure in depth. In this paper, we analyse the scatter broadening of 13 pulsars using the core of the Low Frequency Array (LOFAR; Stappers et al. 2011; van Haarlem et al. 2013). LOFAR provides not only access to low-frequency data, but also a broad-band at these low frequencies. This allows us to channelize the data into several high signal-to-noise (S/N) average profiles within the band, such that a detailed τ spectrum can be calculated. We fit the scatter broadened profiles with two scattering models: an isotropic thin screen scattering model and an extremely anisotropic scattering model (AM). The broadening functions associated with each of these models are described in Section 3.

The paper aims to answer the following questions:

- (i) Are anisotropic scattering mechanisms and/or finite scattering screens required to fit our data set, or are isotropic mechanisms sufficient?
- (ii) What are the mean values of α obtained for this set of pulsars, and how do the values differ with scattering models?
- (iii) What additional information regarding the profile evolution and DM can we derive from the fits for scattering?
- (iv) Do we have any evidence for correlations between flux density and scattering from the data?

The paper is organized as follows: in Section 2, we describe the LOFAR data sets and subsequent data reduction. Thereafter, in Section 3, we discuss the fitting methods used to extract τ values from the scattered profiles. In Section 4, we present a scattering analysis for each pulsar independently, supplemented by the Supporting Information (Online Appendix). Thereafter in Section 5, we discuss our results, returning to the questions posed above.

2 OBSERVATIONS AND DATA REDUCTION

An overview of the 13 chosen sources and their associated parameters is given in Table 1. Three different LOFAR data sets are used, all of which were recorded using the LOFAR core with the High Band Antennas (HBAs, 110–190 MHz). The data sets are LOFAR Commissioning Data, HBA Census Data (Bilous et al. 2016) and Cycle 5 timing data (project code: LT5_003; PI: Verbiest), discussed in more detail below. The pulsars were selected on the basis of being bright and scattered in this frequency band, as well as exhibiting simple average profile shapes, as inferred from less scattered profiles at higher frequencies. Depending on the data set and data quality, 8 or 16 profiles over the HBA band were analysed. The number of frequency channels was typically reduced for average pulse profiles with a peak $S/N < 2.7$. In some cases, individual

Table 1. The list of sources analysed in this paper. The periods are given to two decimal values. The DM values, to four decimals, are the values with which the data files are dedispersed. The quoted distance values (D) are obtained from the ATNF pulsar catalog (see footnote 2) (Manchester et al. 2005), and are mostly computed using the updated YMW16 electron density distribution model (Yao, Manchester & Wang 2017). Bracketed values are older estimates based on the NE2001 (Cordes & Lazio 2002) electron density model. The superscripts indicate, ^edistances derived independently from DM values, e.g. from parallax measurements or the association with objects, such as supernova remnants. These are typically more reliable than values calculated from electron density distribution models; ^csources appearing in Krishnakumar et al. (2015); ^dsources in Lewandowski et al. (2015a); ^bflux density values (at 350 MHz) from Stovall et al. (2014); ^aflux density values (at 408 MHz) and flux density spectral indices, η , taken from Lorimer et al. (1995), where $S_\nu \sim \nu^{-\eta}$, with S the flux density and ν the frequency.

Pulsar J-name	Pulsar B-name	Period (s)	DM (pc cm ⁻³)	D (kpc)	Flux density ^a (mJy)	Flux spectral index ^a , η	Data	MJD
J0040+5716	B0037+56	1.12	92.5146	2.42 (2.99)	5.00 ^b	1.8	Census	56753
J0117+5914	B0114+58	0.10	49.4210	1.77 (2.22)	43.40 ^b	2.4	Commissioning	56518
			49.4207				Census	56781
J0543+2329	B0540+23	0.25	77.7026	1.56 (2.06)	29.00	0.7	Census	56780
J0614+2229 ^c	B0611+22	0.33	96.9100	1.74 (2.08)	29.00	2.1	Cycle 5	57391
			96.9030				Commissioning	56384
J0742–2822 ^{c, d}	B0740–28	0.17	73.7950	2.00 ^e	296.00	2.0	Commissioning	56603
J1851+1259	B1848+12	1.21	70.6333	2.64 (3.50)	8.00	1.8	Census	56687
J1909+1102 ^{c, d}	B1907+10	0.28	150.0050	4.80 ^e	50.00	2.5	Commissioning	56388
J1913–0440 ^{c, d}	B1911–04	0.83	89.3700	4.04 (2.79)	118.00	2.6	Commissioning	56259
			89.3850				Cycle 5	57391
J1917+1353 ^{c, d}	B1915+13	0.19	94.6580	5.00 ^e	43.00	1.8	Commissioning	56525
J1922+2110 ^{c, d}	B1920+21	1.08	217.0220	4.00 ^e	30.00	2.4	Commissioning	56388
J1935+1616 ^{c, d}	B1933+16	0.36	158.6210	3.70 ^e	242.00	1.4	Commissioning	56607
J2257+5909	B2255+58	0.37	151.1330	3.00 ^e	251.90 ^b	0.8	Commissioning	56518
J2305+3100 ^d	B2303+30	1.58	49.5845	25.00 (3.76)	24.00	2.3	Census	56773

low S/N frequency channels were removed from the analysis, as discussed on a pulsar-by-pulsar basis in Section 4.

2.1 Commissioning data

Data recorded using the LOFAR HBA Core (19–23 stations), during the pre-Cycle 0 and Cycle 0 period (ending in 2013 November), are here collectively called Commissioning data. The data are of similar quality as the data presented in Pilia et al. (2016).

The Commissioning data are typically split into 6400 frequency channels across the HBA band, and have a phase bin resolution of 1024 bins across the pulse period. The data are incoherently dedispersed, with the exception of PSR J1913–0440, for which the data are coherently dedispersed. The largest per channel DM smearing of 11 ms is for PSR J1909+1102 at 110 MHz (4 per cent of its pulse period).

From the Commissioning data, we present nine sources that exhibit clear scatter broadening. We mostly form eight average profiles across the observing bandwidth, to which our scattering models are fit independently.

2.2 Census data

The original LOFAR HBA Census data set (Bilous et al. 2016) includes 194 pulsars, observed from 2014 February to May, at declinations $\delta > 8^\circ$, and galactic latitudes $|b| > 3^\circ$. These specifications were chosen to maximize the telescope sensitivity (which is reduced with increasing zenith angle) and to avoid higher background sky temperatures towards the Galactic plane, and are as such not necessarily highly scattered pulsars. From this set of pulsars, we picked the ones that have a high peak S/N, exhibit clear exponential scattering and have simple single-component profiles. All of the pulsars were observed for > 1000 rotations or at least 20 min using the full LOFAR HBA Core.

The recorded bandwidth was split into 400 sub-bands, with either 64 or 128 channels per sub-band. The phase bin resolution varies from 128 to 1024 bins per pulse period. In this paper, the Census

data are typically presented as 16 average profiles across the HBA band. More detail on the observing strategy and data acquisition can be found in Bilous et al. (2016).

2.3 Cycle 5 data

As part of an ongoing timing programme with LOFAR (Cycle 5, project code: LT5_003), two of the pulsars that overlap with the Commissioning data subset are continuously monitored at HBA frequencies. The data are recorded using the full LOFAR Core (23 stations), producing 10 min observations with 400 frequency channels, and then coherently dedispersed. We use Cycle 5 timing data for the two overlapping pulsars, and pick the observations with the highest S/N for each pulsar (ObsIDs L424139 and L423987). The data are averaged to form 16 profiles across the band. We compare the outcomes to the lower S/N Commissioning data.

2.4 Data reduction

All the observations are pre-processed using the standard LOFAR Pulsar Pipeline (PulP, Kondratiev et al. 2016). The complex-voltage data from individual stations are summed coherently, after which the data are dedispersed and folded offline. Radio frequency interference was removed using the `clean.py` tool from the `COASTGUARD`¹ package (Lazarus, Karuppusamy & Graikou 2016). Profiles were flux density calibrated in the same way as described in Kondratiev et al. (2016) resulting in an initial conservative error estimate of 50 per cent (Bilous et al. 2016). Thereafter, we calculate a corrected flux density value for a given averaged pulse profile, which compensates for flux density losses due to the effects of extreme scattering. The correction is determined from the fitting parameter obtained by the scattering model, as described in more detail in the next section.

¹ https://github.com/plazar/coast_guard

3 ANALYSIS AND FITTING TECHNIQUES

After the data are reduced and flux density calibrated, as discussed in Section 2, we write them out to ascii format (using `pdv` in `PSRCHIVE`; van Straten, Demorest & Osłowski 2012). These ascii files are subsequently analysed by our `PYTHON` scattering code, which fits each channelized profile and produces diagnostic plots, as well as τ and scatter-corrected flux density spectra. The scattering method used is the *train + DC* method, described in detail in GK16. This method produces a fit to the scattered profile assuming a Gaussian intrinsic pulse profile and an approximately zero off-pulse baseline. The five fitting parameters are the amplitude (A), the width (σ) and the mean (centroid, μ) of the intrinsic pulse, as well as the characteristic scattering time (τ) imparted by the ISM and a DC fluctuation (on the order of the noise of the data) in the baseline away from zero.

The *train + DC* method also models the profile shapes that result when individual pulses in the pulse train overlap due to high levels of scattering. Under these circumstances, the off-pulse baseline is raised significantly, such that the mean flux density calculated from zero baselined data would lead to an underestimation of the flux density (for more details see GK16). For a given scattering time-scale and intrinsic pulsar parameters, we calculate the associated raised baseline level and use this value to convert the observed *uncorrected flux density* to the *corrected flux density*. Values quoted in the Section 4 are these corrected flux density measurements and their associated errors. We note that from the initial flux calibration conducted during the data reduction stage, these errors should have a minimum value of 50 per cent, as discussed in Bilous et al. (2016).

The underlying Gaussian fitting parameters also allow us to obtain a DM-type value, by fitting

$$\Delta\mu = \Delta\text{DM} \left(\frac{1}{v_i^2} - \frac{1}{v_H^2} \right), \quad (1)$$

where $\Delta\mu = \mu_H - \mu_i$ is the shift in the intrinsic pulse centroid value between a given frequency channel (v_i) and the highest frequency channel (v_H). We label this proportionality constant as ΔDM , since it represents a change in the DM value obtained from dedispersing the scattered pulse profiles during the initial PULP analysis.

We consider two independent scattering mechanisms, in each case using the same fitting procedure as described above. In the first instance, we consider an isotropic scattering model (IM). This model assumes that a single thin scattering screen, which scatters radio waves isotropically (following a circularly symmetric Gaussian distribution), is responsible for the broadened pulse profile. The temporal broadening function associated with the ISM takes the form ,

$$f_t = \tau^{-1} e^{-t/\tau} U(t) \quad (2)$$

The unit step function, $U(t)$, ensures that we only consider time $t > 0$. Equation (2) is valid assuming the scattering screen is infinite transverse to the line of sight. For this model, the theoretically expected frequency dependence is $\tau \propto \nu^{-4}$.

The second scattering model is an extremely AM. In the limiting case, where the anisotropy $\rightarrow \infty$, such a scattering screen will only scatter radio waves along a single dimension. The associated broadening function is then ,

$$f_t = \frac{e^{-t/\tau}}{\sqrt{\pi t \tau}} U(t), \quad (3)$$

with again $\tau \propto \nu^{-4}$. These scattering mechanisms are described in more detail in Cordes & Lazio (2001) and GK16.

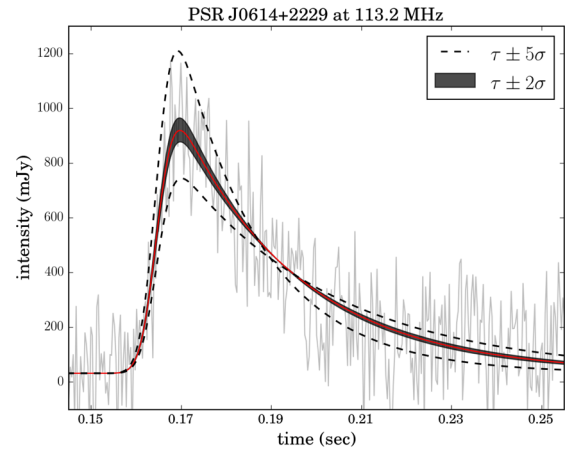


Figure 1. The range of pulse shapes for PSR J0614+2229 resulting from the best-fitting τ value (solid red line) and the best-fitting value with an added 2σ (shaded region) or 5σ error range (dashed lines). To ensure that the error ranges are visible, only 10 s of the pulse period is shown.

In order to account for the frequency integration of the channelized data (e.g. integrating over an 8 MHz band when HBA data are averaged to 16 frequency channels), we make use of equation (6) in GK16 to extract the monochromatic frequency associated with an obtained τ value. The impact of this effect is discussed in detail in GK16. It should be noted that for the LOFAR data in this paper the correction in α is less than 0.5 per cent.

After the τ value and the corresponding frequency value for each channelized profile is extracted, a power-law fit (weighted inversely with the square of the errors) to the τ spectrum is obtained. For both the profiles and τ spectra, we report a 1σ error. A fit to the average profile of PSR J0614+2229 in Fig. 1 shows the typical impact of τ errors on the scatter broadened shape. The dark grey-shaded region around the best-fitting τ value (red solid line) represents a 2σ error, and the dashed line shows the 5σ error margin.

To evaluate the goodness of the model fits we make use of two standard metrics, the reduced Chi-squared (χ_{red}^2) value and the Kolmogorov–Smirnov (KS) test. The KS test is applied to the residuals (data – model) to test the Gaussianity of the residuals. This test provides the probability that the residuals follow a Gaussian distribution. The main objective is to identify examples where the residuals are severely non-Gaussian. We compare the outcomes of these metrics for the two models (isotropic and extremely anisotropic) for all the sources.

4 RESULTS

4.1 Scattering and flux density analysis for each pulsar

Here, we discuss our results for each pulsar individually. For convenience, we provide sub-headings for each pulsar, summarizing the period, scattering time and DM, with no errors, as well as the time and frequency resolution of the data (δt and $\delta \nu$). Data sets are abbreviated as Co, Ce and Cy for Commissioning, Census and Cycle 5 data, respectively.

Thereafter, we show the outcomes of our fitting models and consider the goodness of the fits (detailed results can be found in the Supporting Information, Appendix A). We present the fitted scattering values (τ), along with the computed τ spectra, providing comparisons to values from the literature. We then discuss the flux density spectra that result from the scattering analysis, and consider

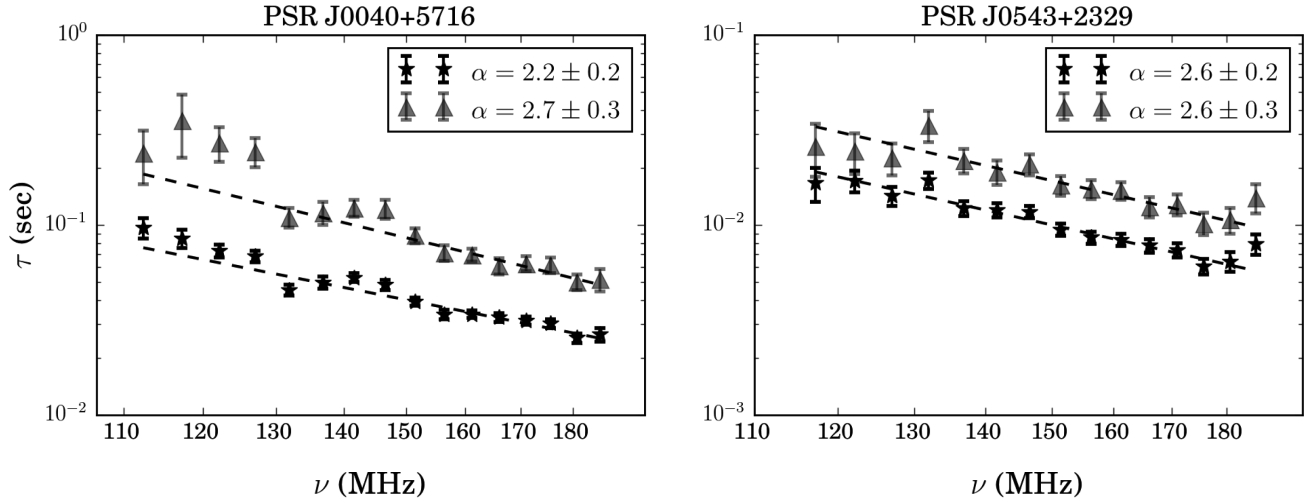


Figure 2. The τ spectra for PSRs J0040+5716 and J0543+2329. IM fits are shown in black (stars) and AM fits in grey (triangles).

how these values compare to published studies. The basic pulsar properties of the set are summarized in Table 1.

4.1.1 PSR J0040+5716 ($P = 1.12$ s, $\tau_{150} = 40$ ms, $DM = 92.5$ pc cm^{-3} , $\delta t = 2.2$ ms, $\delta\nu = 1.5$ kHz)

PSR J0040+5716 was discovered in a search for low-luminosity pulsars at 390 MHz using the 92-m transit telescope at Green Bank (92 m GBT) in West Virginia, US (Dewey et al. 1985), and has the lowest tabulated flux density value for our list of sources. The distance estimate of this pulsar has changed from 4.48 kpc (Taylor & Cordes 1993) to 2.99 kpc (NE2001 model, Cordes & Lazio 2002) to more recently 2.42 kpc (Yao et al. 2017). Its DM value of 92.5 pc cm^{-3} is close to the mean of the set DM values.

We use LOFAR HBA Census data for this pulsar. From the European Pulsar Network (EPN) data base² (Lorimer et al. 1998), we find that it is a single-component pulsar at 408 MHz (Gould & Lyne 1998) and, as it exhibits no clear secondary components in our data set, it is likely a single-component pulsar down to low frequencies. There are currently no scattering measurements published for this pulsar.

The profile fits over all 16 channels (for which the lowest peak S/N is equal to 4.4) produce a τ spectrum with spectral index $\alpha = 2.2 \pm 0.2$ for the IM and $\alpha = 2.7 \pm 0.3$ for the AM fits (Fig. 2, left-hand panel). The error bars on τ and the spread in τ values obtained from the IM (black, stars) are typically smaller than for the AM (grey, triangles). The goodness-of-fit parameters, shown in Table A1 in the Supporting Information, do not favour a particular scattering model.

The τ spectrum appears to have three segments with breaks around 130 and 150 MHz. The residuals of the profile at 136 MHz are less Gaussian than for the other frequency channels.

Splitting the bandwidth into only four channels to increase the S/N and refitting, leads to a similar α value of 2.1 ± 0.3 . We also find that the σ (unscattered pulse width) versus frequency relationship for this pulsar follows a rough power-law dependence (see Section 5.3). Fixing the σ values to this power-law dependence and refitting, increases the α value to 2.3, which is within the errors of the original value. We conclude that the obtained α value is robust, and not critically sensitive to these tested changes in fitting method.

² <http://www.epta.eu.org/epndb/>

The ΔDM values obtained from equation (1) are presented in Table 3.

The flux density values inferred from our fitting models show no clear dependence on frequency (and therefore scattering). Bilous et al. (2016) measured a mean flux density at HBA frequencies of 33 ± 17 mJy. Similarly, we find a frequency-averaged mean (corrected) flux density of 31.4 mJy (IM) and 35.8 mJy (AM). At 151.3 MHz, we measure flux density values of 34 ± 30 and 37 ± 22 mJy (IM and AM). Stovall et al. (2014) published a value of 4.7–5.0 mJy at 350 MHz. Using a simple power-law spectrum and the spectral index from Table 1, the Stovall et al. (2014) result implies a flux density of 21.9 ± 0.7 mJy at 151.3 MHz, well within our flux density error margins.

4.1.2 PSR J0117+5914 ($P = 0.10$ s, $\tau_{150} = 7$ ms (Ce) 8 ms (Co), $DM = 49.4$ pc cm^{-3} , $\delta t = 0.8$ ms (Ce) 0.1 ms (Co), $\delta\nu = 3.1$ kHz (Ce) 12.2 kHz (Co))

PSR J0117+5914 is the fastest rotating pulsar in the set and was discovered in a 92 m GBT survey for short-period pulsars (Stokes et al. 1985). It is one of the closest pulsars in the set (1.77 kpc) and has the lowest DM value (49.4 pc cm^{-3}) of the studied pulsars. This is the only pulsar for which we have both Commissioning and Census data. We use eight frequency channels across the band for the Commissioning data, and 16 for the Census data.

Fig. 3 shows the results from both data sets jointly. The left-hand panel shows the average pulse profile of the Census data at 115 MHz, with the IM fit to the data in red (solid) and the AM fit in blue (dashed). These profiles have lower phase resolution than the other data sets, with only 128 bins across the pulse profile. We note that the τ value obtained using the AM is more than four times that obtained using the IM. The AM seems to fit pulse peak better.

The middle panel shows the τ spectra for both data sets and models, with Census data as solid lines (stars (IM) and triangles (AM) data points) and Commissioning data in dotted (IM) and dash-dotted (AM) lines.

The data sets show similarities, and in the case of the IM, the power α values agree within 1σ . The IM fit produces one of the lowest α values of our set, $\alpha = 1.9 \pm 0.2$ for the Census and $\alpha = 2.2 \pm 0.1$ for the Commissioning data. The high S/N of the Census data constrains the goodness of fit of the two models well (Table A1, Supporting Information).

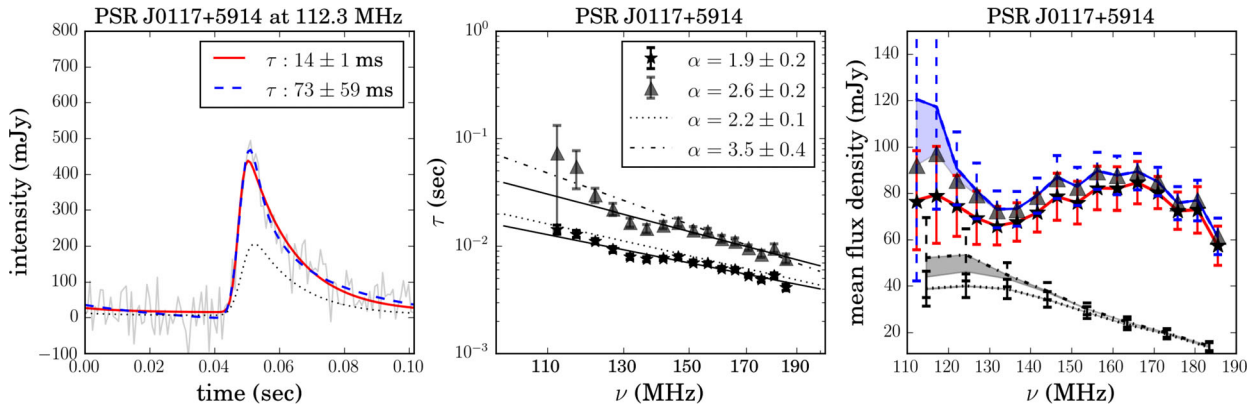


Figure 3. PSR J0117+5914. *Left:* average Census profile with the IM fit in red (solid line) and the AM fit in blue (dashed line). An IM fit to the Commissioning profile at 114.6 MHz is also shown (dotted line). *Middle:* the associated τ spectra. It shows τ values obtained from the IM (Census data: stars with solid line fit and Commissioning data: dotted line) and from the AM (Census data: triangles with solid line fit and Commissioning data: dash-dotted line). *Right:* flux spectra calculated from scattered profiles. Uncorrected flux density values are shown as stars (IM) and triangles (AM) for the Census data, with corrected flux density values as red and blue solid lines, respectively. For the IM, the uncorrected and corrected values are near equal and for the AM, the shaded region represents the increase in flux density when applying a scattering correction. The error bars associated with the corrected flux density values are shown in solid (red, IM) and dashed (blue, AM). The flux density spectrum for the Commissioning data appears at lower mean flux density values (dotted line for corrected IM flux density and dash-dotted line for corrected AM flux density).

The right-hand side of Fig. 3 shows the flux density measurements from the scattering fits. The shaded regions towards low frequency indicate the flux density corrections that account for scattering effects. Corrected flux density values with error bars, range from approximate 50 to 100 mJy (IM) or 40 to 200 mJy (AM) for the Census data. In contrast, the Commissioning data flux density values are much lower. Stovall et al. (2014) recently measured the flux density to be 43.4 mJy at 350 MHz. Using the spectral index from Table 1, this flux density is translated to approximate 330 mJy at 150 MHz – higher than the measured values between 30 and 90 mJy (Co and Ce) at 150 MHz here, even with an additional 50 per cent error range. However, the flux densities obtained from the Census data, do agree well with the mean flux density value of $S_{\text{HBA}} = 79 \pm 39$ mJy, published in Bilous et al. (2016), where flux density values were not corrected for scattering as in this paper.

For both data sets, the flux density values obtained from the AM are higher than the corresponding IM values. The high-quality Census data for this pulsar are shown in the Supporting Information (Appendix A). Below 135 MHz, the data suggest that scattering tails are ‘wrapping around’, i.e. the scattering tail stretches beyond the pulse period. This could be correlated with turnover in the flux density spectrum of the Commissioning data. However, the Census data do not show a clear turnover at these frequencies.

In Table A2 in the Supporting Information, we compare DM corrections for pulsars for which we have more than one data set. We note that applying the Δ DM correction from the AM for PSR J0117+5914, results in DM values that remain more similar between the two observing epochs.

4.1.3 PSR J0543+2329 ($P = 0.25$ s, $\tau_{150} = 10$ ms, $DM = 77.7$ pc cm^{-3} , $\delta t = 1.0$ ms, $\delta \nu = 1.5$ kHz)

This pulsar is associated with the supernova remnant IC 443. It was discovered in one of the earliest pulsar searches with the Lovell telescope at Jodrell Bank, at 408 MHz (Davies, Lyne & Seiradakis 1972). The Census data were channelized to 16 average pulse profiles, of which the lowest channel is excluded from the analysis for having a low peak S/N value. As seen in Fig. 2, the τ spectra for both scattering models have similar power-law indices.

Cordes (1986) gives $\tau = 2.69$ μ s at 1 GHz. Our measurement of $\tau = 0.01$ s at 150 MHz and $\alpha = 2.61$, would translate to $\tau = 66$ μ s at 1 GHz. The required spectral index to link our 186 MHz observation to the 1 GHz measurement, is $\alpha = 4.6$, close to the Kolmogorov value of 4.4. Kuzmin & Losovsky (2007) published $\tau = 15 \pm 5$ ms at 111 MHz, using data from the Large Phased Array Radio Telescope (BSA) at the Pushchino Radio Astronomy Observatory in Russia. Again using our obtained IM power-law index we find $\tau = 22 \pm 6$ ms at 111 MHz, which lies just outside their error bounds.

The flux density measurements show no clear frequency dependence. At 151.4 MHz, the computed flux density values are 46 ± 15 mJy (IM) and 47 ± 12 mJy (AM). To incorporate the uncertainty in the initial flux calibration during the data reduction stage, we augment these values to 46 ± 23 mJy (IM) and 47 ± 24 mJy (AM). Bilous et al. (2016) published a similar mean flux density of 36 ± 18 mJy. The measured flux density of $S_{408} = 28.9 \pm 1.3$ mJy at 408 MHz (Lorimer et al. 1995) leads to an expected flux density of around 58 mJy at 150 MHz, using a simple power-law spectrum with spectral index 0.7 (Table 1). This value lies within 50 per cent of our HBA flux density measurement.

4.1.4 PSR J0614+2229 ($P = 0.33$ s, $\tau_{150} = 15$ ms (Co & Cy), $DM = 96.9$ pc cm^{-3} , $\delta t = 0.3$ ms (Co & Cy), $\delta \nu = 195$ kHz, coherently dedispersed (Cy), 12.2 kHz (Co))

PSR J0614+2229 was discovered in the same survey as PSR J0543+2329. For this pulsar, we have LOFAR Commissioning and Cycle 5 data. The Cycle 5 data lead to a τ spectrum for which $\alpha = 2.1 \pm 0.1$ (IM) and $\alpha = 3.1 \pm 0.3$ (AM), as shown in Fig. 4. The figure also shows α values 1.9 ± 0.1 (IM) and 2.4 ± 0.3 (AM) from the Commissioning data, such that especially for the IM the values are in good agreement.

The left-hand panel of Fig. 4 shows the comparison of profile fits, between the IM (red, solid line) and the AM (blue, dashed line) at 117.1 MHz. The computed τ values differ by a factor of approximate 4, and the AM fit follows the tip of the profile peak more closely. The computed χ_{red}^2 values are consistently lower for

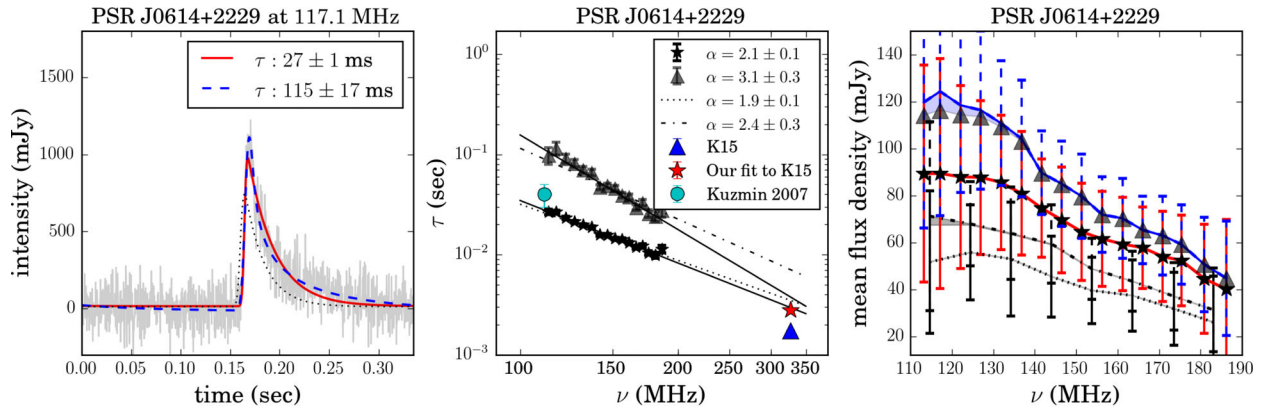


Figure 4. *Left:* the average profile of PSR J0614+2229 at 117.1 MHz (grey), and the IM (red, solid line) and AM fits (blue, dashed line). The dotted line shows the Commissioning data average profile at 124.4 MHz. *Middle:* associated τ spectrum for the IM (Cycle 5 data: stars with solid line fit and Commissioning data: dotted line) and for the AM (Cycle 5: triangles with solid line fit and Commissioning data: dash-dotted line) with added data points from K15 and Kuzmin & Losovsky (2007). *Right:* associated flux density spectra, with Cycle 5 data at the top and Commissioning data at lower flux density values. The markers are similar to Fig. 3.

Table 2. Low-frequency characteristic scattering time values (τ , in ms) from the literature for pulsars with two or more of these values quoted in text. ^aValues at 102 MHz, the rest of the Kuzmin & Losovsky (2007) values are at 111 MHz. See text for full references.

Reference	Kuzmin 2007	This paper	Slee 1980	Alurkar 1986	Löhmer 2004	K15
Freq (MHz)	102 /111	150	160	160	243	327
J0614+2229	40 ± 10	15 ± 0				1.74 ± 0.03
J0724–2822	22 ± 5.3^a	20 ± 2		24.5 ± 2.8		0.71 ± 0.01
J1909+1102		42 ± 3	27 ± 7	26.5 ± 8.1		1.35 ± 0.02
J1913–0440	35 ± 15^a	7 ± 0	32 ± 5	16.7 ± 1.8		0.19 ± 0.01
J1917+1353	40 ± 20^a	11 ± 1	12 ± 3	11.7 ± 1.9		0.36 ± 0.01
J1922+2110		42 ± 2		96.8 ± 50	4.4 ± 1.5	2.3 ± 0.1
J1935+1616	50 ± 15	20 ± 1	25 ± 4	21.7 ± 1.6	4.6 ± 0.2	3.21 ± 0.02
J2303+3100	13 ± 3	9 ± 0		9.9 ± 3.6		

the AM, with mean values quoted in Table A1 in the Supporting Information.

This pulsar lies at a distance of 1.74 kpc (previously estimated to be at 4.74 kpc, see Table 1) and has a DM value of 96.9 pc cm^{-3} , which is similar to PSR J0040+5716. The α values obtained using the IM for these two pulsars are also comparable.

This pulsar is the first in our source list to overlap with an Ooty Radio Telescope data set at 327 MHz, for which characteristic scattering times were recently published (Krishnakumar et al. 2015, hereafter K15³). Their data and methods are different to ours in several ways: (1) the average pulse profiles are far less scatter broadened than our sample set. (2) They follow the method described in Löhmer et al. (2001), in which a high-frequency pulsar is used to estimate and fix the width of a Gaussian template used in the fitting method. (3) Wrap around scattering is not modelled (and not required at this frequency for these pulsars) and (4) for all pulsars marked as ‘double-component’ profiles, only the trailing component of the pulse profile is fitted for.

The K15 characteristic scattering time for this pulsar is $\tau = 1.74 \pm 0.03 \text{ ms}$ at 327 MHz. Refitting their data with our techniques gives $\tau = 2.80 \pm 0.02 \text{ ms}$. The main difference seems to come from their choosing a fixed width. A fit with our code, specifying a fixed width as inferred from a high-frequency profile, leads to a more similar τ value of 1.80 ms, although we note that the fit to the amplitude of the profile becomes considerably worse. We also note that the

pulse profile is not highly scattered at a frequency of 327 MHz, which increases the uncertainty in the obtained τ values. Kuzmin & Losovsky (2007) published a characteristic scattering time of $\tau = 40 \pm 10 \text{ ms}$ at 111 MHz. At 113.2 MHz, we find $\tau = 26.7 \pm 1.6 \text{ ms}$, which translates to $28.1 \pm 2.7 \text{ ms}$ at 111 MHz when using our obtained IM α value. The literature values are shown in the middle panel of Fig. 4. The extrapolations of the Cycle 5 data fits are in good agreement with our (IM) fit to the K15 data at 327 MHz. Low-frequency scattering time results from the literature for this pulsar and subsequent ones are summarized in Table 2.

The flux density and spectral index (see Table 1) suggests a mean flux density of 237 mJy at 150 MHz, much larger than our measured values of $65 \pm 21 \text{ mJy}$ (IM) or $80 \pm 18 \text{ mJy}$ (AM). Again these error bars should be augmented to a minimum value of 50 per cent, such that at 150 MHz they are $65 \pm 33 \text{ mJy}$ (IM) or $80 \pm 40 \text{ mJy}$ (AM). The flux density spectrum associated with the IM flattens out towards the lowest frequencies, with no obvious turnover. The AM shows a more clear turnover towards lowest frequencies, in agreement with both the raised baseline measurements (represented by the shaded area in the flux density spectrum) and the wrapped scattering tails seen in the AM profile fits (Supporting Information, Appendix A).

4.1.5 PSR J0742–2822 ($P = 0.17 \text{ s}$, $\tau_{150} = 20 \text{ ms}$, $DM = 73.8 \text{ pc cm}^{-3}$, $\delta t = 0.2 \text{ ms}$, $\delta \nu = 12.2 \text{ kHz}$)

PSR J0742–2822 is a young pulsar associated with an H_I shell in Puppis (Stacy & Jackson 1982).

³The data used in Krishnakumar et al. (2015) are available from <http://rac.ncra.tifr.res.in/da/pulsar/pulsar.html>.

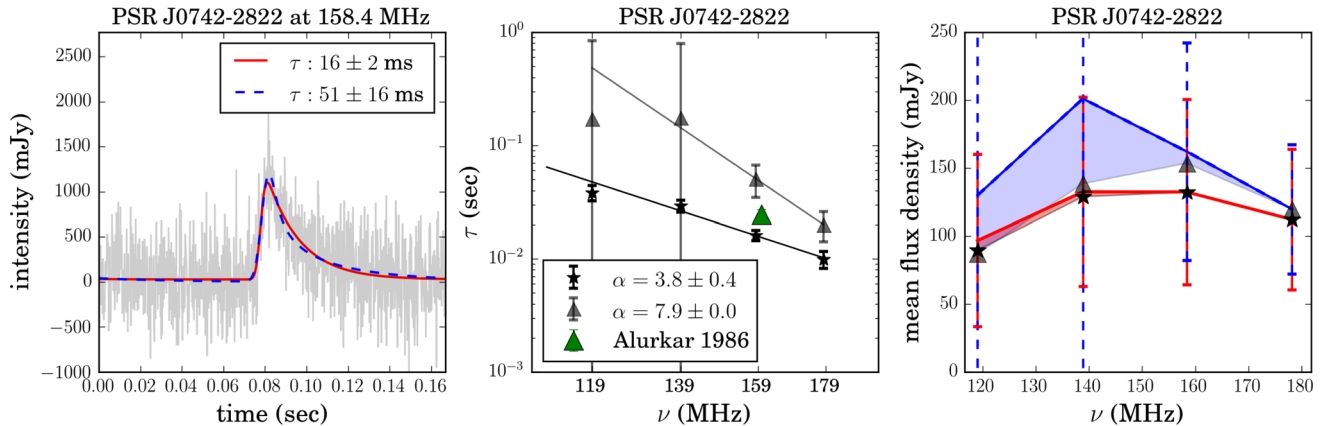


Figure 5. *Left:* low S/N fitted profile from Commissioning data. *Middle:* associated τ spectrum with an added data point from Alurkar et al. (1986). *Right:* flux spectrum showing uncorrected and corrected flux density values. All markers and colours as in previous figures.

The Commissioning data we have for this pulsar have relatively low peak S/N values. Using 16 frequency channels across the band results in profiles for which all have $S/N < 2.7$. We therefore use four channels, which still yield a maximum S/N of only 4.5. Using four channels, we find $\alpha = 3.8 \pm 0.4$ for the IM. This is the first fit for which the theoretical value of $\alpha = 4$ lies within the error bars of the measured α value. Furthermore, the AM fails to produce convincing fits, as can be seen in Fig. 5, resulting in a large α value with a tight error margin, $\alpha = 7.9 \pm 0.0$. The error bars on τ for the first two channels are large (> 350 per cent), such that the power-law fit weighted by the inverse of the errors squared, is dominated by the two higher frequency τ values only, leading to an inaccurate spectrum.

A scattering measurement of $\tau = 24.5 \pm 2.8$ ms at 160 MHz was obtained by averaging nine observations using the Culgoora circular array (Alurkar, Slee & Bobra 1986). This data point is shown in Fig. 5. We find a τ measurement at 159.6 MHz of 16.1 ± 1.6 ms. Since Alurkar et al. (1986) used a fixed width model (obtained from profiles at 408 MHz), a difference is expected. K15 find $\tau = 0.71 \pm 0.01$ ms at 327 MHz. In comparison, our spectral index of $\alpha = 3.8 \pm 0.4$ implies $\tau = 1.02 \pm 0.25$ ms at 327 MHz. Fitting the K15 data with our code, gives $\tau = 1.5 \pm 0.1$ ms, however, at 327 MHz their data show that the top peak of the pulse profile has split into two components. In these cases, they fit only the secondary component (as shown in Fig. 1 in K15), whereas we fit the whole profile. It is worth noting that at 327 MHz, the profile is not highly scattered. Lastly, Kuzmin & Losovsky (2007) published a value of 22 ± 5.3 ms at 102 MHz. This is much lower than predicted by our spectral index. A summary of the relevant literature values is given in Table 2.

The low S/N data make it hard to make definitive statements about this pulsar. A fit using the AM fails, making it an unlikely model. The trend in $\Delta\mu$ versus frequency is very weak, providing a ΔDM value with large error bars (Table 3).

The flux spectral index in Table 1 suggest a mean flux density of over 2 Jy at 150 MHz. The low S/N data lead to corrected flux density values with large error bars. At 140 MHz, the measured values are 133 ± 70 and 201 ± 476 mJy for the IM and AM, respectively.

For both models, the corrections to the flux density values due to scattering are substantial (Fig. 5, shaded), and represent a maximum increase in the best-fitting flux density of 8 per cent (IM) and 50 per cent (AM). The flux density spectrum for this pulsar shows

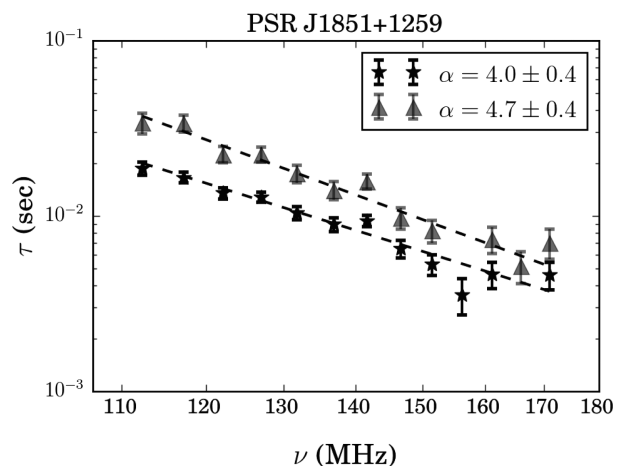


Figure 6. The τ spectra for PSR J1851+1259. IM fits are in black (stars) and AM fits in grey (triangles).

a turnover around 140 MHz, and the profile fits suggest that this could be ascribed to wrap around scattered pulses.

4.1.6 PSR J1851+1259 ($P = 1.21$ s, $\tau_{150} = 6$ ms, $DM = 70.6$ pc cm^{-3} , $\delta t = 1.2$ ms, $\delta\nu = 3.1$ kHz)

This pulsar was discovered in the same survey as PSR J0117+5914 (Stokes et al. 1985). Here, we fit Census data only. Towards the higher end of the HBA band, the profiles appear marginally scattered. For this reason, four of the higher frequency channels were not used. The remaining 12 channels were all fitted with τ values of which the 1σ error bars were less than 23 per cent.

The IM fits to the data result in an α value as predicted by a Gaussian isotropic scattering screen, namely $\alpha = 4.0 \pm 0.4$. For the AM, $\alpha = 4.7 \pm 0.4$, as shown in Fig. 6. This is the second pulsar for which the obtained values match the theoretically predicted spectral index.

The mean Census flux density measurement for this pulsar is equal to 37 ± 19 mJy (Bilous et al. 2016). The expected flux density measurement at 150 MHz using the values in Table 1 is 48.5 mJy. Both these figures are in good agreement with our results, namely 43 ± 29 mJy (IM) and 43 ± 33 mJy (AM) at 151.4 MHz. The flux density spectrum is shown in the Supporting Information (Appendix C).

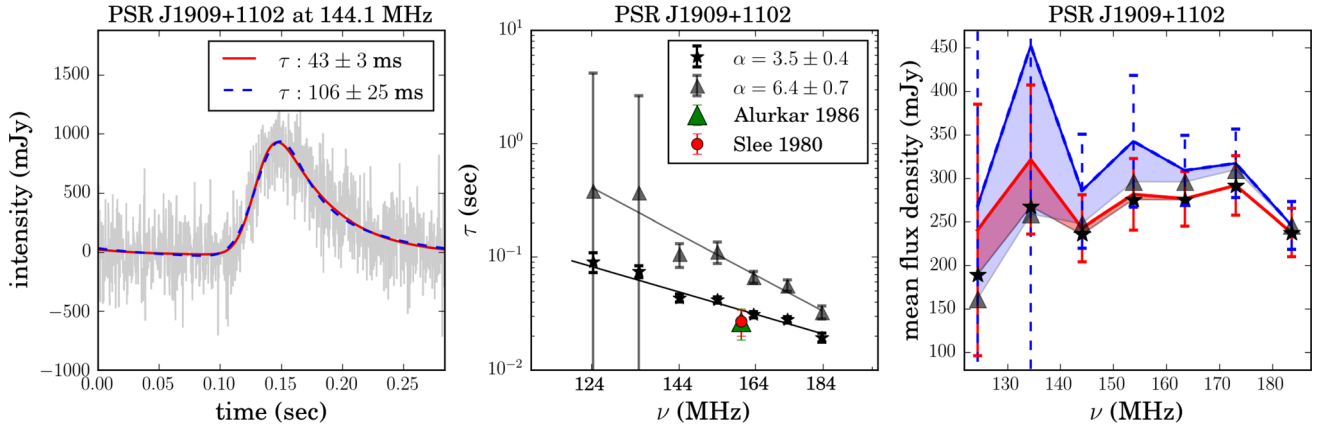


Figure 7. *Left:* scattering fits to the profile of PSR J1909+1102 at 144.1 MHz. IM is shown in red (solid) lines and AM is in blue (dashed) lines. *Middle:* the τ spectra associated with the scattering fits. IM in black (stars) and AM in grey (triangles). *Right:* the uncorrected flux density values (IM, stars and AM, triangles) and corrected flux densities (IM, red line and AM, blue line). The flux density corrections shifts the turnover in the spectrum from higher towards lower frequencies.

4.1.7 PSR J1909+1102 ($P = 0.28$ s, $\tau_{150} = 42$ ms, $DM = 150.0$ pc cm $^{-3}$, $\delta t = 0.3$ ms, $\delta\nu = 12.2$ kHz)

PSR J1909+1102 was discovered in a low-latitude pulsar survey with the Lovell Telescope at Jodrell Bank in 1973 (Davies, Lyne & Seiradakis 1973). This pulsar has one of the higher DM values in our observing set and is highly scattered. In Section 5 (Fig. 23), we show the DM versus distance values for our set of sources. PSR J1909+1102 is one of the outliers on this plot.

Since the pulsar is at a low latitude, we only have Commissioning data. To increase the S/N, we split the HBA band into eight frequency channels. The peak S/N values for all but the lowest frequency channel (which we exclude from the analysis) range from 3.5 to 9.1. The τ spectrum resulting from these measurements is shown in Fig. 7 (middle panel).

Two similar τ measurements at 160 MHz were obtained by Alurkar et al. (1986) and Slee, Otrupcek & Dulk (1980) using the Culgoora circular array, namely 26.5 ± 8.1 and 27 ± 7 ms (Table 2). At 163.5 MHz, we obtain 30.7 ± 1.9 ms, within their estimated error at 160 MHz.

Lewandowski et al. (2015a, hereafter L15) published a spectral index value of $\alpha = 3.61 \pm 0.03$, based on literature values and a fit to a higher frequency profile from the EPN data base. L15 follow the fitting approach as described in Löhmer et al. (2001). L15 do, however, allow for the width of the unscattered profile to change. Many of the error bars on α values (and some of the α values itself) in L15 were updated in Lewandowski et al. (2015b, hereafter L15b). For PSR J1909+1102, the updated value is $\alpha = 3.61^{+0.79}_{-0.74}$. Their α value lies well within the error bars of our spectral index measurement of $\alpha = 3.5 \pm 0.4$ (IM).

K15 published a value of $\tau = 1.35 \pm 0.02$ ms at 327 MHz. Fitting the K15 data ourselves, we find $\tau = 2.4$ ms at 327 MHz. As with PSR J0614+2229, the main difference seems to be coming from whether or not a model uses a fixed width intrinsic profile. Fitting their data with a fixed width template we find $\tau = 1.10 \pm 0.1$ ms, in closer agreement to their published value.

The flux density value and flux spectral index in Table 1 implies a flux density of 610 mJy at 150 MHz (using a simple power-law model) which is more than twice our measured IM value of 281 ± 41 mJy at 154 MHz. At this frequency, the AM predicts 342 ± 76 mJy. To adhere to 50 per cent error margins, we change these to 281 ± 141 mJy (IM) and 342 ± 171 mJy

(AM). The flux density spectrum of PSR J1909+1102 (Fig. 7, right-hand panel) shows significant observed flux density loss due to scattering (shaded areas) that we correct for. The corrected spectrum shows a turnover at around 140 MHz. We note that this pulsar has the largest ratio of τ at 150 MHz to pulse period, namely $\tau_{150}/P = 0.15$, and the scattering tails wrap around the full rotational phase.

4.1.8 PSR J1913–0440 ($P = 0.83$ s, $\tau_{150} = 7$ ms (Cy) 9 ms (Co), $DM = 89.4$ pc cm $^{-3}$, $\delta t = 0.8$ ms (Cy & Co), $\delta\nu = 195$ kHz (Cy & Co), coherently dedispersed)

PSR J1913–0440 features in both the Commissioning and the Cycle 5 data set. From the latter, we obtain $\alpha = 3.3 \pm 0.1$ (IM) and $\alpha = 4.1 \pm 0.2$ (AM). The Commissioning data lead to somewhat lower spectral indices with larger error bars, namely $\alpha = 2.7 \pm 0.2$ (IM) and $\alpha = 3.5 \pm 0.3$ (AM).

In the following, we concentrate on the Cycle 5 data, which, with 16 frequency channels, have higher S/N (each profile has peak S/N > 30). In Fig. 8, we show the profile fits to three frequency channels, along with the τ and flux density spectra and the ΔDM trends. The full set of profiles is shown in the Supporting Information (Appendix A).

We note a small flat feature appearing at frequencies above 130 MHz (see the top middle and right-hand panels of Fig. 8). At low frequencies, the feature is fit together with the primary component leading to an overestimation in τ . This is visible as a deviation in the fitted τ spectrum. Fitting only components above 130 MHz (IM) would lead to a slightly lower spectral index of $\alpha = 3.2 \pm 0.1$.

Previous scattering measurements for this pulsar exist at 102 MHz (Kuzmin & Losovsky 2007) and 160 MHz (Alurkar et al. 1986; Slee et al. 1980; see Table 2). Using these values as well as their own fits to EPN profiles at higher frequencies (up to 408 MHz), L15 published an α value equal to 2.62 ± 0.86 . We note (from e.g. the K15 data) that the profile is nearly unscattered at 327 MHz, such that we do not value the inclusion of ever higher frequency profiles by L15. The L15 value was changed to $\alpha = 4.18 \pm 0.44$ in L15b, after the inclusion of measurements with the GMRT at 150 and 235 MHz.

Using $\alpha = 3.3 \pm 0.1$, we extrapolate to a τ value of 25 ± 2.2 ms at 102 MHz, which lies within the error bars of the Kuzmin &

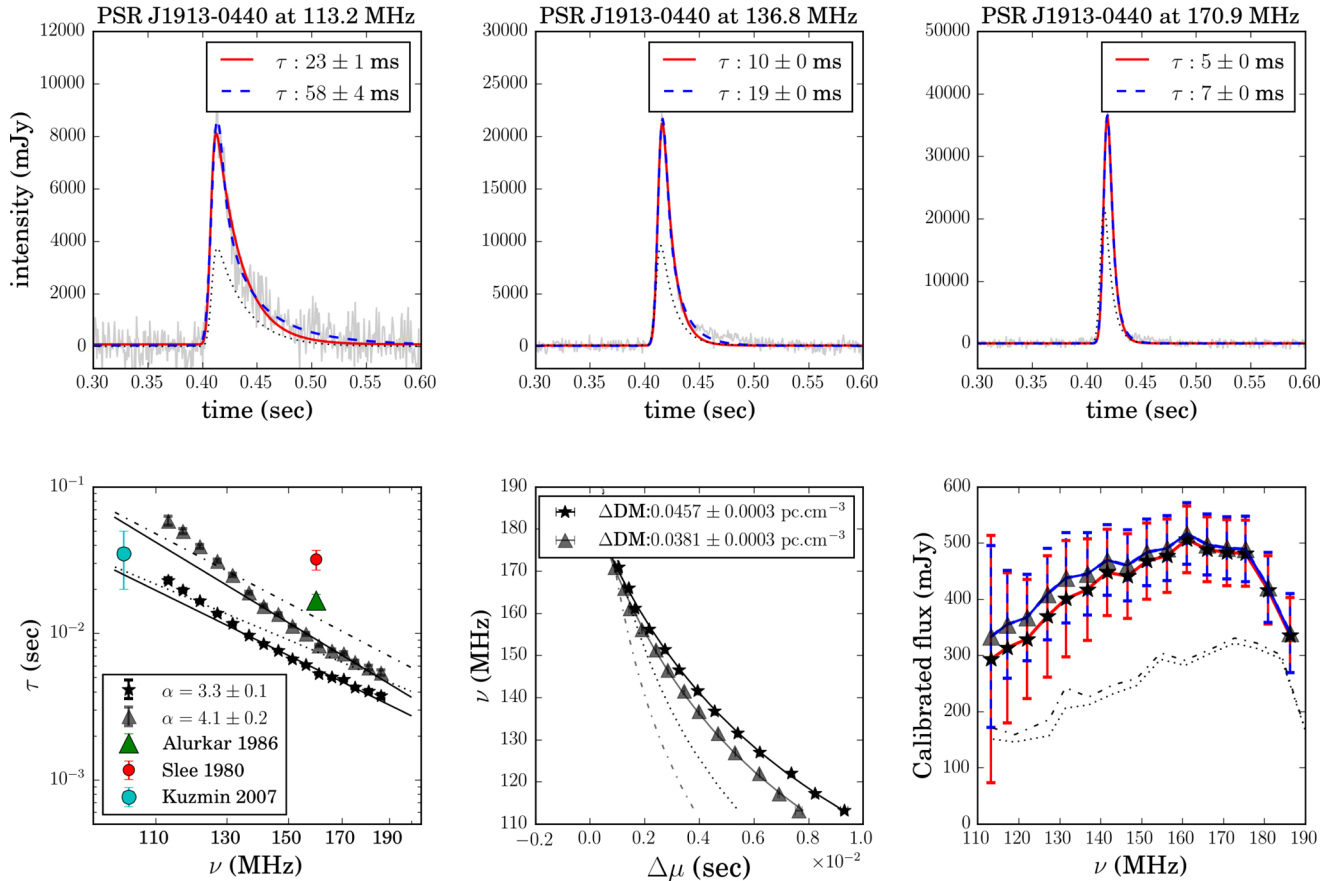


Figure 8. *Top:* scattered broadened profiles of PSR J1913–0440 at three different frequencies in the HBA band (Cycle 5 data: IM fit in solid red and AM fit in blue dashed line. Commissioning data: IM fits at similar frequencies to Cycle 5 profiles in dotted lines). A secondary feature can be made out in the middle and right-hand panels. The profiles are enlarged to show 0.3 s of the 0.83 s pulse period. *Bottom, left:* the τ and flux density spectra for PSR J1913–0440 (IM, stars and AM triangles), along with data points from the literature. The Commissioning data fits are also shown as a dotted line (IM, $\alpha = 2.7 \pm 0.2$) and dash-dotted line (AM, $\alpha = 3.5 \pm 0.3$). *Bottom, middle:* fits to the obtained excess DM values. Markers are as in the previous panel. *Bottom, right:* the flux density spectra for IM (stars: uncorrected flux density and red solid line: corrected flux density) and AM (triangles: uncorrected flux density and blue (top) solid line: corrected flux density). The AM of the lowest two frequency channels is associated with large τ error bars (dashed), leading to flux density errors of several 100 per cent. Flux spectra for the Commissioning data are shown as dotted (IM) and dash-dotted (AM) lines.

Losovsky (2007) published value, 35 ± 15 ms. Our τ value at 161.1 MHz is 5.3 ± 0.1 ms, much lower than the values at 160 MHz of 16.7 ± 1.8 and 32 ± 5 ms in Alurkar et al. (1986) and Slee et al. (1980), respectively. The difference is likely due to their using lower S/N data, in which the secondary component at these frequencies cannot be isolated. K15 find $\tau = 0.19 \pm 0.01$ ms at 327 MHz. Extrapolating our data would lead to a value of around $\tau \sim 54$ ms. We note that K15 have labelled this pulsar as a double-component pulsar, in which case they fit only the secondary component, different from us. However, at 327 MHz, the pulsar is very weakly scattered.

Due to the presence of the low-frequency feature, our fits provide weak average goodness-of-fit statistics (Table A1, Supporting Information). The shape of the AM profiles fit the secondary feature well, leading to residuals that are much more Gaussian, especially at lower frequencies, than the IM. The deviation from a simple power law in the τ spectrum, seen in Fig. 8, therefore also starts at higher frequencies, than for the AM. These better fits lead to an α value close to the theoretically expected value of 4. The secondary feature disappears at high frequencies, i.e. at low scattering. If in fact this low-frequency feature is due to scattering alone it would provide strong support for an extremely anisotropic scattering mechanism

along this line of sight. However, we cannot rule out that the feature is intrinsic to the pulsar.

We see a clear ΔDM trend in both the Commissioning Cycle 5 data for the IM and AM fits (Fig. 8, lower middle panel). Introducing the ΔDM corrections lead to the improved DM values in Table A2 in the Supporting Information. The corrections show that the DM values associated with the two data sets become more equal after the corrections are applied, both for the IM and AM. In this respect, the AM performs more favourably.

The flux density associated with our scattering fits shows a clear turnover at 160 MHz (Fig. 8, lower right panel). This cannot be understood through long scattering tails, since the scattering values with respect to the pulse period are not large enough, and the corrected flux density differs negligibly from the uncorrected flux density. The flux density and spectral index values from Table 1 suggest a flux density of approximate 1590 mJy at 150 MHz. In comparison our measured values at 151 MHz are 468 ± 68 mJy (IM) and 483 ± 59 mJy (AM), which becomes 468 ± 234 mJy (IM) and 483 ± 242 mJy (AM) with increased error margins. The Commissioning data for this pulsar result in even lower values of 246 ± 123 mJy (IM) and 259 ± 130 (AM) mJy at 149 MHz (with increased error margins).

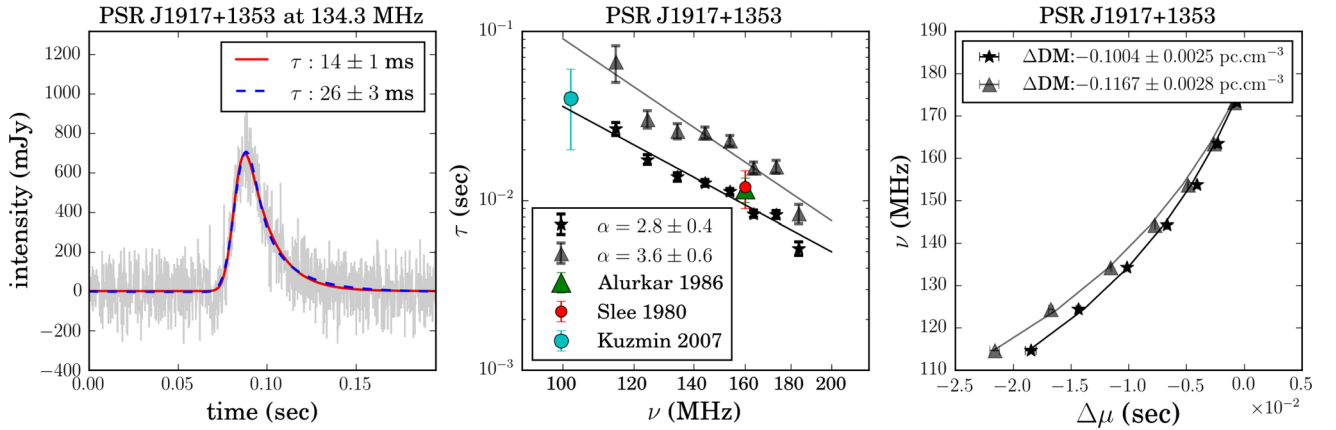


Figure 9. *Left:* the scattering fits to a profile shape of PSR J1917+1352 (IM, red solid and AM, blue dashed). *Middle:* the associated τ spectra along data points from the literature. *Right:* the obtained ΔDM fits for both models (as before: IM, stars and AM, triangles).

4.1.9 PSR J1917+1353 ($P = 0.19$ s, $\tau_{150} = 11$ ms, $DM = 94.7$ pc cm^{-3} , $\delta t = 0.2$ ms, $\delta\nu = 12.2$ kHz)

PSR J1917+1353 was discovered by Swarup, Mohanty & Balasubramanian (1971). It is one of the most distant (5.00 kpc) pulsars in the set. The EPN data base suggests this pulsar has a single component up to 1.4 GHz and the fits are therefore unlikely to be biased by the presence of secondary components.

We channelize the Commissioning data for this pulsar into eight frequency channels, which provides peak S/N values between 5.2 and 12.6. The α values obtained are 2.8 ± 0.4 (IM) and 3.6 ± 0.6 (AM, see Fig. 9, middle panel), the latter of which lies close to theoretical predictions. Scattering values from the literature exist at 102, 160 and 327 MHz (see Table 2).

The K15 data point again underestimates τ according to our own measurements, whereas the data point from Kuzmin & Losovsky (2007) seems in good agreement.

The expected flux density at 150 MHz using the input of Table 1 and a simple power law, is approximate 288 mJy. Our fits suggest flux density values that are similar for both models. At 154 MHz, we find 80 ± 11 mJy (IM) and 86 ± 9 mJy (AM), or 80 ± 40 mJy (IM) and 86 ± 43 mJy (AM) using 50 per cent error margins. Over the HBA band, the flux density changes monotonically in the range 48–126 mJy. At the lowest frequency channel, the profile shows scatter broadening that stretches across the pulse period. This can be seen most clearly for the AM (Supporting Information, Appendix C, shaded region). The flux density spectrum shows no turnover at low frequencies.

4.1.10 PSR J1922+2110 ($P = 1.08$ s, $\tau_{150} = 42$ ms, $DM = 217.0$ pc cm^{-3} , $\delta t = 1.1$ ms, $\delta\nu = 12.2$ kHz)

PSR J1922+2110 has the highest DM value in our data set, and is seen to be an outlier in the DM versus distance plot of Fig. 23. It was discovered in the same low-latitude pulsar survey as PSR J1909+1102 (Davies et al. 1973). We analyse Commissioning data for this pulsar. The high S/N allows us to channelize the band into 16 average profiles. Fitting the IM leads to $\alpha = 2.0 \pm 0.2$ and 3.3 ± 0.4 for the AM (Fig. 10).

Several scattering measurements are available for this pulsar (Table 2). The literature values do not agree well with our estimations. L15 obtained $\alpha = 0.94 \pm 0.88$ for this pulsar, but omitted the value from their subsequent analyses for being ‘suspiciously low’. They measured a τ value at 102.75 MHz of roughly 25 ms,

more than three times lower than our data point of 86.1 ± 6 ms at 112.5 MHz. Their value comes from fitting an EPN data base profile at 102.75 MHz (Kassim & Lazio 1999), for which the phase resolution is poor. L15 further claim that PSR J1922+2110 has an asymmetric profile, such that scattering fits to this pulsar could be fitting profile evolution as well. We note that above 410 MHz, the pulsar has a secondary component. Löhmer et al. (2004) published a τ value of 4.5 ± 1.5 ms at 243 MHz. This was the only frequency at which the authors present an obtained τ value with a standard error. For the higher frequencies, they obtained upper limits on τ only.

We conclude that the LOFAR data set is likely the best data for measuring the scattering parameters, since it provides high peak S/N values (between 6.8 and 16.4) and good phase resolution (1024 bins per pulse period).

As seen from the profile in the left-hand panel of Fig. 10, the IM and AM produce very similar fits to the data. This is true for all the frequency channels. The main difference can be seen in the fit of the scattering tail, where the AM follows a flatter trend. Clear and well-fitted ΔDM trends are shown in the right-hand panel of Fig. 10.

The flux density and a power-law spectral index values of Table 1 lead to an expected flux density of 316 mJy at 150 MHz. The flux density values estimated from our scattered profile fits at 151.4 MHz are again much lower: 89 ± 35 mJy (IM) and 96 ± 30 mJy (AM), or 89 ± 45 mJy (IM) and 96 ± 48 mJy (AM) with increased error margins. The spectra have relatively simple structure, decreasing with frequency. In the AM spectrum, small contributions due to the corrected flux density calculation can be seen, concurrent with the onset of a wrap around profile shape (Supporting Information, Appendices A and C).

4.1.11 PSR J1935+1616 ($P = 0.36$ s, $\tau_{150} = 20$ ms, $DM = 158.6$ pc cm^{-3} , $\delta t = 0.4$ ms, $\delta\nu = 12.2$ kHz)

This pulsar has one of the highest flux density values in the set, having been discovered in a single pulse search using the Lovell Telescope at Jodrell Bank (Davies & Large 1970). In Fig. 23 we see that this pulsar, at a distance of 3.7 kpc, has a higher DM than other pulsars at similar distances.

The Commissioning data for this pulsar are split into eight frequency channels, leading to peak S/N values between 3.6 and 21.2. We obtain an α value of 3.4 ± 0.2 using the IM. This value is in good agreement with the values obtained by Löhmer et al. (2004),

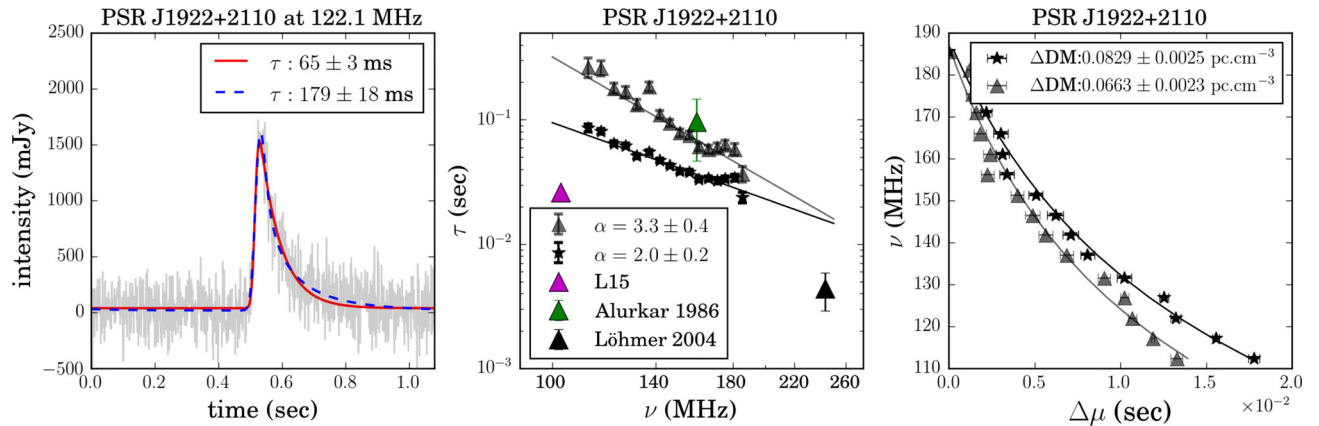


Figure 10. Similar to Fig. 10, for PSR J1922+2110.

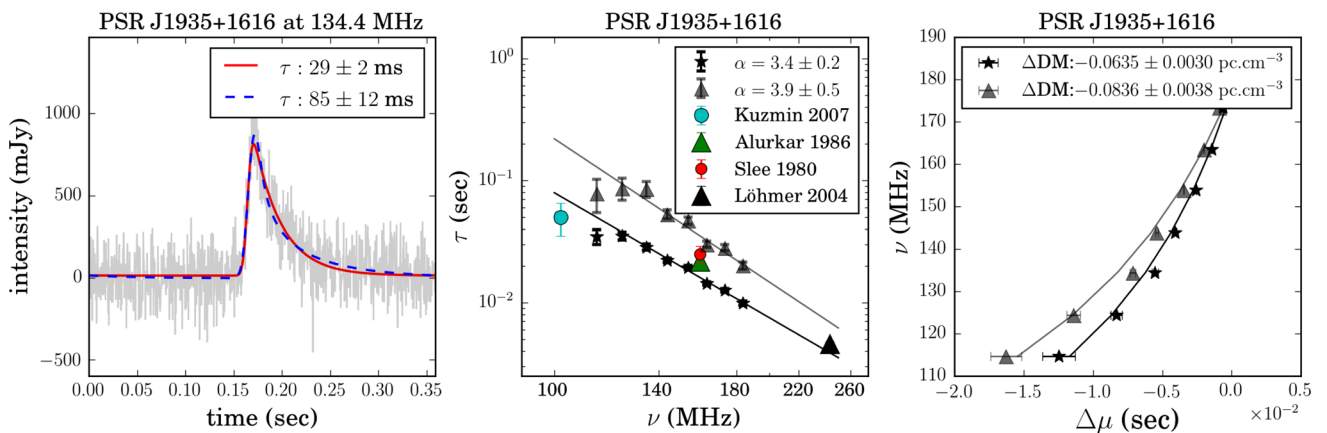


Figure 11. Similar to Fig. 10, for PSR J1935+1616.

$\alpha = 3.4 \pm 0.2$, and L15b, $\alpha = 3.35^{+0.36}_{-0.41}$. Both these literature values of α are determined using other published scattering measurements between 110 and 250 MHz (Rickett 1977; Slee et al. 1980; Alurkar et al. 1986; Löhmer et al. 2001; Kuzmin & Losovsky 2007), and therefore serve as an independent check of our measurements. Our AM leads to $\alpha = 3.9 \pm 0.5$, in agreement with theoretical values of 4 or 4.4. The fits for both models look alike, with the AM reaching slightly higher into the peaks of the pulse profile and having a different slope in the scattering tail.

Published τ measurements from the literature include 50 ± 15 ms at 111 MHz (Kuzmin & Losovsky 2007) and two sets of measurements at 160 MHz of 21.7 ± 1.6 ms (Alurkar et al. 1986) and 25 ± 4 ms (Slee et al. 1980), as shown in Fig. 11 and Table 2. At 327 MHz, K15 published a τ value of 3.21 ± 0.02 ms. Our refitting of the data (which also fits for the underlying width of the intrinsic pulse) leads to a value of 1.8 ± 0.1 ms, whereas keeping the value of σ fixed (as obtained from a 600 MHz template taken from the EPN data base), we find a value of 3.3 ms, in closer agreement to theirs. We note that the K15 profiles at 327 MHz that overlap with our set of pulsars, are generally not very scattered, and that a fixed width method often leads to a fit that does not model the peak of the scattered profile well. Extrapolating to 327 MHz using our obtained isotropic spectral index value, leads to a τ of 1.42 ± 0.18 ms instead, in close agreement to our fit of their data at 327 MHz.

The flux density measurements obtained from our scattering fits (IM and AM) show a turnover at around 170 MHz, i.e. towards the highest observed frequency (Supporting Information, Appendix C).

This turnover is not purely associated with a wrap around scattering tail, as scattering corrections to the flux density only become significant below 145 MHz. The calculated flux density values at 154.1 MHz are 95 ± 27 mJy (IM) and 105 ± 22 mJy (AM). Again, these errors are increased to 50 per cent to reflect the initial flux calibration uncertainties. However, using a simple power law and the flux parameters of Table 1 implies a flux density of approximate 955 mJy at 150 MHz, roughly 10 times larger than our values.

Several authors have noted that the line of sight to PSR J1935+1616 is puzzling, e.g Löhmer et al. (2004). In their study of nine pulsars with intermediate DM values (150–400 pc cm^{-3}), only PSR J1935+1616 had an α value inconsistent with the expected Kolmogorov prediction. The authors suggested the low α value could be due to multiple scattering screens of finite size or varying scattering strengths. Our data certainly point towards anomalous scattering, such as the discussed AM. Alternatively, a truncated scattering screen could provide a basis to interpret the data, as it would lead to both a low α value and a decrease in flux towards low frequencies. A turnover in the flux spectrum (unrelated to a long scattering tail) is seen for PSR J1935+1616. However, as shown in Geyer & Karastergiou (2016), such a scenario would involve an observable change in the pulse profile shapes at low frequencies, which is not evident in the data. Soft edges of the screen, multiple screens and low S/N profiles can render these particular effects difficult to discern. The questions, therefore, surrounding the nature of the scatterer(s) towards this pulsar remain open.

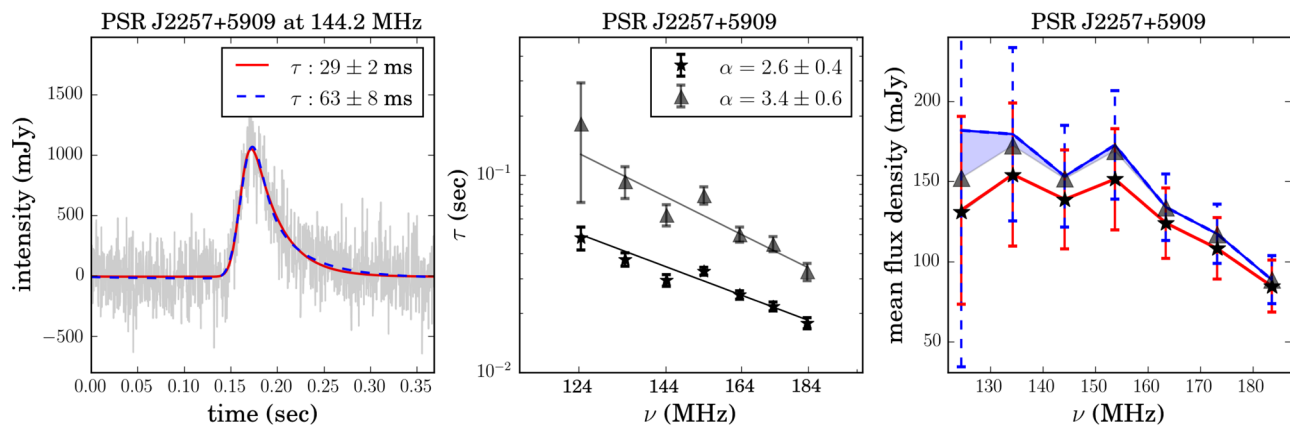


Figure 12. Similar to Fig. 8, for PSR J2257+5909.

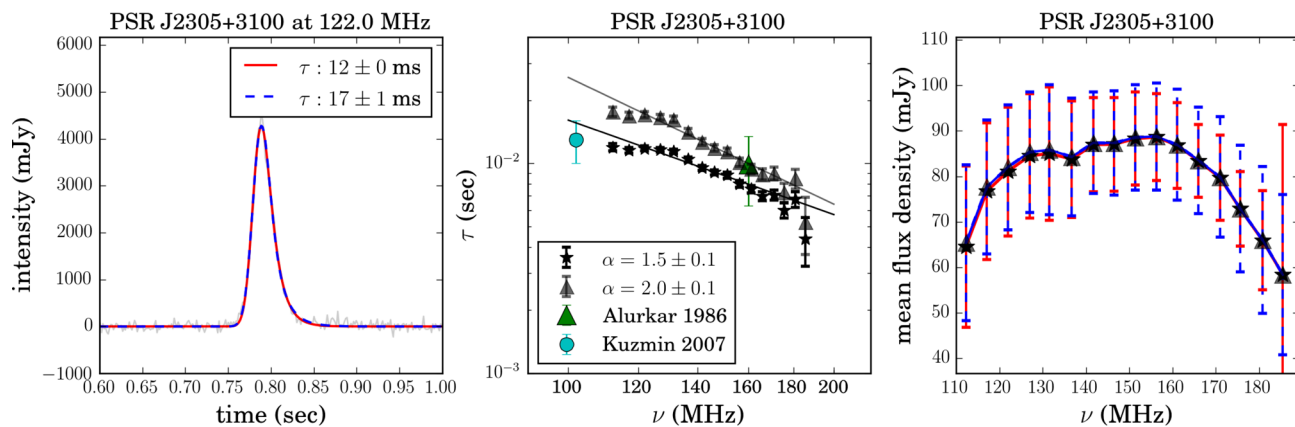


Figure 13. Similar to Fig. 8, for PSR J2305+3100.

4.1.12 PSR J2257+5909 ($P = 0.37$ s, $\tau_{150} = 31$ ms, $DM = 151.1$ pc cm $^{-3}$, $\delta t = 0.4$ ms, $\delta\nu = 12.2$ kHz)

PSR J2257+5909 is a bright pulsar discovered in the same survey as B0540+23 and B0611+22 (Davies et al. 1972). Similar to PSR J1935+1616, it is an outlier on the DM versus distance plot (see Fig. 23). We could not find previously published scattering times for this pulsar. We split the Commissioning data for this pulsar into eight frequency channels, and excluded the lowest frequency channel for which the peak S/N is only 2.34. Fitting the remaining seven scattered profiles, we obtain $\alpha = 2.6 \pm 0.4$ (IM) and $\alpha = 3.4 \pm 0.6$ (AM), which approaches the theoretical value of $\alpha = 4$.

The profile fits obtained by these models are very similar (Fig. 12, left-hand panel). The χ^2_{red} values are near equal, with the AM value consistently smaller than the IM value (Table A1, Supporting Information). The low p -values from the KS test are dominated by two frequency channels. Omitting these two (out of seven) channels, increases the p -values to 85.6 per cent (IM) and 93.8 per cent (AM). The ΔDM trends are less well fit for this pulsar and both models show negative ΔDM fits.

Our flux density spectra, as calculated from the both models, shows the onset of turning over towards lower frequencies. In the case of the AM, the corrected flux density spectrum is straightened out with respect to the uncorrected flux density spectrum (shaded region, right-hand panel of Fig. 12). The associated profile fits of especially the AM show related pulse wrap around at frequencies below 150 MHz (see the Supporting Information, Appendix A).

The calculated flux density values are 151 ± 32 mJy (IM) and 173 ± 34 mJy (AM) at 153.7 MHz, or 151 ± 76 mJy (IM) and 173 ± 87 mJy (AM) with 50 per cent error margins. Table 1 flux parameters, implies a much larger flux density value of approximate 500 mJy at 150 MHz, using a simple power law.

4.1.13 PSR J2305+3100 ($P = 1.58$ s, $\tau_{150} = 9$ ms, $DM = 49.6$ pc cm $^{-3}$, $\delta t = 1.5$ ms, $\delta\nu = 3.1$ kHz)

This pulsar was discovered using Arecibo in 1969 (Lang 1969). It has one of the lowest DM values in the set, but in contrast its distance is estimated to have a lower limit of 25 kpc (Yao et al. 2017). It is the pulsar with the longest pulse period (1.58 s) in the set. We analyse Census data for this pulsar, split into 16 channels. All across the HBA band, the pulse remains only slightly scattered. We find $\alpha = 1.5 \pm 0.1$ (IM) and 2.0 ± 0.1 (AM). An example pulse along with the τ and flux density spectra are shown in Fig. 13. The pulse shape is enlarged, showing the pulse phase from 0.6 to 1.0 s.

An α value of 3.42 ± 0.26 was recently published by L15. They tabulate their own measurements using the GMRT (at 410 MHz to 1.4 GHz), as well as the results from Kuzmin & Losovsky (2007) (at 44, 63 and 111 MHz) and Alurkar et al. (1986) at 160 MHz (see Table 2 for literature values). The τ values published by Kuzmin & Losovsky (2007) are $\tau_{44} = 300 \pm 100$ ms, $\tau_{63} = 110 \pm 20$ ms and $\tau_{111} = 13 \pm 3$ ms. A fit across these three values leads to a spectral index of $\alpha = 3.8 \pm 0.1$. Alurkar et al. (1986) published a

value of $\tau_{160} = 9.9 \pm 3.6$ ms. Our frequency channel closest to an observing frequency of Kuzmin & Losovsky (2007) is 112.3 MHz. For this channel, we find $\tau_{112.3} = 11.9 \pm 0.5$ ms in good agreement with their value at 111 MHz. Extrapolating our τ values to 44 MHz, leads to a τ value of around 55 ms (using the IM), much lower than calculated by Kuzmin & Losovsky (2007).

The p -values for both models are low (Table A1, Supporting Information), but significantly increased, to 79.6 per cent (IM) and 80.8 per cent (AM), when only the first five channels with more notable scattering, are considered.

The near identical scattering fits of the two models and the low levels of scattering, lead to near identical flux density spectra. We compute 88 ± 10 mJy (IM) and 89 ± 12 mJy (AM) at 151.3 MHz. These values are amended to have error bars 44 and 45 mJy, respectively, in line with the original flux calibration uncertainties. The mean published Census flux density value is 70 ± 35 mJy (Bilous et al. 2016), which agrees well with our result. We see a turnover in the flux density spectra at around 150 MHz, however, due to the low τ values compared to the pulse period, this is unlikely due to scattering effects.

5 DISCUSSION

We are now in a position to summarize our results and return to the questions posed in the Introduction, addressing each of them. In order, we first assess the profile fits and address whether AMs are required to fit this LOFAR data set. Thereafter, we consider the distributions of spectral indices obtained by the two models. Next, we investigate what information is gained regarding the profile evolution and DM from the profile fits. This includes analysing the width evolution of the intrinsic profiles. In Section 5.4, we briefly discuss the impact of finite scattering screens, and how this relates to our measurements. Lastly, we return to the well-studied τ versus DM relation and consider how our data correspond to published trends.

5.1 τ measurements using two models

To consider whether the data necessitate AMs, we return to our fits of the scatter broadened data, and thereafter consider the impact on secondary parameters, such as the scattering spectral index α .

We have used χ_{red}^2 values and the KS test to investigate the goodness of fits of the scattering models (Table A1, Supporting Information). Judging from the outcomes of these tests, we do not find any pulsar for which the AM is a requirement. All data are well fitted with the IM. In one case (PSR J0742–2822), the anisotropic result is unreliable, as discussed in Section 4.1.5, producing a spectral index of $\alpha \approx 8$.

We find, as expected, that the fitted τ value for a given profile is larger when applying the AM compared to the IM. Fig. 14 compares the profile shapes modelled with the same τ value. The shapes agree with the intuition that an isotropic scattering medium will scatter more pulsar radiation into the observer’s line of sight, than an equivalent extremely anisotropic scatterer.

We also note that the errors in τ are larger for the extreme AM than for the IM, especially at low frequencies. Fig. 15 shows that the best-fitting profile shape produced by the AM fitting code (black, solid line) is indistinguishable from the shape produced when the τ value is fixed at the best-fitting value plus a 1σ error, and the remaining parameters are refit (cyan, dashed line). The large error bars in τ stem from the anisotropically scattered shape being closer

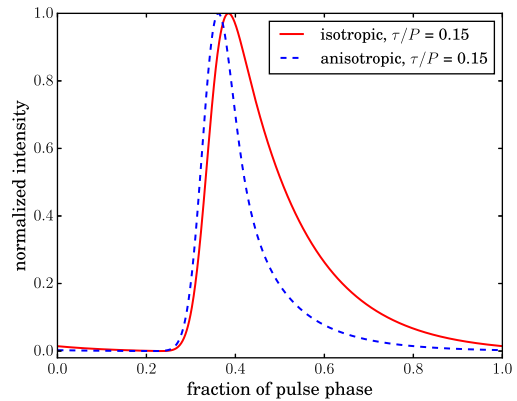


Figure 14. A comparison of modelled isotropic and anisotropic pulse shapes with equal characteristic scattering times. The profiles are plotted to have a peak value equal to unity. All other fitting parameters (σ , μ , A and DC) are equal for both profiles as well.

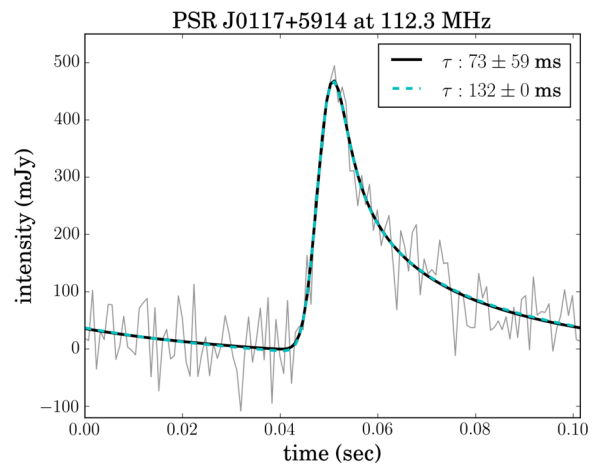


Figure 15. PSR J0117+5914 Census data at the lowest frequency channel of 112.3 MHz. Resulting profile shapes for anisotropic model fits: (1) obtained by calculating the best-fitting τ value (black, solid line), (2) obtained by fixing the τ value to the upper value of the error margin on the best-fitting τ (0.1322 s) and fitting for the rest of the parameters (cyan, dashed). These two model fits are indistinguishable.

in shape to the unscattered Gaussian, which makes it more insensitive to changes in τ at low frequencies. Larger errors in τ lead to larger errors in the spectral indices, as indicated in Table 3.

We note that for four of the pulsars there is some evidence for extreme anisotropy, although it is far from conclusive. In the case of PSRs J0117+5914 and J0614+2229, we find that the χ_{red}^2 value at all frequencies is closer to 1 for the AM and that similarly the p -values from the KS test are higher for the AM. The differences in these values are larger than for most other pulsars in the set. We also find that the α values associated with the two models are well separated for both these pulsars. The other two possible candidates for anisotropy are PSRs J1913–0440 and J2257+5909. In the case of PSR J1913–0440, we see a secondary feature that is well fit by the AM, leading to χ_{red}^2 values closer to 1, and higher p -values in the KS test. The ΔDM correction also minimizes the difference in DM values of the two data sets for this pulsar (Table A2, Supporting Information). Again, the α values obtained by the different models seem to be well separated, with the anisotropic case in agreement with theoretical values. PSR J2257+5909 shows the widest separation in obtained p -values (85.6 per cent versus 93.8 per cent).

Table 3. List of obtained τ values, spectral indices and ΔDM values, using two models.

Pulsar	Isotropic scattering			Extreme (1D) anisotropic scattering		
	τ_{150} (ms)	α	ΔDM (pc cm $^{-3}$)	τ_{150} (ms)	α	ΔDM (pc cm $^{-3}$)
J0040+5716	40 \pm 2	2.2 \pm 0.2	0.0378 \pm 0.0024	86 \pm 8	2.7 \pm 0.3	0.0143 \pm 0.0022
J0117+5914 (Co)	7 \pm 0	2.2 \pm 0.1	0.0082 \pm 0.0009	14 \pm 1	3.5 \pm 0.4	0.0041 \pm 0.0011
J0117+5914 (Ce)	8 \pm 1	1.9 \pm 0.2	0.0064 \pm 0.0006	16 \pm 2	2.6 \pm 0.2	0.0038 \pm 0.0006
J0543+2329	10 \pm 1	2.6 \pm 0.2	0.0155 \pm 0.0020	17 \pm 2	2.7 \pm 0.3	0.0031 \pm 0.0020
J0614+2229 (Co)	15 \pm 1	1.9 \pm 0.1	0.0030 \pm 0.0007	44 \pm 4	2.4 \pm 0.3	-0.0033 \pm 0.0006
J0614+2229 (Cy)	15 \pm 0	2.1 \pm 0.1	-0.0053 \pm 0.0006	44 \pm 3	3.1 \pm 0.3	-0.0109 \pm 0.0008
J0742-2822	20 \pm 2	3.8 \pm 0.4	0.0013 \pm 0.0027	-	-	-
J1851+1259	6 \pm 1	4.0 \pm 0.4	0.0264 \pm 0.0022	10 \pm 1	4.7 \pm 0.4	0.0158 \pm 0.0017
J1909+1102	42 \pm 3	3.5 \pm 0.4	0.0351 \pm 0.0085	120 \pm 27	6.4 \pm 0.7	-0.0276 \pm 0.0077
J1913-0440 (Co)	9 \pm 0	2.7 \pm 0.2	0.0240 \pm 0.0009	16 \pm 1	3.5 \pm 0.3	0.0161 \pm 0.0011
J1913-0440 (Cy)	7 \pm 0	3.3 \pm 0.1	0.0457 \pm 0.0003	12 \pm 0	4.1 \pm 0.2	0.0381 \pm 0.0003
J1917+1353	11 \pm 1	2.8 \pm 0.4	-0.1004 \pm 0.0025	21 \pm 2	3.6 \pm 0.6	-0.1167 \pm 0.0028
J1922+2110	42 \pm 2	2.0 \pm 0.2	0.0829 \pm 0.0025	85 \pm 6	3.3 \pm 0.4	0.0663 \pm 0.0023
J1935+1616	20 \pm 1	3.4 \pm 0.2	-0.0635 \pm 0.0030	46 \pm 4	3.9 \pm 0.5	-0.0836 \pm 0.0038
J2257+5909	31 \pm 2	2.6 \pm 0.4	-0.0317 \pm 0.0058	68 \pm 9	3.4 \pm 0.6	-0.0530 \pm 0.0050
J2305+3100	9 \pm 0	1.5 \pm 0.1	0.0184 \pm 0.0035	11 \pm 0	2.0 \pm 0.1	0.0144 \pm 0.0023
$\langle\alpha\rangle$		2.7 \pm 0.2			3.5 \pm 0.4	

The α values for the two models are also well separated and the anisotropic value is in agreement with theoretical values.

More detailed tests of anisotropy in the temporal domain would require much higher S/N data, to be able to tell the model profile shapes apart. We have only made use of extreme (1D) anisotropic and isotropic models. It would be even more difficult to distinguish between models if lower degrees of anisotropy were included in the scattering models.

Combining temporal analysis with secondary (power) spectra analysis (e.g. Stinebring et al. 2001) and the imaging of pulsars where possible, will increase the efficiency of tests for anisotropy. The very long baseline interferometry (VLBI) constructed image of PSR B0834+06 (Briskin et al. 2010) already provides concrete evidence for highly anisotropic scattering surfaces in the ISM.

5.2 Scattering spectral index distribution

In Table 3, we summarize the obtained spectral indices for each pulsar for a given scattering model. The average spectral index, using the IM, is 2.7 ± 0.2 . This is much lower than the theoretically predicted values of $\alpha = 4$ or 4.4.

Using the IM, the vast majority of pulsars (11 out of 13) have α values smaller than 3.8. Not a single pulsar is measured to have an α value larger than 4.0. Only three pulsars have spectral indices in close agreement with the theoretically predicted values (viz. PSRs J0742-2822, J1851+12 and J1909+1102).

Similar low-frequency spectral indices have been reported in L15 and Lewandowski et al. (2013, hereafter L13), although many of the values were dropped from the subsequent analysis in the papers for being *suspiciously low*. Four of the pulsars that were excluded in L15 for which we also have measurements, include: PSRs J0614+2229 (L15: $\alpha = 1.73 \pm 0.5$, our $\alpha = 2.1 \pm 0.1$), J0742-2822 (L15: 2.5 ± 0.3 , our value: 3.9 ± 0.4), J1917+1353 (L15: 2.11 ± 0.05 , our value: 2.9 ± 0.4) and J1922+2110 (L15: 0.98 ± 0.88 , our value: 2.0 ± 0.2).

In GK16, at the hand of simulated data, we discuss how the accuracy of τ and consequently α measurements, depend on the relative value of τ to the pulse period (P). Large τ/P values lead to scattering tails that wrap around the full rotational phase, and can in extreme cases lead to less accurate estimates of τ values. Fig. 16

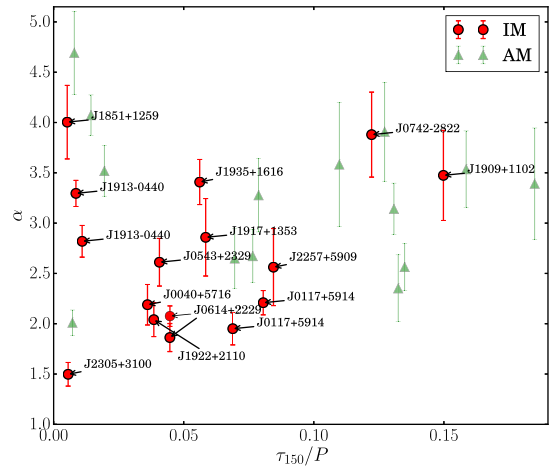


Figure 16. Spectral indices α plotted versus τ values at 150 MHz in units of the pulse period. These τ values are obtained from the best-fitting power law to the τ spectrum of each pulsar. Isotropic values are shown in red (circles), and anisotropic values in green (triangles). Isotropic data points are labelled by the corresponding pulsar names. The larger the τ_{150}/P values, the more the scattering tail of the average pulse profile will wrap around the full rotational phase.

shows the α values as a function of the degree of scattering relative to the pulse period, characterized by the fraction τ_{150}/P , with τ_{150} the scattering time value at 150 MHz. We see that for all pulsars $\tau_{150}/P < 0.15$, using the IM. There is no clear dependence of α on these values. For a given τ_{150}/P value, we find a range of α values. This is reassuring, as it shows no sign of systematic offsets in α values obtained from our code.

In the previous section, we have discussed screen anisotropy. We note that the mean spectral index for the AM is equal to 3.5 ± 0.4 , higher than for the IM and much closer to the theoretically expected values. In 10 out of the 13 objects, the increase in α using an AM is larger than 20 per cent, and for all but 1 the increase is larger than 10 per cent. However, for five objects, the α values associated with the IM and AM lie within the error bars of each other, making the outcomes of the models less distinct. The anisotropic α value for the majority of pulsars (9/13) has error bars reaching to the theoretically

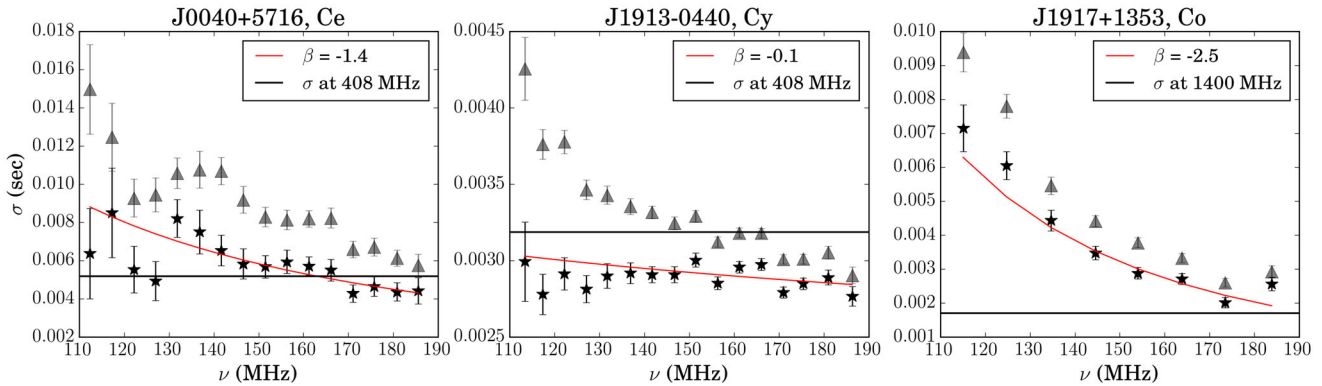


Figure 17. The evolution of intrinsic pulsar widths (represented by σ) with frequency, for a subset of the pulsars. The width evolution is shown for both the isotropic model (stars) and extremely anisotropic model (circles). The high-frequency widths as published in Lorimer et al. (1995, at 408 MHz) and Hobbs et al. (2004, at 1.4 GHz) are shown as horizontal solid lines. We have transformed their full width at half-maximum values (w_{50}) to σ values. The spectral indices of a power-law fit to the isotropic data ($\sigma \propto \nu^\beta$) are shown in the legends. Plots for the rest of the source list can be found in the Supporting Information (Appendix B).

expected values. However, as also noted in the previous section, the error bars on the anisotropic spectral indices are typically larger than for the IM.

In GK16, we have shown that fitting simulated anisotropic pulsar profiles with an IM, leads to incorrect τ values and lower spectral indices. The model-dependent α values obtained here, for which anisotropic values are often closer to theoretically predicted values, can be considered potential evidence for anisotropic scattering. Other possibilities for lower spectral indices include screens that are truncated, that have extreme scattering properties or multiple screens along a given line of sight. In Section 5.4, we discuss whether we find evidence for finite scattering screens.

5.3 Profile evolution and DM corrections

5.3.1 Profile evolution

The simplified canonical pulsar emits a cone-shaped beam along its magnetic axis. Observational evidence shows that pulse profiles are often broader at low frequencies, and that multicomponent separation decreases with frequency. Physically, this is understood to mean that high-frequency radiation is emitted closer to the neutron surface and low frequencies higher up in the magnetosphere (Thorsett 1991), leading to the phenomenon known as *radius-to-frequency mapping* (RFM, Cordes 1978).

Apart from this expected evolution of the pulsar width, a wide variety of intrinsic profile changes with frequency have been observed (see e.g. Lyne & Manchester 1988 and Mitra & Rankin 2002). Hassall et al. (2012) analysed the profile evolution of four pulsars at LOFAR frequencies, and found that none of them are well explained by RFM.

An optimal de-scattering technique would remove the effects of scattering, revealing the intrinsic evolution of the pulsar with frequency. We have picked the sources in this paper not only based on the scattering tails they exhibit, but also for having simple single-component profile shapes that do not show dramatic profile evolution. However, when scattering dominates the observed profile shape, as is the case for most of our sources at HBA frequencies, it is difficult to decouple scattering effects from profile evolution. Ideally, an exact understanding of the scattering mechanism and its dependence on frequency, would allow us to disentangle scattering and profile shape changes. As the evidence for anomalous scatter-

ing and deviations from expected scattering trends (e.g. $\tau \propto \nu^{-4}$) increases, this becomes less straightforward.

Our model assumes an intrinsic Gaussian-shaped profile and fits for the underlying Gaussian components in each frequency channel. The obtained standard deviation of the Gaussian (σ) is used as a proxy for pulse width. We analyse the evolution of σ with frequency. We compare the obtained σ values at HBA frequencies to the pulsar widths measured at higher frequencies by Lorimer et al. (1995, at 408 MHz) and Hobbs et al. (2004, at 1.4 GHz). The results for a subset of pulsars are shown in Fig. 17, the rest of which appear in the Supporting Information (Appendix B).

We find that for the majority of the pulsars, the widths correspond well to the higher frequency results. In most cases, the widths measured at the high-frequency end of the HBA band are close to the corresponding widths at higher frequencies, as can be seen for PSR J0040+5716 in the left-hand panel of Fig. 17. The cases for which the high-frequency widths are greater than the widths obtained by the IM, include PSRs J0117+5914, J0614+2229, J1913–0440 and J1935+1616. In the case of PSR J0117+5914, as was seen in its flux density spectra as well, outcomes differ significantly between the Commissioning and Census data. PSR J1913–0440 (middle panel of Fig. 17) has been discussed as a pulsar with possibly a secondary component, evidence for which is seen not only in the profile shapes, but also in the deviations of the τ spectrum at low frequencies. PSR J1913–0440 has also been considered a candidate for evidence for anisotropy. Here, we see that the width evolution of the intrinsic pulse modelled by the IM and AM is significantly different (middle panel of Fig. 17). The AM shows a clear decrease in width with frequency and is in closer agreement to the high-frequency width obtained by Lorimer et al. (1995). The pulsar which shows the most well-defined width evolution is PSR J1917+1353, as depicted in the right-hand panel of Fig. 17. The isotropic case is fitted with a power law, $\sigma \propto \nu^{-2.5}$. Hobbs et al. (2004) estimated $w_{50} = 4.0$ ms, which translates to $\sigma = 1.7$ ms. Our lowest measured width value for PSR J1917+1353 is 2.0 ± 0.15 ms.

5.3.2 DM corrections

As seen throughout Section 4, by fitting for the centroid values (μ) of the intrinsic Gaussian components, we can estimate small corrections to the DM values, that we have labelled as ΔDM . Fig. 18 shows the distribution in ΔDM values for both models. Although the

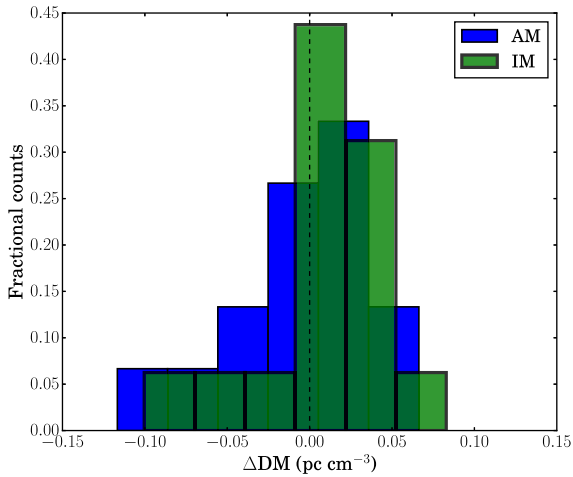


Figure 18. Spread in ΔDM values obtained for our set of pulsars.

histogram represents only a small number of sources, it appears that positive ΔDM values are obtained more frequently than negative values, for both fitting models. A positive value here refers to an overestimation in the original data DM value by an amount of ΔDM . Rerunning the data reduction with a value set to $\text{DM} - \Delta\text{DM}$ removes this dependence of $\Delta\mu$ on frequency.

From Fig. 18, we conclude that small errors in DM values are likely to be introduced by the traditional method in which DM values are obtained. This relies on finding the DM value for which the S/N of the sum of the channelized average pulse profiles is maximized, and is therefore sensitive to the location of the peaks of the channelized data in general. In the case of highly scattered profiles, the true location of the centroid of the intrinsic pulse lies earlier in time to when the peak of the signal is observed. Furthermore, this change is larger at low frequencies and smaller at high frequencies, such that, typically, the DM value required to maximize the S/N of the sum of the intrinsic pulse profiles is lower than the value required to maximize the sum of the scattered pulses.

We also have instances in which the obtained ΔDM is negative, and therefore the original DM was an underestimation. The asymmetric effect of scattering on pulse shapes tends to drag the profile centroids to larger τ values. However, effects such as the intrinsic profile evolution described previously, can cause shifts in either direction. It is therefore possible, through such counteracting impacts, to obtain DM values that are over- or underestimated.

DM corrections are critical to improve pulsar timing models. However, due to both intrinsic pulse evolution and the fact that at high frequencies (where pulsar timing observations are typically conducted), a smaller angular scale of the ISM is sampled than at lower frequencies (Cordes, Shannon & Stinebring 2016), the DM corrections obtained here, cannot straightforwardly be extrapolated to timing observations.

5.4 Finite scattering screens

As discussed in Section 5.2, and in more detail in Cordes & Lazio (2001) and GK16, lower α values can result from finite scattering screens.

If indeed some of the lower α values obtained at low frequencies here, are the result of finite scattering screens in the ISM, we can estimate the scattering screen size for each pulsar at which deviations from theoretical α values (associated with infinite screens)

Table 4. The angular size of mid-way screens at 150 MHz, for six pulsars, based on their obtained τ values at 150 MHz and the distance to the source. The six shown are the ones with the three largest and three smallest associated scattering screens (excluding PSR J2305+3100 at 25 kpc). The last column provides the required baseline ($B = \lambda/2\sigma_\theta$) to resolve such screens with a low-frequency VLBI network, where $\lambda = 2$ m is the wavelength corresponding to 150 MHz.

Pulsar	Screen size ($2\sigma_\theta$, mas)	Baseline (km)
J0040+5716	165	2485
J1922+2110	130	3149
J2257+5909	130	3150
J1851+1259	62	6571
J1917+1353	61	6726
J1913–0440	53	7665

will become observable. For a mid-way screen, τ can be expressed as

$$\tau = \frac{D\sigma_\theta^2}{c}, \quad (4)$$

with D the distance from the pulsar to the observer, σ_θ the standard deviation of the distribution in observing angles and c the speed of light. Using the τ values at 150 MHz for each pulsar (obtained from the τ spectra power-law fits), we calculate the maximum scattering screen size at 150 MHz at which observations become sensitive to the finite nature of the screen. Table 4 shows the associated scattering screen sizes for six pulsars as well as the required observing baseline to be able to resolve them. We have chosen σ_θ as a representation of the radial screen size (such that the diameter is $2\sigma_\theta$).

To show conclusively that the observed low α values are correlated with finite scattering screens, would therefore likely require a low-frequency interferometer with large baselines, as given in Table 4. The current version of the Low Frequency VLBI Network mostly includes 18 and 92 cm receivers in e.g Russia, India and China. An alternative approach, as mentioned in the Introduction, is to use the space-based observatory *RadioAstron*, jointly with ground-based instruments to form extreme baseline interferometers (Smirnova et al. 2014).

A dependence of τ on frequency that shows a break in its power-law spectrum, can too be evidence for truncated screens, as flux density is lost at longer wavelengths where observations become sensitive to the size of the screen, altering the shape of the observed profiles (GK16). None of the pulsars in our set show clear evidence for broken power-law τ spectra across the HBA frequency band. Broad-band observations at higher frequencies are required to investigate whether these breaks are observed. However, it is likely that small scattering screens will not have physically sharp edges, and therefore could feasibly result in increasingly flatter frequency dependencies on τ for a given range of frequencies.

A correlation between low α values and high DM values has been promoted by data sets such as in Löhmer et al. (2001). In Fig. 19, we show the dependence of α with DM. This figure includes data points from several other papers, as described in the legend and the caption of the figure.

Löhmer et al. (2001) suggested that beyond a given DM threshold ($\text{DM} > 300 \text{ pc cm}^{-3}$), α values deviated from the theoretically expected values. This threshold has been revisited by L13 (amongst others), who suggested that deviations in α start occurring at lower DM values, around $\text{DM} = 230\text{--}250 \text{ pc cm}^{-3}$. In their more

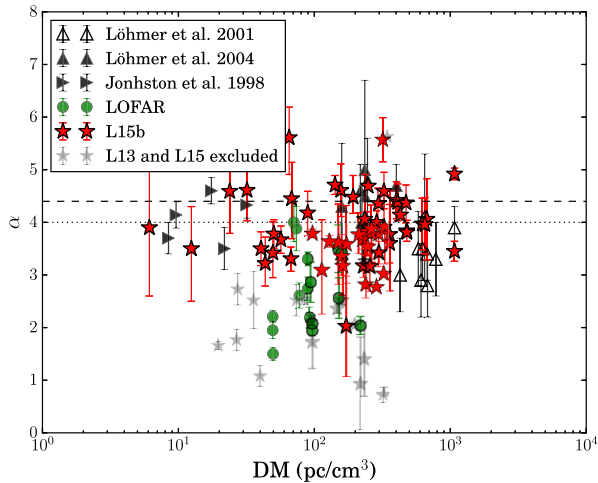


Figure 19. Spectral indices (α) are plotted against the corresponding DM values. The LOFAR data set of this paper is shown in green (dark circles), with other data points from the literature as indicated in the legend. We show the updated L13 and L15 values as given in L15b (red, dark stars), along with the lower α values from these papers, that were excluded from further analyses (grey, lighter stars).

recent paper (L15), however, additional α measurements have led them to conclude that the previously postulated DM threshold was based on data biased by a small number of τ measurements.

The LOFAR data show low α (<4) values in the DM range 49–217 pc cm^{-3} . We investigate whether the distribution of α values with respect to distance (or DM as a proxy for distance) such as seen in Fig. 19 can be produced by a simple picture using truncated scattering screens. As a first step, we simulate the observed scattering of a 0.6 s period pulsar, with a Gaussian shape and a duty cycle of 2.5 per cent (chosen to represent our set of pulsars) behind a circularly truncated screen. We note that the set of LOFAR pulsars all have distances between 1.5 and 5.0 kpc (excluding PSR J2305+3100 at 25 kpc), and an α distribution between 1.5 and 4.0. Fig. 20 shows how this distance and α distribution can be modelled using truncated screens. The setup uses a single-truncated screen of varying size and scattering strength. The scattering strength is defined by the standard deviation of the Gaussian distribution in scattering angles, as described in more detail in GK16. Here, we label a scattering strength of $\sigma_a = 3$ mas as ST = 3. For a range of distance values, a screen is placed mid-way between the pulsar and observer, and the α value over the HBA band calculated. By tweaking the screen size and scattering strength, a set of distance– α pairs are obtained.

In a similar way, low α values, as observed in Löhmer et al. (2001), for more distant pulsars (between 6.3 and 10.2 kpc, and $400 < \text{DM} < 1100$, in units of pc cm^{-3}) can be produced through truncated scattering screens. This, however, would require screens with higher scattering strengths or multiple scattering screens along a given line of sight. It is unlikely that this simplistic picture describes the whole truth. However, evidence for typical sizes and or scattering strengths of screens in the ISM can shed light on the causes of low α values.

5.5 Correlations between scattering and flux density loss

For each data set, we calculated an average mean flux density spectrum by summing the intensities of the best-fitting curve (and dividing it by the number of phase bins across the pulse pro-

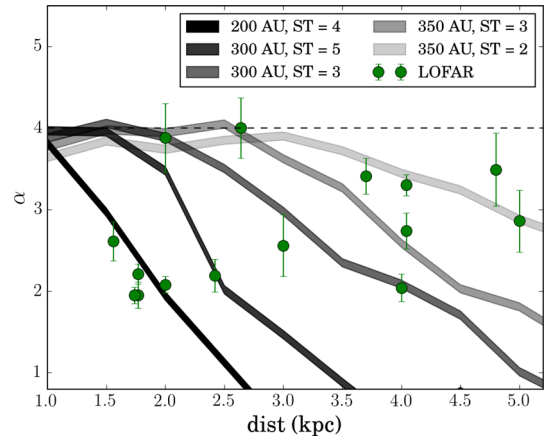


Figure 20. The LOFAR data points from this paper (large green circles), along with computed α models, that are based on a simple truncated screen model. Circular screens are placed mid-way along the line of sight for a set of distances. The screens can differ in size and scattering strength. A simulated pulsar is scattered by the modelled screen and the α value over the HBA frequency range is estimated. The theoretical value of $\alpha = 4$ is shown as a dashed line. The model with the most extremely deviating values of α (darkest line) is based on a screen with radius 200 au and scattering strength, ST = 4 (see the text for definition). The other model screen sizes and strengths are shown in the legend.

file) per frequency channel. This (uncorrected) flux density is corrected for scattering effects through an estimate of the associated raised baseline level (see Section 3). Examining the average profiles for each pulsar, we find six cases in which profiles with wrap around scattering tails are visible. These are the cases in which we would expect to see an associated flux density loss [see Geyer & Karastergiou (2016) for more detail], and therefore a discrepancy between the uncorrected and corrected flux density. The six pulsars are PSRs J0117+5914, J0742–2822, J1909+1102, J1917+1353, J1935+1616 and J2257+5909, as discussed in the results section. The flux density spectra for all the sources can be viewed in the Supporting Information (Appendix C).

From this set of six, four show a correlation between the flux density spectrum turnover and the onset of wrap around scattering tails. This includes PSR J1909+1102 which has the highest τ_{150}/P (IM) value of the set, namely 0.15 (see Fig. 16) and the joint highest τ_{150} value of 42 ± 3 ms (IM, see Table 3). PSRs J1917+1353 and J1935+1616 show wrap around scattering tails that do not correlate with the associated flux density spectra. In the case of PSR J1917+1353, there is no clear turnover in its flux density spectrum, and the turnover in the flux density spectrum of PSR J1935+1616 is at too high a frequency to only be related to long scattering tails. These two pulsars have the lowest τ/P ratio (0.06) of the six pulsars that show pulse run-in. It is therefore perhaps not unexpected that the flux density spectrum is not dominated by the scattering effects. As discussed in more detail in Section 4.1.11 such a turnover could potentially be due to scattering by finite scattering screens.

There are three pulsars for which the spectra appear to turnover without the profiles exhibiting extreme scattering tails. These are PSRs J0614+2229 and J1913–0440 for which the flux density spectrum turns over at high frequencies (around 170 MHz), even though τ_{150}/P is equal to only 0.01, and PSR J2303+3100 which is only weakly scattered, $\tau_{150}/P = 0.01$, but has a turnover at around 150 MHz. It therefore seems clear that when the scattering appears to be weak, the flux density spectrum shape will be dominated by other effects such as thermal absorption (e.g. Rajwade, Lorimer &

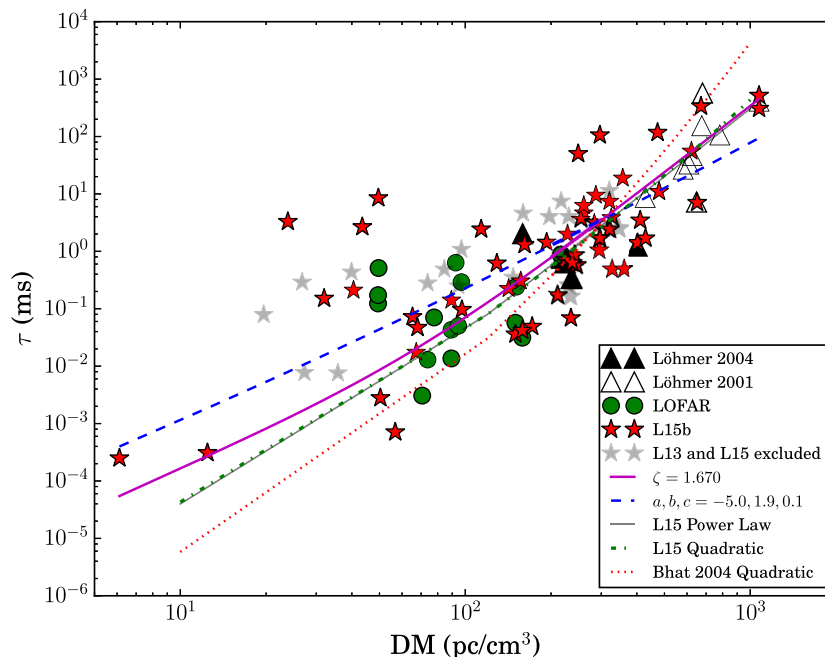


Figure 21. Scattering time (τ) at 1 GHz versus DM values for our data set along with data from Löhmer et al. (2001, 2004) and L15b. L15b contains τ values for most sources in L13 and L15. The data points which were considered erroneous in L13 and L15 are also shown (grey stars). The LOFAR data points from this paper are shown as green (dark) circles. To obtain fits all the data, except those marked as *excluded*, were used. The obtained fits are a power-law fit (magenta, solid thick line) and a parabolic fit (blue dashed line). The plot also includes the parabolic fit from Bhat et al. (2004) (red, dotted line), as well as the power-law and parabolic fits from L15 (grey solid, green dash-dotted lines) respectively.

Anderson 2016) or intrinsic emission properties, or perhaps some form of anomalous scattering. In the cases for which the scattering is large, we do see the expected correlations between scattering and flux density measurements.

Our method estimates the degree to which flux is lost due to scattering effects. However, for the correction to hold an understanding of the scattering mechanisms is required (i.e. the correct scattering model has to be used). It will therefore be valuable to compare these corrected values to flux density estimates obtained from interferometric pulsar images. The authors are currently analysing joint imaging and beam-formed LOFAR data to conduct such a comparison.

5.6 Scattering time versus DM and distance

We now revisit the scattering time (τ) dependence on DM. Bhat et al. (2004) published an empirical relationship between these quantities valid for over 10 orders of magnitude in scattering times, and DM values between 1 and 1000 pc cm^{-3} . A parabolic function, $\log \tau = a + b \log \text{DM} + c (\log \text{DM})^2$, is fitted to their data. Alternatively, power laws of the form $\tau \propto \text{DM}^\gamma (1 + \kappa \text{DM}^\zeta)$, where γ is fixed at 2.2, as determined from a Kolmogorov spectrum, have been used (Ramachandran et al. 1997; Löhmer et al. 2004).

Fig. 21 shows our fits to an ensemble of τ values at 1 GHz versus DM values. Our obtained IM α values have been used to transform τ values to 1 GHz. The data sets of Löhmer et al. (2001, 2004) and L15b are also shown, along with obtained fits. The excluded data points from L13 and L15 are shown as grey stars. The LOFAR data points from this paper are shown as green (dark) circles.

It is clear that the fitted trends obtained by us, L13 and L15 at low DM values, promote higher τ values than originally proposed by the Bhat et al. (2004) fit. Our fit indicates even larger τ values at

the low DM values than L13 and L15. Our parameter fits, compared to L15, are $a = -5.0$ (L15, $a = -6.3$), $b = 1.9$ (L15, $b = 1.5$) and $c = 0.1$ (L15, $c = 0.5$). From the power-law fits, Ramachandran et al. (1997) and Löhmer et al. (2004) have obtained $\zeta = 2.5$ and 2.3, whereas L15 finds 1.74 and we find 1.67.

If indeed, the Bhat et al. (2004) relationship can be considered a true reflection of the τ dependence on DM at higher frequencies (e.g. 1 GHz), then our result shows that in order for the relationship to be upheld, our low spectral index values found at low frequencies, cannot persist up to higher frequencies. In order to reach the Bhat et al. (2004) dependence at higher frequencies with our set of pulsars, their spectral index will need to evolve with frequency. Access to broad-band data at higher than LOFAR frequencies for these pulsars, where scattering is still measurable, will allow us to investigate whether spectral indices indeed change.

Fig. 22 shows a similar plot of τ versus DM, but for τ at 100 MHz. Here, we find $\zeta = 0.96$, much lower than in Fig. 21. The plot shows that our obtained values are in good agreement with the Kuzmin & Losovsky (2007) data set, and again argues for frequency-dependent α .

In Fig. 23, the relationship between the distance and DM for the sources in this paper is shown. Arrows indicate the changes in distance estimates from the NE2001 electron density model (Cordes & Lazio 2002) to the YMW16 model (Yao et al. 2017). The majority of the sources have DM values below 100 pc cm^{-3} . There is no clear increase of DM with distance. Four pulsars are clear outliers on this plot, having higher DM values than the rest of the set. This could point to more complex and dense ISM environments along the lines of sight to these pulsars. In Section 4.1.11, we pointed out that the line of sight to PSR J1935+1616 has been considered anomalous in the literature (Löhmer et al. 2004).

Three of the four outliers have been discussed in Section 5.5 as pulsars with wrap around scattering tails. The fourth pulsar is PSR

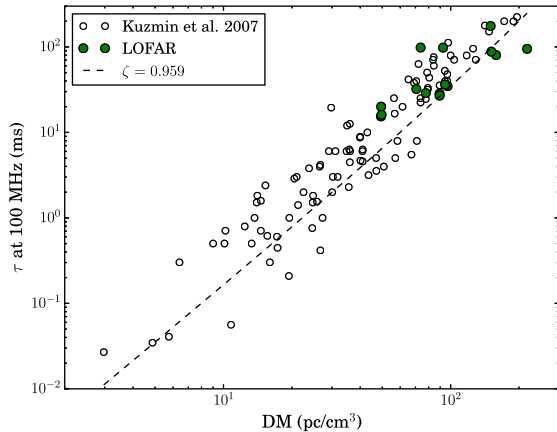


Figure 22. The relationship between DM values and τ at 100 MHz, as obtained from the Kuzmin & Losovsky (2007) data set (empty circles) and the LOFAR data set in this paper (green circles).

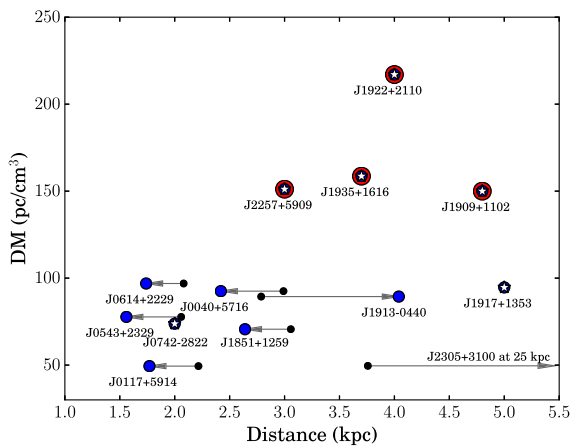


Figure 23. The relationship between DM and the distances for our data set. The DM values of the majority of these pulsars are less than 100 pc cm^{-3} . The blue (small) circles indicate the distances as estimated by the YMW16 model (Yao et al. 2017) or from associated objects (see Table 1). Arrows starting from black dots indicate the change in distance estimates from the NE2001 model (Cordes & Lazio 2002) to the YMW16 model. The data point for PSR J2303+3100 is excluded as it lies far to the right. There are four clear outliers to the typical distance versus DM trend, shown as large circles with red outlines. These high DM values could indicate a more dense and complex ISM along the lines of sight to these sources. Pulsars for which DM-independent distance measurements exist are marked with white stars.

J1922+2110, which together with PSR J1909+1102 has the largest τ_{150} value of 42 ± 2 (IM, Table 3). Its low-frequency profiles along with the flux density spectrum reveal that pulses will likely start overlapping at frequencies just below the lowest observed frequency channel of 112.5 MHz.

6 CONCLUSIONS

In this paper, we show that low-frequency pulsar observations lead to measurements of the scattering spectral index α (obtained by IMs) ranging between 1.5 and 4.0. This is much lower than expected from simple theoretical models. Our analysis in the temporal domain shows potential evidence for anisotropic scattering in 4 out of 13 sources. The low α value distribution can also be modelled using a set of truncated scattering screens. Studies in the temporal domain do not allow us to fully distinguish between anisotropy

and truncated screens. Combining our work with results at higher frequencies, we surmise that the average α across this population is lower at these low frequencies than previous measured values at 1 GHz, suggesting a frequency evolution of α . Interferometric imaging, including space-ground experiments, is key in investigating the typical sizes of scattering surfaces, while scintillation results are required for precise scattering measurements at higher frequencies. Both of these techniques should aid the investigation of the frequency dependence of α . Furthermore, polarization measurements can serve as a sensitive diagnostic to small amounts of scattering, as demonstrated in Karastergiou (2009). Such accurate indicators can assist in distinguishing between intrinsic profile evolution and propagation effects. Lastly, the best tests for anisotropic scattering rely on high-resolution dynamic spectra, with parabolic arcs in secondary spectra arising as a natural consequence of anisotropy (Stinebring et al. 2001). The pulsars discussed in this paper are good candidates for this list of further investigations.

An Online Appendix with supplementary material is provided. It is compiled as a single pdf file, and contains the average pulse profile fits of the pulsars used in this study along with the goodness-of-fit parameters (Supporting Information, Appendix A), additional figures showing the fitted width evolution of the profile shapes (Supporting Information, Appendix B) and additional flux spectra of the target sources (Supporting Information, Appendix C).

ACKNOWLEDGEMENTS

This paper is based (in part) on data obtained with the International LOFAR Telescope (ILT). LOFAR (van Haarlem et al. 2013) is the Low Frequency Array designed and constructed by ASTRON. It has facilities in several countries, that are owned by various parties (each with their own funding sources), and that are collectively operated by the ILT foundation under a joint scientific policy. This study also specifically made use of data from the long-term LOFAR core project LT5_003 (PI: J.P.W. Verbiest). The authors would like to thank the LOFAR Pulsar Working Group for valuable comments and discussions. MG is a Commonwealth Scholar funded by the UK government. VIK, JWTH and DM acknowledge funding from an NWO Vidi fellowship and from the European Research Council under the European Union's Seventh Framework Programme (FP/2007-2013)/ERC Starting Grant agreement no. 337062 ('DRAGNET'). We thank the MNRAS scientific editor and anonymous reviewer for their valuable comments to improve the quality of this manuscript.

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SUPPORTING INFORMATION

Supplementary data are available at [MNRAS](https://www.mnras.org) online.

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