

Division of labour and the evolution of extreme specialisation

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1 **Abstract:** Division of labour is a common feature of social groups, from biofilms to complex
2 animal societies. However, we lack a theoretical framework that can explain why division of
3 labour has evolved on certain branches of the tree of life but not others. We model the divi-
4 sion of labour over a cooperative behaviour, considering both when it should evolve and the
5 extent to which the different types should become specialised. We found that: (1) division
6 of labour is usually—but not always—favoured by high efficiency benefits to specialisation
7 and low within-group conflict; and (2) natural selection favours extreme specialisation, where
8 some individuals are completely dependent upon the helping behaviour of others. We make
9 a number of predictions, several of which are supported by the existing empirical data, from
10 microbes and animals, while others suggest novel directions for empirical work. More generally,
11 we show how division of labour can lead to mutual dependence between different individuals
12 and hence drive major evolutionary transitions, such as those to multicellularity and eusociality.

13
14 Division of labour is a defining feature of complexity at all levels of biological organisation^{1–5}.
15 If individuals specialise to perform certain tasks, more complex social groups can evolve. In
16 the extreme, if the different individuals become dependent upon the tasks performed by oth-
17 ers, then a new ‘higher level’ individual may emerge. Examples include genes with different
18 functions in a genome, cells that form distinct tissues in an animal, and castes that carry out
19 different tasks in social insect societies. Consequently, in order to understand why complex
20 life has evolved, we must understand the evolution of division of labour.

21 We lack theory that can explain why division of labour has evolved on some branches of the
22 tree of life, but not others. Previous work has focused on clonal groups of cells and eusocial
23 insects^{6–14}. In both of these cases, it has often been assumed that the fitness interests of
24 individuals are perfectly aligned, and so the evolution of division of labour is favoured if it
25 increases group fitness (supplementary tables 1 & 2). However, division of labour also arises in
26 species such as bacteria, slime moulds and cooperatively breeding animals where there can be
27 appreciable conflict within groups and so cannot be assumed to be ‘superorganisms’^{2,15,16}. If
28 there is conflict within groups, then division of labour would not be selected for just because it
29 increases group fitness^{17–19}. Furthermore, if division of labour plays a role in driving transitions
30 such as those to multicellularity and eusociality, then we need to understand how it can first
31 evolve from individual level selection^{2,4,20}.

32 Division of labour can take different forms (Figure 1). In the simplest possible scenario, with
33 only one cooperative behaviour, a division of labour consists of ‘helpers’ and ‘reproductives’
34 that may be specialized to varying degrees. The helper could be a fully specialised, sterile
35 helper or a generalist that both helps and reproduces. Similarly, the more reproductive type
36 could be a pure reproductive or a generalist that engages in some helping. This suggests four
37 broad types of division of labour—from two different generalist types that help and reproduce
38 at different rates, to the extreme case of a sterile helper paired with a pure reproductive (Figure
39 1). However, most models assume that only a certain type of division of labour is possible,
40 often with fully specialised sterile helpers^{7,9,10,12,18} (supplementary tables 1 & 2). Therefore,
41 these models cannot be used to explain variation in the form that division of labour takes.

42 We theoretically model how a number of factors could influence selection for division of
43 labour and its various forms. We wish to find the conditions that would favour both the initial
44 evolution of division of labour, and the evolution of extreme specialisation, with individuals
45 losing the ability to reproduce independently. We are interested in insights that could be
46 applied across a range of different biological systems. Consequently, we construct a deliberately

47 simple approximation, focusing on the trade-offs that we hypothesise are likely to be of general
48 importance, rather than a complex model of a specific system²¹.

49 Results

50 We consider an infinite population that is divided into social groups of fixed, finite sizes in
51 which individuals engage in social interactions locally but offspring compete globally for niches
52 in the next generation (island model). The genetic relatedness between individuals in a social
53 group is given by R , which represents the relative probability that they are identical by descent
54 (see methods).

55 We allow individuals to perform a costly cooperative behaviour, which increases the survival
56 or reproductive viability of social group members. Specifically, a fraction $1 - \lambda$ of the benefit
57 of cooperation goes to the focal individual and the remaining fraction λ is distributed to the
58 other members of the social group (Figure 2c). We allow for potential efficiency benefits from
59 greater cooperation with the parameter α (Figure 2b), which determines whether the benefits
60 from increased cooperation are linear ($\alpha = 1$), accelerating ($\alpha > 1$) or decelerating ($\alpha < 1$).
61 We vary the extent to which the cooperative trait is essential for survival with the parameter
62 e . If $e = 1$, then cooperation is essential and individuals that reside in social groups with no
63 cooperation have a fitness of zero. As e decreases, the trait is less essential and the cooperative
64 behaviour becomes more of a luxury activity.

65 We allow for a division of labour into two phenotypes (Figure 2a). At the start of their
66 life cycles, individuals terminally adopt phenotype 1 with probability p and phenotype 2 with
67 probability $1 - p$. Phenotype 1 invests a fraction q_1 of its lifetime efforts toward the cooperative
68 trait and the remaining fraction $1 - q_1$ is allocated toward personal survival or reproduction.
69 In contrast, phenotype 2 invests q_2 into the cooperative trait. When the two phenotypes differ,
70 we will tend to assume that $q_1 > q_2$, such that, without loss of generality, phenotype 1 is more
71 cooperative. Consequently, we are allowing three independent traits to co-evolve in our model:
72 the level of cooperation of each phenotype (q_1, q_2), and the relative ratio of the two phenotypes
73 (p). In our analysis, we used equilibrium theory to determine the strategy that is expected to
74 evolve in the long-term (see methods and supplementary information 1, 2 & 3)^{21,22}. The key
75 predictions of our model are given in Table 1.

76
77 **What types of division of labour are stable?** Our model allows several possible strate-
78 gies: uniform non-cooperation (no individuals help), uniform cooperation (all individuals are
79 identical generalists that both help and reproduce) and four different types of division of labour
80 (Figure 1). The types of division of labour are defined by the presence or absence of the ex-
81 treme possible phenotypes: sterile helpers ($q_1 = 1$) and pure reproductives ($q_2 = 0$) (Figure
82 1). We found that uniform non-cooperation, uniform cooperation and division of labour could
83 all arise as long-term evolutionary strategies (Figure 3).

84 We found that there was an evolutionary bias to more extreme forms of division of labour,
85 where one of the phenotypes does all of the cooperation (Figure 3). The two types of division of
86 labour that could be favoured were those with a pure reproductive ($q_2 = 0$) paired with either
87 a generalist helper ($0 < q_1 < 1$) or with a sterile helper ($q_1 = 1$). In contrast, we did not find
88 a region of parameter space where either of the other two types of division of labour, in which
89 both phenotypes engage in cooperation, could evolve (Figure 3). Specifically, the combination
90 of a generalist ($0 < q_2 < 1$) with either a more cooperative generalist ($q_2 < q_1 < 1$) or with a

91 sterile helper ($q_1 = 1$) was never found to be stable. In supplementary information 4, we show
92 that these results hold if we relax the assumption that cooperative costs are linear.

93 Why are intermediate forms of division of labour, where both phenotypes cooperate, not
94 stable? We hypothesise that there may be an evolutionary feedback loop in which helper
95 specialisation drives reproductives to help less and reproductive specialisation drives helpers to
96 help more. In order to test this hypothesis, we developed dynamic, individual-based simulations
97 as a proof of principle (Figure 4; supplementary information 5).

98 We held the level of cooperation in one phenotype fixed (q_1 or q_2) and allowed the other
99 phenotype to evolve. We found that when phenotype 2 invested more resources into reproduc-
100 tion, phenotype 1 invested more resources into cooperation (lower q_2 drives higher q_1 ; Figure
101 4a). In turn, when phenotype 1 invested more resources into cooperation, phenotype 2 was
102 driven more rapidly to pure reproduction ($q_2 = 0$; Figure 4b). More generally, the higher we
103 fixed the level of cooperation of one phenotype, the higher the investment into reproduction
104 of the other phenotype (Figure 4c).

105 To examine how these effects feedback on to each other, we considered the consequences
106 of allowing just one phenotype to evolve for some time and before allowing both phenotypes
107 to evolve. We initially held fixed the level of cooperation of phenotype 2 ($0 < q_2$ fixed), which
108 lead to the other phenotype evolving to an intermediate level of cooperation ($q_1 < 1$; Figure
109 4d). When we then allowed both phenotypes to evolve, they always drove each other to the
110 specialist extremes of pure reproduction ($q_2 = 0$) and sterile helping ($q_1 = 1$; Figure 4d).

111 The only intermediate form of division of labour that we find to be stable is the pairing of
112 a generalist with a pure reproductive ($0 < q_1 < 1; q_2 = 0$). In a later section, we discuss how
113 one of the conditions required for division of labour to be favoured is that there are efficiency
114 benefits to specialisation ($\alpha > 1$). If division arises, we also found that the same condition
115 ($\alpha > 1$) always favours the stability of pure reproduction ($q_2 = 0$). Consequently, whenever
116 division of labour evolves, one phenotype will always be a pure reproductive ($q_2 = 0$). In
117 contrast, efficiency benefits to specialisation ($\alpha > 1$) are necessary but *not* sufficient for the
118 stability of a sterile helper ($q_1 = 1$). The evolution of a sterile helper therefore requires more
119 restrictive conditions than a pure reproductive and thus an intermediate division of labour
120 composed of the former phenotype but not the latter would never occur ($q_1 = 1; q_2 > 0$).

121

122 **Division of labour in nature.** Our prediction that more extreme forms of division of labour
123 should be observed correspond to the patterns observed in the natural world. Considering
124 cell groups, the most common form of division appears to be between sterile helpers and
125 pure reproductives^{15,23}. One of the clearest examples is the germ-soma divide in multicellular
126 animals. Similarly, in microorganisms such as bacteria, fungi, algae and slime moulds, there
127 are numerous examples of a sterile helper paired with a pure reproductive^{18,24–27}. In contrast,
128 less extreme division of labour involving a generalist paired with either a pure reproductive or
129 a sterile helper appears to be relatively rare, with a single example of each from bacteria and
130 algae respectively^{28,29}.

131 In animal groups, there appears to be two most common forms of division of labour. First,
132 in the social insects, the divide between queens and their workers is between pure reproductive
133 and sterile or effectively sterile-workers^{2,3,7}. Second, in cooperative breeding vertebrates and
134 invertebrates, the division is commonly associated with age—individuals help when young,
135 and breed when old^{2,16}. While our model captures the essence of why division of labour is
136 favoured for these species, they also introduce a number of other factors, such as costs and

137 benefits of cooperation varying with age, relatedness asymmetries, and individuals who are
138 ‘failed breeders’^{16,30}. However, as predicted by our model, there are no known instances of
139 division of labour in animals between a sterile helper and a generalist (that engages both in
140 breeding and in helping others breed).

141 Our examination of the pattern in nature requires two points of clarification. First, in
142 all these cases, the appropriate comparison is one trait at a time. So, pure reproductives
143 with respect to one trait, may engage in other cooperative behaviours. For example, in the
144 cyanobacterial division of labour, the cells that do not fix nitrogen are pure reproductives
145 with respect to that trait, but can perform other cooperative traits, such as photosynthesis²⁴.
146 Second, there may be an observation bias towards discovering more extreme division of labour.
147 Our prediction emphasizes the need for a quantitative survey of the types of division of labour
148 in nature, rather than a reliance on just the systems that are being studied.

149 Our results do not categorically forbid the other two other types of division of labour in
150 nature. Instead, our analysis offers a simple null model such that, if a form of division of labour
151 not predicted by our model has evolved, then there must exist a complexity in the biological
152 system not captured by our model and its assumptions. An example is provided by division
153 of labour between sterile helpers and generalists in some Volvocine algae lineages²⁹. When
154 these algae reproduce, the reproductive cells must grow to the size of offspring colonies before
155 reproduction. As such, any reproduction comes with a large commitment of resources, leading
156 to helper sterility providing a large discontinuous resource bonus not contained in our model⁶.

157 **Relatedness and division of labour.** A standard assumption has been that a higher related-
158 ness favours division of labour^{2,15,23}. Indeed, many models of division of labour have assumed
159 the extreme relatedness of clonality, or that it is group fitness that is being maximised^{6,7,9,10,12}.
160 In contrast, we found that relatedness (R) has no influence on whether division of labour is
161 favoured for essential traits ($e = 1$) that are required for reproduction or survival (Figure
162 3a-3b). A higher relatedness has no influence because the fitness benefit of being a pure re-
163 productive is then exactly cancelled by the indirect fitness cost of not helping relatives in the
164 group.
165

166 However, for non-essential traits ($e < 1$), a higher relatedness (higher R) does favour the
167 evolution of division of labour (Figure 3c-3d). The main reason for this is that, as relatedness
168 decreases, the indirect benefits of cooperation are reduced, and so uniform non-cooperation can
169 outcompete cooperative division of labour¹⁸. Combining our trends, the overall prediction is
170 that a higher relatedness (higher R) will favour division of labour for some traits (non-essential;
171 $e < 1$), but not for other traits (essential; $e = 1$). The extent to which a trait is essential may
172 change over evolutionary time—for example, a trait might start as relatively non-essential, and
173 then become more essential as a group becomes more social, with more division of labour. In
174 this case, relatedness could be more important for the initial evolution of division of labour
175 than for its later maintenance. An empirical example is the subsequent loss of strict lifetime
176 monogamy in some eusocial insects³¹.

177 In the empirical data from multicellular groups, a higher relatedness is correlated with a
178 greater likelihood of division of labour²³. This is consistent with our model if the data are
179 drawn only from non-essential traits, or a mix of essential and non-essential traits. In animal
180 groups, a higher relatedness, due to lower levels of promiscuity, also leads to individuals being
181 more likely to spend time as a helper in cooperative breeding vertebrates^{32,33}. Our predictions
182 suggest that it would be useful to further divide traits on the basis of how essential they are,

183 and then test for how this interacts with relatedness.

184 Considering the different types of division of labour, our model predicts that a higher
185 relatedness (higher R) favours more extreme division of labour regardless of whether the trait
186 is essential or non-essential ($0 < e \leq 1$; Figure 3). In particular, a higher relatedness favours
187 division between a sterile helper and pure reproductive ($q_1 = 1, q_2 = 0$) over division between
188 a generalist and a pure reproductive ($0 < q_1 < 1, q_2 = 0$).

189 Our predicted influence of relatedness is consistent with the empirical data for multicellular
190 groups, where groups with a higher relatedness are more likely to have sterile helpers²³. Exper-
191 imental evolution studies have also found that the sterile helpers are disfavoured at relatively
192 low relatedness, in both slime moulds and fungi^{34,35}. In animal groups, the division between
193 sterile helper and pure reproductive also appears to be favoured by a higher relatedness, with
194 eusociality having only evolved in sexual species that have strict lifetime monogamy, or asexual
195 species that reproduce clonally^{3,31,36}.

196 In contrast to our predictions and the empirical data, some have argued that monogamy
197 (higher R) may sometimes disfavour cooperation and division of labour^{37,38}. However, subse-
198 quent work showed that these conclusions are based on restrictive assumptions. For example,
199 in Nonacs’s model, the best way for individuals to ‘help’ relatives is to disperse and reduce
200 competition for resources rather than to stay and help kin^{37,39}. In turn, the results of Olejarz
201 et al.’s model are an artefact of constraining the analysis to the invasion of unconditionally
202 expressed worker sterility in colonies where only an intermediate proportion of sterile workers
203 is optimal (supplementary information 7.5)^{38,40}.

204

205 **Clonal groups and lifetime monogamy.** While higher relatedness tends to favour division
206 of labour, our model shows that maximal relatedness ($R = 1$) is not required for division of
207 labour to evolve, or even for the most extreme form of division between sterile helpers and
208 pure reproductives ($q_1 = 1, q_2 = 0$; Figure 3)¹⁸. Many previous models of division of labour
209 have assumed maximal relatedness ($R = 1$), such that there is no conflict within-groups, and
210 analysed how division of labour can maximise group fitness^{6,7,9,11,12}. We have shown that
211 division of labour can still be favoured, even with relatively low relatedness ($R < 1$) where
212 there can be appreciable within-group conflict. This is consistent with Hamilton’s rule, which
213 showed how altruistic sterile helping can be favoured when $R < 1$ ^{17,18}. More generally, this
214 emphasises how division of labour can be favoured by kin selection at the level of the individual
215 rather than simply by group efficiency maximisation.

216 Our prediction that maximal relatedness is not necessary is supported by cases where
217 division of labour with sterile and reproductive helpers has been observed in non-clonal mul-
218 ticellular groups^{23,26}. In social insects, lifetime monogamy leads to a potential helper being
219 equally related to their siblings and their own offspring, which is equivalent to $R = 1$ in our
220 asexual model^{3,19,23,31}. Consequently, although eusociality has only evolved in species with
221 lifetime monogamy or asexual reproduction, our theory shows that the initial evolution of
222 division of labour, while favoured by maximal relatedness, does not require this condition in
223 principle.

224

225 **Ecological benefits and further predictions.** Many previous models found that division of
226 labour is favoured when there is an efficiency benefit to specialisation, with non-linear returns
227 to increased cooperation ($\alpha > 1$)^{6,11,12,41}. In supplementary information 7.1, we show that an
228 efficiency benefit to specialisation ($\alpha > 1$) is necessary, but not sufficient for the evolution of

229 division of labour (Figure 3)^{9,42}. Instead our model also makes a suite of predictions for how
230 the efficiency benefits of increased cooperation interact with a number of other factors (Table
231 1; supplementary information 7.2 & 7.3). For example, division of labour is more likely to
232 evolve if the benefits of cooperation are generously shared between individuals (high λ), and
233 if the trait is very essential for survival (high e).

234 Our model also makes predictions about the factors that favour the most extreme form of
235 division of labour, with sterile helpers and pure reproductives (high α , λ , e and R), and the
236 factors that determine the optimal ratio of helpers to reproductives, (p^*) (Table 1; supplemen-
237 tary information 7.4). These different factors can interact in unforeseen ways that qualitatively
238 change predictions. For example, whether an increase in efficiency benefit of specialisation (α)
239 and trait sociality (λ) leads to higher, lower or has no influence on the optimal proportion of
240 helpers (p^*) can depend on the type of division of labour that is favoured (Figure 5).

241

242 **Life-history and population demography.** As we are interested in patterns that hold
243 across a range of different biological systems, we constructed a deliberately simple model,
244 focusing on the factors that we believe are likely to be of broad importance (see methods). For
245 example, we purposefully left relatedness as an independent parameter ('open' model), and
246 assumed that competition for breeding spots was global²¹. In some cases, for specific species,
247 or groups of species, the way that the demographic processes generate relatedness patterns
248 may be important for the evolution of division of labour. For these cases, our predictions
249 may not hold and it could be useful to develop 'closed' models to examine how relatedness is
250 determined by population demography and to make more targeted predictions⁴³. We solve a
251 closed model in supplementary information 6 and show that limited dispersal and overlapping
252 generations both lead to higher relatedness in a way that favours the evolution of sterile helper
253 and pure reproductive division of labour over uniform non-cooperation.

254 Broadly, our conceptual understanding of division of labour has been anchored to a limited
255 number of complex systems, particularly the eusocial insects, cooperative breeders, and certain
256 obligate multicellular organisms. Our model did not incorporate a number of factors that
257 have been argued to be important in these systems, such as haplodiploid genetics, partially
258 overlapping generations and large group sizes^{2,6,17,44-46}. Furthermore, we did not restrict our
259 model to the extreme case of maximal group relatedness, with clonal groups formed from single
260 cells (or family groups from lifetime monogamy). Instead, our results show that the evolution
261 of division of labour does not require such specific life-history characteristics and can evolve in
262 much simpler cases. More generally, there is a rich precedent in evolutionary theory of using
263 the predictions of simple models to better understand the behaviour of complex systems^{2,21,22}.

264 Conclusion

265 To conclude, we found that when division of labour is favoured, it tends to adopt extreme
266 forms, involving pure reproductives that are dependent upon the helping behaviour of others.
267 We found that helper sterility may evolve even with appreciable within-group conflict. This il-
268 lustrates that division of labour is not merely a group level adaptation that evolves to maximise
269 group efficiency¹⁹. Division of labour can be favoured by kin selection at the level of the indi-
270 vidual and play a significant role in members of social groups becoming dependent upon each
271 other. Consequently, division of labour is a driver, not a consequence, of major evolutionary
272 transitions to higher levels of individuality, such as multicellularity and eusociality.

273 Methods

274 **The fitness equation.** We write the fitness of an individual as its expected fitness averaged
 275 across the possible phenotypes. Specifically, the neighbour-modulated (direct) fitness of a focal
 276 mutant with strategy (p, q_1, q_2) is given by:

$$W = p(1 - q_1) \left[(1 - e) + e((1 - \lambda)q_1^\alpha + \lambda(PQ_1^\alpha + (1 - P)Q_2^\alpha)) \right] \\ + (1 - p)(1 - q_2) \left[(1 - e) + e((1 - \lambda)q_2^\alpha + \lambda(PQ_1^\alpha + (1 - P)Q_2^\alpha)) \right],$$

277 where P, Q_1 and Q_2 are the average, others-only trait-values of social group neighbours^{21,48,49}.
 278 The two terms (top row, bottom row) represent the realised fitness when of phenotype 1 (with
 279 probability p) and phenotype 2 (with probability $1 - p$), respectively. Alternatively, the fit-
 280 ness equation may be conceptualized as the fitness of a founding individual of a social group,
 281 expressed as an expectation over the fitness of its descendants in the last generation of the
 282 social group before dispersal (haystack model.) The essentiality of the trait, e , is defined as
 283 the fraction of the realised fitness benefit that arises from cooperation rather than the asocial
 284 environment. The fitness benefit from cooperation in turn is composed of the benefit from per-
 285 sonal investment in cooperation $((1 - \lambda)(\dots))$ and the benefit that arises from the investment
 286 of social group neighbours $(\lambda(\dots))$. The benefit due to cooperation of social group neighbours
 287 is equal to $\sum_{i=1}^N (p_i q_{1,i}^\alpha + (1 - p_i) q_{2,i}^\alpha) / N$, where i is an index of social group members that
 288 does not include the focal individual. We approximate this as $(PQ_1^\alpha + (1 - P)Q_2^\alpha)$, which
 289 holds under rare mutation and weak selection (arithmetic mean is approximately equal to the
 290 geometric mean in this case.)

291
 292 **Equilibrium analysis.** We seek the Evolutionarily Stable Strategy (ESS), (p^*, q_1^*, q_2^*) , which
 293 is the strategy that, when employed by all individuals in the population, is uninvadable by
 294 a rare mutant lineage with an alternate strategy²². In supplementary information 1, we use
 295 numerical methods to determine the equilibria of the model, except in a number of special
 296 cases where we are able to solve for the equilibria analytically. An equilibrium point is defined
 297 as a joint strategy (p, q_1, q_2) for which directional selection in each trait is zero. We employ
 298 the directional selection forms developed by Taylor and Frank and Brown and Taylor^{48,49}. For
 299 example, directional selection in p is given as $W_p(p, q_1, q_2) = \frac{\partial W}{\partial p} + R \frac{\partial W}{\partial P}$, where the partial
 300 derivative are evaluated for a monomorphic population ($p = P, q_1 = Q_1, q_2 = Q_2$) and R is the
 301 relatedness of interacting individuals. We employ an open model approach and assume that
 302 R is a fixed, independent parameter of the model. An equilibrium strategy is then an ESS if
 303 it is uninvadable such that rare mutants are always less fit than an arbitrary individual in the
 304 equilibrium population. In supplementary information 2, we confirm that the equilibria of our
 305 model are uninvadable, and hence ESSs, with an analytical uninvadability analysis, numeri-
 306 cal verification and individual-based simulations. In supplementary information 3, we use the
 307 methodology of Brown and Taylor to show that all of the ESSs analysed are convergent stable,
 308 such that the population is expected to evolve toward the equilibrium in trait-space⁴⁹.

309
 310 **Model assumptions.** The construction of our model and its analysis relies on a set of life
 311 history, demographic and evolutionary assumptions, each of which may limit the applicability of
 312 the model in specific cases, for specific species. For example, we assumed that the population is

313 infinite, structured into groups of fixed size, that reproduction is asexual with non-overlapping
314 generations and that mutations are rare and lead to weak differences in selection. We also
315 assumed that all competition is global. Taken as a whole, this constructs a model for division
316 of labour that is only exact for very simple forms of life and we do not claim that our model
317 makes exact predictions for division of labour in all species. However, we contend that our
318 predictions should also hold broadly in nature when averaged across the tree of life. This
319 will be true so long as our assumptions have not removed or rendered rigid a factor that is
320 consistently important for the evolution of division of labour.

321 In some cases, factors that we have not modelled may be subsumed into the analysis.
322 For example, although our model does not explicitly model the role of group size (N) in the
323 evolution of division of labour, such predictions may be generated if we assume a relationship
324 between group size and the other factors in our model. For example, in the Volvocine algae,
325 it has been argued that the efficiency benefit of specialisation (α) is an increasing function of
326 group size such that $\alpha = \alpha(N)$ and $\alpha'(N) > 0$. In this case, assuming that cooperation is
327 favoured, we recover the previously found result that increasing group size N favours division
328 of labour⁶. Alternatively, if the benefits of cooperation are shared less equally in larger groups
329 (lower λ), then larger groups would disfavour division of labour.

330 In supplementary tables 1 and 2, we summarize how our model compares and links to
331 previous theoretical work on the evolution of division of labour.

332

333 **Code availability.** Custom code used to demonstrate the uninvadability of the equilibria and
334 the feedback effect driving extreme specialisation are available at osf.io/w6tzk.

335

336 **Data availability.** Data that was generated in our equilibrium analysis is available at
337 osf.io/w6tzk.

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452 **Author contributions**

453 G.A.C carried out the modelling work; G.A.C. and S.A.W. conceived the study and wrote the
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455 **Competing interests**

456 The authors declare no competing interests

Figure Legends

Figure 1: the different possible forms of division of labour. There are four broad forms of division of labour, each defined by the presence or absence of the two fully specialised phenotypes: pure reproductives (i.e. germline cells or social insect queens) and sterile helpers (i.e. somatic cells or worker castes). A *sterile helper and pure reproductive* division of labour (top left) is composed of both fully specialised phenotypes. The three other kinds of division of labour contain at least one generalist phenotype that invests in both tasks. In the strategy containing two different generalist phenotypes (bottom right), one of these phenotypes is cooperating at a higher level than the other.

Figure 2: a division of labour model. We consider a cooperative trait that individuals may invest in at a private cost. (a) The evolving traits. At the start of its life-cycle, an undifferentiated individual (top, shaded) stochastically adopts one of two phenotypes (middle). Individuals become phenotype 1 with probability p and phenotype 2 otherwise. Each phenotype invests a fixed amount of lifetime effort (q_1 or q_2) into the cooperative trait (bottom). When the two phenotypes differ, we tend to assume that phenotype 1 invests more into cooperation ($q_1 > q_2$). The traits p, q_1 and q_2 are the characteristics that are allowed to evolve in the model. (b) The benefits of cooperation. We allow for accelerating ($\alpha > 1$) or diminishing ($\alpha < 1$) returns to increased investment in cooperation. Each individual has a baseline benefit $1 - e$ regardless of the social environment. If $e = 1$, the trait is essential. Otherwise ($e < 1$), it is non-essential. The maximal return that can be attained via cooperation is then given by e (trait essentiality). (c) The trait sociality. A proportion λ of the returns from personal investment in cooperation will benefit social group neighbours equally (others-only; focal helper excluded.) The remaining $1 - \lambda$ benefits the focal helper alone. An additional parameter, R (not shown), quantifies the degree of relatedness within social groups of the population (others-only).

Figure 3: the evolution of division of labour. We examine how the various factors influence the strategy that is expected to evolve. Intermediate division of labour composed of generalists and pure reproductives is broadly favoured by increasing benefits to specialisation, high trait sociality, high trait essentiality and high relatedness. If these factors are pushed to further extremes, then an extreme form of division of labour with sterile helpers and pure reproductives may be favoured. No other form of division of labour is observed to be stable. See supplementary information 1-3 for more details.

Figure 4: the evolution of extreme specialisation. We hypothesized that there exists an evolutionary feedback loop whereby helper specialisation drives reproductives to specialise further on reproduction and reproductive specialisation drives helpers to help more. As a proof of principle, we tested this hypothesis with dynamic, individual-based simulations. (a) We find that the level of cooperation of the helper phenotype, q_1 , evolves to higher levels of cooperation when the reproductive phenotype, q_2 , is more fully specialised (low q_2 ; dashed) than when it is less specialised (high q_2 ; solid). (b) We find that the level of cooperation of the reproductive phenotype, q_2 , evolves more quickly to pure reproduction ($q_2 = 0$) when the helper phenotype, q_1 , is more fully specialised (high q_1 ; dashed) than when it is less specialised (low q_1 ; solid). (c) If we hold one phenotype fixed we find that the lower the level of cooperation of the fixed phenotype, the higher the level of cooperation of the evolving phenotype and vice versa. (d) If we hold reproductive specialisation (q_2) fixed for 10,000 generations, then the level of helper cooperation (q_1) evolves stably to an intermediate value. If we then allow the level of cooperation of both phenotypes (q_1 and q_2) to evolve for another 10,000 generations, then both phenotypes are driven to their specialised extremes ($q_1 = 1$ and $q_2 = 0$.) All error bars are 95 percent confidence intervals over simulation repetitions. See supplementary information 5 for more details.

Figure 5: the proportion of helpers and the level of cooperation. Our model makes a number of predictions about what form division of labour should take, including the optimal proportion of helpers and their level of cooperation. We found that the way certain factors affect the proportion of helpers depends on the form of division of labour that is favoured. For example, (a) if the helpers are

508 sterile ($q_1^* = 1$), then an increase in the efficiency benefits of specialisation (higher α) has no effect upon
509 the optimal proportion (p^*) of helpers ($q_1^* = 1$). However, if the helpers are generalists ($0 < q_1^* < 1$),
510 then a higher α decreases the optimal proportion of helpers (lower p^*). Similarly, (b) if the helpers are
511 sterile ($q_1^* = 1$), then an increase in the sociality of the trait (higher λ) increases the optimal proportion
512 (higher p^*) of helpers ($q_1^* = 1$). However, if the helpers are generalists ($0 < q_1^* < 1$), then a higher λ
513 decreases the optimal proportion of helpers (lower p^*). These different predictions arise because, when
514 there are generalists, the amount that they help (q_1^*) also changes (c and d). So for example, with a
515 high efficiency benefit (higher α), we predict few generalists (lower p^* ; a) but who help a lot (high q_1^* ;
516 c). In contrast, an increase in social group relatedness (higher R) or trait essentiality (higher e) leads
517 to an increase in the optimal helper proportion (higher p^*) regardless of the form of division that is
518 favoured ($0 < q_1^* \leq 1$; not shown). See supplementary information 7.4 for more details.

	Model Predictions	Empirical Validation?
<p>When is division of labour favoured?</p>	<p>1. (a) If the trait is non-essential ($e < 1$), higher relatedness (higher R) favours division of labour. (b) If the trait is essential ($e = 1$), there is no effect of the value of relatedness.</p> <p>2. (a) If relatedness, trait sociality and trait essentiality are high (higher R, λ and e), a higher efficiency benefit to specialisation (higher α) favours division of labour. (b) Otherwise, uniform non-cooperation may be favoured.</p> <p>3. Higher trait sociality (higher λ) favours division of labour.</p> <p>4. If relatedness and trait sociality are low and the efficiency benefits are high (low R and λ; high α), a higher trait essentiality (higher e) favours division of labour.</p> <p>5. Depending on how group size (N) influences factors such as the efficiency benefits to specialisation (α), the extent to which the benefits of cooperation are shared (λ) or social group relatedness (R), a larger group may favour or disfavour division of labour.</p>	<p>Clonal cell groups ($R = 1$) are more likely to have a division of labour²³. In animal groups, lower levels of promiscuity (higher R), leads to individuals being more likely to spend time as a helper in cooperative breeding vertebrates^{32,33}. In all cases, distinction between essential and non-essential traits is not tested.</p> <p>Formal test needed. However, greater group size does correlate with division of labour in some systems and this may be due to altered efficiency benefits^{6,25,29}.</p> <p>-</p> <p>-</p> <p>Larger colony sizes have been found to favour division of labour in the <i>Volvocine</i> algae⁶.</p>
	<p>5. The only forms of division that are favoured are those with a pure reproductive ($q_2 = 0$) paired with either a sterile helper ($q_1 = 1$) or a helper-reproductive ($0 < q_1 < 1$).</p>	<p>Formal test needed. Of the 7 discussed examples of microbial division of labour, 5 are sterile helper and pure reproductive, 1 is generalist and pure reproductive and 1 is sterile helper and generalist division of labour^{24-29,47}.</p>
<p>What kind of division is favoured?</p> <p>When are sterile helpers favoured?</p>	<p>6. Higher relatedness (higher R) favours helper sterility.</p> <p>7. (a) If relatedness, trait essentiality and trait sociality are high (high R, e and λ), higher efficiency benefits to specialisation (higher α) favours helper sterility. (b) Otherwise, higher efficiency benefits (higher α) may favour uniform non-cooperation.</p> <p>8. Higher trait sociality (higher λ) favours helper sterility.</p> <p>9. If relatedness and trait sociality are low and the efficiency benefits are high (low R and λ; high α), higher trait essentiality (higher e) favours helper sterility.</p>	<p>Clonal cell groups ($R = 1$) are more likely to have sterile cells²³. Sterile helpers are disfavoured at low relatedness in both slime moulds and fungi^{34,35}. In animal groups, eusociality has only evolved under conditions of strict lifetime monogamy (higher R)^{3,31,36}.</p> <p>-</p> <p>-</p> <p>-</p>
<p>What affects the proportion of helpers?</p>	<p>10. Higher relatedness (higher R) favours a higher proportion of helpers (higher p^*).</p> <p>11. (a) If the helpers are sterile ($q_1 = 1$), a higher efficiency benefits to specialisation (higher α) favours a lower proportion of helpers (lower p^*). (b) Otherwise, there is no effect.</p> <p>12. (a) If helpers are sterile ($q_1 = 1$), higher trait sociality (higher λ) favours a higher proportion of helpers (higher p^*) (b) Otherwise, higher trait sociality (higher λ) favours a lower proportion of helpers (lower p^*).</p> <p>13. Higher trait essentiality (higher e) favours a higher proportion of helpers (higher p^*).</p>	<p>Clonal cell groups ($R = 1$) have a higher proportion of helpers but study lacks phylogenetically independent comparisons and so is not statistically significant (more data needed)²³.</p> <p>-</p> <p>-</p> <p>-</p>

519

520 **Table 1: Model predictions and empirical validation: the evolution of division of labour.**

521 We present the key predictions of our model with respect to the conditions in which division of labour
522 is favoured, what kind of division may be favoured, whether the extreme form of division with sterile
523 helpers and pure reproductives is favoured and the factors that affect the proportion of helpers (if
524 division is favoured.) We also specify whether the predictions have been previously tested empirically.
525 The entry ‘-’ implies that an empirical test is needed.