

# Organizing Conceptual Knowledge in Humans with a Grid-like Code

Alexandra O. Constantinescu<sup>1\*†</sup>, Jill X. O'Reilly<sup>1,2,3,†</sup>, Timothy E. J. Behrens<sup>1,3\*</sup>

<sup>1</sup>Oxford Centre for Functional MRI of the Brain, University of Oxford, John Radcliffe Hospital, Headington, Oxford, OX3 9DU, UK.

<sup>2</sup>Department of Experimental Psychology, University of Oxford, 9 South Parks Road, Oxford OX1 3UD, UK.

<sup>3</sup>Donders Institute, Radboud University, Nijmegen, The Netherlands.

<sup>4</sup>Wellcome Trust Centre for Neuroimaging, University College London, 12 Queen Square, WC1N 3BG, London, UK.

\*Correspondence to: [alexandra.constantinescu@magd.ox.ac.uk](mailto:alexandra.constantinescu@magd.ox.ac.uk) (AOC),  
[behrens@fmrib.ox.ac.uk](mailto:behrens@fmrib.ox.ac.uk) (TEJB).

† These authors contributed equally to this work.

It has been hypothesized that the brain organizes concepts into a mental map, allowing conceptual relationships to be navigated in a similar fashion to space. Grid cells use a hexagonally-symmetric code to organize spatial representations and are the likely source of a precise hexagonal symmetry in the functional magnetic resonance imaging signal. Humans navigating conceptual two-dimensional knowledge showed the same hexagonal signal in a strikingly similar set of brain regions to those activated during spatial navigation. This grid-like signal is consistent across sessions acquired hours and more than a week apart. Our findings suggest that global relational codes may be used to organize non-spatial conceptual representations and that these codes may have hexagonal grid-like pattern when conceptual knowledge is laid out in two continuous dimensions.

**One Sentence Summary:** Non-spatial conceptual knowledge can be organized using a grid-like code in the human brain.

Humans have a remarkable capacity for generalizing experiences to novel situations(1, 2). It has been hypothesized that this capacity relies on a ‘cognitive map’, allowing conceptual relationships to be navigated in a similar fashion to space(3-6). Grid cells use a hexagonally-symmetric code to organize spatial representations(7). Here we ask whether conceptual knowledge may also be organized by grid-like codes.

Human grid cells have been identified during intra-operative recordings(8) and are the likely source of a precise six-fold (hexagonal) symmetry in the functional magnetic resonance imaging (fMRI) signal, as a function of movement direction during virtual navigation(9-11). This hexagonal signal varies depending on whether the direction of moving in space is aligned or misaligned with the orientation of the grid (Fig. 1D-E). Such a signal is a precise and unusual prediction for fMRI (Supplementary text): it is predicted in the bulk activity because grid cells share a common grid axis (12-14), and conjunctive grid cells fire faster on average when movement is aligned to this axis (9). It pertains to the moving direction and cannot be explained by any characteristics of the currently experienced visual scene. It is hexagonal and therefore does not align on average to the cardinal directions. Its temporal waveform is different in every scan and every subject (Fig. S4) and thus cannot be easily predicted by imaging artefacts (Supplementary text and Table S1).

This grid-like signal is not unique to the entorhinal cortex, but can be measured during spatial navigation in prescribed parts of the medial frontal, medial parietal and lateral temporal cortices(9). Despite no report in rodents of grid cells outside the hippocampal formation, direct recordings during brain surgery in humans have confirmed grid-like firing patterns in some of these areas(8). This same network of brain regions, often referred to as the 'default mode network'(15), is also regularly activated in non-spatial tasks that involve the manipulation of conceptual knowledge, such as memory(16), imagination(17), scene

construction(18), valuation(19) and theory of mind (20), and in situations when subjects must generalize learnt concepts to novel situations(1, 2, 21).

The ability to interact with knowledge in this flexible and generalizable fashion is the central advantage of maintaining an explicit cognitive map(3). Together with the regions' established role in non-spatial conceptual generalization, the finding of grid-like activity in these brain regions during spatial navigation therefore raises the possibility of common neural coding mechanisms for storing spatial and conceptual representations. Indeed, this hypothesis is strengthened by the findings that hippocampal cells (analogous to rodent place-cells) encode individual concepts in humans (22) and sound frequency in rodents(23), and that rodent grid cell coding may not be restricted to spatial dimensions, but also represent time(24).

We used fMRI to test if humans use a hexagonally symmetric code when navigating through abstract conceptual representations. We designed a task analogous to the one used for navigation in physical space(9), with the notable difference that our dimensions were organized in an abstract, rather than physical, space.

Twenty-eight healthy subjects performed a stimulus-outcome (S-O) learning task where they learnt that bird stimuli(25) were associated with different Christmas symbols (Fig. 1A). The study therefore resembles other S-O learning tasks except that here, the bird stimuli were not independent fractals or symbols but, instead, they varied according to two continuous dimensions: the lengths of the neck and legs. Each stimulus could therefore be described within a two-dimensional conceptual "bird space" (Fig. 1B). Even though the features of this "bird space" were lengths as in physical maps, here they had to be extracted from a one-dimensional (vertical) visual space where different stimuli did not form any angles (Fig. 1A) and transformed into a two-dimensional conceptual map (Fig. 1B).

Participants had extensive experience of the bird space the day before scanning (26).



Briefly, we first trained them to morph birds with specific neck:legs ratios, using a non-spatial controller (Fig. S1). Next, the participants learned which bird stimuli were paired with outcomes by freely morphing the neck and legs dimensions. The outcome symbols would appear on screen whenever the morph matched the associated bird (Fig. S2). This ensured that subjects became familiar with the entire bird space and not just with the S-O pairings. Indeed, participants progressively refined the locations of the outcomes through training (Fig. 1F and Fig. S6). We periodically tested their knowledge of the bird space by asking them to find specific outcomes from arbitrary start positions, by correctly choosing the appropriate neck:legs ratio. When asked to make such ballistic movements, subjects significantly increased their precision through training, and therefore learned to visualize the target bird (Fig. 1G and Fig. S7). In the scanner, participants continued to improve performance each day, possibly because they received fresh training before each day's scanning (Fig. 1G and Fig. S8).

Each subject participated in 2-4 separate fMRI sessions, spanning two separate days, at least one week apart. In each trial during scanning, subjects watched a video of a bird morphing according to a pre-defined neck:legs ratio (Fig. 1C, Movie S1). They were then instructed to imagine the outcome if the bird continued to morph with the same neck:legs ratio. In some trials, they had to choose one of three offered outcomes: two outcomes they were trained with and a “no outcome” option (black square). Participants reached a performance of  $72.8 \pm 1.0$  % accuracy in predicting outcomes, and 0 out of 28 reported conceiving of the relationships between birds or outcomes as lying in a spatial map(26).

With the ambition to test whether the fMRI signal had hexagonal symmetry, as a proxy for grid cells, we ensured that the orientation of the trajectories for movement in bird-space were dissociated from the properties of the visual scene. That is, trajectories with the same orientation were formed by different stimuli, and trajectories with different orientations

could pass through the same stimulus. Indeed, the critical hexagonal symmetry regressors described below never shared more than 5% variance with any tested basic visual property of the stimuli, outcomes, or behavioral accuracy in any subject (Fig. 1I). The trajectories were sampled evenly across directions both in sum, and when separated according to outcome (Fig. 1H, S5).

Despite the absence of any hexagonal modulation of these confounding factors, we found a hexagonal modulation effect in the neural activity. We first identified hexagonally symmetric signals across the whole brain and then we focused on those regions where the effect was strongest. This approach allowed us to test in an unbiased fashion if this hexagonal symmetry had a consistent grid angle across two sessions acquired on the same day, and more than a week apart.

To identify brain regions sensitive to hexagonal symmetry, we used a Z-transformed F-statistic to test for a significant modulation of the fMRI signal by any linear combination of  $\sin(6\theta)$  and  $\cos(6\theta)$ , where  $\theta$  is the trajectory angle in bird space ((26) and Fig. S3). We found hexagonal symmetry in a network of brain regions that overlapped anatomically with the network found during navigation in physical space(8, 9) and with the default-mode network(15) (Fig. 2A, Fig. S10). However, although these brain regions all survived whole-brain cluster correction, this quadrature test could overestimate the Z-scores(26). Thus, we did not use this test for statistical inference *per se* but rather to create orthogonal regions of interest that allowed us to test in an unbiased fashion if the grid angle was consistent across separate experimental sessions. This was possible because the quadrature test was independent from the phase of the periodic signal, that is, the grid angle. We focused on brain regions where grid cells have been recorded in humans during spatial tasks(8), that is, the anterior cingulate/medial prefrontal cortex (mPFC) and entorhinal cortex (ERH).

Using the peak coordinate of the hexagonal modulation signal in the mPFC located

ventrally (vmPFC), we found that subjects with greater hexagonal modulation had a more accurate performance at the task (Fig. 2B). This region has also been shown to correlate with the performance in memory and conceptual knowledge tests(1, 21). As previously described for spatial hexagonal symmetries(9, 10), we next asked whether the grid angle to which this hexagonal modulation was aligned was consistent between separate experimental sessions. We thus used the data from one session to estimate the grid angle for a given participant, using the beta coefficients for the  $\sin(6\theta)$  and  $\cos(6\theta)$  regressors ((26)and Fig. S3). We then took the data from a separate session and looked for differences in activation between trials in which the trajectories were aligned versus misaligned to this hexagonal grid. This was achieved using the regressor  $\cos(6[\theta(t) - \phi])$ , where  $\theta(t)$  is the trajectory orientation in trial  $t$  and  $\phi$  is the mean grid orientation across the region on interest(9, 10). This “cross-validation” procedure was counter-balanced across sessions. We then performed a one-sample t-test across the group on the resulting regression coefficients.

Using this approach, we tested for hexagonal consistency between separate sessions acquired half an hour apart. We found such an effect at the whole brain level in the vmPFC (Fig. 3A, left). To test if this effect was a function of the presence of outcomes, we included in the design matrix a confound regressor that modeled out the effect of outcomes. We found that the map did not change (Fig. S11). Again, the consistency effect correlated with behavior in subjects who performed better at the task (Fig 3A, right). Thus, we replicated the finding that participants with more grid-like representations performed better at the task, using two independent analyses. The same neural signal was not predicted by the speed of learning of the task during training ((26) and Fig. 1F, G). Grid-like activity was therefore related to the current performance rather than the trajectory of learning.

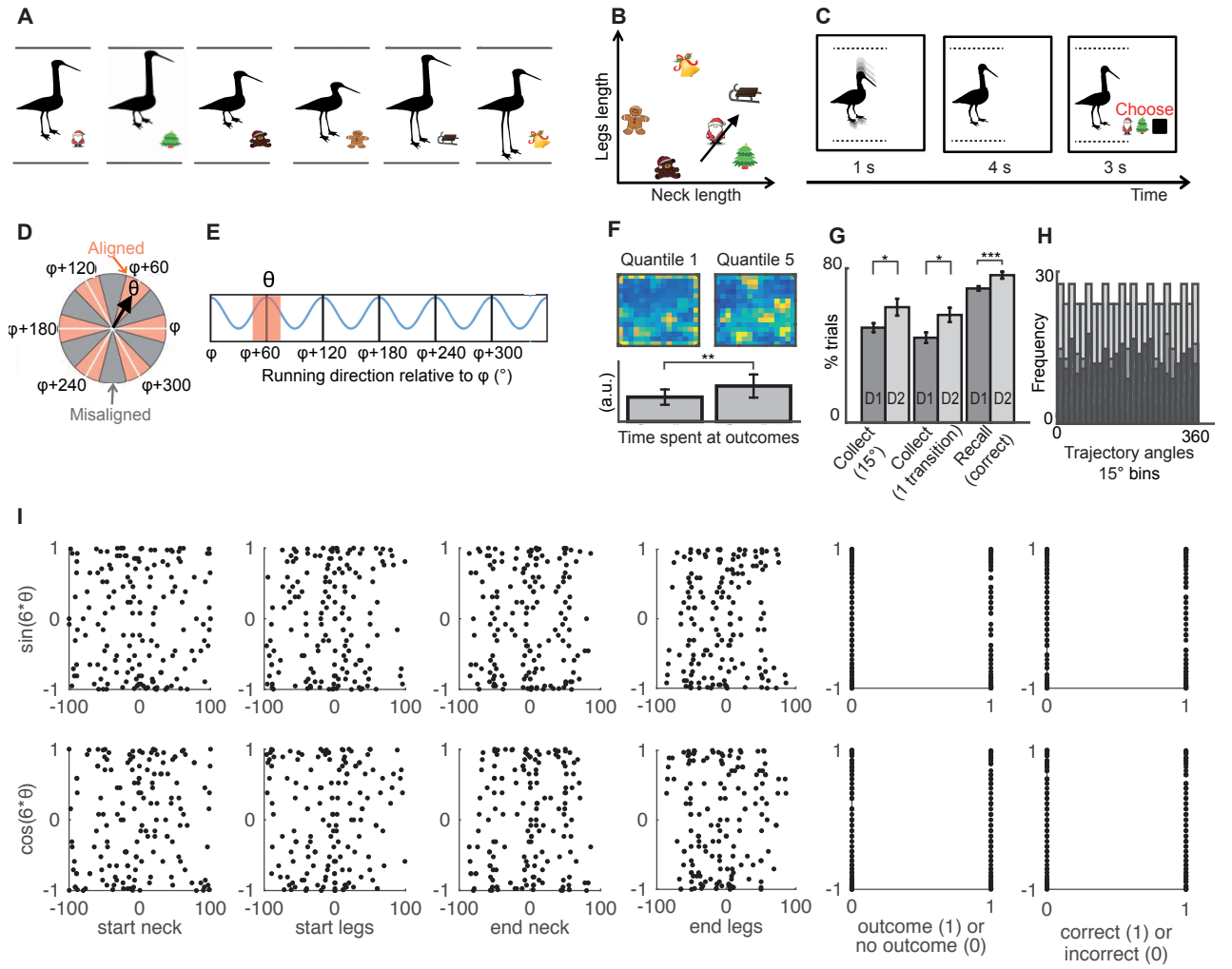
Next, to examine the pattern underlying this hexagonal effect, we separated all aligned (red) and misaligned (grey) trajectories ((26) and Fig. 1D). The signal in the vmPFC

was significantly higher for aligned than misaligned trajectories (Fig. 3B). The same pattern appeared in ERH (Fig. 3C). This effect was significant only for six-fold but not control four-, five-, seven- and eight-fold symmetries (Fig. 3B-C, right panels).

We also tested for hexagonal consistency between separate sessions acquired more than a week apart. We found a significant effect in the vmPFC (Fig. 4A). When grouping together within- and between-day data, the consistency effect was strongest in the vmPFC (Fig. 4B). Moreover, we found hexagonal consistency also between the ERH and vmPFC, suggesting that different brain regions may contain grid-like activity that is aligned to the same angle (Fig 4C). Again, all these effects were significant only in hexagonal but not control symmetries (Fig. 4, right panels).

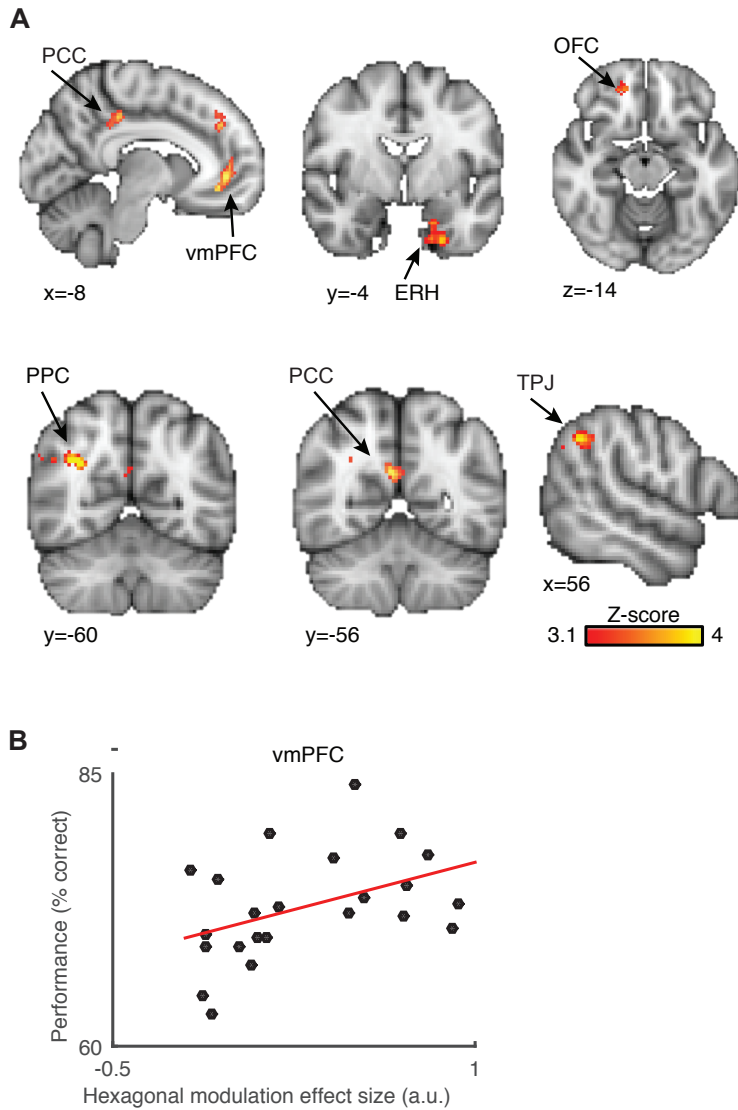
Whilst the coarse nature of the fMRI signal forces caution in making conclusions at the level of neuronal codes, we have reported an unusually precise hexagonal modulation of the fMRI signal during non-spatial cognition. When subjects perform this abstract cognitive task, this signal exists in a strikingly similar set of brain regions to those observed when subjects run in a virtual reality spatial environment((9) and Fig. S9), despite profound differences in the cognitive and perceptual demands of the two tasks. The hexagonal grid is consistently oriented across sessions that are acquired both half an hour and more than a week apart. Together, this evidence suggests that grid-like codes that are known to underlie spatial navigation, and recently discovered in the temporal dimension(24), can also be used to organize abstract knowledge of the type that is difficult to study in nonhuman species. In the event that such conceptual grid cells can be recorded directly, it will be of interest to know whether they share relationships (such as relative phases) across spatial and conceptual tasks, suggesting conceptual tasks can be solved by subconsciously mapping abstract dimensions onto pre-existing spatial maps, or whether new organizations can emerge to represent conceptual problems. It will also be informative to study how such cells behave in conceptual

problems that are not easily mapped onto continuous 2-dimensional spaces(27, 28).



**Fig. 1. Experimental design for navigation in abstract space.** (A) Subjects were trained to associate stimuli (birds) with outcomes (Christmas symbols). (B) Example trajectory in abstract space. A location in this abstract space was represented by a bird stimulus. A trajectory was equivalent to visually morphing one bird into another (Fig. 1C). The direction  $\theta$  of the trajectory depended on the ratio of the rates of change of the legs and the neck (Movie S1). Subjects were not consciously aware that these associations could be organized in a continuous “bird space”. (C) Example trial corresponding to the trajectory with direction  $\theta$ . (D) Trajectories can be categorized as aligned (red sectors) or misaligned (grey sectors) with the mean orientation  $\phi$  of the hexagonal grid. Note that  $\phi$  is different for each participant (see(26) for details on how  $\phi$  was calculated). Here, the direction  $\theta$  is aligned with the grid. (E) fMRI markers of grid cells showing hexagonal symmetry: the signal is bigger for

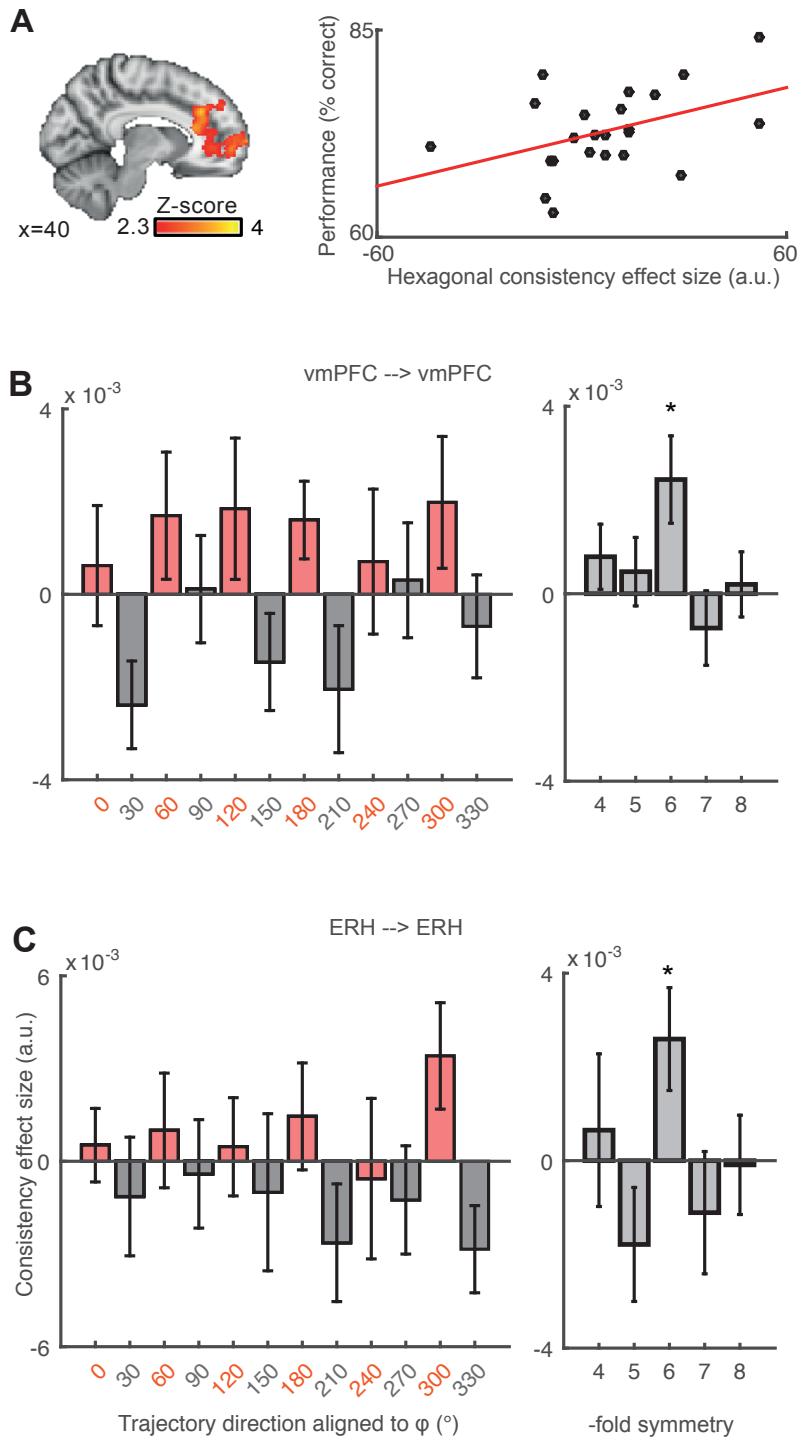
trajectories aligned versus those misaligned with the grid. **(F)** Color-coded trajectory maps illustrating time spent in each part of the environment during the “explore” task in the first (quantile1) and last parts of training (quantile5). Yellow is maximum and dark blue is 0. Barplots showing the amount of time spent at the locations/stimuli paired with outcomes in each epoch relative to the total time spent navigating (“time at outcomes” quantile1 vs quantile5,  $t_{22}=-3.17$ , \*\*  $p<0.01$ ). **(G)** In the “collect” task, participants made significant improvements in training day 2 compared to training day 1: the percentage of trials with an angle error  $< 15^\circ$  ( $t_{33}=2.37$ , \*  $p<0.05$ ) and with only one transition increased ( $t_{33}=2.55$ , \*  $p<0.05$ ). In the “recall” task, participants made significantly more correct responses in day 2 compared to day 1 ( $t_{41}=3.89$ , \*\*\*  $p<0.001$ ). **(H)** Example data from the most commonly used schedule: even distribution of trajectory angles across all trials (light grey), outcome trials (medium grey) and non-outcome trials (dark grey). **(I)** Example data from the most commonly used schedule: we tested if the  $\sin(6\theta)$  and  $\cos(6\theta)$  regressors correlated with multiple confounding factors. These regressors did not correlate with the start neck, start legs, end neck and end legs lengths, whether the subject responded accurately or whether the morph passed through an outcome (all coefficients of determination  $R^2$  averaged across all subjects  $< 0.02$ ). **(D and E)** are adapted by permission from Nature, Doeller et al, 2010).



**Fig. 2: Identifying hexagonally symmetric signals across the whole brain. (A)** Hexagonal modulation in a network of brain regions including the medial prefrontal cortex, with a peak in its ventral region (vmPFC; peak Montreal Neurological Institute coordinates -8/42/0, peak Z-score = 4.09), the medial entorhinal (ERH; -18/0/-38; Z = 4.41), the orbitofrontal (OFC; 6/44/-10; Z = 4.27), the posterior cingulate (PCC; 0/-32/28; Z = 4.3), retrosplenial (RSC; 6/-52/24; Z = 4.73) and lateral parietal cortices (LPC; 30/-62/28; Z = 4.96) and the temporoparietal junction (TPJ; 52/-42/40; Z = 4.13). For visualization purposes, the maps are cluster corrected at a cluster threshold Z = 3.1 and  $p < 0.05$  for all brain regions apart from the ERH where we used a more lenient threshold of Z = 2.3 and  $p < 0.05$ . **(B)** Subjects who



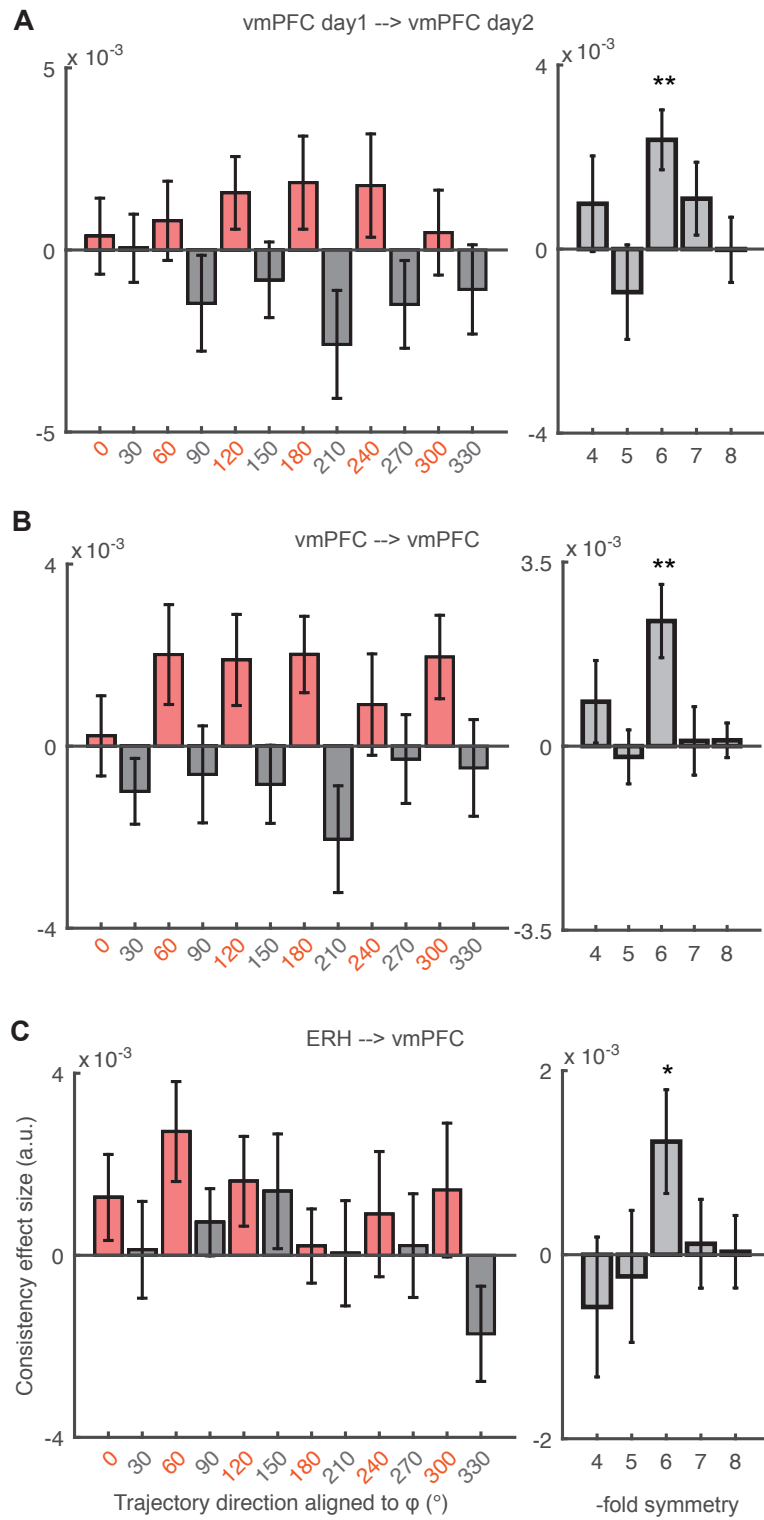
performed better at the task had significantly more hexagonal signal modulation in the vmPFC ( $r = 0.432$ ,  $p = 0.039$ ).



**Fig. 3: Grid angle consistency between separate sessions acquired within the same day.**

(A) Left: Whole brain level grid angle consistency in vmPFC (cluster corrected  $Z = 2.3$  and  $p < 0.05$ ; 16/54/-2;  $Z = 3.76$ ,  $p < 0.0001$ ). Right: participants with higher hexagonal consistency performed more accurately on the task ( $r = 0.431$ ,  $p = 0.039$ ). (B-C) Left panels:

6-fold modulation signals aligned to the same grid angle in the vmPFC ( $t_{26} = 2.61$ , \*  $p < 0.05$ ) and ERH ( $t_{27} = 2.36$ , \*  $p < 0.05$ ). The effect is plotted separately for all aligned (red) and misaligned (grey) trajectories. Right panels: this effect was specific for 6-fold, but not any other control periodicities between 4- and 8-fold (all  $p > 0.15$ ).



**Fig. 4: Grid angle consistency between separate sessions acquired more than a week apart.** (A) Cross-day consistency of the grid angle in vmPFC (left panel  $t_{20} = 3.65$ , \*\*  $p < 0.01$ ; right panel all  $p > 0.18$  for control periodicities). (B) Within- and cross-day consistency in vmPFC (left panel  $t_{20} = 3.41$ , \*\*  $p < 0.01$ ; right panel all control  $p > 0.15$ ). (C)

Cross-region consistency between the ERH and vmPFC (left panel  $t_{21} = 2.18$ , \*  $p < 0.05$ ; right panel all control  $p > 0.46$ ).

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# Supplementary Materials for

## Organizing conceptual knowledge in humans with a gridlike code

Alexandra O. Constantinescu,\* Jill X. O'Reilly, Timothy E. J. Behrens\*

\*Corresponding author. Email: [alexandra.constantinescu@magd.ox.ac.uk](mailto:alexandra.constantinescu@magd.ox.ac.uk) (A.O.C.); [behrens@fmrib.ox.ac.uk](mailto:behrens@fmrib.ox.ac.uk) (T.E.J.B.)

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### This PDF file includes:

Materials and Methods  
Supplementary Text  
Figs. S1 to S11  
Table S1  
Caption for Movie S1  
References

**Other Supporting Online Material for this manuscript includes the following:**  
(available at [www.sciencemag.org/content/352/6292/1464/suppl/DC1](http://www.sciencemag.org/content/352/6292/1464/suppl/DC1))

Movie S1

## Materials and Methods

### Participants and experimental design

28 participants (16 men; mean age 26) reported to be in good health with no history of neurological or psychiatric disease and with normal or corrected-to-normal eye vision participated in the fMRI experiment at the Oxford Centre for Functional MRI of the Brain (FMRIB). Each subject participated in 1-4 separate fMRI sessions, across two separate days, at least one week apart. 22 of them participated in both days, whereas the remaining 6 subjects participated only in the first day and did not return for the second testing day. We split in half the data of the subjects who were scanned only once for subsequent analyses that required cross-validation between separate session. In total, we acquired 94 separate datasets. One participant was excluded from all further analyses because he did not learn how to use the controller for navigation in abstract space. Four participants were trained less than the rest of the group. To avoid a confounding effect of the training regimes, we excluded them from the correlations with behavior. All remaining participants were included in further analyses with the exception of one participant who was excluded from the consistency analysis in the prefrontal cortex as a result of parameter estimates being more than 4 s.d. away from the group mean. Subjects were firstly trained outside the MRI scanner to navigate in a continuous abstract “bird space”. They had to remember which locations were paired with an outcome and then, on a separate day, they did the task in the scanner. We created two versions of the task in the scanner and half of the participants performed one version and the other half performed the other version. All participants gave written informed consent and were paid for participating, as approved by the ethics committee of the University of Oxford (ref. number 2013-171).

### Behavioral training

We developed a set of novel tasks for navigation in an abstract space that were designed to be analogous to those used for navigation in a physical space. We trained the participants extensively to be able to navigate precisely in this abstract space. Using keyboard button presses, subjects learned to morph the birds, to explore the abstract space and learn the locations of the outcomes.

Each location in this abstract space was represented by a bird stimulus. A trajectory through the bird space was equivalent to morphing one bird stimulus into another, that is, watching the neck and legs stretching vertically. The direction  $\theta$  of the trajectory was the ratio between how much the neck and legs were changing relative to each other. Subjects were instructed to learn which bird shape was associated with each outcome and we purposefully did not instruct them that these associations could actually be organized in a continuous 2D “bird space”. Movie S1 illustrates a recording of the task and the rationale of our experimental design.

### *Match task:*

Firstly, subjects played the *match task* where they were trained to use a controller to morph the bird silhouette shown on the left side of the screen to match the bird on the right side of the screen (Fig. S1). The two birds varied only in two dimensions: the lengths of the neck and legs. Thus, the participants could morph the bird by changing the lengths of the neck and legs. To ensure that participants integrated between these two dimensions simultaneously, we precisely instructed them to morph the bird by choosing the ratio between how much the neck and legs change relatively to each other only once and as correctly as possible (as opposed to changing the lengths of the neck and legs separately). To ensure that subjects did not do this task spatially, we



created a non-spatial controller for choosing this ratio. The participants pressed buttons on the keyboard to choose the ratio and then to morph the bird with that ratio. The morphing was continuous and they saw a bird shrinking or stretching its neck and legs. Each of the two black bars of the controller signified how much that dimension would change. If the black bar was positioned on the midline, the corresponding dimension did not change. The closer to the top line the bar was, the more that dimension would increase. Conversely, the closer to the bottom line the bar was, the more that dimension would decrease.

#### *Explore task:*

After the participants learned how to perform the *match task* correctly, they continued with the *explore task* (Fig. S2). In this game, subjects needed to find six outcomes (images of Santa Claus, a Christmas Tree, a gingerbread man, a sledge, a bell and a teddy-bear) by freely morphing the bird. Each outcome was associated with a different bird (Fig. 1A). Participants knew they found an outcome because it would pop up next to its associated bird. Critically, this ensured that subjects became familiar with the entire bird space and not just with the stimuli paired with outcomes and that they had a clear representation of what one unit distance on each axis (neck, legs) looked like. Thus, we did not simply train the participants on the mere associations between the six birds and the six outcomes (i.e. only the locations paired with outcomes in the abstract space). This approach is analogous to exploration tasks in open environments in rodents(29). Indeed, participants did not know a priori which birds were paired with outcomes, hence, they had to morph through many different unpaired birds to find the paired ones (i.e. they explored many locations in the abstract space that were not paired with outcomes).

The locations of the outcomes were identical in all participants. This allowed us to identify learning patterns of the environment across participants, and rule out the possibility that inter-individual differences between participants were caused by the outcome locations. We carefully selected these locations to rule out any potential hexagonal arrangements.

#### *Collect task:*

When subjects knew the stimulus-outcome associations well, they continued to train with the “collect task”. In this task, we periodically tested their knowledge of the bird space by asking them to find specific outcomes from random start positions, by correctly choosing the neck:legs ratio only once. Thus, they had to recall the correct neck/legs ratio associated with that outcome, and generate the abstract trajectory to that bird correctly in one go.

#### Recall task during scanning (Fig. 1):

Subjects were trained with the version of the task that would also be used subsequently during scanning (Movie S1). During fMRI scanning, we wanted to present participants with a controlled set of trajectories, thus, we devised a task in which participants watched videos of birds morphing into different birds according to pre-defined neck:legs ratios. Each trial corresponded to one trajectory and consisted of several stages: morphing, imagination and, in a subset of trials, choice. During the morphing stage, the participants saw only a single trajectory in the abstract space.

Next, they were instructed to imagine the bird continued to morph with the same neck:legs ratio, for the same amount of time and the same speed, and recall if any of the imagined bird stimuli was associated with an outcome. This means they did not only need to estimate equivalents of angles of moving in space, but also equivalents of distances. In other words, we split the trajectories in half, and subjects saw the first half (visual morphing of the bird) and had to imagine the second half (imagined morphing of the bird). Finding grid-like representations during imagined navigation in physical space is indeed possible, as shown in a recent study(11).

We deliberately designed the trajectories to sample the 360° space uniformly, across all trials, as well as separately for trials paired or unpaired with outcomes.

Finally, subjects could choose one out of three possible outcomes (outcome 1, outcome 2 or no outcome) by pressing one out of three keys on a button box. To control for the effect of the outcomes, we designed two versions of the task. In one version, these outcomes were displayed during the entire duration of the trial and subjects made a choice immediately after the imagination period. In the other task version, participants only saw the outcomes at the end of the imagination period, with a 50% probability, and then were asked to make a choice. There were no significant differences between the two versions of the task, at either the neural or behavioral levels, therefore we pooled data from both versions. Overall, the accuracy on the task was  $72.8 \pm 1.02\%$  (mean  $\pm$  SEM across participants – chance is 33%), suggesting that they learned how to navigate the bird space.

#### Post-scanning debriefings

Even though the stimuli were not 2D spatial, it would have been possible for the subjects to solve the problem using conscious and explicit analogy to 2D space. Such a spatial strategy would go beyond the scope of previous reports of the function of grid cells but would retain space as a 2 dimensional anchor for the grid. Alternatively, subjects may have had no conscious knowledge of the spatial arrangement of the birds. To gain some handle on this interesting question, we asked subjects after scanning to describe the strategy they used to do the task and to remember the associations between the birds and the outcomes. For example, some strategies for remembering what bird gave the Christmas Tree were: visualizing the precise lengths of the neck and legs as a mental picture, using internal metrics such as the bird has 4 units of neck and 1 unit of legs, verbally repeating in their minds “long neck, short legs”, finding similarities between the characteristics of the bird and the outcome such as the bird had a long neck (trunk) and short legs (base) like a true Christmas Tree and, also, finding similarities between different birds associated with outcomes (e.g. the Christmas Tree bird had longer neck but similar legs with the Teddy Bear bird). Thus, no participant described being aware that birds could be associated spatially, on a two-dimensional map. For certainty, we subsequently showed them the map of the abstract space (Fig. 1B) and asked them whether this spatial strategy was “easier”, “harder” or “the same” as their own strategy. Two participants reported that the spatial strategy had the same level of difficulty as their own strategy, however they clarified that their approach was not spatial and were unaware that the birds could be arranged into a 2D map. Everyone else reported that the spatial strategy was easier or harder than their own. Overall, no subject reported doing the task spatially.

### MRI data acquisition

We acquired T2-weighted functional images on a 3 Tesla scanner. We used a gradient-echo echo-planar imaging (EPI) pulse sequence that sets the slice angle of 30° relative to the anterior-posterior commissure line, minimizing the signal loss in the orbitofrontal cortex region(30). We acquired 45 slices, 3mm thick, in an interleaved order. We used the following parameters: repetition time (TR) = 3000 ms, echo time (TE) = 30 ms, flip angle = 87°, field of view (FoV) = 192mm, voxel size = 3 x 3 x 3 mm<sup>3</sup>. To correct for deformations in the inferior prefrontal cortex, we also acquired a field map with dual echo-time images covering the whole brain, with the following parameters: TR = 500 ms, TE1 = 5.19 ms, TE2 = 7.65 ms, flip angle = 60°, FoV = 224mm, voxel size = 3.5 x 3.5 x 3 mm<sup>3</sup>. To facilitate an accurate registration of the EPIs to the standard space, we also acquired a T1-weighted structural image using a magnetization-prepared rapid gradient echo sequence (MPRAGE) with the following parameters: TR = 2040 ms, TE = 4.7 ms, flip angle = 8°, FoV = 192mm, voxel size = 1 x 1 x 1 mm<sup>3</sup>. Stimulus presentation and subject button presses were registered and time-locked to the fMRI data.

### Data analysis

We analyzed whole-brain MRI data with FMRIB's Software library (FSL)(31) and we performed all the other analyses in Matlab.

### *Behavioral analyses*

We tested for measures of learning during the “explore” task, where subjects navigated freely to look for the outcomes. We concatenated the data from all training sessions in each subject, and then split it into five equal parts (quantiles). We then computed the amount of time spent in each part of the environment during each quantile and plotted it as color-coded trajectory maps. We then estimated the amount of time spent navigating at the edges (“time at edges”) and at the locations paired with outcomes (“time at outcomes”), relative to the total time spent navigating. At the group level, we averaged these measures across participants.

In the “collect” task, subjects were precisely instructed to find specific outcomes. We computed the mean number of transitions needed to find an outcome, in each trial. A perfect performance is equivalent to making only one transition to find the target outcome, thus, choosing the correct neck:legs ratio only once and generating the abstract trajectory to the target bird in one go. In contrast, a poor performance means making more than one transition. Therefore, we also computed the percentage of trials where participants made only one transition. Finally, a precise trajectory would have a small angle error, defined as the angle between the ideal trajectory angle and the angle of the first transition. Thus, we next computed the percentage of trials where participants had an angle error < 15°.

In the recall task in the scanner, we computed the performance as percentage of correct responses in each scanning session.

### *Pre-processing of functional images*

We segmented brain matter from nonbrain(32). We corrected functional data for motion artefacts and we removed low frequency signals using a high-pass filter at

1/100 Hz. We smoothed the data using a gaussian filter of 7 mm full width at half maximum and we corrected for slice time acquisition differences. We also corrected for geometric distortions in the EPI images using the acquired fieldmaps(33). We registered the EPI images to the high-resolution anatomical image using boundary-based reconstruction and then we normalized them into standard space (Montreal Neurological Institute – MNI152) using non-linear registration. Because of the notable breathing- and susceptibility-related artefacts in the enthorinal cortex, we ran a separate analysis where we pre-cleaned the data with FMRIB's ICA tool, FIX (34,35).

#### *Measures of motion estimation*

We computed four parameters to assess motion in each participant and identify movements bigger than the voxel size (3mm). First, we computed the mean displacement, defined as the amount of head motion (sum of the absolute translational movement in the x, y and z directions) relative to the middle time point across the entire scanning session, averaged across all time points.

Second, we examined the total displacement (TD) from the beginning to the end of the scanning session.

Third, we examined the data for rapid movements because these are the ones that could have disrupted signal intensities. We computed the mean framewise displacement, as the amount of head motion relative to the previous time point, averaged across all time points.

Finally, we computed the maximum framewise displacement (MaxFD) to address the concern of sudden movement more conservatively. We looked for subjects who moved more than 3mm at any time point.

#### *fMRI whole brain analyses*

After pre-processing, we modeled the fMRI time series using two general linear models (GLMs). Both models included regressors for the main effects of the morphing stage and the response stage of the trial and six nuisance regressors to account for motion-related artifacts. Each individual model had various parametric modulations of the regressors for the morphing stage (see below). All these regressors were convolved with the FSL default hemodynamic response function and filtered by the same high pass filter as the fMRI data before entering the GLM.

GLM 1: hexagonal modulation analysis (Fig. 2):

We created two parametrically modulated regressors(9): the sine and cosine of the direction of each trajectory in each trial,  $\theta(t)$ , with a periodicity of  $60^\circ$ , that is,  $\sin(6\theta(t))$  and  $\cos(6\theta(t))$ . The factor 6 means that these regressors will produce coefficients with high amplitude  $\left(\sqrt{\beta_{\sin}^2 + \beta_{\cos}^2}\right)$  for brain regions that are sensitive to hexagonal symmetry. To calculate the magnitude of the hexagonal modulation, we used an F test to investigate which brain regions were significantly modulated by a linear combination of these two regressors:  $\beta_{\sin} \cdot \sin(6\theta) + \beta_{\cos} \cdot \cos(6\theta)$ . We then transformed this statistic to a Z-statistic in each subject, using an asymptotic

approximation (<http://www.fmrib.ox.ac.uk/analysis/techrep/tr00mj1/tr00mj1/>) and, together with a behavioral covariate, we performed a 1-sample t-test across the group. For visualization purposes, the statistic images were thresholded using clusters determined by  $Z$ -statistic = 3.1 and the supra-threshold clusters were corrected for family-wise error using a cluster significance threshold of  $p = 0.05$ . For the entorhinal cortex, we used a more lenient cluster forming threshold at  $Z = 2.3$  and  $p = 0.05$  because this brain region is prone to signal loss and, thus, it is difficult to image with fMRI (see below for discussion of these tests).

This test has the major benefit of identifying periodic signals across the whole brain without knowing the phase of these signals. However, although the reported clusters survive multiple comparison correction across the whole brain, this test is unusual and should not be used for statistical inference because it can overestimate the  $Z$ -scores. Thus, we used it instead as a method to identify informative brain regions that we could then use to create ROIs for subsequent unbiased tests.

In detail, the first level statistic that is being brought to the group level relies on the mean and variance of the first-level estimates in such a way that mis-estimating the variance can cause a bias in the mean (for example if the variance is under-estimated, the  $F$ -statistic will be overestimated, and the expectation of the transformed  $Z$ -statistic will be greater than zero even in null data). Estimating unbiased variances from autocorrelated fMRI data is notoriously difficult. Therefore, the reader should be cautious in interpreting the results of this test as statistically significant. In the current manuscript, we use this test as a method for generating candidate regions of interest for tests that are certainly unbiased (consistency tests). This allows us to extract the grid angle from these ROIs in one dataset and test it in another. These subsequent tests do not use first level variances and are therefore unbiased tests performed with the standard fMRI GLM machinery.

## GLM 2: hexagonal consistency analysis (Fig. 3A):

We created a parametric regressor  $\cos(6[\theta(t) - \phi])$ , where  $\theta(t)$  is the trajectory angle for each trial  $t$  within one session and  $\phi$  is the grid angle from another session acquired on the same day(9,10) (Fig. S3). This regressor had higher values for grid-like activity with the same grid angle as in the other session. Thus, if the trajectories from one session aligned with the predicted grid angle taken from a different session, then this regressor would have high values. This resulted in subject-specific parameter estimates for each experimental session.

In the next stage, participant-specific linear contrasts of these parameter estimates were averaged across the experimental sessions and, together with a behavioral covariate represented by the behavioral accuracy, they were entered into a series of one-sample t-tests, each constituting a group-level statistical parametric map. The statistic images were thresholded using clusters determined by  $Z$ -statistic = 2.3 and the supra-threshold clusters were corrected for family-wise error using a cluster significance threshold of  $p = 0.05$ .

To estimate the grid angle  $\phi$ , we used a similar approach to the one for navigating in physical space(9). We first averaged the coefficients for the sine ( $\beta_{\sin}$ ) and cosine ( $\beta_{\cos}$ ) regressors across all voxels in the ROI. Then, we calculated the grid angle  $\phi$  (varying between 0 and 59°) as  $\arctan [(\beta_{\sin}/\beta_{\cos})]/6$  within regions of interest (ROIs),

where arctan was mapped into the 360° space, varying between -30° to 30°, according to the signs of  $\beta_{\sin}$  and  $\beta_{\cos}$ .

#### *ROI analyses (Fig. 3-4)*

We defined all ROIs from the whole-brain quadrature filter analysis for hexagonal modulation (GLM 1 and Fig. 2), which was orthogonal to the contrasts of interest. This allowed statistical tests to be performed in an unbiased fashion. To make it clear why this is the case: in the null case, two scans that both had high hexagonal magnitude would have randomly oriented hexagonal phase (grid angle) and so all analyses that relied on aligned grid angle would result in mean zero signal. The ROIs were 5-mm spheres centered on the voxels with the highest hexagonal magnitude activity (GLM 1) in the ventromedial prefrontal (vmPFC) and the entorhinal cortex (ERH) (Fig. 2A). We used these ROIs as seeds for estimating the values of the grid angle and to test for grid angle consistency between separate experimental sessions.

To examine the pattern underlying the hexagonal magnitude effect, we ran separate regression analyses for trajectories that were aligned and misaligned with the grid, using fMRI time series from the vmPFC and ERH ROIs. We aligned the trajectory angles to the grid angle  $\phi$  and we split these aligned trajectories into 12 equal bins of 30°. We thus created 12 separate regressors for trajectories that belonged to one of these 12 bins, resampled them at a resolution of 100ms and convolved them with the hemodynamic response function. To match the resolution of the fMRI timeseries, we then resampled the regressors to the duration of the fMRI repetition time. Next, we ran 12 separate regression analyses in each individual experimental session. The 12 resulting regression coefficients were then averaged separately across various sessions, and expressed as mean  $\pm$  sem (Fig. 3B-C and Fig. 4). Given our strong *a priori* hypotheses of hexagonal symmetry, we performed a t-test on the differences between the resulting betas aligned and misaligned to the grid angle  $\phi$ , across subjects, to investigate if these differences were significantly different from zero.

We tested for consistency within-day (Fig. 3), across-day (Fig. 4A), and all data combined within- and across-day (Fig. 4B-C). Again, to allow statistical unbiased testing, we aligned data from one session to the grid angle from the other session.

#### *Control analyses*

fMRI data:

To test for the specificity of the six-fold symmetric sinusoidal modulation, we used the same approaches as above, but using control models with directional periodicities of 90°, 72°, 51.4° and 45° (that is, four-fold, five-fold, seven-fold and eight-fold rotational symmetry).

## Supplementary Text

### Ruling out alternative explanations for the fMRI hexagonally symmetric signal

The trial-by-trial fMRI activity resembles a periodic wave with six peaks only if the angles of the trajectories the participants are running at are sorted in an ascending order (modulo 60) from 0° to 360° (Fig. 1E, Fig. S4A). However, participants did not move along trajectories in a sorted order, but in a random fashion and the signal looks random when the order of the trajectory angles is shuffled (Fig. S4C). Moreover, the trial-to-trial fMRI activity is different from day-to-day in each participant because they navigated along various random angles in each day. These responses are also different from person-to-person because each subject has their own grid angle. For example, if two participants have grid angles at 30° from each other, then trajectories that are aligned in one person, thus leading to fMRI responses with big amplitudes, will be misaligned in the other person, leading to fMRI responses with low amplitudes.

Therefore, potential confounds of this signal need not resemble a periodic wave with six peaks regardless of the order of the trials. Instead, the artifacts need to be consistently and significantly happening with a hexagonal periodicity that depends precisely on the order of the trajectories of moving in space, be aligned to one grid angle in one participant and to another grid angle in another participant. It is therefore unlikely that motion or physiological artifacts (such as breathing and heart rate) would cause the hexagonal pattern. For example, subjects would need to move more during aligned versus misaligned trajectories, according to the random order these trajectories are presented, which is different from day-to-day, and according to the orientation of the grid, which is different from person-to-person. The hexagonal pattern of fMRI activity is therefore difficult to explain with unspecific fMRI artefacts.

### Subject estimates of motion

The average mean displacement across participants was  $0.4 \pm 0.043$  mm, thus less than 1 voxel-diameter (3 mm).

We found 7 subjects who had a total displacement > 3mm. This is a very conservative measure of subject movement as it penalizes many incremental movements that are well corrected by linear methods. Nevertheless, we tested using region of interest analyses whether our results survived the exclusion of these 7 subjects. Despite the inevitable loss of statistical power entailed by removal of data from more than 25% of the participants, we were able to confirm the majority our findings. All results presented except for two (the correlation between behavior and hexagonal consistency in vmPFC and the hexagonal consistency vmPFC within-day) remained significant in this re-analysis (Table S1). We next focused on measures of rapid motion of the kind that cause a bigger problem for fMRI.

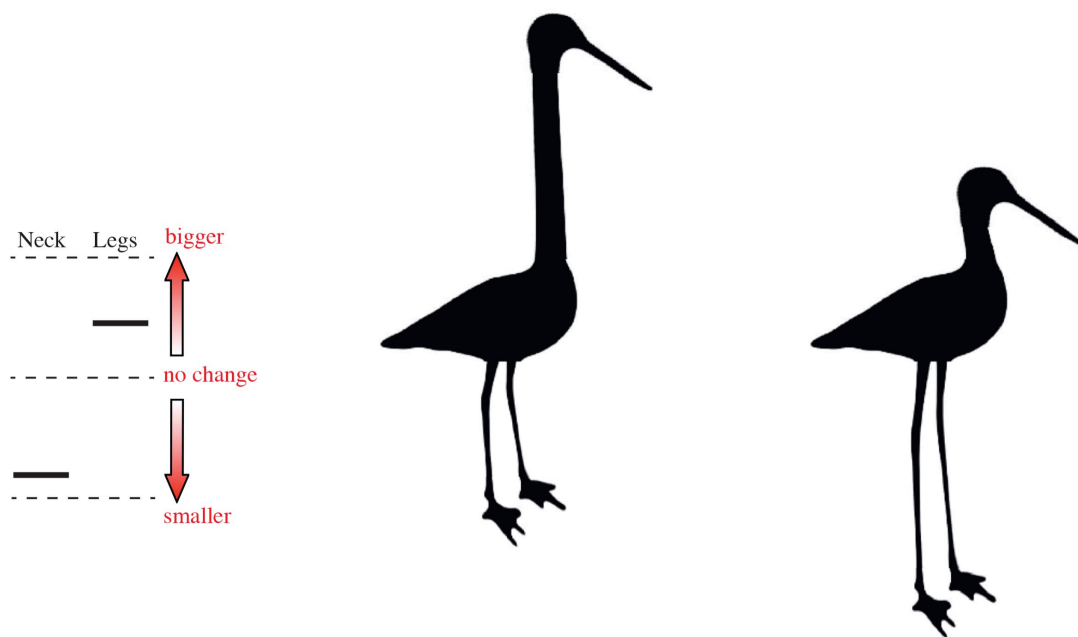
The average mean framewise displacement across participants was  $0.031 \pm 0.0045$

mm, thus less than 3mm. Indeed, participants did not tend to make sudden head movements throughout scanning.

We found that 3 subjects made 1-2 rapid head movements in one scanning session, as assessed by the maximum framewise displacement (MaxFD). It is very unlikely that these events could have potentially affected the observed hexagonally symmetric signal because they did not occur frequently, with hexagonal periodicity, and they would have needed to be precisely aligned with the grid angle. Despite this improbable situation, we tested again using region of interest analyses whether our results survived the removal of these 3 subjects. All the presented results remained significant in this re-analysis, except for one, which approached significance (the correlation between behavior and hexagonal signal modulation in vmPFC).

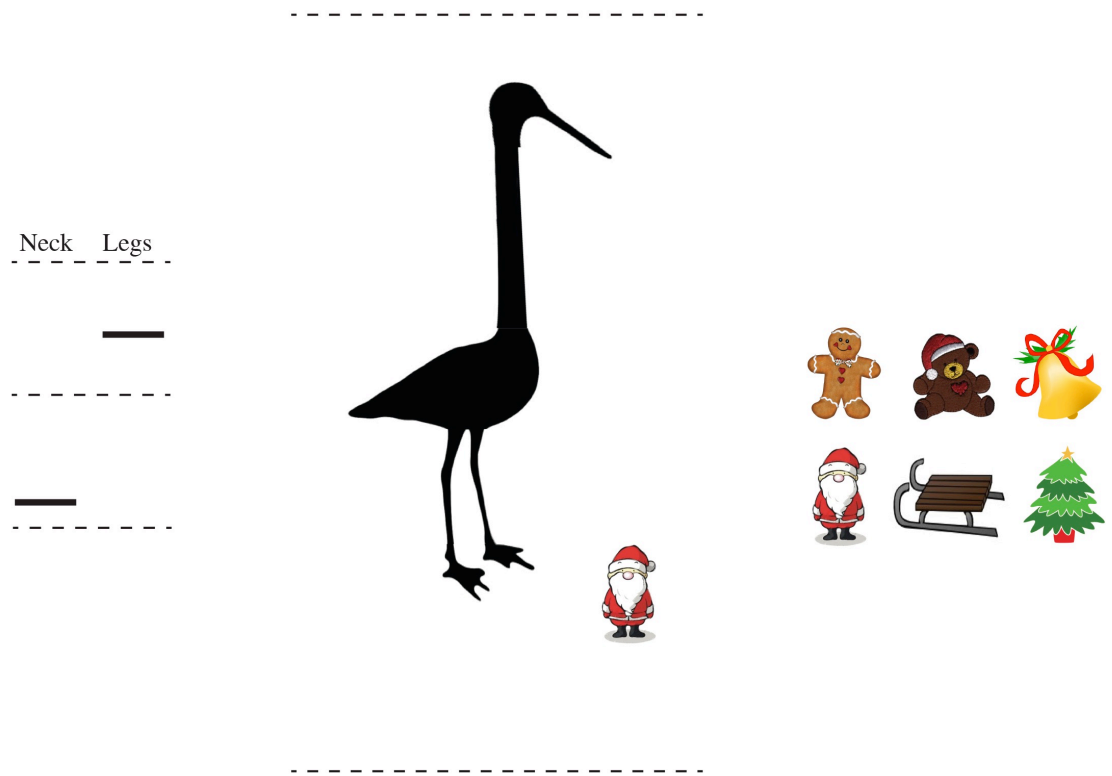
To sum up, we re-analyzed data after excluding subjects who moved more than 3mm in the scanner. Although the occasional results changed when we remove these subjects, in each case the vast majority of assessments survived. The statistical tests from these two re-analyses, one that is common within FSL and SPM analysis standards (MaxFD) and another more conservative measure (TD) are presented in table S1.





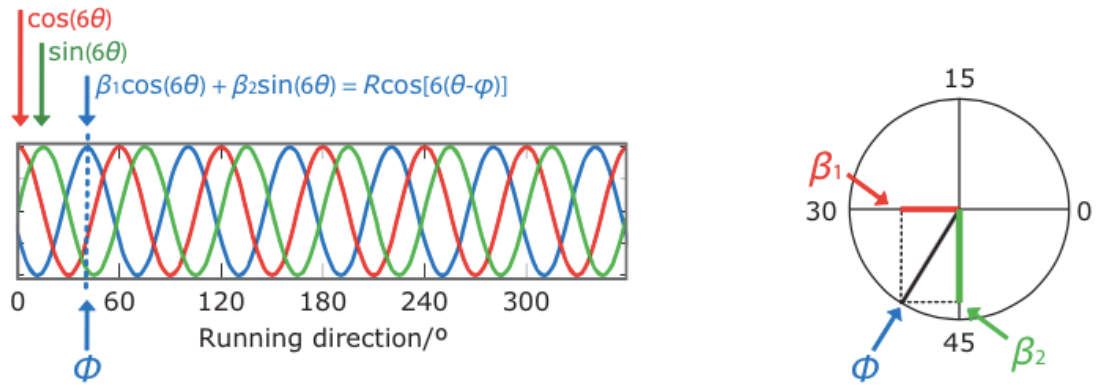
**Fig. S1.**

Example screenshot of the match task. Here, to morph the bird on the left into the one on the right, the neck needed to decrease more than the legs needed to increase. The correct neck:legs ratio to achieve this is shown on the controller on the left side of the screen (notice the position of the two black bars).



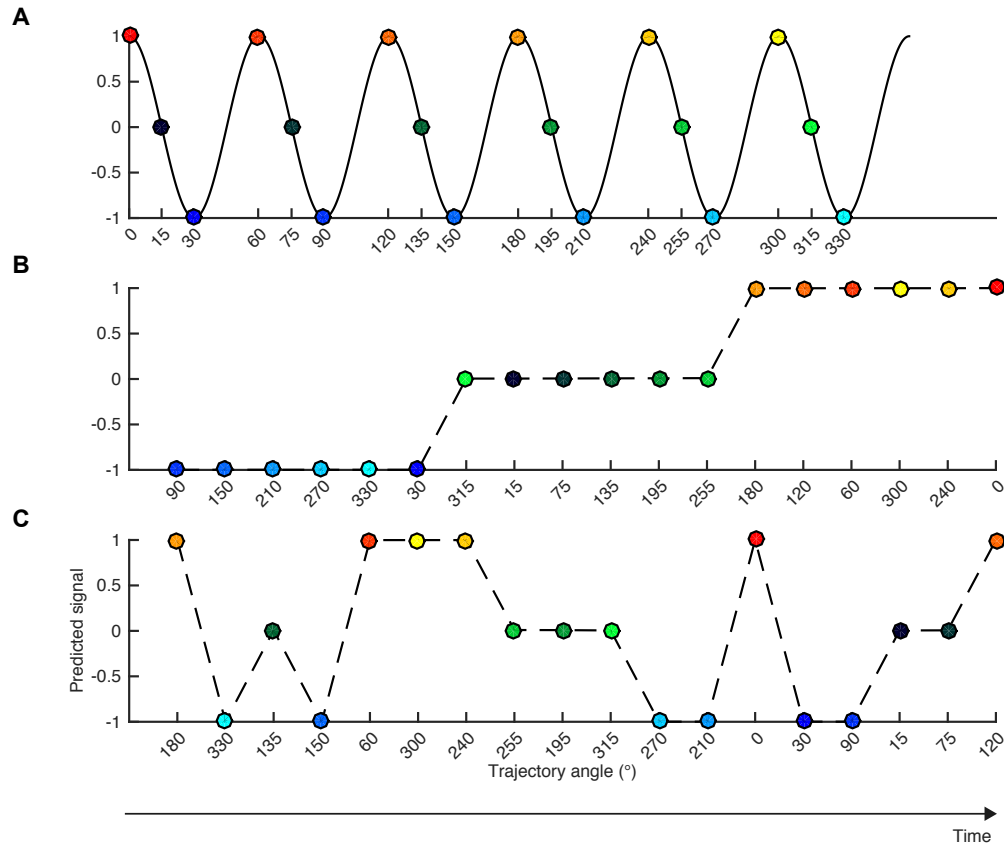
**Fig. S2**

Example screenshot in the explore task where the subject found Santa Claus.



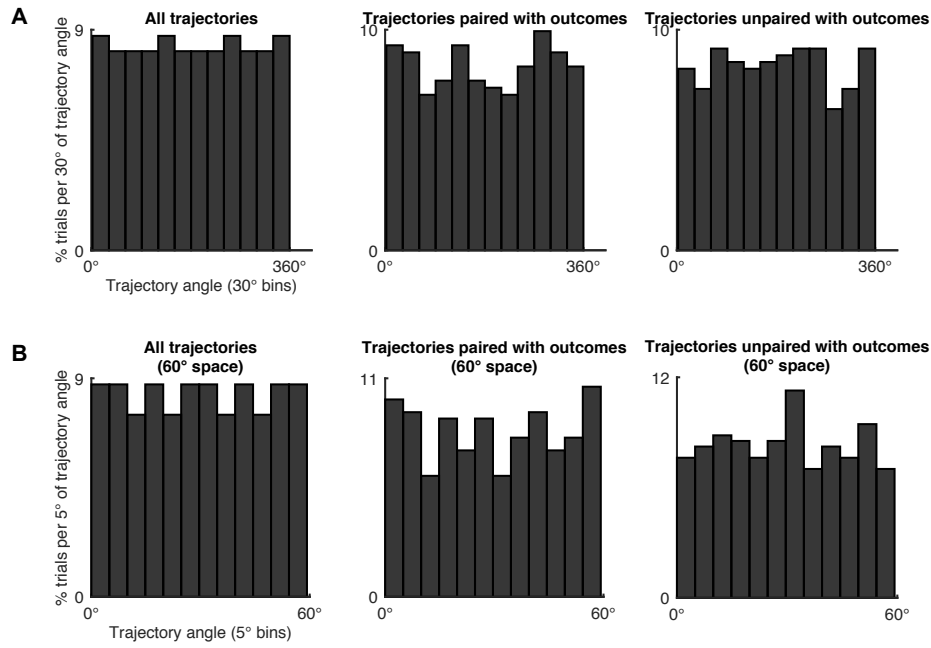
**Fig. S3**

Estimation of the grid angle (reproduced with permission from Nature, Doeller et al, 2010).



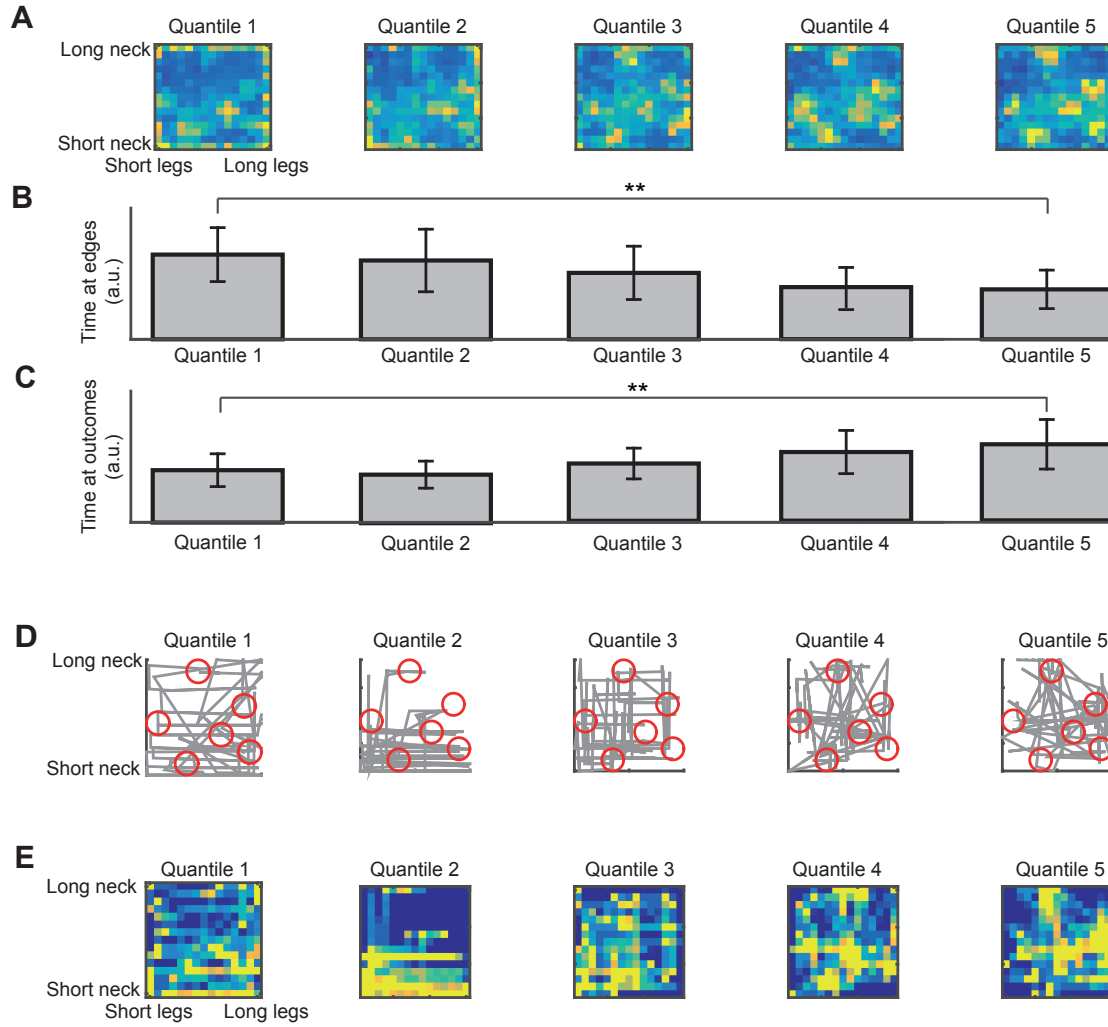
**Fig. S4**

(A) The hexagonal symmetry pattern in the fMRI response becomes evident when the trajectory angles are sorted in an ascending order. (B) When the angles are ordered first as completely misaligned with the grid angle  $\phi$ , then right in the middle between aligned and misaligned, and then completely aligned with the grid angle, the fMRI response will show a step-wise pattern, from a small response, to no change, and to a big response. (C) When shuffled randomly, the fMRI response also becomes random.



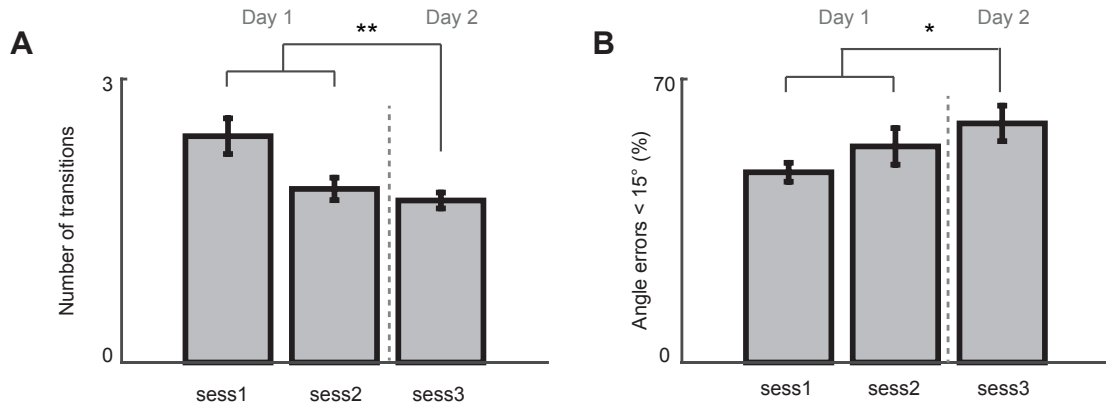
**Fig. S5**

Distribution of trajectory angles. **(A)** Trajectory angles were evenly sampled across the 360° space (varying between 0°-360°). Histograms are shown for trajectory angles passing through all locations in conceptual space, and categorized as a function of passing through an outcome or not (Rayleigh's test,  $p=1$ ,  $p=0.626$  and  $p=0.64$ , respectively). **(B)** To investigate the distribution of angles relative to hexagonal symmetry, we transformed the angles into a 60° space (varying between 0°-60°), using the modulo operation, which computes the remainder after division of the angles by 60. For example, a 70° trajectory in 360° space corresponds to a 10° trajectory in 60° space. We found that the trajectory angles were evenly sampled across the 60° space for all locations in sum, and separately for the locations paired and unpaired with outcomes (Rayleigh's test,  $p=1$ ,  $p=0.623$  and  $p=0.637$ , respectively).



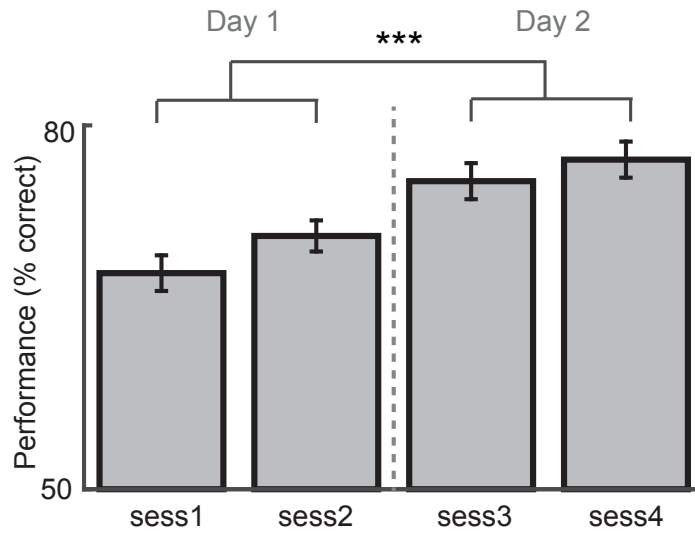
**Fig. S6**

Analysis of the explore task at the group level (A-C) and in one representative subject (D-E). (A) Color-coded trajectory maps illustrating the amount of time spent in each part of the environment (yellow is maximum, dark blue is 0). Note how subjects first navigate in most parts of the abstract space, choosing random trajectories to find the outcomes, and spend most of their time near the boundaries of bird-space. As training progresses, (B) they spend less time at the edges (times at edges, quantile1 vs quantile5,  $t_{22}=3.1776$ , \*\*  $p<0.01$ ) and (C) more time navigating directly between locations paired with outcomes (time at outcomes, quantile1 vs quantile5,  $t_{22}=-3.1773$ , \*\*  $p<0.01$ ). These results demonstrate that the identities of the birds paired with outcomes were well learnt in the subject cohort, conceptually equivalent to learning object locations in a 2D spatial environment. This means that subjects did not only need to indicate if an outcome occurred somewhere on the imagined trajectory, but also at which distance. (D) Trajectories (grey lines) with locations paired with outcomes (red circles) in one representative subject. (E) Corresponding color-coded trajectory maps. Note how this subject spends more time at the edges in quantile1 and explore more the lower area of the environment in quantile 2.



**Fig. S7**

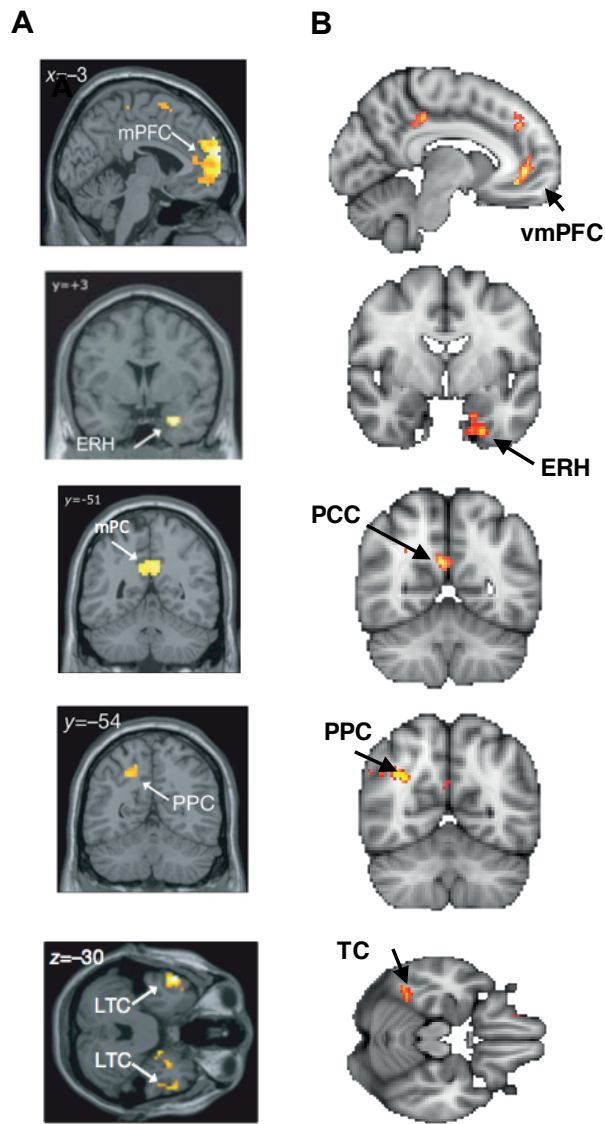
Measures of learning during the collect task. Participants made significant improvements in training day 2 compared to training day 1. (A) Subjects made fewer transitions ( $t_{33}=-2.89$ ,  $** p<0.01$ ) in day 2 than day1, and (B) the percentage of angle errors < 15° increased ( $t_{33}=2.37$ ,  $* p<0.5$ ).



**Fig. S8**

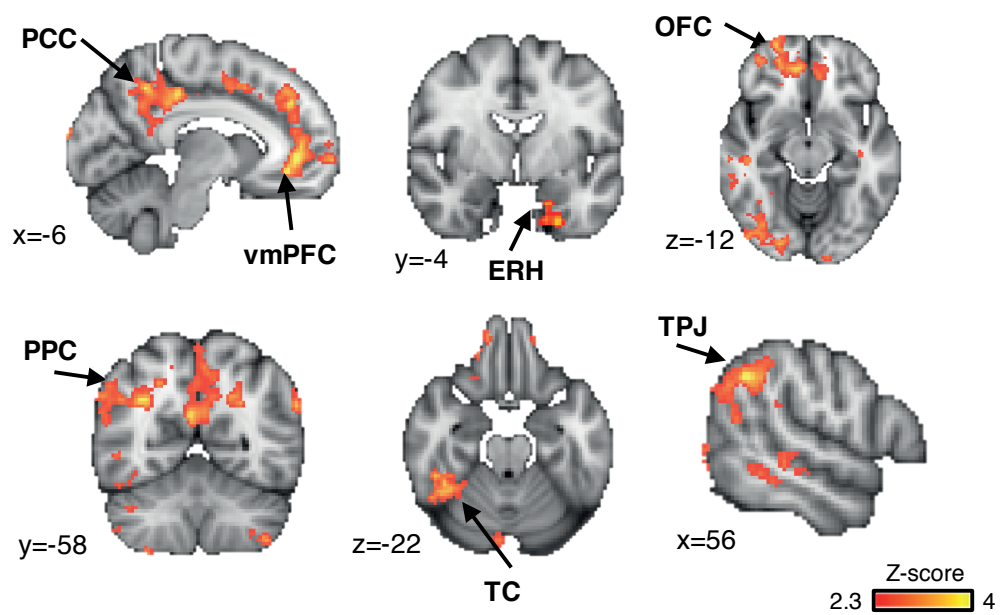
Learning in the recall task. Effects of fresh training on subsequent performance in the scanner. Participants made significantly more correct responses in day 2 compared to day 1 ( $t_{41}=3.89$ , \*\*\*  $p<0.001$ ).





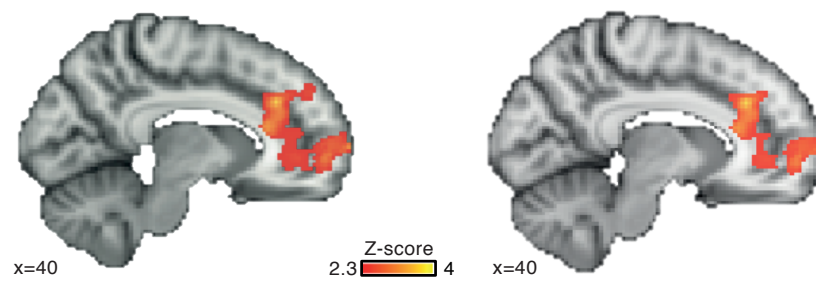
**Fig. S9**

The brain network for navigation in physical space (A) and conceptual space (B). Abbreviations: ventromedial prefrontal cortex (vmPFC), entorhinal cortex (ERH), posterior cingulate cortex (PCC), posterior parietal cortex (PPC), temporal cortex (TC). A is adapted by permission from Nature, Doeller et al, 2010.



**Fig. S10**

Same network of brain regions as in Fig. 2A from the main text, but whole-brain cluster corrected at a more lenient cluster threshold  $Z=2.3$  and  $p<0.05$ , for illustrative purposes. Note that, as in the main text, this analysis is subject to potential bias caused by the mis-estimation of the autocorrelation of fMRI data(26).



**Fig. S11:**

The vmPFC consistency map (left and also shown originally in Fig. 3A) did not change after including a confound regressor that modeled out the effect of outcomes (right).

<b>Test</b>	<b>Presented in</b>	<b>Value including subjects after motion correction</b>	<b>Value excluding subjects with MaxFD &gt; 3mm</b>	<b>Value excluding subjects with TD &gt; 3mm</b>
Correlation between behavior and hexagonal signal modulation in vmPFC	Fig. 2B	$r=0.432$ , $p=0.039$	$r=0.41$ , $p=0.07^*$	$r=0.4$ , $p=0.09^*$
Correlation between behavior and hexagonal consistency in vmPFC	Fig. 3A, right	$r=0.431$ , $p=0.039$	$r=0.49$ , $p=0.02$	$r=0.32$ , $p=0.19^{**}$
Hexagonal consistency vmPFC, within-day	Fig. 3B, left	$t(26)=2.61$ ; $p<0.05$	$t(23)=2.17$ ; $p<0.05$	$t(20)=1.54$ , $p=0.13^{**}$
Control periodicities, vmPFC, within-day	Fig. 3B, right	All $p>0.26$	All $p>0.3$	All $p>0.29$
Hexagonal consistency ERH, within-day	Fig. 3C, left	$t(27)=2.36$ ; $p<0.05$	$t(24)=2.3$ , $p<0.05$	$t(21)=2.65$ ; $p<0.01$
Control periodicities, ERH, within-day	Fig. 3C, right	All $p>0.15$	All $p>0.18$	All $p>0.31$
Hexagonal consistency vmPFC, cross-day	Fig. 4A, left	$t(20)=3.65$ ; $p<0.01$	$t(17)=2.97$ ; $p<0.01$	$t(15)=2.77$ , $p<0.05$
Control periodicities, vmPFC, cross-day	Fig. 4A, right	All $p>0.18$	All $p>0.3$	All $p>0.12$
Hexagonal consistency vmPFC, within- and cross-day	Fig. 4B, left	$t(20)=3.41$ , $p<0.01$	$t(17)=2.66$ ; $p<0.05$	$t(15)=2.35$ , $p<0.05$
Control periodicities, vmPFC, within- and cross-day	Fig. 4B, right	All $p>0.29$	All $p>0.6$	All $p>0.54$
Hexagonal consistency, cross region ERH --> vmPFC	Fig. 4C, left	$t(21)=2.04$ , $p=0.053$	$t(18)=2.21$ ; $p<0.05$	$t(16)=2.32$ , $p<0.05$
Control periodicities, cross region ERH -->	Fig. 4C, right	All $p>0.8$	All $p>0.55$	All $p>0.25$

vmPFC				
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**Table S1.**

Statistical tests from the data re-analyses after excluding participants who moved more than 3mm. \*approaching significance, \*\*no longer significant.

## **Movie S1**

Experimental design. Example trajectories for movement in bird-space at various orientations correspond to morphing of visual stimuli with specific neck:legs ratios. Note that the trajectories were dissociated from the properties of the visual scene, such that trajectories with the same orientation were formed by different stimuli, and trajectories with different orientations could pass through the same stimulus. We designed multiple trajectories in bird-space, and each trajectory corresponded to one trial. Participants had to choose what outcome (Christmas symbol) they received in a trial. They also had the option of choosing “nothing” (black square), meaning that the trajectory did not go through an outcome. We then looked for the hexagonal coding pattern, depending on whether the trajectories were aligned or misaligned with the grid.

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