

# Joint constraints on cosmology and the impact of baryon feedback: combining KiDS-1000 lensing with the thermal Sunyaev-Zeldovich effect from *Planck* and ACT

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## ABSTRACT

We conduct a pseudo- $C_\ell$  analysis of the tomographic cross-correlation between  $1000\text{deg}^2$  of weak lensing data from the Kilo-Degree Survey (KiDS-1000) and the thermal Sunyaev-Zeldovich (tSZ) effect measured by *Planck* and the Atacama Cosmology Telescope (ACT). Using HMX, a halo-model-based approach that consistently models the gas, star, and dark matter components, we are able to derive constraints on both cosmology and baryon feedback for the first time from this data, marginalising over redshift uncertainties, intrinsic alignment of galaxies, and contamination by the cosmic infrared background (CIB). We find our results to be insensitive to the CIB, while intrinsic alignment provides a small but significant contribution to the lensing–tSZ cross-correlation. The cosmological constraints are consistent with those of other low-redshift probes and prefer strong baryon feedback. The inferred amplitude of the lensing–tSZ cross-correlation signal, which scales as  $\sigma_8(\Omega_m/0.3)^{0.2}$ , is low by  $\sim 2\sigma$  compared to the primary cosmic microwave background constraints by *Planck*. The lensing–tSZ measurements are then combined with pseudo- $C_\ell$  measurements of KiDS-1000 cosmic shear into a novel joint analysis, accounting for the full cross-covariance between the probes, providing tight cosmological constraints by breaking parameter degeneracies inherent to both probes. The joint analysis gives an improvement of 40% on the constraint of  $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$  over cosmic shear alone, while providing constraints on baryon feedback consistent with hydrodynamical simulations, demonstrating the potential of such joint analyses with baryonic tracers like the tSZ effect. We discuss remaining modelling challenges that need to be addressed if these baryonic probes are to be included in future precision-cosmology analyses.

**Key words.** cosmology: observations, cosmological parameters, large-scale structure of the Universe, gravitational lensing: weak

## 1. Introduction

Gravitational lensing by large-scale structure induces an angular correlation of galaxy shapes on the sky, which in principle contains a wealth of information about the constituents of the Universe. The signal from this ‘weak’ gravitational lensing is determined by both the Universe’s expansion history and the growth of perturbations. Exquisite measurements of hundreds of millions of galaxy shapes that are expected to be made in the coming decade by galaxy surveys, such as the Legacy Survey of Space and Time (LSST) of the Vera C. Rubin Observatory (Ivezić et al. 2019), the *Euclid* Mission (Laureijs et al. 2011), and the Nancy Grace Roman Space Telescope (Spergel et al. 2015), will allow for the impact of dark energy to be assessed with pre-

cision that has never before been possible. Perhaps most excitingly, the manner of growth of large-scale structure is precisely determined by the underlying gravity theory, and thus general relativity will be robustly tested in a cosmological setting.

The details of how galaxy shapes are distorted is governed by the degree of clustering of large-scale structure between the observed galaxy and Earth. Unfortunately, those structures that contribute most to the correlation of galaxy shapes (over the range of scales where they are best measured) are dense ‘non-linear’ structures whose evolution cannot be calculated via linear (or even quasi-linear) perturbation theory. Structure formation must therefore be simulated, and the clustering statistics extracted from the simulations, in order to compare models to observed data. The simplest clustering statistic is the two-point function, which can be precisely measured from simulations

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(e.g., Heitmann et al. 2010; although see Smith et al. 2014). Emulators (e.g., Lawrence et al. 2017; Angulo et al. 2021; Euclid Collaboration: Knabenhans et al. 2021) can then be constructed to interpolate intelligently between simulation outputs for different cosmological parameters, or physically-motivated fitting formulae (e.g., Takahashi et al. 2012; Mead et al. 2021) can be developed.

If gravity were the only important force in the Universe, then the modelling of structure formation at the level of precision required for the measurements from forthcoming surveys would be a solved problem. Unfortunately, non-gravitational processes can have a significant impact on the distribution of matter. Gas cools, contracts and forms stars, some of which eventually explode as energetic supernovae; black holes form and complicated feedback mechanisms transfer gravitational energy from accretion events into the gas surrounding galaxies. In cosmology these processes are known collectively as ‘baryonic feedback’ and the complex physics of how they operate is poorly understood in comparison with pure gravitational clustering. While it is possible to run accurate *hydrodynamic* simulations that incorporate gas physics (e.g., Springel 2010) such as cooling and radiating, the details of processes like active galactic nucleus (AGN) and supernovae feedback must be included schematically, via *sub-grid* recipes (e.g., Schaye et al. 2010; McCarthy et al. 2017), and it is difficult to assess the numerical convergence and accuracy of such simulations. The unknown impact of feedback on the matter distribution is one of the biggest uncertainties in current lensing analyses (e.g., Chisari et al. 2019b), and if not addressed will limit the ability of forthcoming surveys to test dark energy and gravity theories. Attempts have been made to use these effects of baryon feedback on lensing observables as a probe of galaxy formation (e.g., Harnois-Déraps et al. 2015; Foreman et al. 2016; MacCrann et al. 2017; Huang et al. 2021; Yoon & Jee 2021) but the inferred constraints on baryon feedback have been weak for past and current surveys.

The thermal Sunyaev-Zeldovich (tSZ; Sunyaev & Zeldovich 1972) effect arises when cosmic microwave background (CMB) photons are Compton-scattered off free electrons, predominantly hot electrons in galaxy clusters. This results in a spectral distortion of the CMB black-body spectrum with a characteristic frequency dependence. Maps of this Compton- $y$  signal can be extracted from multifrequency CMB temperature data (e.g., Planck Collaboration XXII et al. 2016). The tSZ effect therefore traces hot ionised gas in the Universe, which is itself correlated with large-scale structure. This correlation contains useful cosmological information (e.g., Planck Collaboration XXII et al. 2016; Horowitz & Seljak 2017; Bolliet et al. 2018; Makiya et al. 2020; Mitchell et al. 2021) and exhibits a particularly strong scaling with the amplitude of perturbations (Refregier & Teyssier 2002; Komatsu & Seljak 2002). Of particular interest to weak-lensing cosmology is the fact that it is this same hot gas that has been redistributed by baryonic feedback, and therefore the tSZ effect provides an important external constraint on the magnitude of baryonic feedback.

The tSZ–galaxy cross-correlation has been investigated (e.g., Vikram et al. 2017; Makiya et al. 2018; Pandey et al. 2019; Tanimura et al. 2020; Chiang et al. 2020; Koukoufilippas et al. 2020; Schaan et al. 2021; Amodeo et al. 2021; Yan et al. 2021), but constraints on cosmological parameters are dependent on the unknown galaxy bias, which must either be taken from external data or else modelled in the data analysis. Stacking of tSZ observations of large-scale structure filaments (e.g., Tanimura et al. 2019; de Graaff et al. 2019) has shed light on the distribution of diffuse gas. In this paper we utilise measurements of weak

lensing and the tSZ effect to place simultaneous constraints on the cosmological model and on the strength of baryonic feedback. The cross-correlation between lensing and the tSZ effect has been measured previously for both CMB lensing (e.g., Hill & Spergel 2014), and for galaxy lensing (e.g., van Waerbeke et al. 2014; Hojjati et al. 2017; Osato et al. 2020; Gatti et al. 2021; Pandey et al. 2021). In these works, model parameters were either fixed or only varied within tight priors, with no coupling between parameters that describe the effect of baryon feedback on the lensing and the tSZ effect. Here we build on these previous works and analyse the tomographic cross-correlation between the tSZ effect and weak lensing from the 1000deg<sup>2</sup> release of the Kilo-Degree Survey (KiDS-1000) in a fully Bayesian manner, deriving posteriors on cosmological and baryon feedback parameters, while marginalising over redshift uncertainties, intrinsic alignment of galaxies, and contamination by the cosmic infrared background (CIB). We then combine the lensing–tSZ cross-correlation with KiDS-1000 cosmic shear in a novel joint analysis. By using the Mead et al. (2020) HMX model, which consistently accounts for gas, stars, and dark matter in the whole joint-data vector, we are able to infer constraints on cosmology, as well as the ‘AGN temperature’ parameter that governs the impact of feedback on both the lensing–tSZ cross-correlation and cosmic shear.

This paper is organised as follows: In Sect. 2, we summarise the lensing and tSZ data, as well as the estimators and summary statistics used; in Sect. 3, we present the modelling of the signal, its covariance, and systematics; Sect. 4 presents the results, including measured data vectors and inferred cosmological constraints; and we summarise our findings in Sect. 5.

## 2. Data

### 2.1. Kilo-Degree Survey

We analyse the fourth data release of the Kilo-Degree Survey (KiDS-1000, Kuijken et al. 2019), which spans  $\sim 1000\text{deg}^2$ , split equally between an equatorial and southern imaging stripe. KiDS is unique in terms of its complete matched-depth nine-band imaging across the optical to the near-infrared, with relatively uniform and high-resolution seeing in the  $r$ -band. This combination of spatial and wavelength resolution provides an exquisite data set for weak gravitational lensing studies, allowing for sensitive control of data-related systematics (Giblin et al. 2021; Hildebrandt et al. 2021).

Galaxy shear estimates are determined using the model-fitting *lensfit* method (Miller et al. 2013), validated and calibrated using realistic KiDS image simulations (Kannawadi et al. 2019). The percent-level uncertainty on this calibration correction is accounted for in our covariance calculation (see section 3.4 of Joachimi et al. 2021, for details). Tomographic galaxy redshift distributions are determined using overlapping spectroscopic training data and a self-organising map to account for incompleteness in the training sample (Wright et al. 2020a). The accuracy of the resulting distributions are validated with a cross-correlation clustering analysis and mock survey analysis (Hildebrandt et al. 2021). The measured uncertainty from these tests is used as a prior for a set of correlated nuisance parameters that account for any residual correlated calibration errors in the mean redshift of each tomographic bin (see section 3.3 of Joachimi et al. 2021, and Sect. 3.4.1 for details). The full suite of KiDS-

1000 data products, including imaging, catalogues, shear and redshift calibrations, is available to download<sup>1</sup>.

## 2.2. Compton- $\gamma$ maps

The construction of Compton- $\gamma$  maps, which trace the tSZ effect, usually proceeds by taking linear combinations of intensity maps at different frequencies of CMB experiments, potentially with scale-dependent or spatially-varying weights. [Planck Collaboration XXII et al. \(2016\)](#) provide two such Compton- $\gamma$  map reconstructions, using two different internal linear combination (ILC) methods: MILCA (modified internal linear combination algorithm; [Hurier et al. 2013](#)) and NILC (needlet independent linear combination; [Remazeilles et al. 2011](#)). We use the MILCA map as our fiducial  $\gamma$ -map in our analysis but confirm that the results hold for the NILC map as well. Furthermore, we check our sensitivity to CIB contamination by using Compton- $\gamma$  maps from [Yan et al. \(2019\)](#) where the CIB has been subtracted from the *Planck* frequency maps. Assessment and mitigation of possible CIB contamination of our  $\gamma$ -maps is further discussed in Sect. 3.4.3.

We apply a Galactic mask that covers the 40 % of the sky with the strongest dust emissions, as well as a point-source mask, as provided by [Planck Collaboration XXII et al. \(2016\)](#). The extra-galactic lensing signal is assumed not to be correlated with emissions from the Milky Way, such that the Galactic mask primarily serves to reduce noise in the measurement. Furthermore, as the KiDS-1000 footprint avoids the Galactic plane, the Galactic mask has only a small effect on the overlap between the shear and Compton- $\gamma$  maps, such that the unmasked area of the overlap between the KiDS-1000 and *Planck* data makes up 85 % of the footprint of the KiDS-1000 data. The maps are provided in HEALPIX ([Górski et al. 2005](#)) format, with  $n_{\text{side}} = 2048$ , in Galactic coordinates.

The *Planck*-derived  $\gamma$ -maps have a resolution of 10 arcmin, which limits the amount of small-scale information that can be extracted. In contrast, Compton- $\gamma$  maps constructed from the combination of the fourth data release of the Atacama Cosmology Telescope (ACT; [Mallaby-Kay et al. 2021](#)) and *Planck* data, benefit from a much smaller beam of 1.6 arcmin ([Madhavacheril et al. 2020](#)). Unlike the *Planck*-derived maps, the ACT  $\gamma$ -maps only partially cover the northern KiDS-1000 patch, while they do not overlap with the southern KiDS-1000 patch at all. After applying the same 40 % Galactic and point source masks as for the *Planck*-derived maps, the overlap between the ACT and KiDS-1000 data is reduced to 30 % of the area covered by the KiDS-1000 data, or 35 % of the area of the overlap between the *Planck*-derived  $\gamma$ -maps and KiDS-1000.

We transform the ACT  $\gamma$ -maps into HEALPIX format ( $n_{\text{side}} = 2048$ ) using `PIXELL`<sup>2</sup>. Unlike the *Planck*-derived maps, the ACT maps are provided in equatorial coordinates, the same as the KiDS-1000 data. When measuring the shear-tSZ cross-correlations with the *Planck*-derived maps, we use a shear catalogue that has been transformed into Galactic coordinates (see, e.g., [Xia et al. 2020](#)), which avoids interpolation artefacts that would be introduced if the  $\gamma$ -map were transformed into a different coordinate system.

## 2.3. Summary statistics and estimators

Our summary statistic are the angular (cross-)power spectra of the shear field and tSZ effect. We estimate the angular power spectra using the pseudo- $C_\ell$  method, specifically the MASTER ([Hivon et al. 2002](#)) estimator as implemented in the NAMASTER<sup>3</sup> ([Alonso et al. 2019](#)) software. The method proceeds by first naively estimating the angular power spectra of the masked maps. These estimates are biased and thus give the method its name: pseudo- $C_\ell$ . The bias introduced by the masks can be calculated and is encoded in the so-called mode-mixing matrices. Given the mode-mixing matrices, an unbiased estimate of the (binned) angular power spectra can be obtained from the biased pseudo- $C_\ell$  estimates. We refer the interested reader to [Alonso et al. \(2019\)](#), who map these steps out in detail (see their equations (7), (9), (D2), and (13) for the steps outlined above).

Estimating shear power spectra using pseudo- $C_\ell$  methods comes with a number of subtleties due to the amount of small-scale power in the masks involved, which can affect the numerical stability of the algorithm. Here we closely follow the methodology of [Nicola et al. \(2021\)](#). We pixelise the shear catalogues into HEALPIX maps  $\hat{\gamma}$  with  $n_{\text{side}} = 2048$ :

$$\hat{\gamma}(\mathbf{n}_i) = \frac{1}{w(\mathbf{n}_i)} \sum_{j \in \mathbf{n}_i} w_j \epsilon_j, \quad (1)$$

where  $\mathbf{n}_i$  denotes the position of the  $i$ -th pixel and the sum runs over all galaxies in that pixel, which are characterised by their weight  $w_j$  and the two ellipticity components, which we denote here with  $\epsilon_j$ . In our case, the weights  $w_j$  are given by the *lensfit* weights and account for uncertainty in the shape measurement. The weight map  $w(\mathbf{n}_i)$  is defined as

$$w(\mathbf{n}_i) = \sum_{j \in \mathbf{n}_i} w_j. \quad (2)$$

The multiplicative shear bias is accounted for by scaling all ellipticity estimates in a tomographic bin by  $\epsilon \rightarrow \frac{1}{1+m_z} \epsilon$ , where we use the multiplicative bias values  $m_z$  in [Giblin et al. \(2021\)](#). The additive shear bias is accounted for by subtracting the weighted ellipticity mean in each tomographic bin. The weight maps of Eq. (2) take the role of the masks for the shear maps of the pseudo- $C_\ell$  estimator. All cross-power spectra are estimated using their respective masks, that is, the measurements are not restricted to the overlap region.

The auto-power spectra are subject to a noise bias, which we account for analytically, using the estimate ([Nicola et al. 2021](#))

$$N_\ell = \Omega_{\text{pix}} \left\langle \sum_{j \in \mathbf{n}_i} w_j^2 \sigma_{\gamma,j}^2 \right\rangle_{\text{pix}}, \quad (3)$$

where  $\Omega_{\text{pix}}$  is the pixel area,  $\sigma_{\gamma,j}^2 = \frac{1}{2} |\epsilon_j|^2$  with  $|\epsilon|^2 = \epsilon_1^2 + \epsilon_2^2$ , and the average is taken over all pixels. The accuracy of this estimate has been confirmed using a large number of Gaussian random field mocks with realistic noise and the real data weight maps of Eq. (2).

The angular power spectra are estimated in 12 logarithmically-spaced bins between  $\ell = 51$  and  $\ell = 2952$ . When discarding the lowest two and highest two  $\ell$ -bins, this binning scheme results in the same eight logarithmically-spaced multipole bins between  $\ell = 100$  and  $\ell = 1500$  that were used in the KiDS-1000 analyses ([Joachimi et al. 2021](#); [Asgari et al.](#)

<sup>1</sup> KiDS-1000 data access: <http://kids.strw.leidenuniv.nl/DR4/lensing.php>

<sup>2</sup> <https://github.com/simonsobs/pixell>

<sup>3</sup> <https://github.com/LSSTDESC/NaMaster>



2021; Heymans et al. 2021; Tröster et al. 2021). Since the KiDS-1000 cosmic shear methodology was validated only on the  $\ell \in (100, 1500)$  range, we restrict our analysis to the same  $\ell$ -range. Furthermore, this  $\ell$ -range captures most of the signal, with the signal-to-noise ratio increasing by only  $\sim 10\%$  for the full  $\ell \in (51, 2952)$  range.

We note that our pseudo- $C_\ell$  approach differs from the KiDS-1000 cosmic shear band power methodology of Asgari et al. (2021) and from the recent pseudo- $C_\ell$  methodology of Loureiro et al. (in prep.). Our analysis choice, which does not impact the KiDS-1000 cosmic shear-only constraints (see Appendix B), is motivated by the requirements of the lensing–tSZ cross-correlation analysis and support for the computation of the full spin-2 Gaussian data covariance by NAMASTER (see Sect. 3.3). The angular power spectrum estimates have also been checked against those estimated with POLSPICE<sup>4</sup> (Szapudi et al. 2001; Chon et al. 2004) and found to be in excellent agreement. The measurement scripts, associated tools, and the measurements themselves are being made publicly available<sup>5</sup>.

### 3. Modelling

#### 3.1. Three-dimensional power spectra

To model our data and extract meaningful cosmological constraints we follow Mead et al. (2020) and use the HMX approach, which is designed to reproduce power spectra measured from the BAHAMAS (McCarthy et al. 2017) suite of cosmological hydrodynamic simulations, which in turn are calibrated to reproduce the observed galaxy stellar mass function and baryon fraction in groups and clusters. HMX works at the three-dimensional level, providing  $P(k)$  rather than  $C_\ell$ , because once  $P(k)$  is accurate the  $C_\ell$  are automatically also accurate via the projection integrals; modelling and physical understanding are also more straightforward in three dimensions where the fields naturally live. The three-dimensional source of the tSZ effect is the electron pressure, while that of shear is the matter overdensity, and HMX reproduces the electron pressure–matter power spectrum from BAHAMAS at the 15 per-cent level for  $z < 2$  and  $k \lesssim 7 h\text{Mpc}^{-1}$  while at the same time providing matter–matter power spectra that are accurate at the 2 per-cent level. Ultimately we wish to use HMX to extract meaningful constraints from combined shear–shear and shear–tSZ data.

Underpinning HMX is the halo model (e.g., Cooray & Sheth 2002), where halo density profiles are broken down into their constituent dark matter, gas and stellar components. The gas is then given thermal properties such that the halo electron pressure can be simultaneously calculated with the matter. This occurs both at the level of individual haloes and the expelled background gas, which is assumed to be heated by AGN activity. Fitting parameters of the model to data from BAHAMAS provides the link in HMX between gas thermal properties and the density. Any standard halo model cross-correlation calculation (e.g., Hill & Spergel 2014; Ma et al. 2015) provides a degree of cross-talk between the two fields through the common linear spectrum, halo mass function and bias, but most often the halo profiles of the two fields are taken to be independent. For example, to model the shear–tSZ signal, an Arnaud et al. (2010) profile may be adopted for the pressure while a (completely separate) Navarro, Frenk, & White (1997; NFW) profile may be adopted for the matter. The advantage of HMX is that the halo profiles

are also directly coupled to each other, which allows the electron pressure (which probes the hot gas) to directly affect the overall matter profile. The model parameters, consisting of the concentration of dark matter halo density profiles and its redshift evolution, the polytropic index of gas bound in haloes, the halo mass below which haloes have lost half their initial gas content, the ratio of halo temperature to that of the virial equilibrium, and the temperature of the warm-hot intergalactic medium with its redshift evolution, are fit to power spectra from simulations with different feedback strengths. All fitted parameters are then related to a single ‘AGN temperature’ parameter,  $\log_{10}(T_{\text{AGN}}/\text{K})$ , which governs the strength of feedback; increasing the temperature increases the tSZ signal while simultaneously decreasing the matter signal as gas is forced from the halo by the increased AGN activity. This is particularly helpful in gaining an understanding of the impact baryonic feedback may have on the matter power spectrum, currently one of the largest uncertainty in cosmic shear studies at small scales (e.g., Chisari et al. 2019b).

The halo model power spectrum calculation is known to be inaccurate in detail, particularly in the ‘transition region’ between the two- and one-halo terms (Tinker et al. 2005; Valageas & Nishimichi 2011; Fedeli et al. 2014), which is primarily because linear bias is an overly simplistic treatment of halo–halo correlations (Mead & Verde 2021). There are also other errors at larger scales (for example, the lack of perturbation theory) and smaller scales (such as assumed halo sphericity) that arise because of other simplifying assumptions that enter into the standard halo-model calculation. To side-step these problems, rather than predicting the raw power, HMX predicts the ratio of the power spectrum in question to the gravity-only matter–matter spectrum (adopting NFW profiles for all matter) calculated for the same cosmological model. The halo-model prediction for this ratio has been shown to be more robust than the absolute power (e.g., Cataneo et al. 2019) as the underlying cosmology is varied<sup>6</sup>. Once we have this halo-model ratio, we must multiply by an accurate prescription for the matter–matter power, such as provided by an emulator, or a semi-analytic model, such as Mead et al. (2021). Here we use the HMCODE-2016 (Mead et al. 2016) model for this matter–matter power prediction, since the more accurate HMCODE-2020 (Mead et al. 2021) was not yet available when this analysis was performed.

#### 3.2. Angular power spectra

Neither the three-dimensional matter–matter nor the matter–electron pressure power spectra are directly observable. Instead we observe the angular auto and cross-power spectra of the gravitational lensing shear effect induced by the matter distribution and the tSZ effect caused by the electron pressure. The angular power spectrum  $C_\ell^{AB}$  at multipole  $\ell$  between fields  $A$  and  $B$  can be related to the three-dimensional power spectrum  $P_{AB}(k, z)$  corresponding to these fields through (e.g., Kaiser 1992; LoVerde & Afshordi 2008; Kilbinger et al. 2017)

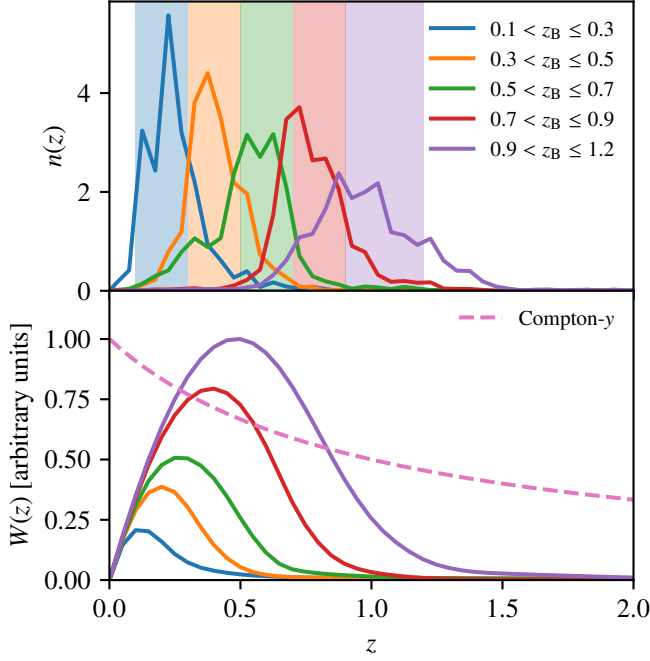
$$C_\ell^{AB} = \int_0^{\chi_H} \frac{d\chi}{\chi^2} W^A(\chi) W^B(\chi) P_{AB} \left( \frac{\ell + \frac{1}{2}}{\chi}, z(\chi) \right). \quad (4)$$

The integral is taken over the comoving distance  $\chi$ , from the observer to the distance of the horizon  $\chi_H$ . Throughout this

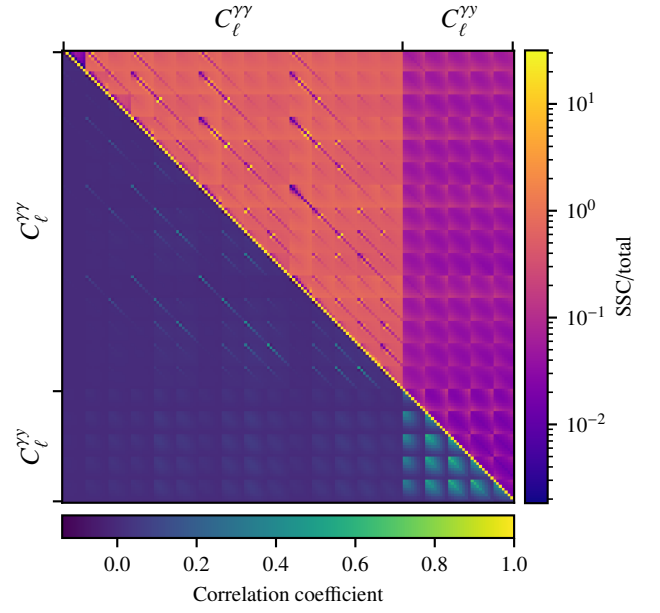
<sup>4</sup> <http://www2.iap.fr/users/hivon/software/PolSpice/>

<sup>5</sup> <https://github.com/tilmantroester/KiDS-1000xtSZ>

<sup>6</sup> Mead et al. (2020) showed that this works reasonably well for matter–electron pressure, but noted that the transition scale between the two- and one-halo terms occurs at quite different scales depending on the fields being cross-correlated. More work is needed to assess the full impact of this.



**Fig. 1.** *Top:* Redshift distributions  $n_i(z)$  of the five tomographic source samples (solid lines). The shaded bands indicate the selection window on the photometric redshift point estimate  $z_B$ . *Bottom:* Line-of-sight window function,  $W(z)$ , to project the three-dimensional power spectra  $P(k)$  (in comoving units) into their angular counterparts  $C_\ell$ . The lensing window functions (solid lines, Eq. (5)) are normalised by the maximum of the window function of the last tomographic bin, while the Compton- $y$  window function (dashed line, Eq. (6)) is normalised by its maximum value.



**Fig. 2.** *Upper right:* Contribution of the super sample covariance (SSC) to the joint cosmic shear, shear-tSZ data covariance. Shown is the ratio between the absolute value of the SSC contribution and the absolute value of the total covariance in Eq. (8). The ratio can exceed unity, since different contributions to total covariance can cancel to a certain degree. *Lower left:* Correlation coefficients corresponding to the data covariance matrix.

work we shall assume a flat  $\Lambda$ CDM cosmology with a minimal neutrino mass, as there has been no evidence for extensions to this model (e.g., Planck Collaboration VI et al. 2020; Alam et al. 2021; Tröster et al. 2021). The shear field derives from the three-dimensional matter overdensity field. Hence, for  $C_\ell^{\gamma\gamma}$  the power spectrum  $P_{AB}$  in Eq. (4) is the matter-overdensity power spectrum  $P_{mm}$ . In the case of the angular cross-power spectrum between shear and the tSZ effect,  $C_\ell^{\gamma y}$ , the relevant three-dimensional power spectrum is the cross-power spectrum of matter overdensity and electron pressure,  $P_{mP}$ . Unless noted otherwise, the auto and cross-correlations involving the shear field shall refer to the  $E$ -mode of the  $E/B$ -mode decomposition of the spin-2 shear field. That is, we shall use  $C_\ell^{\gamma\gamma}$  and  $C_\ell^{\gamma y}$  as a notational short-hands for  $C_\ell^{\gamma E \gamma E}$  and  $C_\ell^{\gamma E y}$ , respectively. The window function  $W^i(\chi)$  of the shear field of the  $i$ -th source sample is given by

$$W^i(\chi) = \frac{3}{2} \left( \frac{H_0}{c} \right)^2 \Omega_m \frac{\chi}{a(\chi)} \int_\chi^{\chi_H} d\chi' n_i(\chi') \frac{\chi' - \chi}{\chi'}, \quad (5)$$

where  $H_0$  denotes the present-day Hubble rate,  $c$  the speed of light,  $\Omega_m$  the matter density,  $a(\chi)$  the scale factor at comoving distance  $\chi$ , and  $n_i(\chi)d\chi = n_i(z)dz$  the redshift distribution of source sample  $i$ . The window function  $W^y(\chi)$  of the tSZ effect is

$$W^y(\chi) = \frac{\sigma_T}{m_e c^2} \frac{1}{a^2(\chi)}, \quad (6)$$

where  $\sigma_T$  is the Thompson scattering cross section and  $m_e$  is the electron mass. Here the three-dimensional power spectra are

given in comoving units, including the electron pressure. That is, the matter-electron pressure cross-power spectrum  $P_{mP}$  has units of  $[(\text{comoving length})^3 \times \text{energy}/(\text{comoving length})^3] = [\text{energy}]$ . The redshift distributions  $n_i(z)$  of the source samples, as well as the window functions of Eqs. (5) and (6) are illustrated in Fig. 1.

In order to compare our model of the angular power spectra in Eq. (4) to the measured power spectra described in Sect. 2.3, we need to account for the binning in multipoles, residual effects of the mode-mixing matrices, and  $E/B$ -mode mixing. To this end we apply the pseudo- $C_\ell$  bandpower window function  $\mathcal{F}_{b\ell}^{AB}$ , which maps the angular power spectrum  $C_\ell^{AB}$  to the pseudo- $C_\ell$  bandpower power spectrum  $C_b^{AB}$  at bin  $b$ :

$$C_b^{AB} = \sum_\ell \mathcal{F}_{b\ell}^{AB} C_\ell^{AB}. \quad (7)$$

The pseudo- $C_\ell$  bandpower window function  $\mathcal{F}_{b\ell}^{AB}$  can be computed analytically and is given by equation (16) in Alonso et al. (2019). Since our model does not predict any  $B$ -modes,  $E/B$ -mode mixing does not affect the model for the  $E$ -modes. These window functions are illustrated in Figure B.2 for the case of  $E$ -mode cosmic shear.

### 3.3. Covariance

To estimate the uncertainty associated with our measured data vector, we largely follow the methodology of Joachimi et al. (2021), with minor modifications to account for the pseudo- $C_\ell$  estimator and allow the computation of the tSZ parts of the covariance matrix. In contrast to simulation or resampling-based

methods, this analytic approach is free of sampling noise and allows us to cleanly separate the different covariance contributions, as well as match the cosmology to that preferred by the data.

We decompose the covariance  $\mathbf{C} = \text{Cov}[\hat{C}_{\ell_1}^{ij}, \hat{C}_{\ell_2}^{kl}]$  of the measured angular (cross-)power spectra  $\hat{C}_{\ell}^{ij}$  between fields  $i$  and  $j$  at the effective multipole  $\ell$  into

$$\mathbf{C} = \mathbf{C}_G + \mathbf{C}_{\text{SSC}} + \mathbf{C}_T + \mathbf{C}_m, \quad (8)$$

where  $\mathbf{C}_G$  is the Gaussian contribution,  $\mathbf{C}_{\text{SSC}}$  is the super-sample covariance (SSC),  $\mathbf{C}_T$  is the non-Gaussian contribution due to the non-zero trispectrum, and  $\mathbf{C}_m$  accounts for the uncertainty in the shear calibration.

We compute the Gaussian covariance term  $\mathbf{C}_G$  using NA-MASTER, accounting for the effect of partial and weighted sky observations (García-García et al. 2019). While this can be done exactly, the calculation scales as  $O(\ell_{\text{max}}^6)$  for the sample variance term. Instead, we use the improved narrow kernel approximation (NKA) introduced in Nicola et al. (2021) for the cosmic shear sample variance and the parts of the covariance that involve tSZ cross-correlations. For cosmic shear, the noise terms can be computed exactly with little extra effort by calculating the different terms in Eq. (2.29) of Nicola et al. (2021) separately. We find that this exact calculation reduces the Gaussian cosmic shear covariance by up to 20 % compared to the case where the NKA is used for both sample variance and noise terms. Some of the Compton- $y$  maps have no readily available noise maps necessary for the exact noise computation, and we thus use the NKA for all terms of covariance involving the tSZ effect. As the signal-to-noise ratio of the tSZ cross-correlation is lower than that of the cosmic shear measurement, this is of little concern, however. The sample variance of the cosmic shear and shear-tSZ terms in the Gaussian covariance are computed using the model for the angular power spectra of Sect. 3.2 at the best-fit cosmology of Heymans et al. (2021). By contrast, the tSZ auto-power spectrum term is based on a smoothed version of the measured auto-power spectrum of the  $y$ -maps. This choice is motivated by the fact that HMX was not calibrated for accurate predictions of the pressure auto-power spectrum. Since the overlap between the KiDS-1000 footprint and the Compton- $y$  maps constitutes a small fraction of the full  $y$ -maps, the measured tSZ auto-spectra are largely independent of the shear spectra.

Osato & Takada (2021) found that the SSC term can be the dominant contribution to the data covariance in analyses of the tSZ auto-power spectrum. In cosmic shear analyses, the SSC term is the dominant non-Gaussian contribution (e.g., Barreira et al. 2018). We thus account for SSC in the full cosmic shear, shear-tSZ, and joint covariance. The SSC  $\mathbf{C}_{\text{SSC}}$  and trispectrum terms  $\mathbf{C}_T$  are computed using the halo model formalism as implemented in CCL<sup>7</sup> (Chisari et al. 2019a). The halo matter density and pressure profiles are computed with the HMX prescription, using PYHMCODE<sup>8</sup>, such that the modelling of the signal and the covariance is consistent. The version of CCL used in this work only includes the one-halo contribution to trispectrum term. This is not an issue, however, since for cosmic shear the trispectrum term is subdominant everywhere (Joachimi et al. 2021) and for the tSZ effect it is dominated by the one-halo term (Cooray 2001). The SSC term is found to be sub-dominant for the shear-tSZ cross-correlation but can reach up to  $\sim 20\%$  of the total covariance for off-diagonal terms. This is illustrated in

Fig. 2, showing the relative contribution of the SSC to the total covariance. We find that not accounting for the SSC term leads to an underestimate of the inferred parameter uncertainties of about 10 %.

To account for the uncertainty of the multiplicative shear bias  $\mathbf{C}_m$ , we follow Joachimi et al. (2021), that is, we assume that the multiplicative bias corrections are fully correlated between the tomographic bins. Asgari et al. (2021) showed that this approach gives very similar constraints to allowing the multiplicative biases to vary, while not requiring sampling over an extra five parameters.

Another approach to the estimation of the data covariance is through large ensembles of simulated mock data. This approach has some considerable downsides for the present analysis, however. Obtaining mock data that accurately models both the tSZ effect, as well as weak lensing, over large sky areas and with a sufficient number of realisations to reduce the sampling noise, is a challenging proposal. While Tröster et al. (2019) demonstrated a deep-learning method to augment weak lensing-optimised  $N$ -body simulations with gas physics that accurately predict the tSZ effect, this approach is not easily amenable to different cosmological parameters. Furthermore, accounting for the SSC is difficult, unless one employs costly ‘separate universe’ simulations (Li et al. 2014). Finally, the covariance is dominated by the Gaussian term (Joachimi et al. 2021), which can be accurately computed analytically, even for large survey areas.

Our data covariance model has been checked against jackknife estimates. We find good agreement at small scales but find that the jackknife approach underestimates the covariance at large scales. However, since these scales break the assumption of independence between the jackknife patches, the jackknife estimates need to be interpreted with caution.

### 3.4. Systematics

#### 3.4.1. Photometric redshift uncertainties

The redshift distributions of the KiDS-1000 source samples have been estimated and validated to a high degree of accuracy (Hildebrandt et al. 2021). To account for the residual uncertainty in the redshift distributions of the source samples, we follow Asgari et al. (2021) and allow the redshift distribution for each tomographic bin to shift. We impose a multivariate Gaussian prior on these shifts, where the mean and covariance are derived from the calibration of the redshift estimation method to realistic mock data. We refer the interested reader to Wright et al. (2020b); Hildebrandt et al. (2021); Asgari et al. (2021) for further details on the estimation of the redshift distributions and their uncertainties.

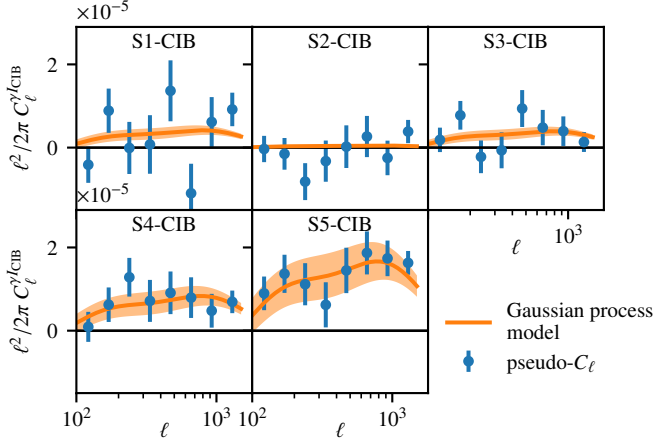
#### 3.4.2. Intrinsic alignments

Since the tSZ effect is correlated with large-scale structure, source galaxies aligning with the same large-scale structure can mimic a gravitational lensing signal, and thus the correlation between the tSZ effect and these intrinsic alignments (IA) could bias our shear-tSZ cross-correlation analysis. We account for this intrinsic alignment effect using the same model as in the KiDS-1000 analyses (see Joachimi et al. 2021; Asgari et al. 2021; Heymans et al. 2021). Specifically, we employ the non-linear alignment (NLA; Hirata & Seljak 2004; Bridle & King 2007) model and allow the amplitude parameter  $A_{\text{IA}}$  to vary, while keeping the redshift-evolution parameter  $\eta_{\text{IA}}$  fixed. Asgari et al. (2021) showed that letting  $\eta_{\text{IA}}$  vary serves to slightly

<sup>7</sup> <https://github.com/LSSTDESC/CCL>

<sup>8</sup> <https://github.com/tilmantroester/pyhmcodes>





**Fig. 3.** Measured angular cross-power spectra between KiDS-1000 shear and the 545 GHz CIB map (blue points). The best-fit Gaussian process (GP) model is shown as the orange line, with the orange shaded band indicating the 68th percentiles of the GP model uncertainty.

loosen the constraints on  $S_8$  but does not affect its central value. For a detailed discussion of the choice of IA model for the KiDS-1000 data, we refer the interested reader to appendix D of Heymans et al. (2021). We find that IA has a small but significant impact on the shear–tSZ cross-correlation signal, in agreement with findings of Gatti et al. (2021); Pandey et al. (2021). Its relative contribution to the total signal, as well as its fraction of the measurement error, is comparable to the IA contribution in the case of cosmic shear.

### 3.4.3. Cosmic infrared background

The tSZ maps are contaminated by CIB (Hurier 2015; Planck Collaboration XXII et al. 2016; Planck Collaboration XXIII et al. 2016). To assess and correct for this contamination in our shear–tSZ cross-correlation, we consider two complementary approaches. The first approach models the effect of the CIB contamination based on the observed correlation between the shear field and maps of the CIB, while the second approach uses Compton-y maps where the CIB has been subtracted during the reconstruction process.

For the first, model-based approach, we follow the simple but commonly used method of Hill & Spergel (2014); Vikram et al. (2017), where the contamination of the observed Compton-y map  $y_{\text{obs}}$  is modelled as

$$y_{\text{obs}} = y_{\text{true}} + \alpha_{\text{CIB}} I_{\text{CIB}} + N, \quad (9)$$

where  $y_{\text{true}}$  is the map of the uncontaminated tSZ effect,  $I_{\text{CIB}}$  is a map tracing the CIB,  $\alpha_{\text{CIB}}$  is a scalar parameter, and  $N$  denotes the collection of noise and other contaminants that are not expected to correlate with the shear field, unlike the other two terms.

This model is quite simplistic; the use of a single frequency CIB map assumes that the CIB is not varying with frequency, and the single, scalar parameter  $\alpha_{\text{CIB}}$  assumes that the contamination is not varying spatially. Neither of these assumptions strictly hold true: the CIB is the result of complex astrophysical processes, whose detailed frequency dependence is not constant, and the reconstruction algorithms used for the y-maps in this work employ scale-dependent filters, resulting in scale-

dependent ILC coefficients, and would thus require a scale-dependent  $\alpha_{\text{CIB}}$  as well.

In practice, these assumptions appear to be sufficient, however, at least for the applications considered in the present work, since we find CIB contamination to be negligible (see Sect. 4.2). Compton-y maps using scale-independent ILC weights (e.g. van Waerbeke et al. 2014; Hill & Spergel 2014) are consistent with those using MILCA and NILC reconstructions used here and the CIB is strongly correlated between different frequency bands (e.g., Planck Collaboration XXX et al. 2014; Lenz et al. 2019; Stein et al. 2020). Nonetheless, future work will have to revisit these approximations. Potential improvements include the use of a multi-band analysis, such as in Chiang et al. (2020), where the signal in each frequency band is modelled separately, or the use of other CIB maps (e.g. Lenz et al. 2019).

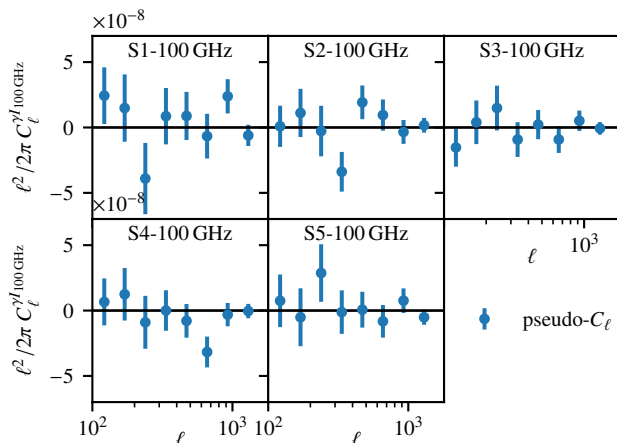
Under the model of Eq. (9), the cross-power spectrum between the shear field and the observed Compton-y map is then given by

$$C_\ell^{\gamma_{\text{obs}}} = C_\ell^{\gamma_{\text{true}}} + \alpha_{\text{CIB}} C_\ell^{\gamma I_{\text{CIB}}}, \quad (10)$$

where  $C_\ell^{\gamma_{\text{true}}}$  corresponds to the shear–tSZ cross-correlation model in the absence of CIB contamination and  $C_\ell^{\gamma I_{\text{CIB}}}$  is a model for the shear–CIB cross-correlation. The scaling parameter  $\alpha_{\text{CIB}}$  can be found by comparing the measured cross-correlation between the Compton-y map and the CIB map with their auto-correlations. Here we use the 545 GHz CIB map from Planck Collaboration XLVIII et al. (2016) as a proxy for  $I_{\text{CIB}}$  in Eq. (9) together with  $\alpha_{\text{CIB}} = (2.3 \pm 6.6) \times 10^{-7} \text{ MJy}^{-1} \text{ sr}$ , as derived in Alonso et al. (2018).

To model  $C_\ell^{\gamma I_{\text{CIB}}}$  we choose a phenomenological approach, since modelling the CIB within the HMX framework is not possible at this point. Instead, we measure the tomographic cross-power spectra between the KiDS-1000 source samples and the 545 GHz CIB map (smoothed to a beam size of  $10'$  and masked with the y-map mask) and then fit a Gaussian process (GP) to these observed cross-power spectra. The shear–CIB cross-spectra, together with the Gaussian process model and its uncertainty are shown in Fig. 3. The Gaussian data covariance is computed in an iterative process. First, the covariance is computed by NAMASTER using the cosmic shear model of Sect. 3.2 and the measured and smoothed auto-power spectrum of the CIB map, with zero cross-correlation. After fitting the GP model using this initial covariance, the covariance is recomputed, now including the GP model for the cross-correlation term. Finally, the GP model is refit using the new covariance. The GP model is implemented using GPYTORCH<sup>9</sup> (Gardner et al. 2018). The model is a multi-task GP (Bonilla et al. 2008), with a fixed data covariance. The fitted parameters consist of the length-scale of the squared exponential kernel, which accounts for the correlation between  $\ell$ -modes, and the task covariance, which accounts for the correlation between the tomographic bins and is parameterised as the sum of a rank-one matrix and a diagonal component, for a total of 11 free parameters. Being a multi-task GP, the model thus accounts for the correlation between the redshift bins, as well as between  $\ell$ -bins. Using a fixed data covariance ensures that the GP regression does not fit to spurious or excess (co)-variances. This formalism can be extended to account for the correlation between the shear–tSZ and shear–CIB cross-correlations, such that the GP model is conditioned on the shear–tSZ model. Due to the small effect of the CIB on the present analysis, we leave this sophistication to future work.

<sup>9</sup> <https://pytorch.ai/>



**Fig. 4.** Measured angular cross-power spectra between KiDS-1000 shear and the *Planck* 100GHz intensity map.

To account for residual biases in our treatment of the CIB contamination, we marginalise over the  $\alpha_{\text{CIB}}$  parameter in our fiducial analysis, using a Gaussian prior based on the value derived in [Alonso et al. \(2018\)](#) but with a variance that is four times larger. Alternatively, being a linear parameter, the marginalisation over  $\alpha_{\text{CIB}}$  could have been accounted for analytically by an appropriate term in the data covariance (e.g., [Bridle et al. 2002](#)), analogous to the treatment of the multiplicative shear bias.

In our second approach to assess the sensitivity of our cross-correlation measurements to CIB contamination, we compute the shear-tSZ cross-correlation using CIB-subtracted y-maps from [Yan et al. \(2019\)](#). These maps subtract the CIB contributions in the 353 GHz, 545 GHz, and 845 GHz bands, based on the CIB maps constructed in [Planck Collaboration XLVIII et al. \(2016\)](#). The CIB contributions at lower frequencies are extrapolated from these maps, using a grey body spectrum with the best-fit parameters from [Planck Collaboration XXX et al. \(2014\)](#).

A different approach was used in the construction of the ACT Compton-y map ([Madhavacheril et al. 2020](#)) and the y-maps of the recent Dark Energy Survey (DES) Y3 cross-correlation analyses ([Gatti et al. 2021](#); [Pandey et al. 2021](#)). During the ILC procedure, rather than projecting out the primary CMB, they deproject a grey body spectrum. In these works, the emissivity index  $\beta$  of the grey body spectrum, which modifies the slope of the black body spectrum at low frequencies, lies between 1 and 1.4. This is significantly lower than the  $\beta = 1.75 \pm 0.06$  derived from the CIB power spectrum in [Planck Collaboration XXX et al. \(2014\)](#) and which we use in our CIB subtracted y-maps. Other works, such as the WebSky mocks ([Stein et al. 2020](#)) use the model parameters derived in [Viero et al. \(2013\)](#) based on *Herschel* CIB data, which prefer  $\beta = 1.6 \pm 0.1$ . To check our CIB-subtracted Compton-y map against changes in  $\beta$ , we also generate a map that extrapolates the CIB to the lower frequency bands assuming a value of  $\beta = 1.2$ . In Sect. 4.2, we show that our results are robust with respect to all of these choices.

### 3.4.4. Radio sources

Unresolved radio sources are another potential contamination in the Compton-y map. [Shirasaki \(2019\)](#) suggest that unresolved radio sources can bias shear-tSZ cross-correlations by up to 30%. Their study however differs in key assumptions from ours.

To calculate the expected contamination from unmasked radio sources, they assume a flux cut of 400 mJy. In our analysis, we use the point-source and 40% Galactic mask provided in [Planck Collaboration XXII et al. \(2016\)](#). The mask covers sources with fluxes  $> 300$  mJy of the second *Planck* catalogue of compact sources (PCCS2; [Planck Collaboration XXVI et al. 2016](#)), with none of the unmasked sources lying within the KiDS-1000 footprint. The flux cut assumed in [Shirasaki \(2019\)](#) therefore overestimates the number and flux from unmasked sources. Considering the sizeable bias estimated in [Shirasaki \(2019\)](#), even a lower flux cut might still give rise to a significant amount of radio contamination in our Compton-y maps. We therefore follow a similar approach to our treatment of the CIB contamination, namely estimate the effect on the shear-tSZ cross-correlation based on the cross-correlation of the shear field with the contaminant. To this end, we measure the angular cross-power spectrum between the KiDS-1000 source samples and the *Planck* 100GHz map as a tracer of radio emissions. The cross-correlation with Gaussian errors is shown in Fig. 4. Unlike the cross-correlation with the CIB, we detect no significant correlation between the shear field and the 100GHz map. We hence conclude that our estimates of the shear-tSZ cross-correlation are not significantly affected by contamination of our y-maps due to unresolved radio sources. This finding is also in agreement with [Planck Collaboration XXII et al. \(2016\)](#), who find that radio sources are a subdominant contribution to the Compton-y auto-power spectrum, as well as with [Gatti et al. \(2021\)](#), who find that masking radio sources does not affect their shear-tSZ cross-correlation.

### 3.5. Inference pipeline

Our inference pipeline is based on a modified version<sup>10</sup> of COSMOSIS<sup>11</sup> ([Zuntz et al. 2015](#)). The linear matter power spectrum is calculated using CAMB<sup>12</sup> ([Lewis et al. 2000](#)). The non-linear matter and electron pressure power spectra are computed using HMX, after which the modelling proceeds as described in Sects. 3.2 and 3.4. The computational cost of the model prediction is dominated by the calculation of the non-linear power spectra, specifically the calculation of the halo profiles, since the matter and electron pressure profiles have no analytic Fourier transforms, necessitating numerical transforms. To mitigate this, we evaluate the three-dimensional power spectra at eight redshifts between  $z = 0$  and  $z = 1.5$ , which reduces the evaluation time of a single likelihood to  $\sim 30$ s. The smoothness of the power spectra and kernels in the integral of Eq. (4) limits the numerical error incurred by this coarse redshift sampling. We find that this redshift sampling is accurate to 1% of the measurement uncertainty for the shear-tSZ cross-correlation and to 0.5% for cosmic shear. We assume a Gaussian likelihood, given by the model described above; a data vector consisting of either the cosmic shear or shear-tSZ data, as described in Sect. 2.3, or the concatenation of the two in the case of the joint analysis of cosmic shear and shear-tSZ; and the data covariance described in Sect. 3.3.

In our fiducial setup, we sample 13 parameters, listed in Table 1, using the nested sampling implementation of MULTINEST ([Feroz & Hobson 2008](#); [Feroz et al. 2009, 2013](#)), using 500 or 1000 live points, and an efficiency parameter of 0.3. The maximum of the posterior is found by running multiple Nelder-Mead

<sup>10</sup> <https://github.com/KiDS-WL/kcap>

<sup>11</sup> <https://bitbucket.org/joezuntz/cosmosis>

<sup>12</sup> <https://github.com/cmbant/CAMB>



**Table 1.** Sampled parameters and priors.

Parameter	Symbol	Prior
Dimensionless Hubble constant	$h$	$U(0.64, 0.82)$
Physical baryon density	$\omega_b$	$U(0.019, 0.026)$
CDM density	$\omega_c$	$U(0.051, 0.255)$
Density fluctuation amplitude	$S_8$	$U(0.1, 1.3)$
Scalar spectral index	$n_s$	$U(0.84, 1.1)$
Intrinsic alignment amplitude	$A_{IA}$	$U(-6, 6)$
CIB contamination amplitude	$\alpha_{CIB} [10^7 \text{ MJy}^{-1} \text{ sr}]$	$\mathcal{N}(2.3, (13.2)^2)$
AGN feedback strength	$\log_{10} \left( \frac{T_{AGN}}{\text{K}} \right)$	$U(7.1, 8.5)$
Redshift offsets (5)	$\delta_z$	$\mathcal{N}(\mu_{\delta_z}, C_{\delta_z})$

**Notes.** The first section lists the primary cosmological parameters, while the second section lists the astrophysical and observational nuisance parameters for intrinsic galaxy alignments, CIB contamination, baryon feedback, and uncertainties in the redshift calibration. The five redshift offset parameters are drawn from a multivariate Gaussian prior with mean  $\mu_{\delta_z}$  and covariance  $C_{\delta_z}$ , see Sect. 3.4.1 for details.

(Nelder & Mead 1965) optimisations, starting from samples with the highest posterior values.

## 4. Results

Figure 5 presents the measurements of our fiducial data vector, consisting of the pseudo- $C_\ell$  estimates of the KiDS-1000 cosmic shear angular power spectra and the shear-tSZ angular cross-power spectra, using the *Planck* MILCA Compton- $\gamma$  map. Overplotted are the 68 and 95 percentiles of the posterior predictive distribution (PPD) and samples of the translated posterior distribution (TPD; Köhlinger et al. 2019) for the joint data vector, coloured by their value of  $\log_{10}(T_{AGN}/\text{K})$ , which characterises the strength of AGN feedback in our model. The PPD describes fictional observations, conditioned on the data and model, and is a useful diagnostic to assess consistency within and between data vectors (e.g., Gelman et al. 2013; Köhlinger et al. 2019; Doux et al. 2021). The TPD translates the model parameter posterior into data-space, thus capturing the distribution of model predictions, conditioned on the data.

The cosmic shear signal is detected at  $20.9\sigma$  significance, while the shear-tSZ cross-correlation is detected at  $9.4\sigma$  significance. The significance is estimated as  $\sqrt{\mathbf{d}^T \mathbf{C}^{-1} \mathbf{d}}$ , where  $\mathbf{d}$  is the pseudo- $C_\ell$  data vector and  $\mathbf{C}$  is the data covariance, given by Eq. (8). The  $B$ -modes of our measurements are consistent with zero, with details discussed in Appendix A.

Parameter constraints on  $\Omega_m$  and  $\sigma_8$  derived from the cosmic shear, shear-tSZ, and joint data are shown in Fig. 6. Our cosmic shear constraints exhibit the usual ‘cosmic banana’ degeneracy and are in good agreement with the KiDS-1000 bandpower analysis of Asgari et al. (2021, cf. Appendix B). The cosmic shear signal scales approximately as  $\propto \sigma_8^2 \Omega_m$  and is thus usually summarised with the parameter  $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$ . Depending on the specific estimator, the exact scaling can deviate slightly from  $S_8$ , such that the parameter  $\Sigma_8^\alpha = \sigma_8 (\Omega_m/0.3)^\alpha$ , with an appropriately chosen  $\alpha$ , is a better description of the direction orthogonal to the degeneracy. For example, the  $\sigma_8$ - $\Omega_m$  degeneracy for the bandpower estimator in Asgari et al. (2021), as well as the pseudo- $C_\ell$  estimator in this work, is better described by  $\Sigma_8^{0.58}$  than  $S_8$ .

The shear-tSZ cross-correlation is more sensitive to  $\sigma_8$  (e.g., Refregier & Teyssier 2002; Komatsu & Seljak 2002; Mead et al. 2020) than cosmic shear, resulting in a degeneracy direction that is shallower in  $\sigma_8$ . We find that the cross-correlation signal scales

approximately as  $\propto \sigma_8^5 \Omega_m$ . We will use the parameter  $\Sigma_8^{0.2}$  when comparing different shear-tSZ cross-correlation constraints in the remainder of this analysis. In our fiducial analysis, which uses the *Planck* MILCA Compton- $\gamma$  map, we infer

$$\Sigma_8^{0.2} = 0.723_{-0.032}^{+0.046}. \quad (11)$$

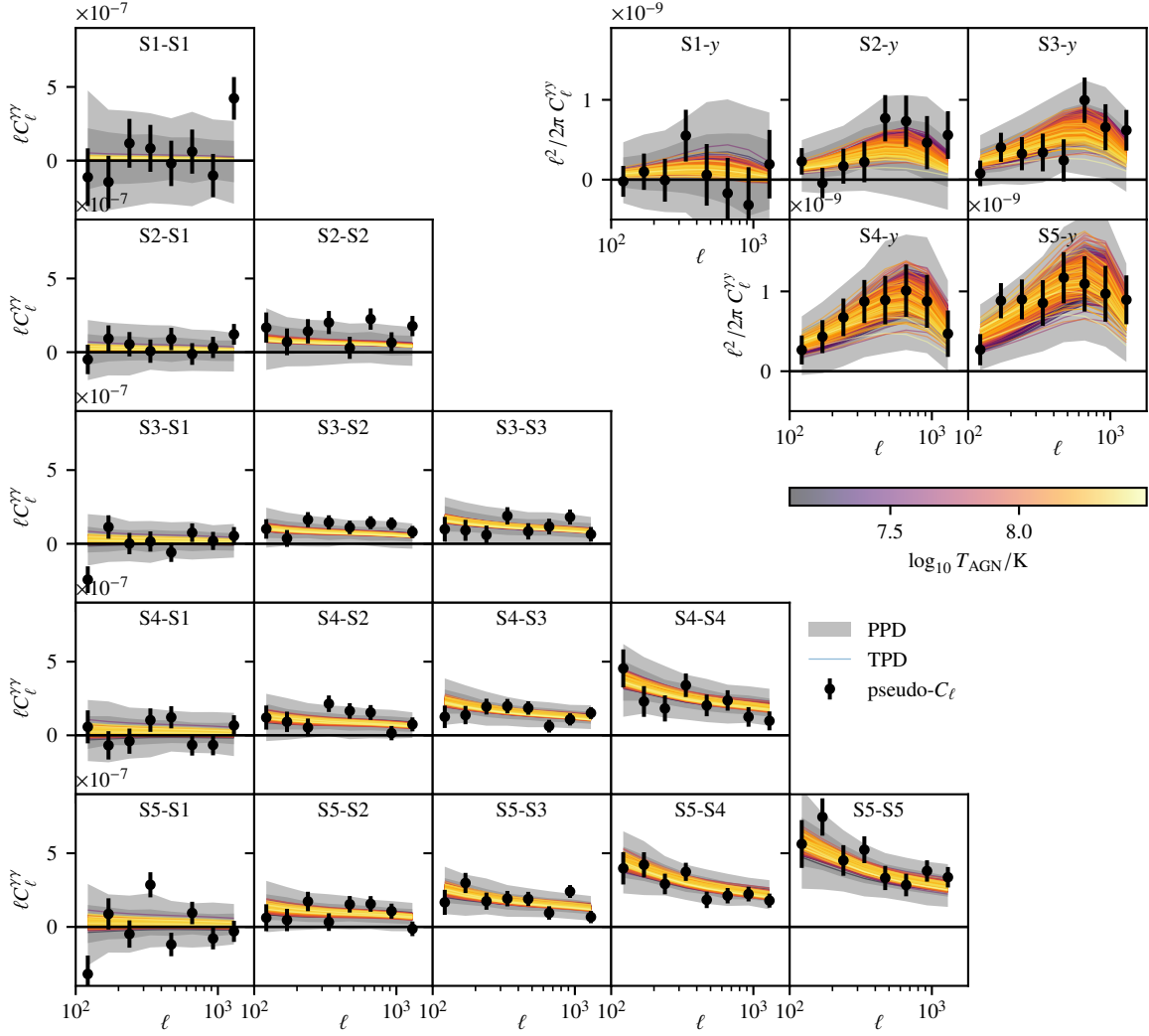
The different degeneracy directions of the cosmic shear and shear-tSZ cross-correlations allow the joint analysis of the two to break these degeneracies and provide tight cosmological constraints. We find

$$\begin{aligned} \Omega_m &= 0.342_{-0.037}^{+0.042} \\ \sigma_8 &= 0.692_{-0.039}^{+0.05} \\ S_8 &= 0.751_{-0.017}^{+0.02}, \end{aligned} \quad (12)$$

for the maximum of the marginal posterior and marginal highest posterior density credible intervals (CI). The  $S_8$  constraints are improved by a factor of 40% over cosmic shear alone and are in excellent agreement with the KiDS-1000  $3 \times 2$ pt analysis of Heymans et al. (2021). This improvement is driven by the breaking of the residual degeneracy between  $S_8$  and  $\Omega_m$ , since  $S_8$  does not optimally capture the direction orthogonal to the  $\sigma_8$ - $\Omega_m$  degeneracy for the estimator considered here. Using instead  $\Sigma_8^{0.58}$ , as in Asgari et al. (2021), which is better constrained than  $S_8$  by the pseudo- $C_\ell$  estimator, we find a 15% improvement of the constraining power of the shear-tSZ + cosmic shear joint analysis over cosmic shear alone.

The joint analysis also strongly tightens the constraints on  $\Omega_m$  and  $\sigma_8$ . This is to be expected, however, since the cosmic shear constraints on these parameters are prior-dominated, and any breaking of the ‘cosmic banana’ will yield comparatively tight constraints compared to cosmic shear alone (see, e.g., Tröster et al. 2021, for examples of this effect in the joint analyses of KiDS-1000 cosmic shear with CMB lensing or super novae).

The shear-tSZ cross-correlation prefers lower values of  $\sigma_8$  than those inferred from the CMB by *Planck*; the discrepancy between our inferred value of  $\Sigma_8^{0.2}$  and that of Planck Collaboration VI et al. (2020; using the TTTEEE+lowE likelihood) is  $2.2\sigma$ . This trend is also seen in the recent shear-tSZ cross-correlation analysis with DES Y3 data (Gatti et al. 2021), although they impose *Planck* priors on  $\sigma_8$  and  $\Omega_m$ , making a direct comparison with the results in this work difficult. The constraints on  $S_8$  and



**Fig. 5.** Measured angular power spectra of KiDS-1000 cosmic shear (bottom left) and the angular cross-power spectra between KiDS-1000 shear and the tSZ effect (top right). Shown here is the cross-correlation using the MILCA *Planck* Compton- $y$  map. The grey bands indicate the 68th and 95th percentile of the posterior predictive distribution of the joint-analysis posterior. Coloured lines are samples of the translated posterior distribution, with the colour corresponding to the baryon feedback strength.

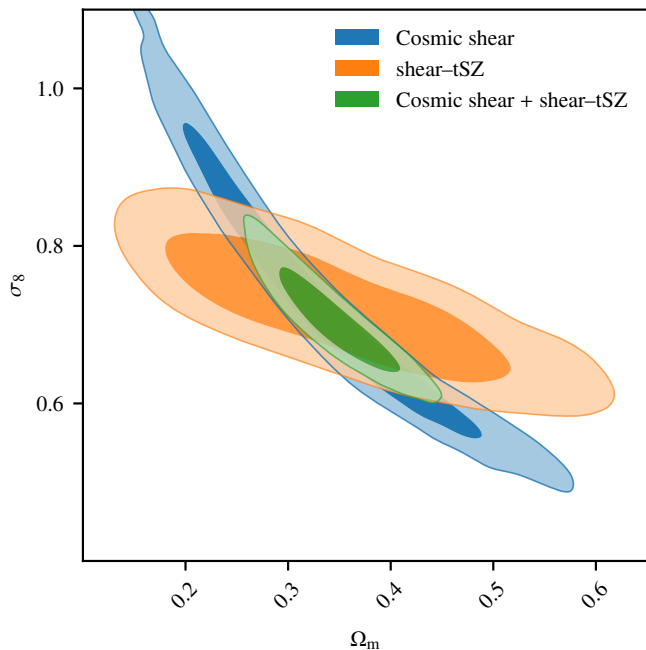
$\Sigma_8^{0.58}$  inferred from the joint analysis are in  $3.4\sigma$  and  $2.9\sigma$  tension with those of *Planck*, similar to previous joint analyses of KiDS-1000 with other data sets (Heymans et al. 2021; Tröster et al. 2021), as well as KiDS-1000 cosmic shear by itself (Asgari et al. 2021). The full parameter-space constraints are shown in Fig. C.1.

We note here that the considerable challenges of the accurate and consistent modelling of the cross-correlation signal warrant revisiting these results in the future, when the modelling has matured and more data have become available. In particular, accounting for the dependencies of, and interactions between, cosmology, baryon feedback, and intrinsic alignment requires both models that consistently include these effects and simulations

that sufficiently cover this parameter space to validate said models. These points are further discussed in Sect. 4.3.

#### 4.1. Goodness of fit

We find that the data is well-described by our model. The  $\chi^2$  of the pseudo- $C_\ell$  cosmic shear data with respect to the model of the maximum a posteriori (MAP) estimate is 150.7, with 117.1 effective degrees of freedom. The effective model dimensionality is estimated following Raveri & Hu (2019), and accounts for the fact that many of the varied parameters in the model are prior-dominated and as such do not contribute extra degrees of freedom to the model. Our fiducial shear-tSZ cross-correlation has a  $\chi^2$  of 28.0, with 36.2 effective degrees of freedom, while



**Fig. 6.** Constraints from KiDS-1000 cosmic shear (blue), the cross-correlation of shear and the tSZ effect from *Planck* (orange), and their joint analysis (green) on  $\Omega_m$  and  $\sigma_8$ .

the joint analysis has a  $\chi^2$  of 179.3, with 155.4 effective degrees of freedom. The goodness of fit values of our measurements are summarised in Table 2.

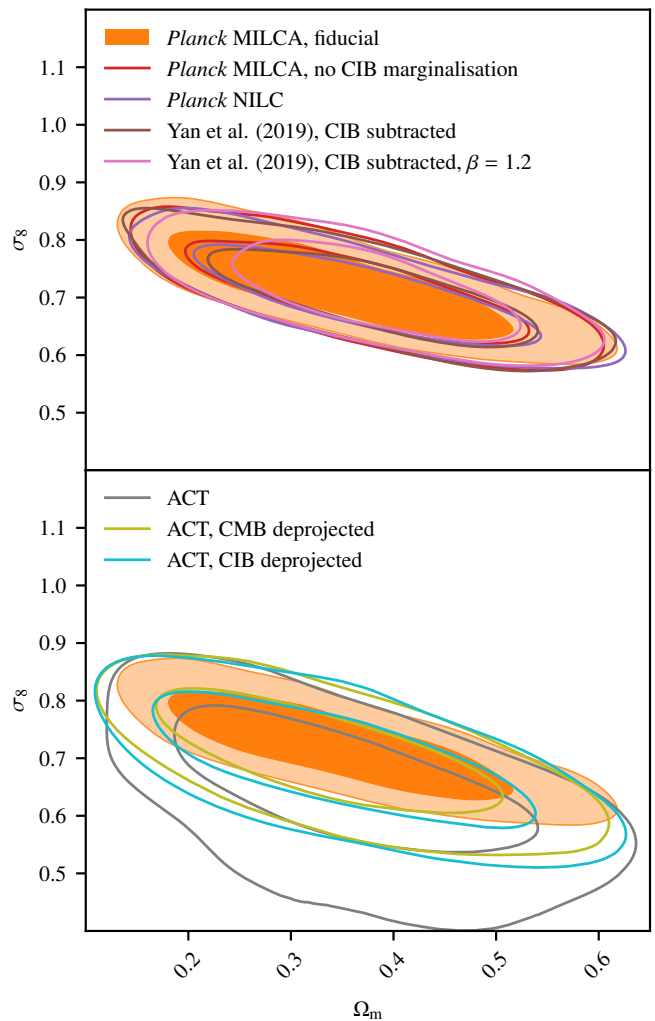
#### 4.2. Alternative Compton-y maps and effect of the CIB

To assess the degree to which y-map reconstruction and CIB contamination treatment affect our results, we derive constraints using a range of Compton-y maps and compare the resulting  $\Omega_m$ - $\sigma_8$  and  $\Sigma_8^{0.2}$  constraints to those derived based on our fiducial setup, consisting of the *Planck* MILCA y-map and CIB marginalisation using the GP model described in Sect. 3.4.3. The  $\Omega_m$ - $\sigma_8$  constraints based on the other Compton y-maps are shown in Fig. 7. The constraints on  $\Sigma_8^{0.2}$  are compared in Fig. 8.

The *Planck*-derived maps yield tighter constraints than those from ACT, owing to the larger overlap between the KiDS-1000 and *Planck* data. Among the ACT maps, we find that the y-map where no other component has been deprojected leads to weaker constraints, with a tail to low values of  $\Sigma_8^{0.2}$ . Both the CMB-deprojected and CIB-deprojected y-map give very similar constraints, with no systematic shift between them. If the cross-correlation was significantly affected by CIB contamination, we would expect to find different constraints in these two cases.

We find good agreement between all maps and no evidence that the CIB causes significant biases in our constraints. This is in contrast to the finding in Gatti et al. (2021), who find that deprojecting a grey body spectrum during the construction of their *Planck*-derived Compton-y map leads to significantly different cross-correlation signals compared to the case where no such deprojection was applied. The origin of this discrepancy is currently unknown, however, and will require a detailed comparison of the different Compton-y maps. We leave this for future work.

The mask of our Compton-y maps is potentially correlated with the lensing signal, as the point source mask includes some



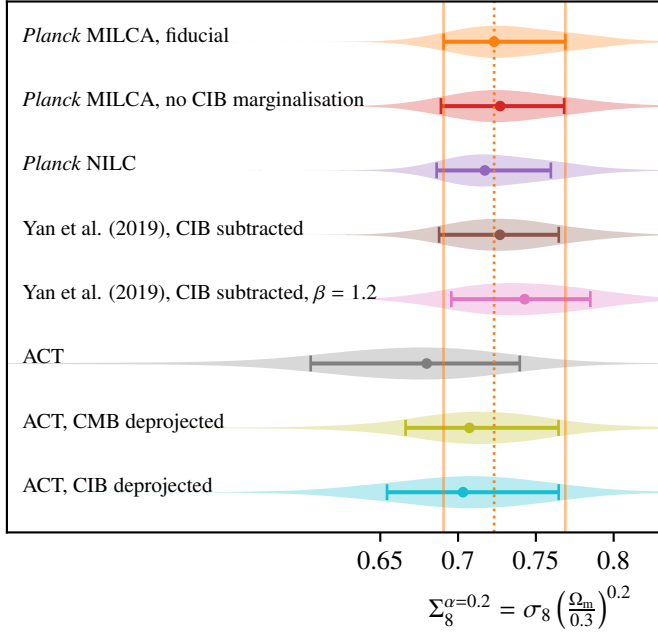
**Fig. 7.** Effect of different Compton-y map reconstruction methods on the shear-tSZ cross-correlation constraints on  $\Omega_m$  and  $\sigma_8$ . *Top:* Compton y-maps derived from *Planck* data. *Bottom:* Compton-y maps from ACT.

clusters. Since these clusters are sources of both tSZ and weak lensing signals, this could in principle cause the estimated signal to be biased low. As the number of masked point sources in the KiDS-1000 footprint is low, this effect is likely not relevant in our case.

#### 4.3. Baryon feedback

A key goal of this analysis has been to constrain baryonic feedback through the gas physics probed by the tSZ effect. In our model, the effect of baryonic feedback, specifically AGN feedback, is parameterised by the parameter  $\log_{10}(T_{\text{AGN}}/\text{K})$ . The fiducial BAHAMAS model assumes  $\log_{10}(T_{\text{AGN}}/\text{K}) = 7.8$ , since this value reproduces the observed present-day galaxy stellar mass function and the hot gas mass fractions of groups and clusters in the simulations (McCarthy et al. 2017). The constraints on this parameter, as inferred from cosmic shear alone, the shear-tSZ cross-correlation, and the joint analysis are shown in Fig. 9. While the KiDS-1000 cosmic shear bandpower and pseudo- $C_\ell$  data by themselves have weak preference for low feedback strength (Asgari et al. 2021; Tröster et al. 2021), the shear-tSZ





**Fig. 8.** Marginal posterior densities of  $\Sigma_8^{0.2} = \sigma_8 (\Omega_m/0.3)^{0.2}$  from the cross-correlation of KiDS and different Compton- $y$  maps. The orange band and dashed line indicate the marginal 68th percentile CI and mode of the marginal posterior of the fiducial setup.

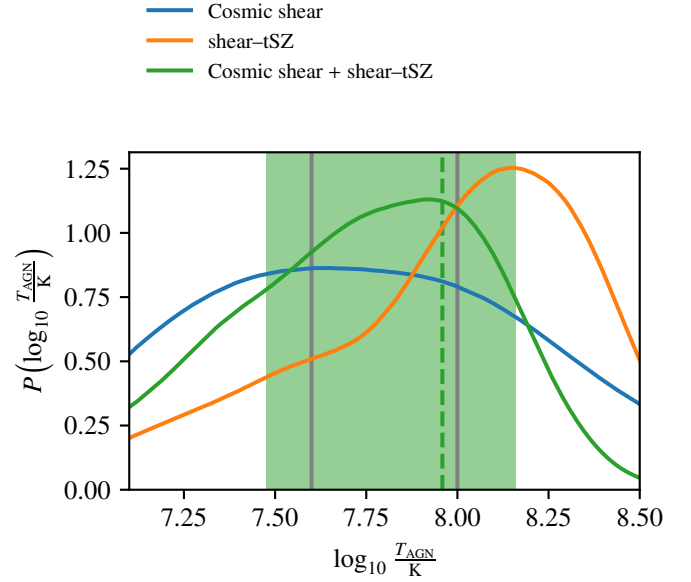
cross-correlation data prefer strong feedback. For the joint analysis we find

$$\log_{10} \left( \frac{T_{\text{AGN}}}{\text{K}} \right) = 7.96_{-0.48}^{+0.2}, \quad (13)$$

in good agreement with the BAHAMAS model. We note that this constraint does not strictly pass the criterion of [Asgari et al. \(2021\)](#) for a parameter to count as constrained by the data: the marginal posterior density at the (lower) prior edge is not less than 13 % of the posterior density at the marginal mode.

This result should be interpreted with caution, however. The model for the matter and electron pressure power spectra underlying our analysis, HMX, is calibrated against the BAHAMAS suite of hydrodynamical simulations. The range of feedback strength considered in BAHAMAS ranges from 7.6 to 8.0, indicated by the grey band in Fig. 9, and is chosen such that the simulations reproduce the observed galaxy stellar mass function and gas fraction in groups and clusters. Outside of this range the model extrapolates from the simulations it is calibrated on. While the physical nature of the model makes this extrapolation viable to a certain degree, there is significant modelling uncertainty at the edges of the  $\log_{10}(T_{\text{AGN}}/\text{K}) \sim U(7.1, 8.5)$  prior we use in our inference pipeline. Furthermore, the fitting of the HMX model parameters and their relation to  $\log_{10}(T_{\text{AGN}}/\text{K})$  is done at a single, fixed cosmology. It has been shown that the effects of cosmology and galaxy formation are largely independent (e.g., [van Daalen et al. 2011](#); [Mummery et al. 2017](#); [van Daalen et al. 2020](#); [Pfeifer et al. 2020](#)). Residual interplay between feedback parameters and cosmology, for example through the baryon fraction, can affect the inferred values of  $\log_{10}(T_{\text{AGN}}/\text{K})$  to a small degree, however ([Mead et al. 2021](#)).

The shear-tSZ cross-correlations using the ACT maps do not constrain  $\log_{10}(T_{\text{AGN}}/\text{K})$ . This can be attributed to the generally



**Fig. 9.** Marginal posterior densities of the baryon feedback strength, parameterised by  $\log_{10}(T_{\text{AGN}}/\text{K})$ . The green band and dashed line indicate the 68th percentile marginal CI and MAP, respectively, of the joint analysis of cosmic shear and the shear-tSZ cross-correlation. The grey lines indicate the range of the feedback strength implemented in the BAHAMAS suite of hydrodynamical simulations, which our HMX model is calibrated on.

weaker constraints of the ACT maps due to the much smaller overlap with the KiDS-1000 data and the associated statistical scatter.

While the shear-tSZ cross-correlation by itself prefers strong feedback, the joint constraints on the feedback parameter agree with the BAHAMAS model. This shift in the preferred feedback strength is due to the interaction of IA and baryon feedback: both have the effect of a broadband suppression of the shear-tSZ cross-power spectra, such that high IA amplitudes can be compensated to a certain degree by weak baryon feedback. The joint analysis with cosmic shear restricts the range of allowed IA amplitudes, excluding the parts of parameter space with strong feedback. The IA model used in this analysis is quite simplistic, and the HMX model is getting extrapolated to feedback strengths outside the range it is calibrated on. To better understand this IA-baryon feedback interaction, especially away from their fiducial parameters, a more holistic model is required, for example through including the halo-model IA formalism of [Fortuna et al. \(2021\)](#) in HMX, as well as expanding the calibration set of hydrodynamical simulations.

One might have expected the shear-tSZ cross-correlation to yield tighter constraints on baryon feedback, since it is sensitive to both the effect of AGN feedback on gas physics and its suppression of the matter power spectrum. At large scales,  $k \lesssim 0.3 h\text{Mpc}^{-1}$ , stronger feedback increases the matter-electron pressure cross-power spectrum due to heating of the warm-hot intergalactic medium. These scales are largely outside of our scale cuts of  $\ell \in (100, 1500)$ , however. At small scales,  $k \gtrsim 0.3 h\text{Mpc}^{-1}$ , increasing the feedback strength suppresses the matter-electron pressure cross-power spectrum (see figure 9 in [Mead et al. 2020](#)). For the scales considered in this analysis, the effect of AGN feedback is thus largely restricted to a suppression of the angular cross-power spectrum over a large range of multi-

**Table 2.** Goodness-of-fit of our measurements.

Data	$\chi^2_{\text{MAP}}$	$N_{\text{data}}$	$N_{\text{dof,eff}}$	PTE
pseudo- $C_\ell$ cosmic shear	150.7	120	117.1	0.02
shear-tSZ	28.0	40	36.2	0.83
Cosmic shear + shear-tSZ	179.3	160	155.4	0.09

**Notes.** We list the  $\chi^2$  value at the maximum of the posterior, the size of the data vector, the effective number of degrees of freedom, and the probability to exceed (PTE) the measured  $\chi^2$  value.

poles, similar to its effect on cosmic shear. This is illustrated in Fig. 5, where the colouring of the samples of the TPD indicates the effect of  $\log_{10}(T_{\text{AGN}}/\text{K})$  on the model prediction: except at scales of  $\ell \sim 100$ , the effect of  $\log_{10}(T_{\text{AGN}}/\text{K})$  is limited to a suppression of the angular power spectra. Conversely, ongoing and future large-area surveys, such as DES Y3, LSST, or *Euclid*, have access to larger angular scales and thus could make use of the different behaviour at small and large scales to derive tighter constraints on baryon feedback.

## 5. Conclusion

We conduct a pseudo- $C_\ell$  cosmic shear analysis of the KiDS-1000 weak gravitational lensing data and find excellent agreement with previous KiDS-1000 angular power spectrum analyses (Asgari et al. 2021; Loureiro et al. in prep.). We then measure the cross-correlation of KiDS-1000 weak lensing and the tSZ effect, detecting the cross-correlation at  $9.4\sigma$  significance.

Using the HMX model, which allows for the consistent modelling of both cosmic shear and the shear-tSZ cross-correlation – including the effect of baryon feedback – we derive constraints on cosmology and the baryon feedback parameter from the shear-tSZ cross-correlation. While the inferred value of the amplitude of the shear-tSZ signal, as parameterised by  $\Sigma_8^{0.2}$ , is fully consistent with other KiDS analyses, it is low by  $2.2\sigma$  compared to CMB constraints from *Planck*. Finally, we conduct a joint analysis of our cosmic shear and shear-tSZ cross-correlation data, taking into account the full cross-covariance between these data vectors. By breaking degeneracies, the inferred cosmological parameter constraints of the joint analysis are tighter than those of either probe by itself. For example, the constraints on  $S_8$  of the joint analysis improve by 40% over cosmic shear by itself. We find that our cross-correlation data prefer strong baryon feedback, while we infer  $\log_{10}(T_{\text{AGN}}/\text{K}) = 7.96^{+0.2}_{-0.48}$  from the joint analysis, consistent with the BAHAMAS hydrodynamical simulations. Unlike recent work by Gatti et al. (2021) on shear-tSZ cross-correlation using DES Y3 data, we find no evidence of significant CIB contamination in our *Planck*-derived Compton-y maps.

While the analysis presented here demonstrates the power of shear-tSZ cross-correlations and their joint analyses with cosmic shear to constrain both cosmology and baryonic processes of galaxy formation, there are still significant challenges in the detailed interpretation of these results. The modelling of the non-linear matter spectrum to the accuracies required by current and future weak lensing surveys is already a challenging proposition. Accounting for the electron pressure field required to predict the tSZ effect adds a further level of complexity to the modelling framework. While the consistent modelling of various probes in HMX is a significant improvement on earlier works that treat the profiles of different components as independent, its current

accuracy for matter–electron pressure power spectrum is limited at the 15 percent level and will need to be improved for future high-precision measurements, for example through the inclusion of non-linear halo biasing in the core halo model (Mead & Verde 2021).

If these challenges can be overcome, the joint analysis of weak lensing from forthcoming galaxy surveys such as LSST and *Euclid* with low-noise and high-resolution measurements of the tSZ effect from future CMB experiments, such as the Simons Observatory (Ade et al. 2019), can be used to extract more information on galaxy formation processes and cosmology from these data sets than when analysed independently. Another avenue would be to combine the measurements considered here with other data sets. The combination of weak lensing, the clustering of galaxies, and their cross-correlations into ‘ $3 \times 2$ pt’ analyses has provided some of the tightest constraints on cosmology from the low-redshift Universe (e.g., DES Collaboration et al. 2018; Heymans et al. 2021; DES Collaboration et al. 2021). A lensing-tSZ  $3 \times 2$ pt analysis, through inclusion of the tSZ auto-correlation in the measurements considered in this work, would thus be a logical next step and build on previous work of joint analyses of the tSZ auto-power spectrum and lensing (Osato et al. 2020; Makiya et al. 2020). Beyond the shear-tSZ cross-correlation considered in this work, cross-correlations of galaxies with both the tSZ and the kinetic Sunyaev-Zeldovich effect have been shown to be a potent probe of the thermodynamics of haloes (e.g., Battaglia et al. 2017; Schaan et al. 2021; Amodeo et al. 2021). Adding these various SZ-effect cross-correlations into the framework of  $3 \times 2$ pt analyses could therefore improve the constraining power of the data that is already available.

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## References

- Ade, P., Aguirre, J., Ahmed, Z., et al. 2019, *J. Cosmology Astropart. Phys.*, 2019, 056
- Alam, S., Aubert, M., Avila, S., et al. 2021, *Phys. Rev. D*, 103, 083533
- Alonso, D., Hill, J. C., Hložek, R., & Spergel, D. N. 2018, *Phys. Rev. D*, 97, 063514

- Alonso, D., Sanchez, J., Slosar, A., & LSST Dark Energy Science Collaboration. 2019, MNRAS, 484, 4127
- Amodeo, S., Battaglia, N., Schaen, E., et al. 2021, Phys. Rev. D, 103, 063514
- Angulo, R. E., Zennaro, M., Contreras, S., et al. 2021, MNRAS[arXiv:2004.06245]
- Arnaud, M., Pratt, G. W., Piffaretti, R., et al. 2010, A&A, 517, A92
- Asgari, M., Lin, C.-A., Joachimi, B., et al. 2021, A&A, 645, A104
- Barreira, A., Krause, E., & Schmidt, F. 2018, J. Cosmology Astropart. Phys., 2018, 053
- Battaglia, N., Ferraro, S., Schaen, E., & Spergel, D. N. 2017, J. Cosmology Astropart. Phys., 2017, 040
- Becker, M. R. & Rozo, E. 2016, MNRAS, 457, 304
- Bolliet, B., Comis, B., Komatsu, E., & Macías-Pérez, J. F. 2018, MNRAS, 477, 4957
- Bonilla, E. V., Chai, K., & Williams, C. 2008, in Advances in Neural Information Processing Systems, ed. J. Platt, D. Koller, Y. Singer, & S. Roweis, Vol. 20 (Curran Associates, Inc.)
- Bridle, S. & King, L. 2007, New Journal of Physics, 9, 444
- Bridle, S. L., Crittenden, R., Melchiorri, A., et al. 2002, MNRAS, 335, 1193
- Cataneo, M., Lombriser, L., Heymans, C., et al. 2019, MNRAS, 488, 2121
- Chiang, Y.-K., Makiya, R., Ménard, B., & Komatsu, E. 2020, ApJ, 902, 56
- Chisari, N. E., Alonso, D., Krause, E., et al. 2019a, ApJS, 242, 2
- Chisari, N. E., Mead, A. J., Joudaki, S., et al. 2019b, The Open Journal of Astrophysics, 2, 4
- Chon, G., Challinor, A., Prunet, S., Hivon, E., & Szapudi, I. 2004, MNRAS, 350, 914
- Cooray, A. 2001, Phys. Rev. D, 64, 063514
- Cooray, A. & Sheth, R. 2002, Physics Reports, 372, 1
- de Graaff, A., Cai, Y.-C., Heymans, C., & Peacock, J. A. 2019, A&A, 624, A48
- DES Collaboration, Abbott, T. M. C., Abdalla, F. B., et al. 2018, Phys. Rev. D, 98, 043526
- DES Collaboration, Abbott, T. M. C., Aguena, M., et al. 2021, arXiv e-prints [arXiv:2105.13549]
- Doux, C., Baxter, E., Lemos, P., et al. 2021, MNRAS, 503, 2688
- Euclid Collaboration: Knabenhans, M., Stadel, J., Potter, D., et al. 2021, MNRAS, 505, 2840
- Fedeli, C., Semboloni, E., Velliscig, M., et al. 2014, J. Cosmology Astropart. Phys., 8, 28
- Feroz, F. & Hobson, M. P. 2008, MNRAS, 384, 449
- Feroz, F., Hobson, M. P., & Bridges, M. 2009, MNRAS, 398, 1601
- Feroz, F., Hobson, M. P., Cameron, E., & Pettitt, A. N. 2013, arXiv e-prints [arXiv:1306.2144]
- Foreman, S., Becker, M. R., & Wechsler, R. H. 2016, MNRAS, 463, 3326
- Fortuna, M. C., Hoekstra, H., Joachimi, B., et al. 2021, MNRAS, 501, 2983
- García-García, C., Alonso, D., & Bellini, E. 2019, J. Cosmology Astropart. Phys., 2019, 043
- Gardner, S., Pleiss, G., Weinberger, K. Q., Bindel, D., & Wilson, A. G. 2018, in Advances in Neural Information Processing Systems, ed. S. Bengio, H. Wallach, H. Larochelle, K. Grauman, N. Cesa-Bianchi, & R. Garnett, Vol. 31 (Curran Associates, Inc.)
- Gatti, M., Pandey, S., Baxter, E., et al. 2021, arXiv e-prints [arXiv:2108.01600]
- Gelman, A. et al. 2013, Bayesian data analysis, third edition. edn., Chapman & Hall, CRC texts in statistical science (Boca Raton, Fla.: CRC Press)
- Giblin, B., Heymans, C., Asgari, M., et al. 2021, A&A, 645, A105
- Górski, K. M., Hivon, E., Banday, A. J., et al. 2005, ApJ, 622, 759
- Hamana, T., Shirasaki, M., Miyazaki, S., et al. 2020, PASJ, 72, 16
- Harnois-Déraps, J., van Waerbeke, L., Viola, M., & Heymans, C. 2015, MNRAS, 450, 1212
- Heitmann, K., White, M., Wagner, C., Habib, S., & Higdon, D. 2010, ApJ, 715, 104
- Heymans, C., Tröster, T., Asgari, M., et al. 2021, A&A, 646, A140
- Hikage, C., Oguri, M., Hamana, T., et al. 2019, PASJ, 71, 43
- Hildebrandt, H., van den Busch, J. L., Wright, A. H., et al. 2021, A&A, 647, A124
- Hill, J. C. & Spergel, D. N. 2014, J. Cosmology Astropart. Phys., 2, 030
- Hirata, C. M. & Seljak, U. 2004, Phys. Rev. D, 70, 063526
- Hivon, E., Górski, K. M., Netterfield, C. B., et al. 2002, ApJ, 567, 2
- Hojjati, A., Tröster, T., Harnois-Déraps, J., et al. 2017, MNRAS, 471, 1565
- Horowitz, B. & Seljak, U. 2017, MNRAS, 469, 394
- Huang, H.-J., Eifler, T., Mandelbaum, R., et al. 2021, MNRAS, 502, 6010
- Hunter, J. D. 2007, Computing in Science & Engineering, 9, 90
- Hurier, G. 2015, A&A, 575, L11
- Hurier, G., Macías-Pérez, J. F., & Hildebrandt, S. 2013, A&A, 558, A118
- Ivezić, Ž., Kahn, S. M., Tyson, J. A., et al. 2019, ApJ, 873, 111
- Joachimi, B., Lin, C. A., Asgari, M., et al. 2021, A&A, 646, A129
- Jones, E., Oliphant, T., Peterson, P., et al. 2001, SciPy: Open source scientific tools for Python
- Kaiser, N. 1992, ApJ, 388, 272
- Kannawadi, A., Hoekstra, H., Miller, L., et al. 2019, A&A, 624, A92
- Kilbinger, M., Heymans, C., Asgari, M., et al. 2017, MNRAS, 472, 2126
- Köhlinger, F., Joachimi, B., Asgari, M., et al. 2019, MNRAS, 484, 3126
- Komatsu, E. & Seljak, U. 2002, MNRAS, 336, 1256
- Koukoufilippas, N., Alonso, D., Bilicki, M., & Peacock, J. A. 2020, MNRAS, 491, 5464
- Kuijken, K., Heymans, C., Dvornik, A., et al. 2019, A&A, 625, A2
- Laureijs, R., Amiaux, J., Arduini, S., et al. 2011, arXiv e-prints [arXiv:1110.3193]
- Lawrence, E., Heitmann, K., Kwan, J., et al. 2017, ApJ, 847, 50
- Lenz, D., Doré, O., & Lagache, G. 2019, ApJ, 883, 75
- Lewis, A. 2019, arXiv e-prints [arXiv:1910.13970]
- Lewis, A., Challinor, A., & Lasenby, A. 2000, ApJ, 538, 473
- Li, Y., Hu, W., & Takada, M. 2014, Phys. Rev. D, 89, 083519
- Loureiro, A. et al. in prep.
- LoVerde, M. & Afshordi, N. 2008, Phys. Rev. D, 78, 123506
- Ma, Y.-Z., Van Waerbeke, L., Hinshaw, G., et al. 2015, J. Cosmology Astropart. Phys., 9, 046
- MacCrann, N., Aleksić, J., Amara, A., et al. 2017, MNRAS, 465, 2567
- Madhavacheril, M. S., Hill, J. C., Naess, S., et al. 2020, Phys. Rev. D, 102, 023534
- Makiya, R., Ando, S., & Komatsu, E. 2018, MNRAS, 480, 3928
- Makiya, R., Hikage, C., & Komatsu, E. 2020, PASJ, 72, 26
- Mallaby-Kay, M., Atkins, Z., Aiola, S., et al. 2021, ApJS, 255, 11
- McCarthy, I. G., Schaye, J., Bird, S., & Le Brun, A. M. C. 2017, MNRAS, 465, 2936
- Mead, A. J., Brieden, S., Tröster, T., & Heymans, C. 2021, MNRAS, 502, 1401
- Mead, A. J., Heymans, C., Lombriser, L., et al. 2016, MNRAS, 459, 1468
- Mead, A. J., Tröster, T., Heymans, C., Van Waerbeke, L., & McCarthy, I. G. 2020, A&A, 641, A130
- Mead, A. J. & Verde, L. 2021, MNRAS, 503, 3095
- Miller, L., Heymans, C., Kitching, T. D., et al. 2013, MNRAS, 429, 2858
- Mitchell, M. A., Arnold, C., Hernández-Aguayo, C., & Li, B. 2021, MNRAS, 501, 4565
- Mummery, B. O., McCarthy, I. G., Bird, S., & Schaye, J. 2017, MNRAS, 471, 227
- Navarro, J. F., Frenk, C. S., & White, S. D. M. 1997, ApJ, 490, 493
- Nelder, J. A. & Mead, R. 1965, The computer journal, 7, 308
- Nicola, A., García-García, C., Alonso, D., et al. 2021, J. Cosmology Astropart. Phys., 2021, 067
- Oliphant, T. E. 2006, A guide to NumPy, Vol. 1 (Trelgol Publishing USA)
- Osato, K., Shirasaki, M., Miyatake, H., et al. 2020, MNRAS, 492, 4780
- Osato, K. & Takada, M. 2021, Phys. Rev. D, 103, 063501
- Pandey, S., Baxter, E. J., Xu, Z., et al. 2019, Phys. Rev. D, 100, 063519
- Pandey, S., Gatti, M., Baxter, E., et al. 2021, arXiv e-prints [arXiv:2108.01601]
- Pfeifer, S., McCarthy, I. G., Stafford, S. G., et al. 2020, MNRAS, 498, 1576
- Planck Collaboration VI, Aghanim, N., Akrami, Y., et al. 2020, A&A, 641, A6
- Planck Collaboration XLVIII, Aghanim, N., Ashdown, M., et al. 2016, A&A, 596, A109
- Planck Collaboration XXII, Aghanim, N., Arnaud, M., et al. 2016, A&A, 594, A22
- Planck Collaboration XXIII, Ade, P. A. R., Aghanim, N., et al. 2016, A&A, 594, A23
- Planck Collaboration XXVI, Ade, P. A. R., Aghanim, N., et al. 2016, A&A, 594, A26
- Planck Collaboration XXX, Ade, P. A. R., Aghanim, N., et al. 2014, A&A, 571, A30
- Raveri, M. & Hu, W. 2019, Phys. Rev. D, 99, 043506
- Refregier, A. & Teyssier, R. 2002, Phys. Rev. D, 66, 043002
- Remazeilles, M., Delabrouille, J., & Cardoso, J.-F. 2011, MNRAS, 410, 2481
- Schaen, E., Ferraro, S., Amodeo, S., et al. 2021, Phys. Rev. D, 103, 063513
- Schaye, J., Dalla Vecchia, C., Booth, C. M., et al. 2010, MNRAS, 402, 1536
- Schneider, P., van Waerbeke, L., Kilbinger, M., & Mellier, Y. 2002, A&A, 396, 1
- Shirasaki, M. 2019, MNRAS, 483, 342
- Smith, R. E., Reed, D. S., Potter, D., et al. 2014, MNRAS, 440, 249
- Spergel, D., Gehrels, N., Baltay, C., et al. 2015, arXiv e-prints [arXiv:1503.03757]
- Springel, V. 2010, MNRAS, 401, 791
- Stein, G., Alvarez, M. A., Bond, J. R., van Engelen, A., & Battaglia, N. 2020, J. Cosmology Astropart. Phys., 2020, 012
- Sunyaev, R. A. & Zeldovich, Y. B. 1972, Comments on Astrophysics and Space Physics, 4
- Szapudi, I., Prunet, S., Pogossyan, D., Szalay, A. S., & Bond, J. R. 2001, ApJ, 548, L115
- Takahashi, R., Sato, M., Nishimichi, T., Taruya, A., & Oguri, M. 2012, ApJ, 761, 152
- Tanimura, H., Hinshaw, G., McCarthy, I. G., et al. 2019, MNRAS, 483, 223
- Tanimura, H., Hinshaw, G., McCarthy, I. G., et al. 2020, MNRAS, 491, 2318
- Tinker, J. L., Weinberg, D. H., Zheng, Z., & Zehavi, I. 2005, ApJ, 631, 41
- Tröster, T., Asgari, M., Blake, C., et al. 2021, A&A, 649, A88



- Tröster, T., Camera, S., Fornasa, M., et al. 2017, *MNRAS*, 467, 2706
- Tröster, T., Ferguson, C., Harnois-Déraps, J., & McCarthy, I. G. 2019, *MNRAS*, 487, L24
- Valageas, P. & Nishimichi, T. 2011, *A&A*, 527, A87
- van Daalen, M. P., McCarthy, I. G., & Schaye, J. 2020, *MNRAS*, 491, 2424
- van Daalen, M. P., Schaye, J., Booth, C. M., & Dalla Vecchia, C. 2011, *MNRAS*, 415, 3649
- van Uitert, E., Joachimi, B., Joudaki, S., et al. 2018, *MNRAS*, 476, 4662
- van Waerbeke, L., Hinshaw, G., & Murray, N. 2014, *Phys. Rev. D*, 89, 023508
- Viero, M. P., Wang, L., Zemcov, M., et al. 2013, *ApJ*, 772, 77
- Vikram, V., Lidz, A., & Jain, B. 2017, *MNRAS*, 467, 2315
- Wright, A. H., Hildebrandt, H., van den Busch, J. L., & Heymans, C. 2020a, *A&A*, 637, A100
- Wright, A. H., Hildebrandt, H., van den Busch, J. L., et al. 2020b, *A&A*, 640, L14
- Xia, Q., Robertson, N., Heymans, C., et al. 2020, *A&A*, 633, A89
- Yan, Z., Hojjati, A., Tröster, T., Hinshaw, G., & van Waerbeke, L. 2019, *ApJ*, 884, 139
- Yan, Z., van Waerbeke, L., Tröster, T., et al. 2021, *A&A*, 651, A76
- Yoon, M. & Jee, M. J. 2021, *ApJ*, 908, 13
- Zuntz, J., Paterno, M., Jennings, E., et al. 2015, *Astronomy and Computing*, 12, 45

## Appendix A: $B$ -modes

Figure A.1 presents the  $B$ -modes of our measurements, which are expected to be consistent with zero in the absence of systematics. To be more specific, for cosmic shear the  $\gamma_B\gamma_B$ -component of the angular power spectra is shown, while for the shear–tSZ cross-correlation, the  $\gamma_B\gamma$  component is depicted. Both pseudo- $C_\ell$  measurements are consistent with zero, with  $\chi^2_{\gamma_B\gamma_B} = 128.3$  and  $\chi^2_{\gamma_B\gamma} = 36.5$ , for 120 and 40 degrees of freedom, respectively. This translates to PTEs of 0.29 and 0.63, which makes us confident in the robustness of our measurements. The same is true for the other  $y$ -maps considered in this work. Furthermore, the  $B$ -modes remain consistent with zero at the same level of significance when considering the whole  $\ell \in (51, 2952)$  range they were measured on, rather than the  $\ell \in (100, 1500)$  range used for parameter inference.

## Appendix B: Comparison with previous KiDS-1000 cosmic shear results

The cosmic shear analysis presented here closely follows that of Asgari et al. (2021) but differs in two aspects: the choice of angular power spectrum estimator and the modelling of baryonic feedback.

### Appendix B.1: Comparison of the bandpowers and pseudo- $C_\ell$ estimators

Different two-point statistics estimators can give slightly different results (e.g., Hikage et al. 2019; Hamana et al. 2020; Asgari et al. 2021), as they are sensitive to different scales and are thus differently affected by statistical fluctuations in the underlying data. Here we compare our pseudo- $C_\ell$  estimates and derived cosmological constraints to those from the bandpower estimator used in Asgari et al. (2021). That bandpower estimator is based on the integral transform of the two-point correlation function (e.g., Schneider et al. 2002; Becker & Rozo 2016; Tröster et al. 2017; van Uitert et al. 2018; Joachimi et al. 2021) and has attractive properties, such as being insensitive to the footprint geometry nor requiring subtraction of the noise bias.

We find excellent agreement between the measured data vectors, illustrated in Fig. B.1. Since both are estimators for the angular power spectrum, this is to be expected to a certain degree but it is reassuring to see this level of agreement. The uncertainties differ somewhat between the estimators, likely due to differences in the details of the data covariance calculation, for example, in the treatment of the mixed term of the Gaussian contribution. The window functions for the  $EE$ -component that translate the model prediction into data-space, accounting for example for residual effects of the mode-mixing matrices and  $E/B$ -mode mixing, are shown in Fig. B.2 for the two estimators. The largest differences are at large scales, where mask effects and the finite angular range on which the correlation function were measured become important.

We derive cosmological constraints from both data vectors, taking care to homogenise the inference pipeline as much as possible. We use the same HMCode-2016 model (Mead et al. 2016) for the matter power spectrum, as well as the multiplicative shear bias values from Giblin et al. (2021) used in Asgari et al. (2021). The marginal posteriors in the  $\Omega_m$ - $S_8$  plane and for  $S_8$  are shown in Figs. B.3 and B.4, demonstrating good agreement between the two estimators. Due to differences in the way the data covariances for the two estimators are being computed, small differences in the parameter constraints are to be expected.

Our methodology differs in a more subtle manner from the pseudo- $C_\ell$  methodology of Loureiro et al. (in prep.), however, even though both approaches make use of the pseudo- $C_\ell$  formalism. In the present work the data vector has been deconvolved with the mode-mixing matrices, the mode-mixing matrices are calculated using the weight map, and we use analytic estimates for the noise bias and data covariance. On the other hand, Loureiro et al. (in prep.) forward-model the effect of the mode mixing, use a binary mask to compute the mode-mixing matrices, and estimate their noise bias and data covariance from simulated mock data.

### Appendix B.2: Impact of baryon modelling

The second significant difference between the analysis choices of the present work and Asgari et al. (2021) is in the non-linear model for the matter power spectrum. Asgari et al. (2021) used HMCode-2016 (Mead et al. 2016), which was calibrated on the OWLS suite of hydrodynamical simulations. The HMX model used here has been calibrated against the BAHAMAS suite of simulations instead. Importantly, it models gas, stars, and dark matter separately. The model therefore does not have a dark-matter-only limit, in contrast to HMCode-2016.

Figures B.3 and B.4 show the effects of the different matter power spectrum model choices, comparing the HMCode-2016 and HMX models. The comparison also includes the HMCode-2020 (Mead et al. 2021) model, which has been optimised for the modelling of the matter power spectrum. Like HMX, the baryonic feedback has been calibrated on BAHAMAS but unlike HMX, it only predicts the matter power spectrum and thus cannot model the cross-correlations considered in the present analysis. As discussed in appendix A of Tröster et al. (2021), HMCode-2020 allows for slightly higher values of  $S_8$  because the finite amount of AGN feedback in the model always causes a degree of suppression of power. The same effect can be observed for HMX, for the same reasons: the physical model for gas in the model prevents it from behaving as if it were dark matter.

## Appendix C: Other parameter constraints

Figure C.1 shows the marginal posteriors for all 13 sampled parameters in our fiducial cosmic shear, shear–tSZ, and joint analyses.

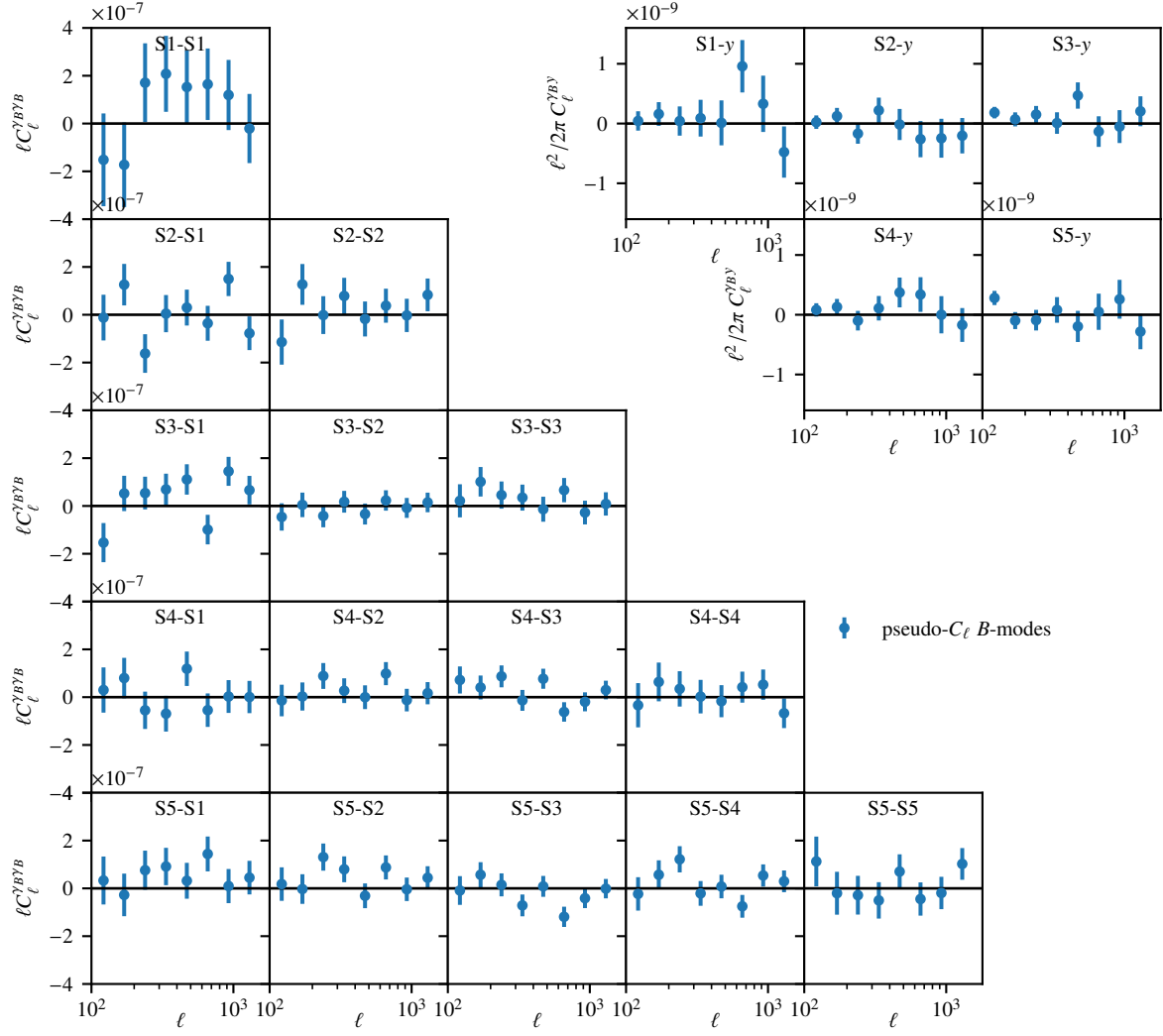
## Appendix D: PYHMCODE

We provide an easy to use and unified Python interface to HMCode and HMX, called PYHMCODE<sup>13</sup>. A usage example is shown below. It assumes a CCL cosmology object `ccl_cosmology` and arrays of the linear matter power spectrum `pofk_lin`, redshift `z`, and wave number `k` (in units of  $h\text{Mpc}^{-1}$ ) and computes the auto- and cross-power spectra between the matter and electron pressure fields.

```
import pyhmc
from pyhmc.halo_profile_utils import
    ccl2hmc_code_cosmo

# Create the pyhmc cosmology object.
hmc_code_cosmology = ccl2hmc_code_cosmo(
    ccl_cosmo=ccl_cosmology,
    pofk_lin_k_h=k,
    pofk_lin_z=z,
    pofk_lin=pofk_lin,
```

<sup>13</sup> <https://github.com/tilmantroester/pyhmc>



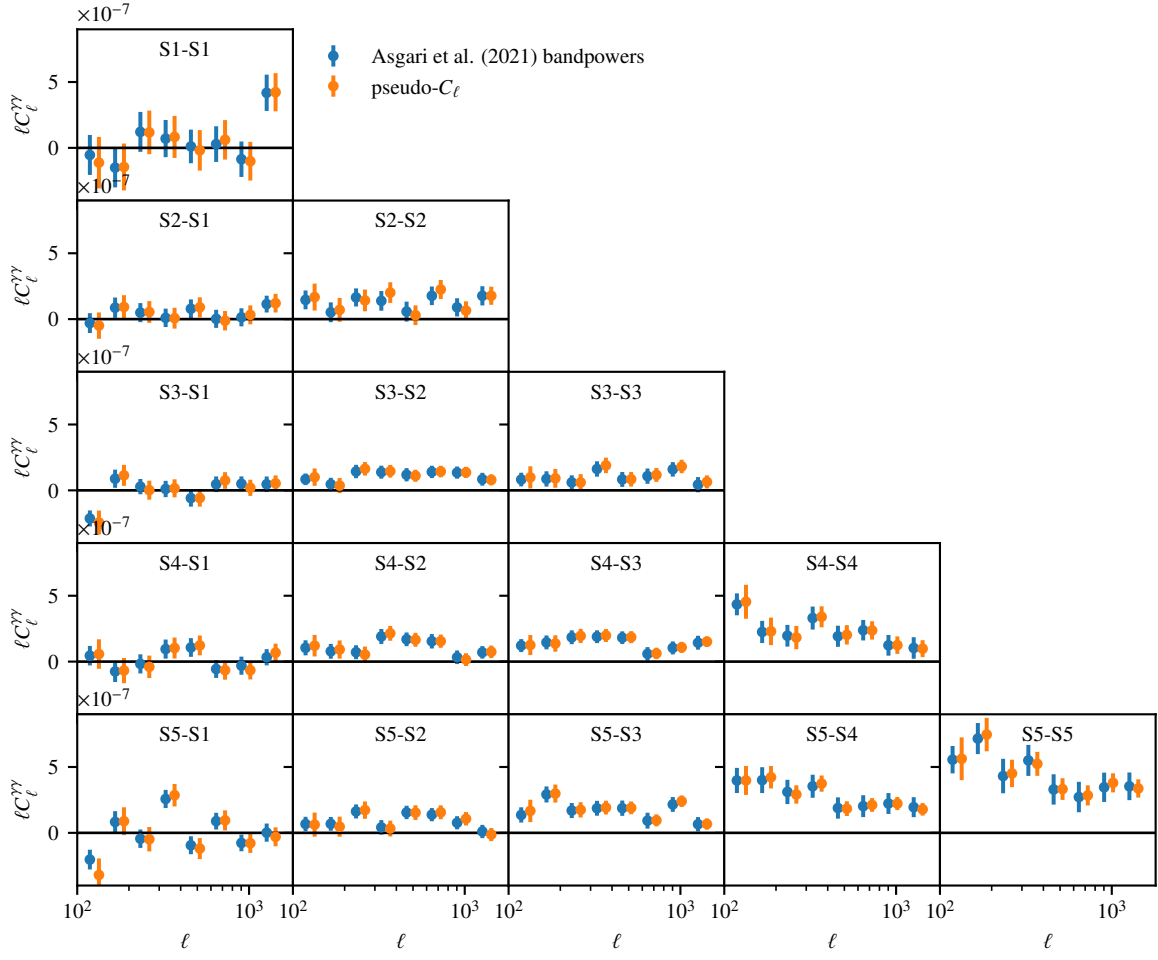
**Fig. A.1.** *B*-modes of the measurements considered in this work. The cosmic shear *BB*-component is shown on the left, for which we find  $\chi^2_{\gamma_B \gamma_B} = 128.3$ , corresponding to a PTE of 0.29. The *B*-mode of the shear–tSZ cross-correlation is shown in the upper right. It has  $\chi^2_{\gamma_B \gamma_y} = 36.5$ , for a PTE of 0.63.

```
log10_T_heat=7.8)

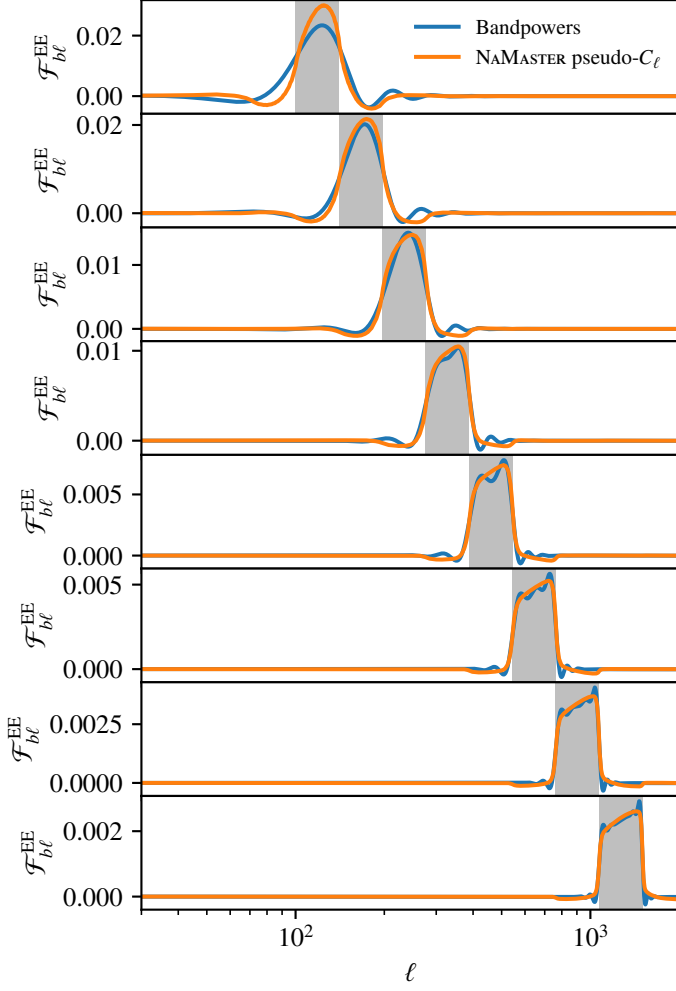
# Create the halo model object, which holds
# information on the specific halo model
# to use. E.g., the HMCode or HMX version.
hmcode_model = pyhmcode.Halomodel(
    pyhmcode.HMX2020_matter_pressure_w_temp_scaling)

# Now we can compute the non-linear power spectrum,
# given the cosmology, halo model,
# and a list of fields.
hmcode_pofk = pyhmcode.
    calculate_nonlinear_power_spectrum(
        cosmology=hmcode_cosmology,
        halomodel=hmcode_model,
        fields=[pyhmcode.field_matter,
                pyhmcode.field_electron_pressure])
```

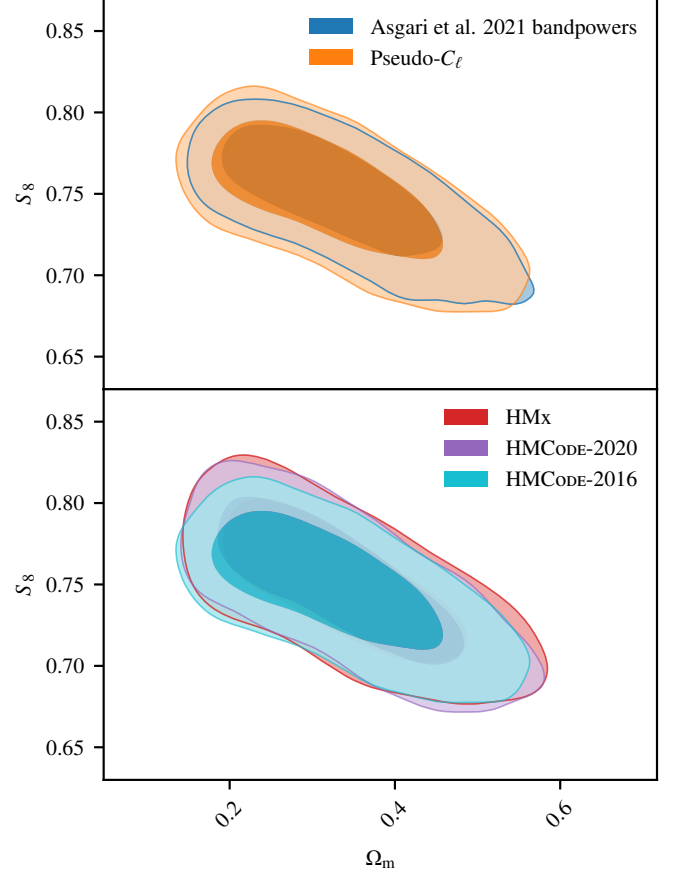




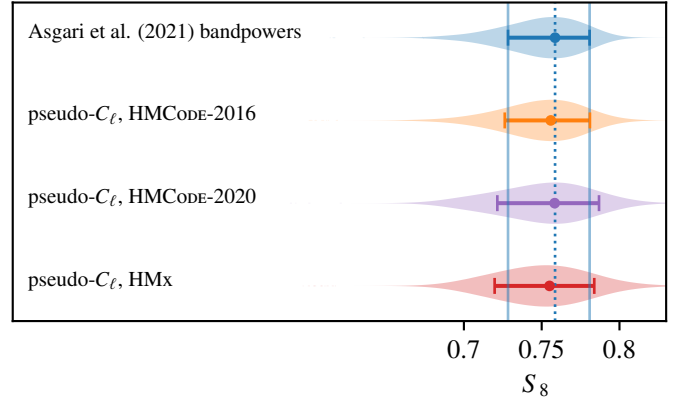
**Fig. B.1.** Comparison of KiDS-1000 angular power spectrum estimates. The pseudo- $C_\ell$  estimates used in this work are shown in orange, while the bandpower estimates of [Asgari et al. \(2021\)](#) are shown in blue.



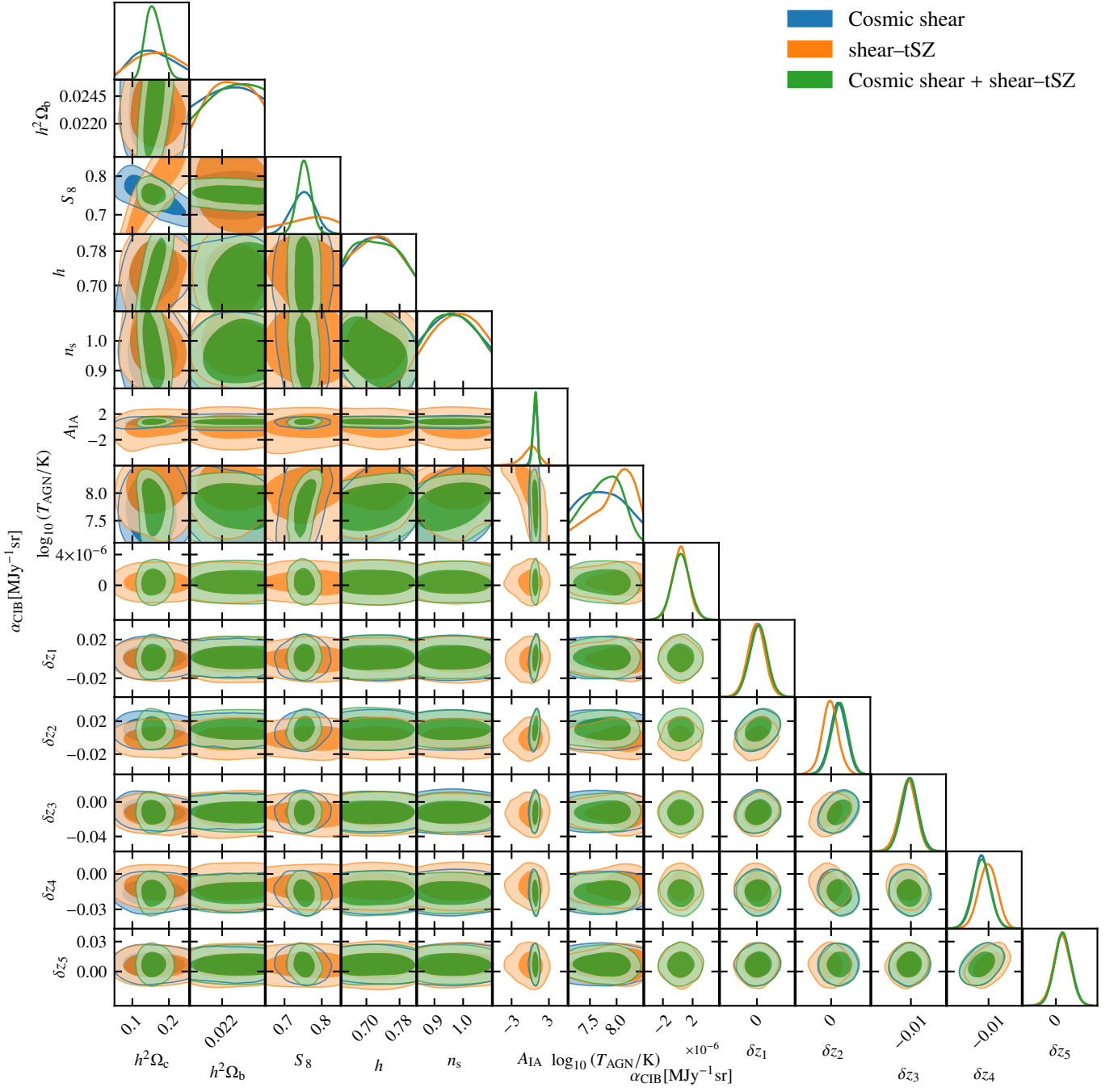
**Fig. B.2.** The window functions of Eq. (7), relating the smooth angular power spectrum model to the binned prediction compatible with the measured data vector. The differences between the multipole bin (grey bands) and the window function are due to masking and weighting of the shear maps in the case of the pseudo- $C_\ell$  estimator (orange), and the finite angular range used for the bandpower estimator (blue).



**Fig. B.3.** *Top:* Comparison of the constraints on  $\Omega_m$  and  $S_8$  between the bandpower analysis of [Asgari et al. \(2021\)](#) and pseudo- $C_\ell$  analysis of this work. *Bottom:* Effect of different non-linear matter power spectrum modelling approaches on the cosmology constraints of the pseudo- $C_\ell$  cosmic shear measurements.



**Fig. B.4.** Marginal posterior densities of  $S_8$ , for the same data and models as in Fig. B.3. The blue band and dashed line indicate the 68th percentile marginal CI and MAP of the [Asgari et al. \(2021\)](#) bandpower analysis, respectively.



**Fig. C.1.** Constraints on all sampled parameters from KiDS-1000 cosmic shear, the cross-correlation of shear and the tSZ effect, and their joint analysis.