















Promise and Peril: Stellar Contamination and Strict Limits on the Atmosphere Composition of TRAPPIST-1 c from JWST NIRISS Transmission Spectra

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Abstract

Attempts to probe the atmospheres of rocky planets around M dwarfs present both promise and peril. While their favorable planet-to-star radius ratios enable searches for even thin secondary atmospheres, their high activity levels and high-energy outputs threaten atmosphere survival. Here we present the 0.6–2.85 μm transmission spectrum of the 1.1 R_{\oplus} , ~ 340 K rocky planet TRAPPIST-1 c obtained over two JWST NIRISS/SOSS transit observations. Each of the two spectra displays 100–500 ppm signatures of stellar contamination. Despite being separated by 367 days, the retrieved spot and facula properties are consistent between the two visits, resulting in nearly identical transmission spectra. Jointly retrieving for stellar contamination and a planetary atmosphere reveals that our spectrum can rule out hydrogen-dominated, $\lesssim 300\times$ solar metallicity atmospheres with effective surface pressures down to 10 mbar at the 3σ level. For high mean molecular weight atmospheres, where O_2 or N_2 is the background gas, our spectrum disfavors partial pressures of more than ~ 10 mbar for H_2O , CO , NH_3 , and CH_4 at the 2σ level. Similarly, under the assumption of a 100% H_2O , NH_3 , CO , or CH_4 atmosphere, our spectrum disfavors thick, >1 -bar atmospheres at the 2σ level. These nondetections of spectral features are in line with predictions that even heavier, CO_2 -rich atmospheres would be efficiently lost on TRAPPIST-1 c given the cumulative high-energy irradiation experienced by the planet. Our results further stress the importance of robustly accounting for stellar contamination when analyzing JWST observations of exo-Earths around M dwarfs, as well as the need for high-fidelity stellar models to search for the potential signals of thin secondary atmospheres.

Unified Astronomy Thesaurus concepts: Low mass stars (2050); Exoplanet atmospheres (487); Extrasolar rocky planets (511); Planetary atmospheres (1244); Exoplanets (498)

1. Introduction

The detection and characterization of the atmospheres of rocky, Earth-sized planets is one of the key science goals of JWST. Not only is the presence of an atmosphere a top-level requirement for potential habitability (J. L. Grenfell 2020), but constraining the composition of terrestrial planet atmospheres also has direct implications for our understanding of the formation and evolution of small-planet atmospheres (E. Bolmont et al. 2017; K. J. Zahnle & D. C. Catling 2017; J. Krissansen-Totton & J. J. Fortney 2022; J. Krissansen-Totton 2023; M. Turbet et al. 2023).

In recent years, the focus of such studies has been on small planets orbiting M dwarf stars, as the small size of late-type stars boosts the planet's atmosphere signal, in either transmission or emission, compared to Sun-like stars (e.g., J. De Wit et al. 2016; L. Kreidberg et al. 2019; H. R. Wakeford et al.

2019; T. P. Greene et al. 2023; O. Lim et al. 2023; E. M. May et al. 2023; J. Kirk et al. 2024; M. Zhang et al. 2024).

However, the potential promise of increased atmosphere observability also comes with a corresponding peril for atmosphere retention. Late-type stars have significantly longer pre-main-sequence phases than Sun-like stars, during which time orbiting planets are subjected to large amounts of high-energy radiation (R. D. Wordsworth & R. T. Pierrehumbert 2013; P. J. Wheatley et al. 2017). Even at late times, during the M dwarf's main-sequence phase, they still maintain large outputs of high-energy radiation, with L_X/L_{bol} ratios significantly higher than those of earlier-type stars (N. Pizzolato et al. 2003; N. J. Wright et al. 2011; P. J. Wheatley et al. 2017; R. O. P. Loyd et al. 2021), reaching up to $\sim 2000\times$ that of the Sun for ultracool M dwarfs like TRAPPIST-1 (V. Bourrier et al. 2017; P. J. Wheatley et al. 2017). The increased amounts of high-energy radiation received by M dwarf planets result in the potential for corresponding increases in the efficiency of atmosphere-loss processes (e.g., R. D. Wordsworth & R. T. Pierrehumbert 2013; R. Luger & R. Barnes 2015; E. Bolmont et al. 2017; M. Turbet et al. 2023), resulting in uncertainty as to whether rocky planets around M dwarf stars can retain atmospheres to the present day (K. J. Zahnle & D. C. Catling 2017).

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Moreover, late-type stars also maintain higher levels of activity and photospheric inhomogeneities (i.e., the presence of spots and faculae) than Sun-like stars (S. Peacock et al. 2019; R. O. P. Loyd et al. 2021). Unocculted spots and faculae on the host star's photosphere (i.e., inhomogeneities that lie outside of a planet's transit chord), in particular, are a pernicious problem preventing the detection of atmospheres around Earth-like planets orbiting M dwarfs via transit observations (B. V. Rackham et al. 2018, 2019; H. R. Wakeford et al. 2019; L. J. Garcia et al. 2022; TRAPPIST-1 JWST Community Initiative et al. 2024; B. V. Rackham & J. de Wit 2024). The presence of unocculted inhomogeneities can impart spurious features on the transmission spectra of rocky planets, which can often be significantly larger than expected atmosphere features (B. V. Rackham et al. 2018, 2023; O. Lim et al. 2023; TRAPPIST-1 JWST Community Initiative et al. 2024; B. V. Rackham & J. de Wit 2024). This phenomenon is often referred to as the transit light source effect (TLSE). Despite these challenges, transit observations using the Hubble Space Telescope (HST) and now with JWST have been able to widely rule out cloud-free, H/He-dominated atmospheres for rocky M dwarf planets (J. De Wit et al. 2016; H. R. Wakeford et al. 2019; L. J. Garcia et al. 2022; J. E. Libby-Roberts et al. 2022; O. Lim et al. 2023; J. Lustig-Yaeger et al. 2023; C. Cadieux et al. 2024; M. Damiano et al. 2024; J. Kirk et al. 2024), although such extended atmospheres are often already disfavored based on mass and radius measurements alone (e.g., E. Agol et al. 2021). In many cases, though, the TLSE still prevents us from robustly probing secondary or high mean molecular weight (MMW) atmospheres in transmission (e.g., H. R. Wakeford et al. 2019; O. Lim et al. 2023; E. M. May et al. 2023; S. E. Moran et al. 2023; C. Cadieux et al. 2024).

Observations of M dwarf planets in eclipse geometry circumvent the TLSE problem but bring with them their own sets of challenges: the planet's orbital eccentricity must be well-known to calculate the phase of the eclipse; emission observations favor planets with high temperatures, potentially ruling out habitable-zone worlds; etc. Though, even without the impacts of the TLSE, emission studies of rocky M dwarf planets, both in the JWST era and previously, have been either negative (i.e., favor atmosphereless interpretations; L. Kreidberg et al. 2019; T. P. Greene et al. 2023; J. Ih et al. 2023; M. W. Mansfield et al. 2024; Q. Xue et al. 2024; M. Zhang et al. 2024) or unable to provide definitive evidence for the presence of a high-MMW atmosphere (e.g., A. P. Lincowski et al. 2023; S. Zieba et al. 2023), often due to degeneracies between atmospheric absorption and surface reflectivity (e.g., J. Ih et al. 2023; A. P. Lincowski et al. 2023).

Here we present transit observations of TRAPPIST-1 c with JWST NIRISS/SOSS. TRAPPIST-1 c is the second-innermost planet ($a = 0.01580$ au, $T_{\text{eq}} = 340$ K) of the TRAPPIST-1 system, with a mass and radius of $1.3\times$ and $1.1\times$ that of Earth, respectively (M. Gillon et al. 2016; E. Ducrot et al. 2020; E. Agol et al. 2021). It was first observed in transit by J. De Wit et al. (2016) with HST/WFC3 from 1.1 to $1.7\ \mu\text{m}$. Their observations rule out cloud-free, H/He-dominated atmosphere scenarios at $>10\sigma$ but lack the precision to constrain the presence of a wide range (e.g., H_2O -rich, Venus-like) of higher-MMW atmospheres.

TRAPPIST-1 c was then observed in emission with JWST MIRI/F1500W photometry by S. Zieba et al. (2023) at $15\ \mu\text{m}$. Their dayside brightness temperature of 380 ± 31 K rules out

thick (>10 bars), CO_2 -rich atmospheres but remains consistent with a thin (0.01 bar) atmosphere composed purely of CO_2 , or trace amounts of CO_2 in thinner (0.1–10 bar), O_2 -dominated atmospheres at a $\sim 2\sigma$ level. This was then followed up by A. P. Lincowski et al. (2023), who compared the S. Zieba et al. (2023) eclipse depth to a broader range of potential atmosphere scenarios using a self-consistent modeling framework. Their results generally agree with those of S. Zieba et al. (2023), in that trace amounts of CO_2 in a thin O_2 -dominated atmosphere provide the best matches to the data. However, they also find that ~ 0.1 -bar pure O_2 and even $\lesssim 3$ -bar steam atmospheres are consistent with the data within $\lesssim 2\sigma$. Venus-like atmospheres, though, are disfavored at $\gtrsim 3\sigma$.

This paper is organized as follows: We present the observations and data analysis in Section 2. We describe our analysis of the stellar photosphere in Section 3 and joint modeling of the atmosphere and stellar contamination in Section 4. We then discuss our results in Section 5 and follow up with a short conclusion in Section 6.

2. Observations and Data Analysis

We observed two transits of TRAPPIST-1 c with the SOSS mode of JWST's NIRISS instrument (L. Albert et al. 2023; R. Doyon et al. 2023) as part of program GO 2589 (PI: O. Lim). The first visit started at 18:37:51 UTC on 2022 October 28, and the second started at 21:09:46 UTC on 2023 October 31. Each visit lasted a total of 4.6 hr and consisted of 159 integrations with 18 groups per integration.

2.1. Data Reduction

We reduce the time-series observations (TSOs) with the `exoTEDRF` pipeline⁹ (A. D. Feinstein et al. 2023; M. Radica et al. 2023; M. Radica 2024), closely following standard procedures as described in, e.g., M. Radica et al. (2024), C. Cadieux et al. (2024), and C. Piaulet-Ghorayeb et al. (2024). Concretely, we perform the standard `exoTEDRF` stage 1 calibrations, including the correction of $1/f$ noise at the group level (that is, before ramp fitting) using the `scale-achromatic-window` method introduced in `exoTEDRF v1.4.0`. With this algorithm, we only use rows within 30 pixels of the trace to estimate the $1/f$ level, which can potentially help to reduce residual red noise in SOSS TSOs, particularly with high group numbers (e.g., A. D. Feinstein et al. 2023; M. Holmberg & N. Madhusudhan 2023). We then proceed with the standard Stage 2 calibrations (e.g., flat-field correction, bad pixel interpolation). Notably, we perform a ‘‘piecewise’’ background subtraction (e.g., O. Lim et al. 2023; M. Fournier-Tondreau et al. 2024; M. Radica et al. 2024), whereby the standard STScI SOSS background model is scaled separately on either side of the background ‘‘step,’’ as we found that a single scaling for the whole detector did not adequately remove the background signal. As a final step in the calibrations, we performed a principal component analysis (PCA) on the 2D detector images (e.g., L.-P. Coulombe et al. 2023; M. Radica et al. 2024) to identify any detector-level trends (i.e., mirror tilt events, trace position drifts), which could impact the light curves.

We extract the stellar spectrum using a simple box aperture with a width of 40 pixels, as the dilution effects due to the SOSS first- and second-order overlap are expected to be

⁹ <https://github.com/radicamc/exoTEDRF>

negligible for transit measurements (A. Darveau-Bernier et al. 2022; M. Radica et al. 2022). Finally, there are several undispersed contaminants due to background field stars (so-called “order 0” contaminants) present on the detector for both visits, several of which partially intersect the target spectral traces. These contaminants are located at wavelengths $0.670\text{--}0.675\ \mu\text{m}$, $1.642\text{--}1.658\ \mu\text{m}$, and $2.064\text{--}2.072\ \mu\text{m}$ for visit 1 and $0.975\text{--}1.001\ \mu\text{m}$, $1.251\text{--}1.279\ \mu\text{m}$, and $1.567\text{--}1.578\ \mu\text{m}$ for visit 2. We simply mask these contaminants in the extracted spectra.

2.2. White Light-curve Fitting

We construct white light curves for each visit and each order by summing all flux on the detector in order 1 ($\sim 0.85\text{--}2.8\ \mu\text{m}$) and only wavelengths $< 0.85\ \mu\text{m}$ in order 2. We fit these white light curves using the flexible `EXOUPRF` library (M. Radica 2024b). For each visit, we jointly fit the first- and second-order white light curves, as in M. Radica et al. (2024). Concretely, we fit an astrophysical transit model, as computed by `BATMAN` (L. Kreidberg 2015), with the orbital parameters (T_0 , the time of midtransit; inc , the orbital inclination; and a/R_* , the scaled orbital semimajor axis) shared between both orders, and the scaled planet radius, R_p/R_* , fit to each order individually. We furthermore assume a circular orbit and fix the orbital period to 2.421937 days (E. Agol et al. 2021). We fit, separately for each order, the two parameters of the quadratic limb-darkening law, $u_1, u_2 \in [-1, 1]$, in order to avoid potential biases that can be introduced by employing the D. M. Kipping (2013) parameterization (e.g., L.-P. Coulombe et al. 2024). We also tested several other limb-darkening treatments but found that the choice of parameterization did not impact the final spectra.

We also fit a systematics model to the light curve for each order. For each visit, the first component of the systematics model is a linear trend with time. TRAPPIST-1 is well-known to be a highly active star (O. Lim et al. 2023); therefore, we include a Gaussian process (GP) with a Matérn 3/2 kernel, to model residual red noise in the visit 1 light curves not captured by the aforementioned detrending. We train the GP on the time series of the second eigenvalue extracted from the PCA, which roughly corresponds to subpixel drifts of the trace position on the detector, as we find that this reduces the residual scatter in the light curves by a further $\sim 10\%$ compared to training the GP on the light-curve time axis. The characteristic amplitude of the GP was fit independently for each order, but the timescale was shared between both (e.g., M. Radica et al. 2024).

During the pre-transit baseline of the second visit, there was a large flare event on the host star. We correct this flare in the light curves by detrending against the $H\alpha$ flux, computed for each integration by measuring the area between the flux in the $H\alpha$ line and a local quadratic continuum, shown in the second row of Figure 1. However, this avenue was unsuccessful, as there is a slight time delay between the appearance of the flare in the $H\alpha$ time series and that in the white light curve, likely due to lags in energy release as a function of wavelength (W. S. Howard et al. 2023). However, given the broad structure of this flare compared to others seen in TRAPPIST-1 light curves (e.g., W. S. Howard et al. 2023), we found that we were able to adequately include the flare in our light-curve fits using a GP that again employed the Matérn 3/2 kernel. As above, we fit the characteristic amplitude separately to each order, but we shared the timescale between both.

Finally, we include an error inflation term for each order of each visit, which is added in quadrature to the extracted flux errors. Our final models consist of 20 parameters for each visit—we use wide and uninformative priors in all cases. The results of the white light-curve fits are shown in Figure 1, and the best-fitting astrophysical parameters are summarized in Table 1.

2.3. Spectroscopic Light-curve Fitting

To construct the spectrophotometric light curves, we sum the first-order flux in bins of 80 pixels (corresponding to a constant resolving power of approximately $R=25$). The combined effects of the spectrum of the late M host star and the low throughput of the SOSS order 2 mean that the second-order trace is very faint for observations of TRAPPIST-1 planets (e.g., O. Lim et al. 2023). We therefore do not bin order 2 further and simply include the white light-curve results in our transit spectrum. The orbital parameters from both visits are consistent between visits (Table 1), as well as with literature values (e.g., E. Agol et al. 2021), and so we fix them to the weighted average between the two visits when fitting the spectroscopically binned light curves. We include the same systematics model as mentioned above for each visit, except that we fix the characteristic timescale of the GP to the best-fitting value from the white light-curve fit for each visit and allow the amplitude to freely vary, since we can reasonably expect the impacts of stellar variability to be more prominent at bluer versus redder wavelengths (e.g., M. Radica et al. 2024).

We also reduce and fit the TSOs from each visit using the independent `NAMELESS` pipeline (L.-P. Coulombe et al. 2023; A. D. Feinstein et al. 2023). Further details of this analysis are presented in Appendix A, and a comparison of the spectra from both pipelines is shown in Figure 7. Since the spectra from each pipeline are consistent to within 1σ for both visits (or $\lesssim 1$ via a χ^2 -per-data-point metric), we only consider the `EXOEDRF` spectrum for the remainder of our analysis.

3. Modeling of the Stellar Photosphere

Before undertaking any planet atmosphere analysis, we first seek to better constrain the properties of TRAPPIST-1’s photosphere and thereby aid in our attempts to disentangle veritable atmosphere signals from the TLSE. To this end, we perform two independent but complementary analyses: one of the in-transit data via the TLSE (Section 3.1), and another focusing on the out-of-transit data via modeling the stellar spectrum itself (Section 3.2).

3.1. Transit Light Source Effect Modeling

We first model the transmission spectrum of TRAPPIST-1 c assuming that the TLSE can completely explain each visit’s transmission spectrum. This approach is motivated by the presence of small features resembling water absorption (e.g., around $1.4\ \mu\text{m}$; Figure 2) and a pronounced slope toward short wavelengths in the spectrum of the first visit. We use the open-source code `stctm` (C. Piaulet-Ghorayeb 2024; C. Piaulet-Ghorayeb et al. 2024) to perform the TLS retrievals. We model the presence of two populations of heterogeneities: spots (covering a fraction f_{spot} of the photosphere, and cooler than the photosphere at a temperature $T_{\text{spot}} < T_{\text{phot}}$) and faculae (with f_{fac} representing their covering fraction and $T_{\text{fac}} > T_{\text{phot}}$ their temperature).

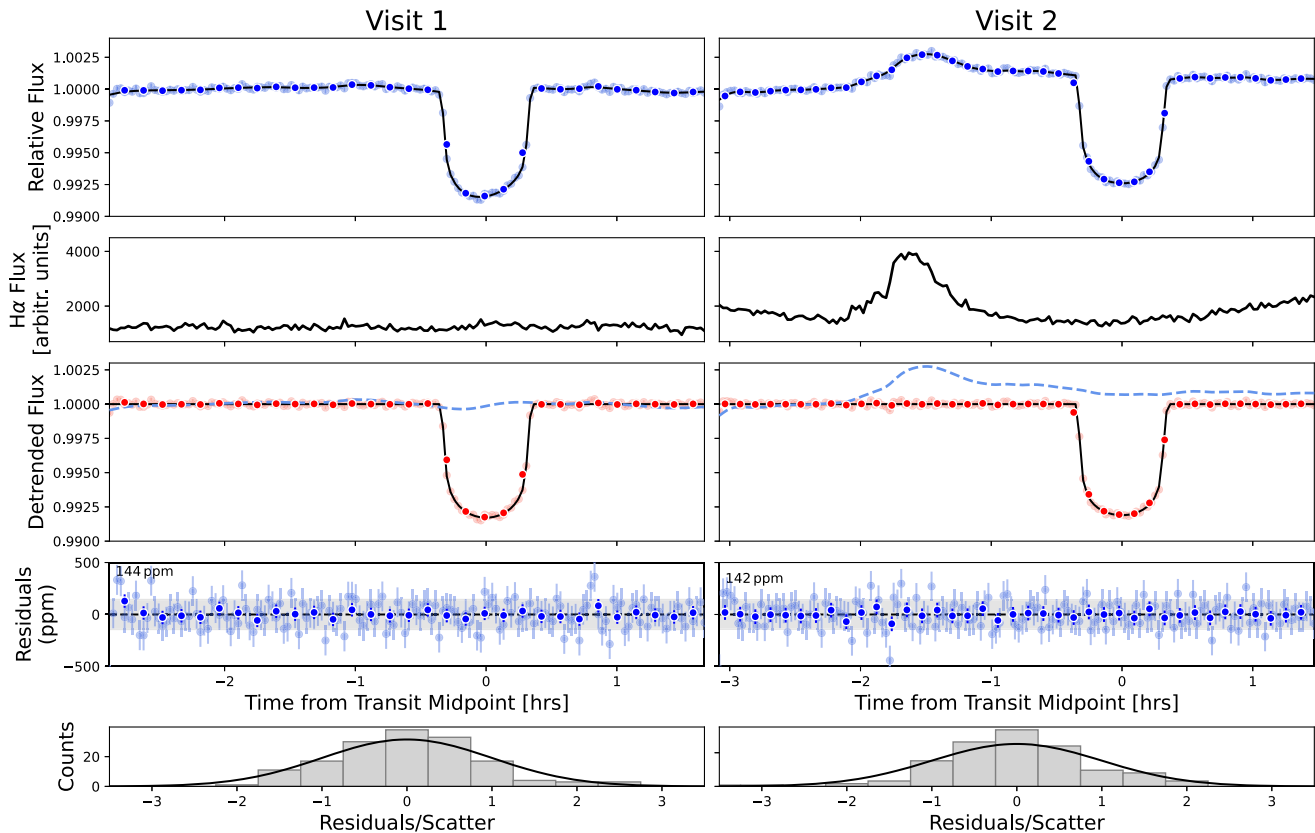


Figure 1. White light curves and fits results for both visits. Top row: raw white light curves for order 1, with the best-fitting astrophysical + systematics model overlotted in black. A flare is visible in the pre-transit baseline for visit 2. Second row: $H\alpha$ time series (in arbitrary units) for each visit. The time series is relatively quiescent in visit 1 but traces the flare structure in visit 2. Third row: white light curves after removal of the systematics model described in Section 2. The best-fitting astrophysical transit model is overlotted in black, and the systematics model that has been removed from the data is shown with the blue dashed line. Fourth row: residuals after the removal of the astrophysical and systematics models. Bottom row: histogram of residuals.

For each population of heterogeneities, we fit for the temperature difference to the photosphere ($T_{\text{het}} = T_{\text{phot}} + \Delta T_{\text{het}}$) and place a conservative uniform prior from 0% to 50% on the covering fraction for each of the components, f_{het} . The stellar photosphere temperature is fitted using a Gaussian prior, with the mean set by the literature value of 2566 K (E. Agol et al. 2021) and a standard deviation of 50 K. We allow faculae to be at most 1000 K hotter than the photosphere (with an otherwise uniform prior on $\Delta T_{\text{fac}} > 0$), while the minimum temperature of spots is set by the minimum temperature for which stellar models are available in our grid (2300 K). In the retrieval, we select at each iteration the closest-matching model (in effective temperature and surface gravity space) for the photosphere, spot, and facula components from a finely sampled precomputed grid obtained with the MSG module (R. Townsend & A. Lopez 2023) using the PHOENIX (T.-O. Husser et al. 2013) stellar model grid. We also introduce the fitting of $\Delta \log g_{\text{het}}$ (C. Piaulet-Ghorayeb et al. 2025, in preparation), the $\log g$ difference between the photosphere and heterogeneity components, allowing the heterogeneity spectra to use a lower $\log g_{\text{het}}$ than that of the photosphere, motivated by recent work (e.g., M. Fournier-Tondreau et al. 2024).

We use the affine-invariant Markov Chain Monte Carlo (MCMC) sampler `emcee` (D. Foreman-Mackey et al. 2013) to explore the parameter space, with the number of walkers set as 20 times the number of fitted parameters, and run the chains for 5000 steps, visually monitoring for convergence and discarding the first 60% as burn-in. In addition to the stellar heterogeneity

properties, we fit the wavelength-independent transit depth of TRAPPIST-1 c, D . We perform independent fits to the spectrum of each visit, as they are separated by about 1 yr and should not, a priori, be affected by the same TLS contribution. We also perform additional retrievals considering only faculae or only spots in addition to the quiet stellar photosphere.

We find that when either only spots or both spots and faculae are included in our model, we obtain a very good match to the observed spectra, without the need for a planetary atmosphere. The addition of faculae enables us to fit better the shortest-wavelength data points with a tentative downward slope that cannot be created by spots alone (Figure 2) and results in broader distributions on the spot properties given the interplay with a facula component. However, when only faculae are included in our retrievals, the resulting TLS model does not capture the observed spectral features, particularly the broad absorption features around 1.4 and 1.9 μm (as faculae would predict these features to instead be inverted). The resulting parameters from these retrievals are therefore not presented, as they result in poorer fits.

We find that similar spot and facula properties can explain both visits (Figure 2; Table 2), which motivates the use of a shared stellar contamination component in our joint retrievals of stellar and planetary atmosphere contributions to the spectra in Section 4. There is, however, a slight ($<1\sigma$) offset between the “bare-rock” transit depths retrieved in the fit to visit 1 ($D_{\text{v1}} = 7035^{+152}_{-170}$ ppm) and in the fit to visit 2 ($D_{\text{v2}} = 6859^{+141}_{-136}$ ppm). Finally, our

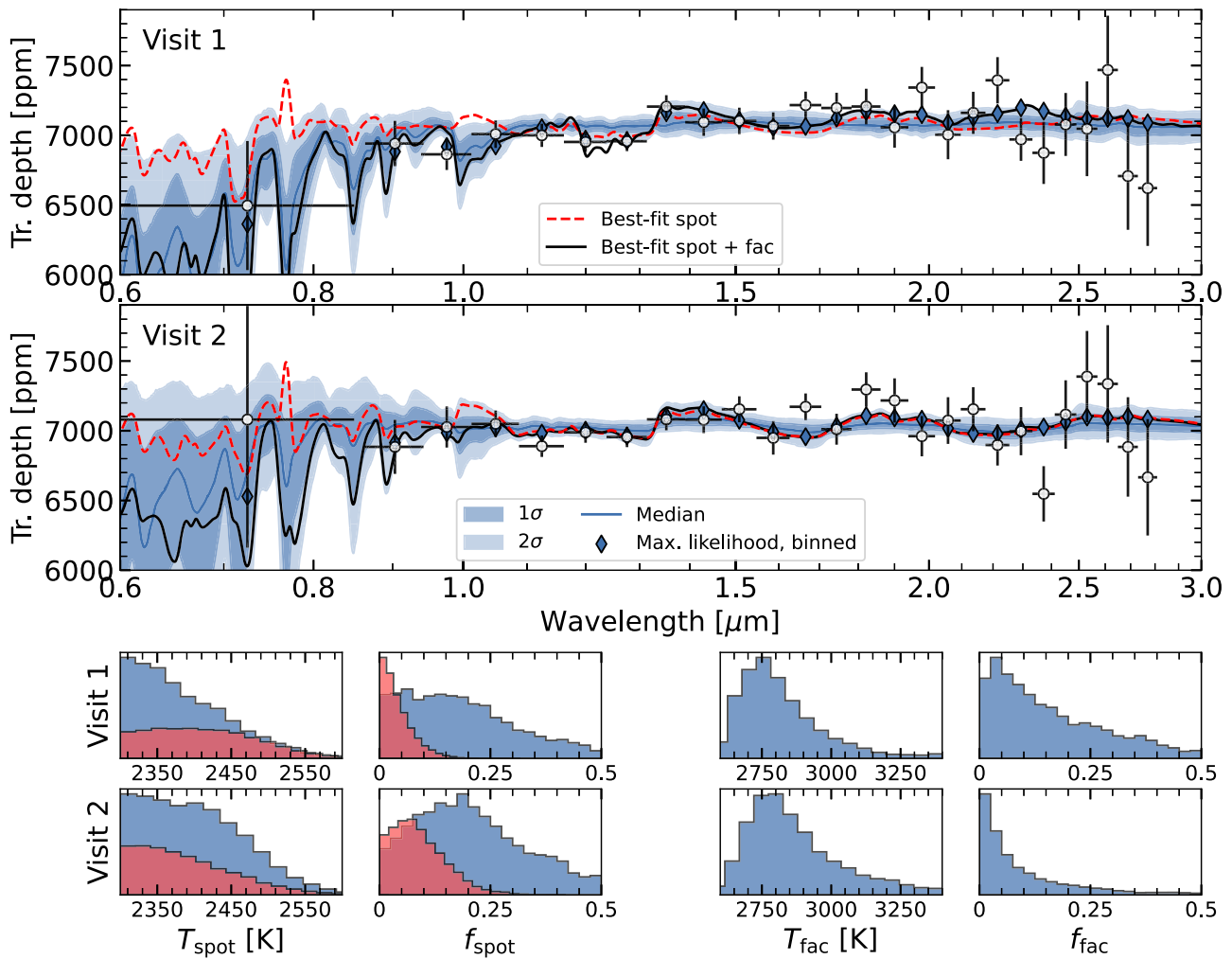


Figure 2. Results from the stellar-contamination-only fits to the transmission spectrum of each visit of TRAPPIST-1 c. Top panel: best-fitting unocculted heterogeneity model (black line) to the observed visit 1 spectrum (black points). The median, 1σ , and 2σ ranges from the posterior spectra (color shading, smoothed to a resolving power of 100) are also shown, integrated within each of the spectral wavelength bins (diamonds), for easier comparison. We assume a contribution from both spots and faculae and that the photosphere component represents the transit chord. The best-fitting model obtained from a retrieval where only spots are considered is shown with a dashed red line. Middle panel: Same as the top panel, but for the fit to the visit 2 spectrum. Bottom panels: posterior probability distributions of the spot and faculae temperatures, T_{spot} and T_{fac} , and covering fractions, f_{spot} and f_{fac} , for both visits. The corresponding distributions of spot properties from the spot-only retrieval are overlaid in red. Stellar contamination alone can explain the wavelength-dependent variations in the spectrum, and the retrieved heterogeneity parameters are largely consistent across both visits.

retrievals do not support the use of different $\log g$ values for the photosphere and heterogeneity components, as we only find lower limits on $\Delta \log g_{\text{het}}$ (e.g., Figure 8).

We use these TLS-only retrievals to produce “TLS-corrected” spectra, which we use to explore the limiting effect of stellar contamination on the constraining power of our observations (see Section 5.5; Figure 9), and for visualization purposes in order to interpret the results from our atmosphere retrievals (Figures 4 and 5). For each visit, the TLS-corrected spectrum is produced by dividing the observed spectrum by the best-fitting stellar contamination model and then multiplying the result by the best-fit model bare-rock transit depth (6776 ppm for visit 1, 6730 ppm for visit 2). These spectra aim to quantify the precision we could reach on atmospheric inferences given our observing setup if stellar contamination were not a factor.

Finally, to obtain the joint visit 1+2 TLS-corrected spectrum shown in Figures 4 and 5 (but not used in the retrievals), we simply offset the visit 2 spectrum by the difference between the

best-fit model bare-rock transit depths of each visit and then average the two spectra.

3.2. Out-of-transit Stellar Spectrum Modeling

In order to verify the reliability of our TLS retrievals described above, as well as gain additional insights into the heterogeneous nature of the photosphere of TRAPPIST-1, we directly model the out-of-transit stellar spectrum, roughly following the methodologies of H. R. Wakeford et al. (2019) and S. E. Moran et al. (2023). For each visit, we first create a median stack of the stellar spectrum considering only the out-of-transit integrations. For visit 1, this includes both the pre- and post-transit baseline. For visit 2, we only include integrations before the flare event in the pre-transit baseline. The post-transit baseline appears, by eye, to be at a slightly higher level than the pre-transit baseline. We test fits for visit 2 using only the pre-transit and only the post-transit baselines, as well as both, and note that we do not find any difference in the inferred photosphere or heterogeneity parameters as a result of

these choices, and we therefore proceed using both the pre- and pos-transit baseline for the fits.

We then flux-calibrate the stellar spectra, following the procedure presented in O. Lim et al. (2023). Like S. E. Moran et al. (2023), we use the standard deviation of the stellar spectra as a function of time as the errors on each wavelength point, as we find this more representative than the pipeline-extracted flux errors.

As with the TLS fits, we proceed to fit one-, two-, and three-component models (i.e., photosphere-only, photosphere + spots/faculae, photosphere + spots + faculae) directly to the stellar spectra using the `StellarFit`¹⁰ package. For consistency with the in-transit fits, we explore a grid of PHOENIX model spectra (T.-O. Husser et al. 2013), but we also test a grid of SPHINX models (A. R. Iyer et al. 2023), which include temperatures as low as 2000 K, more appropriate for modeling cold spots on ultracool dwarfs like TRAPPIST-1. All models in a given grid are scaled by R_*^2/D^2 to represent the flux received at Earth, using $R_* = 0.1192 R_\odot$ for the stellar radius (E. Agol et al. 2021) and $D = 12.1$ pc for the distance of the system to Earth (M. Gillon et al. 2016).

One-component fits have four free parameters: the stellar effective temperature T_{phot} , the surface gravity, and a spectrum scaling factor (e.g., H. R. Wakeford et al. 2019; S. E. Moran et al. 2023), and a multiplicative error inflation term. The photosphere temperature was allowed to vary from 2300 to 5000 K for the PHOENIX grid or from 2000 to 4000 K for the SPHINX grid, the log gravity was allowed to vary from 3.5 to 5.5 (PHOENIX) or from 4.0 to 5.5 (SPHINX), and the scale factor was allowed to vary from 0.8 to 1.2. Multicomponent fits also include the spot/facula temperature ($T_{\text{spot}}/T_{\text{fac}}$), the covering fraction ($f_{\text{spot}}/f_{\text{fac}}$), and the gravity of the heterogeneity (e.g., O. Lim et al. 2023; M. Fournier-Tondreau et al. 2024). Spot/facula temperatures are required to be at least 100 K and up to 1000 K cooler/warmer than the photosphere, whereas their gravity must be within 1.0 of the photosphere value.

Unlike previous works, we do not simply consider a “best-fitting” model, but instead explore the full parameter space of model fits to obtain distributions on the photosphere and heterogeneity parameters analogous to our TLS retrievals. We use nested sampling for the posterior exploration, as implemented in the `dynesty` (J. S. Speagle 2020) package, which also allows us to assess the statistical evidence for including heterogeneities in our models. The best-fitting three-component models for both stellar grids are shown in Figure 3 and are in excellent agreement with the in-transit TLS results. The best-fitting parameters from both the in-transit and out-of-transit analyses are also presented in Table 2.

4. Joint Modeling of Atmosphere and Stellar Contamination

We follow up our analysis of stellar contamination by using SCARLET (B. Benneke & S. Seager 2012, 2013; B. Benneke 2015; B. Benneke et al. 2019a, 2019b; S. Pelletier et al. 2021; C. Piaulet et al. 2023) to more thoroughly explore the potential atmosphere scenarios consistent with our observation, while still accounting for the contributions of stellar contamination. The forward modeling component of SCARLET iteratively solves the radiative transfer equation and the 1D

vertical structure of the atmosphere under the assumption of hydrostatic equilibrium, given the vertical temperature–pressure profile and the molecular abundances in each atmospheric layer. In the retrieval, the planetary radius is optimized for each set of sampled parameters to obtain the best match to the observed spectrum.

We perform three categories of retrievals corresponding to different assumptions about the planetary atmosphere: (1) H₂/He-dominated scenarios, (2) single-component high-MMW atmospheres, and (3) two-component high-MMW atmospheres with one infrared absorber present in the atmosphere and either N₂ or O₂ acting as the background gas.

We parameterize H₂/He-dominated atmospheres in the retrieval with a H₂/He mixture as the background gas (assuming He/H₂ = 0.157); log-uniform priors on the abundances of N₂, CH₄, H₂O, CO, CO₂, and NH₃; and a log-uniform prior on the pressure at which the atmosphere becomes opaque (due to either the presence of a cloud deck or a solid surface). We use the HELIOS-K (S. L. Grimm & K. Heng 2015; S. L. Grimm et al. 2021) compiled line lists for CH₄ (R. J. Hargreaves et al. 2020), H₂O (O. L. Polyansky et al. 2018), CO (R. J. Hargreaves et al. 2019), CO₂ (S. N. Yurchenko et al. 2020), and NH₃ (P. A. Coles et al. 2019).

For single-component high-MMW atmospheres, we only explore absorbers with prominent features over the NIRISS/SOSS wavelength range, namely, atmospheres made of 100% CH₄, H₂O, CO, or NH₃. We also fit for the “effective surface pressure” at which the atmosphere becomes opaque.

Finally, we also explore potential N₂-dominated atmospheres (similar to some terrestrial objects in the solar system) or O₂-dominated atmospheres (motivated by the possible O₂–CO₂ atmosphere consistent with the MIRI eclipse observations of TRAPPIST-1 c; S. Zieba et al. 2023) where only one of CH₄, H₂O, CO, or NH₃ acts as an additional absorber beyond the broad N₂–N₂ or O₂–O₂ collision-induced absorption features. In this retrieval setup, we fit for the partial pressure of each component. Unfortunately, the CH₄ line lists does not extend all the way to the short-wavelength end of NIRISS/SOSS order 2 (R. J. Hargreaves et al. 2020). Therefore, we exclude the order 2 data points from the spectrum for the 100% CH₄, N₂–CH₄, and O₂–CH₄ retrievals.

We assume that the vertical temperature structure is isothermal, motivated by the fact that our transmission spectra would not have the precision to measure any temperature gradient in the thin transit photosphere region we are probing. We use the nested sampling method (J. Skilling 2004, 2006) to sample the full parameter space, with the multiellipsoid method implemented using the `nestle` module¹¹ within the SCARLET retrieval framework. The final posterior distributions are obtained from retrievals performed using at least 1000 live points. We compute forward models at $R = 31,250$ before convolving them to the resolution of the spectrum, assuming a uniform throughput within each bin for the likelihood calculation.

We also calculate forward models for 1 and 100× solar metallicity, H₂/He-dominated atmospheres with varying cloud-top pressures (Figure 4; left panel) and models for several high-MMW compositions (Figure 5; top panel), to put our retrieval results in context. For each model, the temperature–pressure

¹⁰ <https://github.com/radicamc/StellarFit>

¹¹ <https://github.com/kbarbary/nestle>

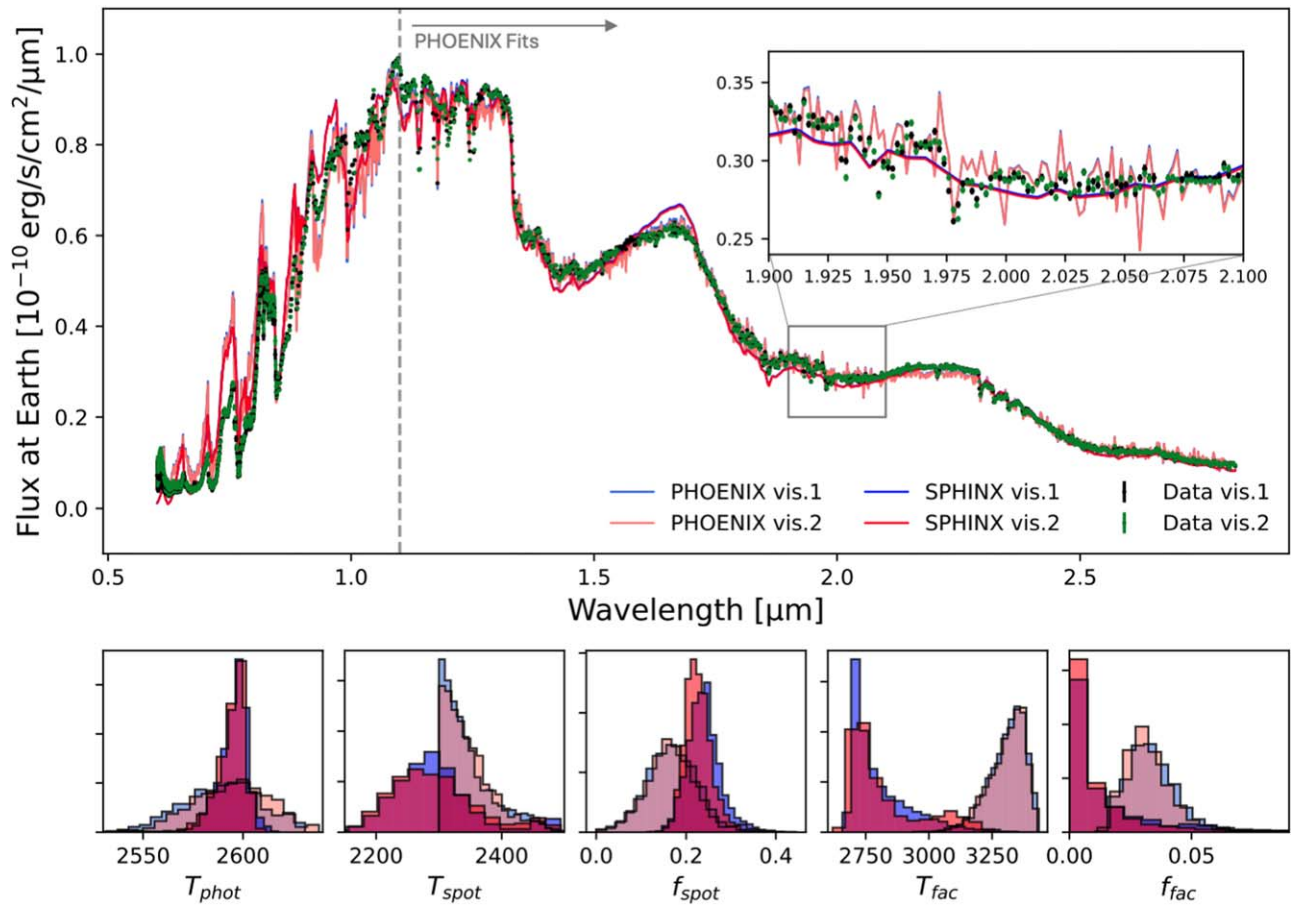


Figure 3. Results from the out-of-transit stellar spectrum fits. Top: flux-calibrated stellar spectra for visit 1 (black) and visit 2 (green), along with best-fitting PHOENIX and SPHINX three-component (i.e., photosphere + spots + faculae) stellar models. Visit 1 models are shown in blue and visit 2 in red, whereas PHOENIX models are denoted by lighter colors and SPHINX models by darker colors. PHOENIX models are only fit to wavelengths $>1.1 \mu\text{m}$, as the fits to the shortest wavelengths were exceptionally poor. A zoom-in to a region of the spectrum is also included to visualize fine structure. Bottom: posterior distributions for the photosphere temperature, as well as spot and facula temperatures and distributions. As above, visit 1 is shown in blue and visit 2 in red, whereas darker colors indicate SPHINX models and lighter colors indicate PHOENIX models. Note that the cutoff in the spot temperature at 2300 K for the PHOENIX grid is due to models not being available at colder temperatures.

profile is assumed to be isothermal at the equilibrium temperature of TRAPPIST-1 c.

For each set of retrievals we account for the impacts of stellar contamination, thereby marginalizing over the interplay between unocculted stellar heterogeneities and planetary absorption features. In addition to the planetary atmosphere properties, motivated by the results in Section 3, we assume two heterogeneity populations: spots (cooler than the photosphere) and faculae (hotter than the photosphere). For each heterogeneity component, we fit a covering fraction (with a wide uniform prior of 0%–50%) and a temperature contrast to the photosphere (following the uniform priors of the TLS-only fit). We also fit for the photosphere temperature itself, with a Gaussian prior based on the value reported by E. Agol et al. (2021).

We allow the photosphere $\log g$ to vary within the range [2.5, 5.5] as lower $\log g$ values are required to obtain a good match of the PHOENIX models to the out-of-transit spectrum of TRAPPIST-1 (see, e.g., O. Lim et al. 2023; see also Section 3.2). Given that the TLS-only fit did not provide evidence for a difference in $\log g$ between the photosphere and heterogeneity components, we fix them to the same value for each model evaluation. Finally, we fit for an offset between the

visit 1 and visit 2 spectra, motivated by the `stctm` retrieval results.

Given the consistency between the stellar heterogeneity parameters inferred from both the TLS and stellar spectrum fits, we assume that the heterogeneity components for both visits are identical in our joint atmosphere fits. However, we note that we also performed one set of atmosphere+stellar contamination retrievals where we fit for visit-specific stellar heterogeneity properties, and we found that this does not affect our inferences. We show the results for H_2/He -dominated atmospheres in Figure 4 and those for high-MMW atmospheres in Figures 5 and 6.

5. Discussion

5.1. Inferences of the Stellar Photosphere

For the out-of-transit stellar modeling using both grids and visits, the photosphere temperature is generally higher than, but still broadly consistent with, literature values (e.g., E. Agol et al. 2021; F. Davoudi et al. 2024). The retrieved \log gravities (~ 3.8 for PHOENIX and ~ 4.2 for SPHINX) are both significantly lower than the ~ 5.2 found by E. Agol et al. (2021) and F. Davoudi et al. (2024), though this discrepancy was also noted in the TRAPPIST-1 spectra obtained with

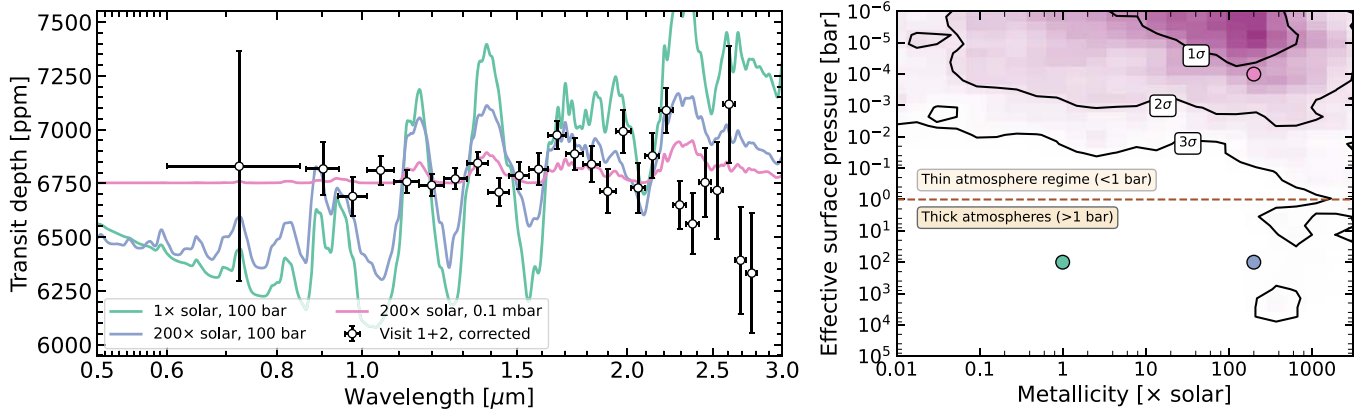


Figure 4. Constraints on H_2/He -dominated atmospheres on TRAPPIST-1 c from joint atmosphere and TLSE modeling. Left panel: joint visit 1+2 spectrum, corrected by the best-fitting stellar contamination model (black points), with three representative atmosphere forward models overplotted. Right panel: joint posterior probability on the effective surface pressure of a H_2/He -dominated atmosphere and its metallicity from the SCARLET atmosphere retrievals (color shading). We show the 1σ , 2σ , and 3σ confidence regions and three markers corresponding to the three models shown in the left panel. At low metallicities, we obtain a strict 3σ upper limit of ~ 10 mbar on the effective surface pressure of any H_2/He -dominated atmosphere, although thick high-metallicity atmospheres ($>100\times$ solar) are possible within the 3σ contours.

NIRISS/SOSS by O. Lim et al. (2023) in their observations of planet b.

Our results from both grids are broadly consistent with the TLS retrievals (e.g., Figures 2, 3; Table 2). For SPHINX, a two-component model including a photosphere and spots is preferred at $\sim 4\sigma$ (using the B. Benneke & S. Seager 2013 Bayesian evidence to σ -level conversion) over a homogeneous photosphere model and at $\sim 2\sigma$ over a model including both spots and faculae for both visits. Like in the TLS retrievals, when faculae are included, the fits push the covering fraction to zero in order to minimize their contribution. Both the spot covering fraction and temperature are in excellent agreement with the TLS results. The spot temperatures are also consistent with those inferred by previous studies (e.g., H. R. Wakeford et al. 2019; L. J. Garcia et al. 2022; O. Lim et al. 2023; F. Davoudi et al. 2024). For the PHOENIX grid, the results are also in excellent agreement with both the SPHINX grid and the TLS fit results (Table 2). In this case, the three-component fit is preferred (though the significance is low; $\sim 1.8\sigma$). The facula covering fraction is also only $\sim 3\%$ and therefore essentially negligible. For all grids tested, we find that the gravity of the heterogeneities is always consistent with that of the photosphere.

We note, though, that the overall quality of the fits is unsatisfactory, with χ^2_ν values generally >350 . The short wavelengths ($\lesssim 1.1\ \mu\text{m}$) are especially badly fit by the PHOENIX grid in particular. In fact, the PHOENIX grid struggled to fit both the short and long wavelengths simultaneously, routinely overestimating the flux $>1.7\ \mu\text{m}$ and finding photosphere temperatures that were highly inconsistent with literature values. We therefore restricted the models to wavelengths $>1.1\ \mu\text{m}$ for the PHOENIX grid, where the models were better matches to the data. Performing the same test for the SPHINX grid does not alter the retrieved parameter distributions.

Another caveat is that the high resolution of NIRSpec/G395H (~ 2700) allowed S. E. Moran et al. (2023) to fit to individual stellar lines. However, in our case, the medium resolution of NIRISS/SOSS (~ 700) does not provide this same capability (see the inset in Figure 3), and our fits are more sensitive to the broadband structures in the spectrum. In all, though we confirm the results of the in-transit TLS fits, our

stellar spectrum analysis demonstrates the clear need for improved stellar models for ultracool stars. Moreover, we posit that since the in-transit analysis relies on *ratios* of stellar models instead of *absolute fits*, it may be more robust to the aforementioned model inaccuracies than direct fits to stellar spectra—something that should be explored further.

5.2. Cloud-free and Thick Hydrogen-rich Atmospheres Are Ruled Out

We find that, similarly to the closer-in planet TRAPPIST-1 b (O. Lim et al. 2023), we can confidently rule out thick or cloud-free hydrogen-dominated atmospheres, with a 3σ limit of <10 mbar on the effective surface pressure of a H_2/He -dominated atmosphere atop TRAPPIST-1 c (Figure 4). The thin hydrogen-rich atmosphere scenarios allowed by the transmission spectrum are, moreover, unlikely from an atmospheric evolution standpoint—TRAPPIST-1 c was exposed to large cumulative amounts of high-energy XUV irradiation from its host star, sufficient to strip away any primordial atmosphere (Y. Hori & M. Ogihara 2020; M. Turbet et al. 2020) even when considering hydrogen outgassing (R. Hu et al. 2023). The transmission spectrum still allows within the 3σ confidence contours for thick, high-metallicity ($>100\times$ solar) atmospheres, which may be more resilient against escape owing to their higher MMWs.

5.3. Limits on High Mean Molecular Weight Atmospheres

We therefore turn to evaluating the range of plausible high-metallicity atmosphere scenarios for TRAPPIST-1 c, and we focus on the detectability of H_2O , NH_3 , CO , and CH_4 in high-MMW atmospheres, as these infrared absorbers have sufficient opacity within the NIRISS/SOSS wavelength range to enable meaningful constraints.

As expected from the high-metallicity tail of the surface pressure–metallicity distribution (Figure 4), the densest atmosphere cases we tested do not provide strong upper limits on the effective surface pressure. We find that deep, 100% H_2O , NH_3 , and CH_4 atmospheres remain compatible with our spectrum at the 3σ level, although >1 -bar atmospheres are disfavored at the 2σ level (Figure 5). In the 100% CO case, we exclude even a 1-bar atmosphere at the 3σ level. However, we caution that this result mostly stems from the fact that CO has minimal

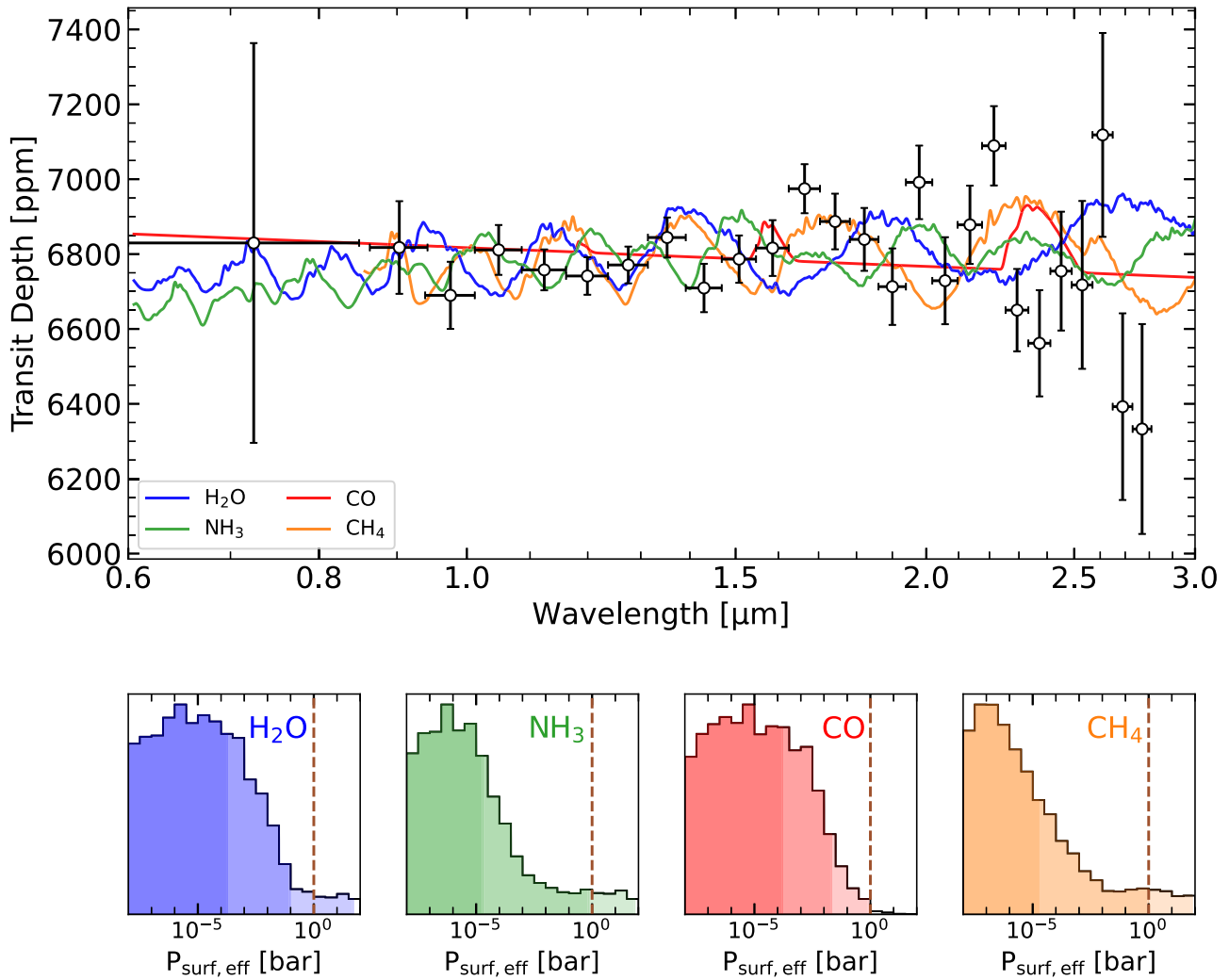


Figure 5. Constraints on high-MMW atmosphere compositions for TRAPPIST-1 c. Top panel: combined visit 1+2 spectrum of TRAPPIST-1 c corrected by the best-fitting stellar contamination model (black points; see text) and atmosphere models for deep, 100-bar atmospheres composed of 100% H₂O (blue), NH₃ (green), CO (red), and CH₄ (orange). Bottom panels: marginalized posterior distributions on the effective surface pressure for different atmosphere compositions (labeled, with colors corresponding to the models in the top panel). The shaded areas correspond to the 1 σ , 2 σ , and 3 σ upper limits obtained on the effective surface pressure in each composition scenario. When marginalizing over the impact of stellar contamination, the transmission spectrum disfavors thick, >1-bar atmospheres for all molecules at the 2 σ level.

opacity in the SOSS wave band from 2 to 2.5 μm , and a pure-CO atmosphere would elsewhere yield a perfectly flat spectrum. Therefore, this example only rules out 100% CO atmospheres, but likely not cases where a CO-rich atmosphere is mixed with small amounts of another infrared absorber.

We then turn to models that allow for lower atmospheric MMWs, where the infrared absorber can be a trace species rather than a dominant component—representative of the atmospheres of some solar system planets. In this scenario, the background gas is N₂ or O₂, with only one of the aforementioned species as the active infrared absorber (Figure 6). We compare these limits, where available, with measured compositions of solar system bodies. In particular, we highlight in Figure 6 the amount of H₂O in Earth’s N₂-dominated atmosphere (using 0.4% as the mean mole fraction over the entire 1-bar atmosphere, although it can reach about 1% at sea level; Y. Kasai et al. 2011; V. Kelsey et al. 2022), or the amount of CH₄ in Titan’s atmosphere, assuming either a cloud-free Titan scenario (where one can see down to the surface) with 5% CH₄ or a hazy scenario accounting for the fact that hydrocarbon haze opacity raises the effective surface

pressure to ~ 10 mbar, and with a factor of three less methane in the upper atmosphere (see, e.g., B. Charnay et al. 2014).

We find that similar amounts of water to what is observed in Earth’s atmosphere are disfavored at the 2 σ level for TRAPPIST-1 c, while the transmission spectrum alone is not sensitive enough to the CH₄ abundance to offer meaningful constraints on Titan-like atmospheres. Although our observations cannot rule out atmospheres where NH₃ or CH₄ makes up the entire volatile budget (or they are trace species in N₂- or O₂-dominated atmospheres), the presence of methane and ammonia is unlikely on TRAPPIST-1c from a modeling standpoint because of its vulnerability to destruction via photochemistry (M. Turbet et al. 2018).

Since O₂ is a heavier molecule than N₂, the O₂ background scenarios generally correspond to more compact, higher-MMW atmospheres. Therefore, although the results are qualitatively similar to the N₂-background constraints, our transmission spectrum allows for larger amounts of the tested molecular absorbers in an O₂-dominated atmosphere. Further, because of the lack of sensitivity to CO₂ absorption with NIRISS/SOSS spectroscopy, we are not able to rule on any of the possible

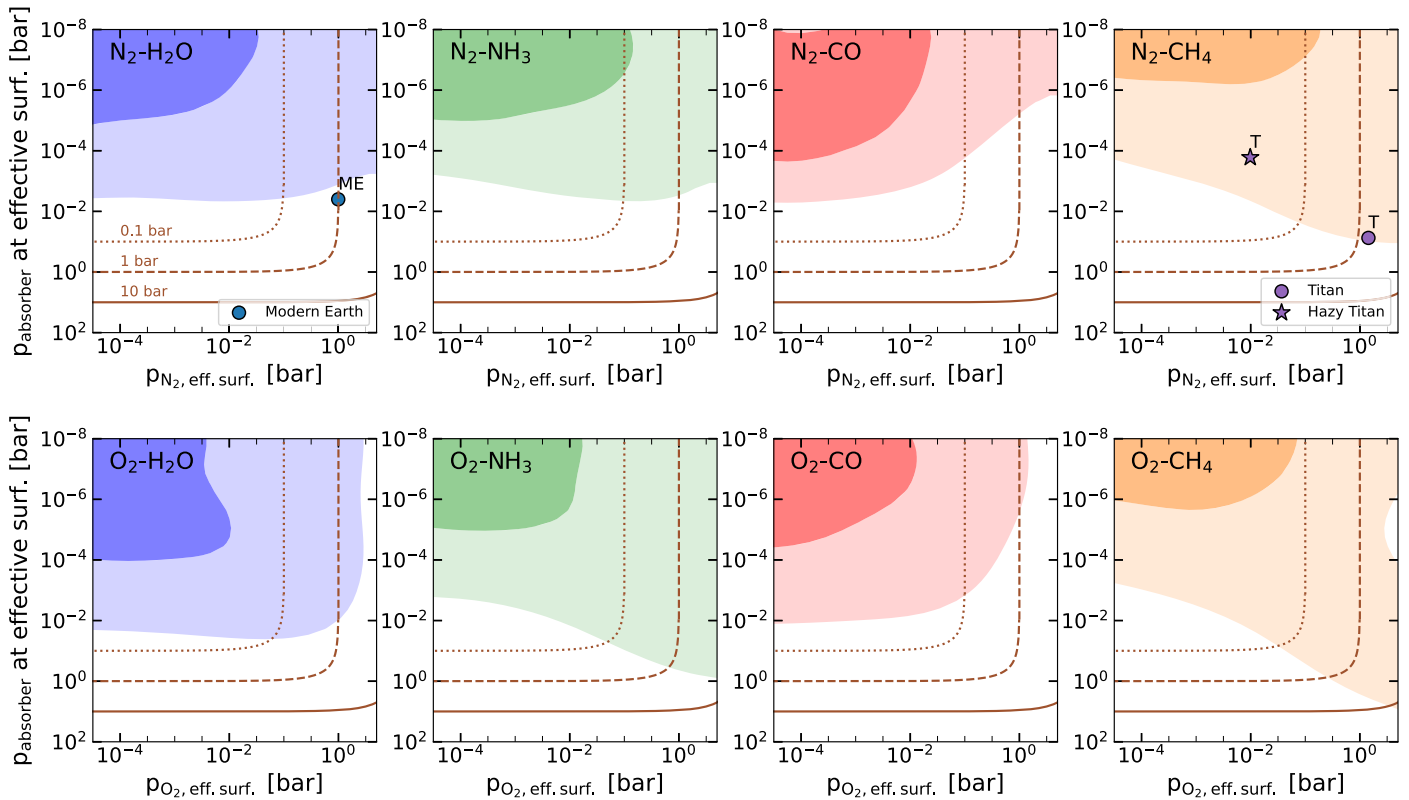


Figure 6. Constraints on N_2 - and O_2 -dominated atmospheres from the transmission spectrum of TRAPPIST-1 c. Top panels: two-dimensional posterior distribution of the partial pressure of the considered absorber at the effective surface pressure (left to right: H_2O , NH_3 , CO , CH_4) as a function of the partial pressure of the background gas N_2 at the effective surface probed by the transmission spectrum. The 1σ and 2σ contours are filled with different color shadings. The parts of the parameter space corresponding to effective surface pressures of 0.1, 1, and 10 bars are outlined by the dotted, dashed, and solid sienna lines, respectively. We also illustrate where the amounts of methane in the atmosphere of Titan (with or without aerosols; purple markers; B. Charnay et al. 2014) and of water in the atmosphere of modern Earth (blue marker; Y. Kasai et al. 2011; V. Kelsey et al. 2022) would lie relative to our posterior distributions. Bottom panels: same as the top panels, but for the retrievals with O_2 rather than N_2 as the background gas.

scenarios presented by S. Zieba et al. (2023) based on their MIRI eclipse observations of this planet. The photometric eclipse depth of 421 ± 94 ppm at $15 \mu m$ was broadly consistent (better than 2σ) with a 0.01-bar pure CO_2 atmosphere, or trace amounts of CO_2 in a O_2 -dominated atmospheres with a surface pressure less than ~ 10 bars. We find that such an O_2 - CO_2 atmosphere would give rise in transmission to a ~ 40 ppm CO_2 absorption feature at $2.7 \mu m$ (at the red edge of the SOSS detector) and a larger ~ 90 ppm absorption band at $4.3 \mu m$. As demonstrated by J. Taylor et al. (2023), CO_2 cannot be reliably probed at $2.7 \mu m$ with SOSS alone, even for a hot Jupiter, whereas the $4.3 \mu m$ feature could potentially be detectable with approximately five transits with NIRSpec/G395M or PRISM.

5.4. Implications for the Presence of an Atmosphere on TRAPPIST-1c

Although it could still be explained by some high-metallicity scenarios, our nondetection of any significant atmospheric signature in the transmission spectrum of TRAPPIST-1 c is also in line with modeling predictions that TRAPPIST-1 c could be a bare rock, as any substantial atmosphere is expected to be stripped over the 5–9 Gyr lifetime of its host star (A. J. Burgasser & E. E. Mamajek 2017), regardless of its initial volatile content (J. Krissansen-Totton 2023).

Even if they remain tentative (at the 2σ level), our atmospheric retrieval results disfavor thick >1 -bar atmospheres, even for high-MMW compositions. The thin

atmosphere scenarios that remain consistent with our observations given their smaller spectral features are, however, unlikely to be retained on TRAPPIST-1 c from a theoretical perspective. Even if Jeans escape (generally less efficient than blow-off) is expected to dominate for high-MMW atmospheres atop TRAPPIST-1 c, the escape rates even for resilient N_2 - CO_2 atmospheres range from one Earth atmosphere mass per Myr to one Earth atmosphere mass per Gyr (G. Van Looveren et al. 2024) at the present-day irradiation of this planet. The implications are even stricter when considering the fact that any atmosphere on TRAPPIST-1 c also would have had to withstand the early XUV-active stages of the late M dwarf’s evolution (E. Bolmont et al. 2017), and its position inside of the runaway greenhouse limit (M. Turbet et al. 2020) indicates that water could not have been efficiently shielded from escape via condensation in a liquid water ocean, even if this limit is pushed to closer host star–planet distances around M dwarfs in 3D models (M. Turbet et al. 2023).

5.5. Impacts of Stellar Contamination on the Transmission Spectra

Our two-transit study of TRAPPIST-1 c aptly summarizes the promise and peril of transmission observations of rocky planets around M dwarf host stars. There are now a plethora of studies that have shown that stellar contamination is a true bottleneck in the attempt to detect atmospheres around rocky, M dwarf planets via transmission spectroscopy (e.g., Z. Zhang

et al. 2018; H. R. Wakeford et al. 2019; O. Lim et al. 2023; E. M. May et al. 2023; S. E. Moran et al. 2023; C. Cadieux et al. 2024; B. V. Rackham & J. de Wit 2024). In most cases, different manifestations of the TLSE (i.e., different temperature distributions, covering fractions, etc., of stellar spots and faculae) give rise to obviously different transmission spectra between visits, allowing for a clear inference of the impacts of the TLSE, even without undertaking in-depth modeling. Consistency in the location and shapes of spectral features between visits has been argued to lend credence to an interpretation favoring a planetary atmosphere origin (e.g., E. M. May et al. 2023).

However, despite the high level of consistency between the transmission spectra ($\sim 1.1\sigma$ on average), our retrieval analysis still finds that both visits can be entirely explained by stellar contamination. As shown in Figure 8 and summarized in Table 2, we find very similar stellar heterogeneity parameters (spot/facula temperatures and covering fractions) for both visits. We also find both visits to be spot dominated, with minimal contributions from faculae, whereas O. Lim et al. (2023) have one spot-dominated visit and one facula-dominated visit in their two-transit analysis of TRAPPIST-1 b.

The consistency between visits would perhaps be unsurprising if they were separated by a very small period of time, which would therefore probe similar spot and facula distributions on the host star. However, our two visits are separated by ~ 367 days, significantly longer than the 3.3-day stellar rotation period (R. Luger et al. 2017). When phase-folded to the stellar rotation period, this corresponds to a phase difference of ~ 0.21 —similar to the observations of O. Lim et al. (2023), who, as mentioned above, found no such consistency between their two visits. Moreover, both of our visits are at comparable stellar phases to those of O. Lim et al. (2023). This highlights the fact that the distributions of spots and faculae in the host star’s photosphere are entirely stochastic, and therefore TLSE models are nonpredictive of future stellar contamination.

Irrespective of whether we perform TLS-only or joint TLS-atmosphere retrievals, we still infer consistent stellar contamination parameters (Figure 8). This is consistent with our finding that the retrieval does not pick up on any “true” atmosphere signature that would warrant changes in the inferred TLS parameters.

Finally, we evaluated the limiting effect of having to marginalize over stellar contamination on our sensitivity to thin 100% H₂O atmospheres. This choice was motivated by the fact that water is the molecule most affected by this marginalization, given that its features coincide with prominent unocculted stellar spot signatures, but we refer the reader to C. Piaulet-Ghorayeb et al. (2025, in preparation) for a more detailed exploration of the impact of TLSE marginalization on other infrared absorbers. We performed a retrieval on the TLS-corrected spectra from both visits (see Section 3.1), using the same setup as the joint atmosphere + TLS retrieval except that only the atmosphere properties are retrieved.

We find that our sensitivity drops by about two orders of magnitude through accounting for stellar contamination. As shown in Figure 9, without stellar contamination we could rule out at the 2σ (3σ) level 100% H₂O atmospheres with surface pressures down to ~ 1 mbar (1.6 bars). However, when marginalizing over the TLSE, we can only rule out at the 2σ (3σ) level cases with surface pressures of less than ~ 0.1 bar (45 bars). Therefore, we are in a regime where the unknown

TLS contribution to the spectrum, rather than the precision of the measured transit depths themselves, is the limiting factor in our sensitivity to the presence of high-MMW atmospheres. Furthermore, this effect will be even more problematic in other data sets where one needs to marginalize over different stellar contamination realizations for each visit in joint retrievals (e.g., C. Piaulet-Ghorayeb et al. 2025, in preparation).

6. Conclusions

Here we presented the first JWST transmission spectrum of the second-innermost planet in the TRAPPIST-1 system, TRAPPIST-1 c. Our 0.6–2.85 μm NIRISS/SOSS spectrum reveals strong contamination by the TLSE in both visits. However, unlike in previous multivisit analyses of rocky planets around M dwarfs (e.g., E. M. May et al. 2023; S. E. Moran et al. 2023; C. Cadieux et al. 2024), including TRAPPIST-1 b (O. Lim et al. 2023), we find consistent stellar heterogeneity properties between our two visits. Via an analysis of the in-transit data (i.e., the TLSE) and direct modeling of the out-of-transit stellar spectrum, we find the stellar photosphere to be dominated by spots ~ 300 K cooler than the ambient photosphere temperature and with a covering fraction of $\sim 25\%$. Faculae have negligible contributions to both visits, irrespective of the analysis technique or choice of stellar models. This results in nearly identical manifestations of the TLSE and thus transmission spectra. Our results support the need for joint modeling of the TLSE and atmosphere properties to achieve robust constraints on rocky, M dwarf planets in the era of JWST. Importantly, further stellar model fidelity is critically required to accurately model out the impact of the TLSE and reach the sensitivity to detect or rule out thin atmospheres on small planets via their transit spectra.

When accounting for stellar contamination in our atmosphere analysis, we find that thick, clear hydrogen-dominated compositions are ruled out at better than 3σ significance. The level of precision we reach does not enable us to rule out the cases with the highest MMW, where the atmosphere would be composed of 100% of a heavy volatile species such as H₂O, NH₃, or CH₄, but even these scenarios are disfavored for >1 -bar atmospheres at the 2σ level, due to the flatness of the TLSE-corrected spectrum. The sensitivity increases to partial pressures of about $\lesssim 10$ mbar at 2σ for the same species in atmospheres with N₂ or O₂ as the background gas.

Regardless, as shown by J. Krissansen-Totton (2023), even if TRAPPIST-1 c is completely atmosphereless, this does not imply a similar fate for the outer habitable zone planets. Our work, though, does highlight the fact that we cannot simply rely on consistency of transmission spectra between different visits to infer the presence of a planetary atmosphere and rule out stellar contamination.

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Facilities: JWST(NIRISS), Exoplanet Archive.

Software: `astropy` (Astropy Collaboration et al. 2013, 2018), `celerite` (D. Foreman-Mackey et al. 2017), `exoTEDRF` (M. Radica 2024a), `exoUPRF` (M. Radica 2024b), `ipython` (F. Pérez & B. E. Granger 2007), `juliet` (N. Espinoza et al. 2019), `jwst` (H. Bushouse et al. 2023), `matplotlib` (J. D. Hunter 2007), `numpy` (C. R. Harris et al. 2020), `pymultinest` (J. Buchner 2016), `scipy` (P. Virtanen et al. 2020).

Appendix A

NAMELESS Reduction and ExoTEP Light-curve Fitting

We reduce our two JWST NIRISS/SOSS visits of TRAPPIST-1 c, starting from the uncalibrated raw data up to the extraction of the stellar spectra, using the NAMELESS pipeline (L.-P. Coulombe et al. 2023; A. D. Feinstein et al. 2023). We first go through the Stage 1 and 2 steps of the STScI `jwst` pipeline (v1.12.5; H. Bushouse et al. 2023), which include superbias subtraction, reference pixel correction, nonlinearity correction, ramp fitting, and flat-fielding. We then proceed with a sequence of custom steps to correct for remaining sources of noise such as bad pixels, nonuniform background, cosmic rays, and $1/f$ following the methods described in B. Benneke et al. (2024). We flag bad pixels by looking for pixels whose second derivatives are significant ($>7\sigma$) outliers in the spatial domain. The counts of all flagged pixels are then corrected using the bicubic interpolation method of the `scipy.interpolate.griddata` function. We

correct for the nonuniform background by individually scaling the two regions of the STScI model background¹² that are separated by the sudden jump in background flux situated around spectral pixel $x \sim 700$. Any remaining cosmic rays are corrected by clipping any count that is more than four standard deviations away from the running median for all pixels. As for the $1/f$ noise correction, we follow the same method described in L.-P. Coulombe et al. (2023) and B. Benneke et al. (2024), where we scale individually each column of the first and second spectral orders considering only pixels that are within a 30-pixel distance from the center of the traces to compute the $1/f$ noise. We then extract the stellar spectra from both spectral orders using a simple box aperture with a width of 36 pixels.

We perform the broadband and spectroscopic fits of the light curves with the ExoTEP framework (B. Benneke et al. 2019a, 2019b). For our fit of the white light curve, which is obtained by summing all wavelengths of the first spectral order (0.85–2.85 μm), we keep free the midtransit time (T_0 , considering uniform priors spanning the time of the observations for each visit), planet-to-star radius ratio (R_p/R_* , $\mathcal{U}[0.01,0.2]$), semimajor axis (a/R_* , $\mathcal{U}[15,45]$), and the impact parameter (b , $\mathcal{U}[0,1]$). We consider the quadratic limb-darkening law and fit directly for u_1 and u_2 assuming large uniform priors ($\mathcal{U}[-3,3]$) following L.-P. Coulombe et al. (2024). For the first visit, we consider a quadratic trend for the systematics model. We also include in the fit a Matérn 3/2 GP using the `celerite` Python (D. Foreman-Mackey et al. 2017) to remove higher-frequency trends that are not corrected by our systematics model. The timescale and amplitude of the GP model are kept free assuming large uninformative uniform priors in log-space. As for the second visit, we cut the first 2.1 hr of the TSOs and consider solely a linear slope for the systematics model. The transit light curves are then modeled in ExoTEP using the `batman` (L. Kreidberg 2015) Python package, and we explore the parameter space using the MCMC sampler `emcee` (D. Foreman-Mackey et al. 2013). We run the MCMC for 10,000 steps and discard the first 6000 steps as burn-in. The same procedure is repeated for the spectroscopic light curves (assuming the same systematics model and GP for each visit), where we have fixed the orbital parameters of TRAPPIST-1 c to the best-fit values from the white light curve of the first visit ($a/R_* = 28.55$, $b = 0.112$). The light curves are fit using 100 and 30 equal-pixel bins for the first and second spectral orders, respectively. The resulting spectra, binned to a fixed resolving power of $R = 25$, are shown in Figure 7.

¹² <https://jwst-docs.stsci.edu/>

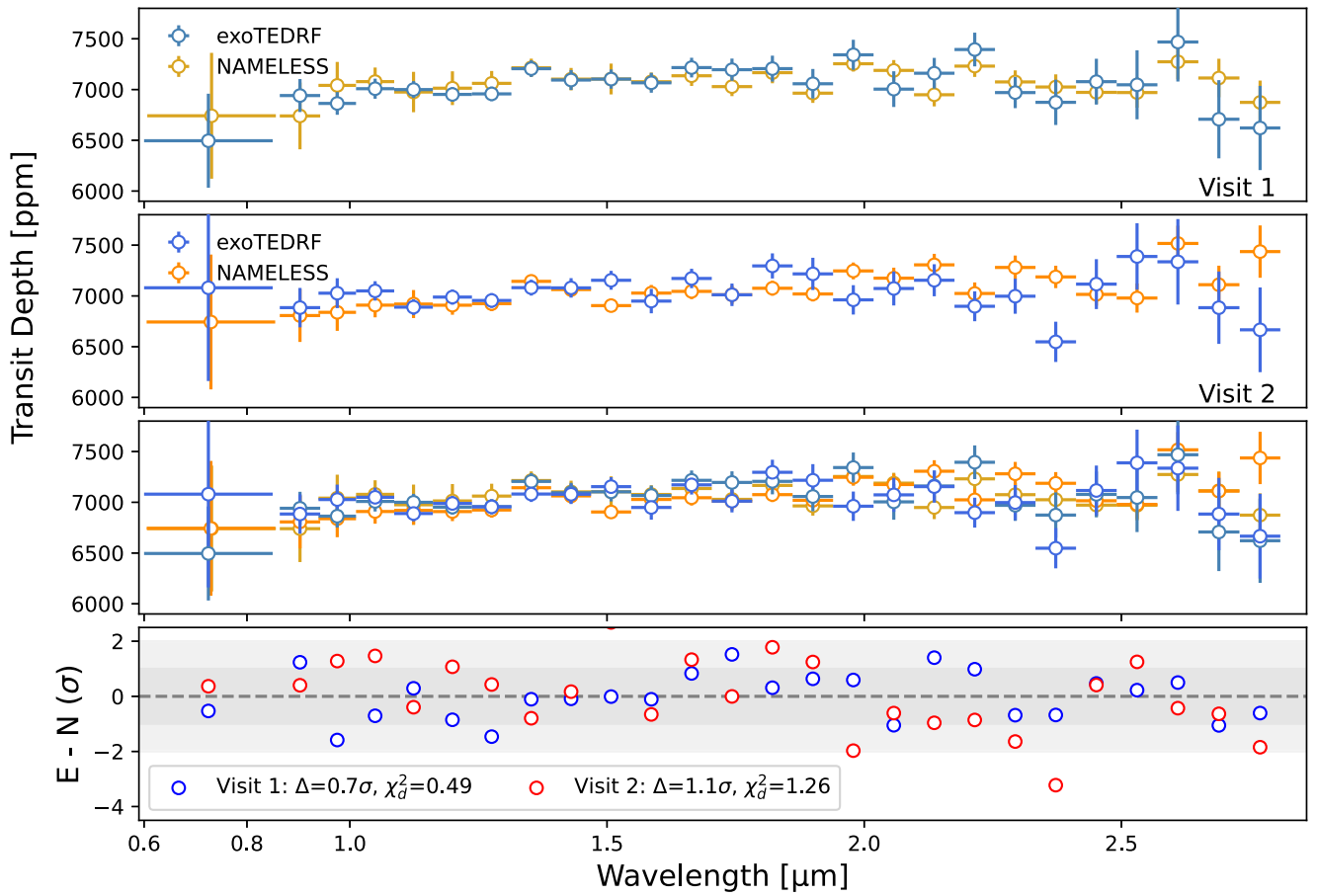


Figure 7. Comparison of transmission spectra from the `exoTEDRF` and `NAMELESS` pipelines. Top panel: spectrum comparison for visit 1. Second panel: same as the top panel, but for visit 2. Third panel: all four spectra from both pipelines and for both visits overplotted to show consistency. Bottom panel: differences between spectra from each pipeline for visit 1 (blue) and visit 2 (red) divided by the error bar on each transit depth. The `exoTEDRF` and `NAMELESS` spectra are consistent to within 0.7σ on average for visit 1 and to within 1.1σ for visit 2. Also quoted are comparisons between the two reductions using a χ^2 -per-data-point metric.

Appendix B Additional Figure and Tables

Table 1 contains the best-fitting white light-curve parameters for both NIRISS/SOSS visits. The orbital parameters (a/R_* , inc) are consistent with each other and with previous literature (e.g., E. Agol et al. 2021).

Table 2 contains the best-fitting parameters from the three-component stellar models via both the in-transit (TLS) and out-of-transit analyses.

Table 3 has the `exoTEDRF` transmission spectrum used in this work.

We compare the posterior distributions of the spot, facula, and photosphere properties inferred from the TLS-only fit to the visit 1 and visit 2 spectra, as well as the joint atmosphere and stellar contamination retrievals (for the single-component atmosphere cases), in Figure 8.

Finally, we also present the results of our sensitivity study assessing the impact of marginalizing over the TLS effect on the atmosphere thicknesses that can be ruled out by our spectrum in Figure 9.

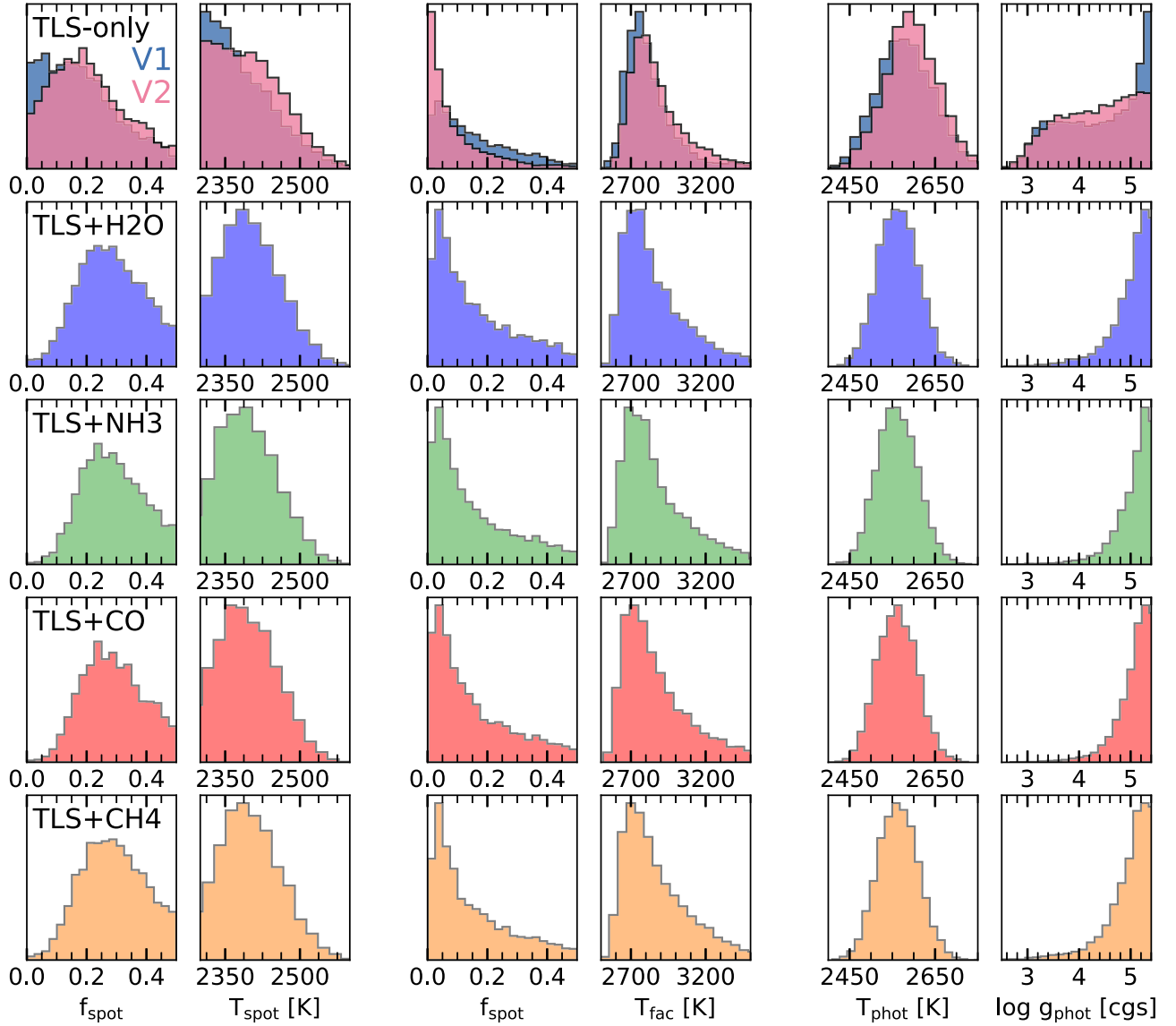


Figure 8. Posterior distributions of the inferred stellar surface properties from the TLS-only `stctm` retrieval (top row; visit 1 in blue, visit 2 in pink) and from the joint stellar heterogeneity + planetary atmosphere retrievals performed with SCARLET, for the 100% H₂O, NH₃, CO, and CH₄ cases (subsequent rows; labeled).

Table 1
Best-fitting `exOTEDRF` White Light-curve Transit Parameters

Parameter	Prior Range	Value		
		Visit 1	Visit 2	Weighted Average
T0 (BJD)	$\mathcal{U}[T0 \pm 2 \text{ hr}]$	2459881.401528 ^{+0.000033} _{-0.000033}	2460249.515031 ^{+0.000042} _{-0.000041}	...
$R_p/R_{*,O1}$	$\mathcal{U}[0.01, 0.9]$	0.08346 ^{+0.00092} _{-0.00097}	0.08344 ^{+0.00163} _{-0.00141}	0.08345 ± 0.00112
$R_p/R_{*,O2}$	$\mathcal{U}[0.01, 0.9]$	0.08364 ^{+0.00260} _{-0.00265}	0.08415 ^{+0.00881} _{-0.00970}	0.08379 ± 0.00472
inc	$\mathcal{U}[70, 90]$	89.73 ^{+0.17} _{-0.22}	89.38 ^{+0.32} _{-0.26}	89.64 ± 0.24
a/R_*	$\mathcal{U}[5, 50]$	28.35 ^{+0.27} _{-0.51}	28.18 ^{+0.85} _{-1.05}	28.3 ± 0.54
$u_{1,O1}$	$\mathcal{U}[-1, 1]$	0.405 ^{+0.100} _{-0.105}	0.283 ^{+0.197} _{-0.212}	0.344 ± 0.134
$u_{2,O1}$	$\mathcal{U}[-1, 1]$	0.168 ^{+0.187} _{-0.174}	0.346 ^{+0.299} _{-0.289}	0.257 ± 0.217
$u_{1,O2}$	$\mathcal{U}[-1, 1]$	0.671 ^{+0.229} _{-0.348}	0.302 ^{+0.442} _{-0.510}	0.487 ± 0.344
$u_{2,O2}$	$\mathcal{U}[-1, 1]$	-0.098 ^{+0.509} _{-0.402}	0.105 ^{+0.567} _{-0.561}	0.003 ± 0.477

Note. For each visit, R_p/R_* and the limb-darkening parameters (u_1 and u_2) were fit separately for each order. All other parameters were jointly fit to both.

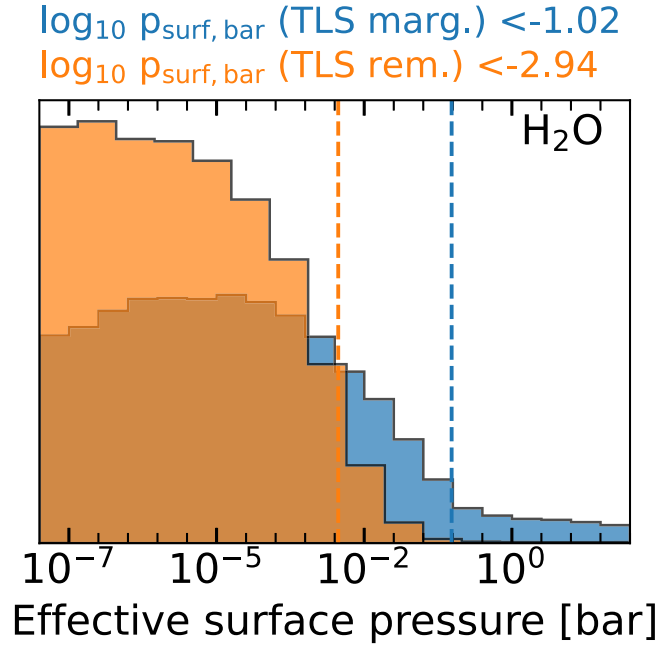


Figure 9. Impact of marginalizing over all the possible TLS realizations rather than retrieving directly on a “TLS-corrected” spectrum with the same error bars. The posterior distribution on the H₂O effective partial pressure (from the 100% H₂O atmosphere retrieval) is shown for two cases: one where we perform a joint stellar contamination + planetary atmosphere retrieval on the observed spectrum (blue), and one where an atmosphere-only retrieval is performed on our best estimate of a TLS-free spectrum (orange). The 2σ upper limits we obtain are quoted at the top of the figure and shown as dashed vertical lines. Marginalizing over the TLSE worsens our sensitivity to 100% H₂O atmospheres by roughly two orders of magnitude.

Table 2

Retrieved Parameters for the `stctm` Retrievals Performed on the Transmission Spectra (In-transit, TLS Effect) Assuming No Atmosphere and Two Heterogeneity Components, and from the Three-component Fit to the Out-of-transit Spectra Using `StellarFit`

Parameter	Model	In-transit (TLS)		Out-of-transit	
		Visit 1	Visit 2	Visit 1	Visit 2
T_{eff} (K)	PHOENIX	2578^{+68}_{-63}	2594^{+64}_{-59}	2591^{+18}_{-22}	2595^{+19}_{-21}
	SPHINX			2597^{+5}_{-8}	2596^{+5}_{-9}
$\log g_{\text{phot}}$	PHOENIX	$4.5^{+0.7}_{-1.0}$	$4.3^{+0.7}_{-0.8}$	$3.6^{+0.1}_{-0.1}$	$3.5^{+0.1}_{-0.1}$
	SPHINX			$4.2^{+0.1}_{-0.1}$	$4.2^{+0.1}_{-0.1}$
T_{spot} (K)	PHOENIX	<2510	<2523	<2437	<2432
	SPHINX			2286^{+55}_{-54}	2284^{+74}_{-58}
f_{spot}	PHOENIX	$0.19^{+0.14}_{-0.11}$	$0.19^{+0.14}_{-0.11}$	$0.17^{+0.06}_{-0.05}$	$0.17^{+0.06}_{-0.05}$
	SPHINX			$0.24^{+0.03}_{-0.03}$	$0.22^{+0.03}_{-0.02}$
$\log g_{\text{spot}}$	PHOENIX	>2.6	>2.7	$3.6^{+0.1}_{-0.1}$	$3.6^{+0.1}_{-0.1}$
	SPHINX			$4.2^{+0.1}_{-0.1}$	$4.2^{+0.1}_{-0.1}$
T_{fac} (K)	PHOENIX	2783^{+175}_{-102}	2831^{+225}_{-117}	3324^{+55}_{-85}	3396^{+49}_{-71}
	SPHINX			<3054	<3133
f_{fac}	PHOENIX	<0.39	<0.32	$0.03^{+0.01}_{-0.01}$	$0.03^{+0.01}_{-0.01}$
	SPHINX			<0.07	<0.05
$\log g_{\text{fac}}$	PHOENIX	>2.6	>2.7	$3.6^{+0.1}_{-0.2}$	$3.6^{+0.2}_{-0.2}$
	SPHINX			$4.1^{+0.2}_{-0.2}$	$4.3^{+0.2}_{-0.1}$













Note. We quote the median parameters and $\pm 1\sigma$ intervals, or 2σ limits when a parameter hits the edge of a prior.

For the `stctm` fits, the values quoted for T_{spot} and T_{fac} are derived from the posterior samples of ΔT_{spot} , ΔT_{fac} , and T_{phot} , and the intervals reported for the heterogeneity $\log g$ are derived from the $\log g_{\text{phot}}$ and $\Delta \log g_{\text{het}}$ samples.

Table 3
 exoTEDRF Transmission Spectrum of TRAPPIST-1 c Used in This Work

Wavelength (μm)	Wavelength Error (μm)	Transit Depth (Visit 1) (ppm)	Transit Depth (Visit 2) (ppm)
0.72	0.12	6495.76 \pm 463.23	7080.25 \pm 918.63
0.90	0.04	6940.96 \pm 162.46	6884.63 \pm 193.99
0.98	0.04	6863.36 \pm 112.06	7026.99 \pm 147.35
1.05	0.04	7008.37 \pm 98.91	7049.40 \pm 95.48
1.12	0.04	6999.78 \pm 83.35	6889.46 \pm 77.15
1.20	0.04	6952.18 \pm 71.99	6988.60 \pm 74.63
1.28	0.04	6957.36 \pm 70.95	6955.08 \pm 72.35
1.35	0.04	7205.70 \pm 81.75	7081.42 \pm 78.11
1.43	0.04	7093.85 \pm 98.13	7079.19 \pm 95.84
1.51	0.04	7103.09 \pm 94.84	7154.09 \pm 93.00
1.59	0.04	7066.62 \pm 97.78	6949.11 \pm 120.23
1.66	0.04	7216.39 \pm 96.84	7171.97 \pm 95.48
1.74	0.04	7195.63 \pm 109.50	7011.15 \pm 110.87
1.82	0.04	7206.13 \pm 127.63	7295.62 \pm 123.62
1.90	0.04	7057.07 \pm 145.74	7217.11 \pm 158.78
1.98	0.04	7342.25 \pm 148.19	6961.31 \pm 144.52
2.06	0.04	7004.14 \pm 175.93	7073.29 \pm 167.36
2.14	0.04	7160.88 \pm 151.13	7154.43 \pm 157.82
2.21	0.04	7394.33 \pm 166.09	6897.93 \pm 147.24
2.29	0.04	6970.20 \pm 153.40	6997.21 \pm 172.76
2.37	0.04	6874.09 \pm 223.18	6547.71 \pm 198.38
2.45	0.04	7077.64 \pm 225.76	7116.19 \pm 245.70
2.53	0.04	7046.87 \pm 340.02	7388.53 \pm 327.30
2.61	0.04	7468.39 \pm 389.34	7336.15 \pm 420.91
2.69	0.04	6707.51 \pm 385.19	6884.10 \pm 356.58
2.77	0.04	6621.37 \pm 414.79	6666.19 \pm 417.26

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