

Prediction of microtunnelling jacking forces using a probabilistic observational approach

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1 **ABSTRACT**

2 Microtunnelling is an increasingly popular means of locating utilities below ground. The ability to
3 predict the total jacking force requirements during a drive is highly desirable for anomaly detection,
4 to ensure the available thrust is not exceeded, and to prevent damage to the pipe string and/or
5 launch shaft. However, prediction of the total jacking force is complicated by site geology, the use of
6 a lubricated overcut, work stoppages, tunnel boring machine driving style and pipe misalignment.
7 This paper introduces a probabilistic observational approach for forecasting jacking forces during
8 microtunnelling. Gaussian process regression is adopted for this purpose which allows forecasts to
9 be performed within a probabilistic framework. The proposed approach is applied to two recent UK
10 microtunnelling monitoring projects and the forecasts are appraised through comparisons to
11 predictions determined using design methods currently applied in industry. The results show that the
12 proposed framework provides excellent forecasts of the monitored field data and highlights a
13 significant opportunity to complement existing prescriptive design methods with probabilistic
14 forecasting techniques.

15 INTRODUCTION

16 There is a vast network of buried infrastructure and services in the UK extending to well over 1.5
17 million km comprising water, sewer, gas and electricity. To keep pace with growing populations
18 and to meet future infrastructure demands, a substantial amount of construction work on buried
19 infrastructure is required (Royston et al. 2020a, 2020b). Relative to traditional open-cut
20 construction, microtunnelling is an increasingly popular means of locating utilities below ground
21 due to the reduction in costs, noise and air pollution, and impact on the surrounding infrastructure
22 and environment (Phillips et al. 2019).

23 Long-distance drives, often with curves, are desirable in the industry to avoid costly intermediate
24 shafts and provide a greater range of solutions for accommodating surface disruptions in sensitive
25 areas (Bergeson 2014). One of the greatest risks in long-drive microtunnelling is the development
26 of excessive soil-structure penetration resistances, to the point where they exceed the total
27 available jacking thrust. Prediction of the total jacking force is also complicated by site geology, the
28 use of a lubricated overcut, work stoppages, tunnel boring machine (TBM) driving style and pipe
29 misalignment (Meskele and Stuedlein 2015, Cheng et al. 2017, Sun et al. 2019). This does not
30 lend itself easily to simplification through theoretical relationships or numerical modelling. Instead,
31 site engineers rely on a combination of empiricism from experience on site and ad hoc theoretical
32 relationships which have not been rigorously validated.

33 The proliferation of data collected by modern TBMs presents a substantial opportunity for the
34 application of data analysis and pattern recognition techniques to support the decision-making
35 process on site with timely and meaningful information (Shen et al. 2016, Sheil et al. 2020a).
36 Originally proposed by Peck (1969), the observational method is an acceptable verification method
37 for limit states in Eurocode 7 and is now well-established in geotechnical engineering (Spross and
38 Johansson 2017). Data-driven modelling and forecasting has quickly developed into an essential
39 tool in a broad range of practical domains including seismology (e.g. Holliday et al. 2005),
40 healthcare (e.g. Reis and Mandl, 2003) and financial markets (e.g. Kim 2003). These approaches
41 advance the traditional observational method by employing machine learning systems, predicated

42 on the assumption of the presence of a sufficient amount of data to describe the modelled system's
43 physics.

44 This paper describes the development of a probabilistic observational approach for the prediction
45 of jacking forces during microtunnelling. Gaussian process (GP) regression is adopted for this
46 purpose which allows forecasts to be performed within a probabilistic framework. This allows a
47 project-specific approach to be adopted in which a GP is automatically constructed using data from
48 each individual project. The proposed approach is applied to two recent UK microtunnelling
49 monitoring projects and the forecasts are appraised through comparisons to predictions
50 determined using design methods currently applied in industry.

51

52 **BACKGROUND: FACTORS INFLUENCING MICROTUNNELLING JACKING FORCES**

53 Accurate forecasting of the total jacking force requirements for microtunnelling drives is desirable
54 to (a) develop a model of 'normality' from which anomalous observations can be inferred (short-
55 term), (b) inform (expensive) inter-jack installation ('medium'-term), and (c) predict maximum likely
56 jacking to avoid damage to the shaft and / or pipe string (long-term). The total jacking force, F_T , is
57 composed of the TBM face resistance, F_0 , and the soil-structure frictional resistance, F_s , acting
58 along the length of the pipe string. For long drives, F_T is almost entirely governed by F_s and the
59 adopted pipe-soil lubrication system becomes a key factor in the development of jacking forces.
60 Lubrication during microtunnelling serves three main purposes: (a) stabilisation of the tunnel bore,
61 (b) flotation of the pipe string, and (c) reduction of the pipe-soil interface friction coefficient (Milligan
62 and Marshall 1998). Based on nine monitored microtunnelling drives, Pellet-Beaucour and Kastner
63 (2002) observed that the use of lubricants can reduce frictional stresses by anywhere between
64 50% and 90%. From a field monitoring case study, Shi et al. (2018) presented significantly lower
65 interface friction coefficients for a lubricated steel-soil interface compared to values documented in
66 the literature relating to concrete pipes. From a back-analysis of two drives in silty sand, O'Dwyer
67 et al. (2018) noted that lubrication was very effective at maintaining low skin friction levels, and that
68 the pipe string was almost fully buoyant for the majority of the drive.

69 Work stoppages also have a considerable influence on F_s where a peak in jacking force is typically
70 observed upon resumption of tunneling (Cheng et al. 2017). Stoppages on site can vary in duration
71 from < 30 mins for pipe changes to between 12 and 48 hours for overnight and weekend
72 stoppages respectively. However, a general consensus has yet to be reached in the literature as to
73 the primary cause. Norris and Milligan (1992) suggested that these increases in jacking forces are
74 attributable to differences in shearing rates in cohesive soils. Pellet-Beaucour and Kastner (2002)
75 postulated that these effects are related to differences in dynamic and static friction coefficients.
76 More recently, O'Dwyer et al. (2019) concluded that jacking force increases following a stoppage
77 were largely governed by the stoppage duration, suggesting that these effects are instead a
78 consolidation phenomenon.

79 While our understanding of these factors have improved greatly over the past thirty years, the
80 literature contains many examples where prescriptive design methods fail to provide satisfactory
81 prediction of field behaviour. Norris and Milligan (1992) used instrumented pipe sections on five
82 construction projects to measure pipe-soil contact stresses. The measured contact stresses were
83 highly-localised and proved difficult to capture with theoretical relationships. Chapman and Ichioka
84 (1999) reported that one of the main obstacles to an accurate estimation of pipe jacking forces is
85 the inherent variability of the construction operation itself. Those authors noted that closed-form
86 design approaches are not capable of predicting fluctuations in jacking force that arise from site-
87 specific variations. Milligan and Norris (1999) reported that jacking force fluctuations are often due
88 to unanticipated pipe / TBM misalignments. Rahjoo et al. (2012) documented significant
89 incongruities when jacking forces measured in the field were compared to predictions determined
90 using a range of published empirical models. Similarly, Reilly and Orr (2012) noted that existing
91 design methods provided poor predictions of jacking forces measured during drives in coarse-
92 grained soils. Choo and Ong (2015) applied site-specific direct shear results to well-established
93 empirical models for the prediction of jacking forces. Although good agreement was observed, the
94 models were only capable of predicting the average jacking force and not variations due to
95 stoppages. Even in rock, where the tunnel bore can be assumed stable, Barla et al. (2006) and
96 Sheil et al. (2016) have attested to the difficulty in predicting jacking forces. These investigations

97 highlight the poor track record of closed-form design methods in this area and provides significant
98 motivation for the consideration of a complementary data-driven approach.

99

100 **FIELD MONITORING**

101 *Overview*

102 Tunnelling and lubrication data from two drives, 'Drive A' and 'Drive B', in Blackpool, UK are
103 considered in this paper (shown in Fig. 1). A total drive length of 295 m and 272 m was measured
104 for Drives A and B respectively. Drive A had an initial launch invert depth of 7.59 m below ground
105 level (BGL) and a cover depth which varied between 6.2 m and 7.8 m. Drive B had an initial launch
106 invert depth of 7.61 m BGL and a cover depth which varied between 5.2 m and 6.3 m. The slurry
107 shield TBM (Herrenknecht AVN 1200) had a cutterhead diameter, D_c , of 1515 mm whereas each
108 concrete pipe had an outer diameter, D_p , of 1490 mm. This created a 25 mm 'overcut' into which
109 lubricant was pumped. The length and mass of each pipe was 2.5 m and 3660 kg respectively.

110 A bentonite solution was adopted for the lubrication comprising Hydraul-EZ and water in the ratio
111 1:18 (by weight) with minor additions of MX polymer, torque reducer and soda ash. Bentonite
112 stations were located on every fifth pipe along the string with the first station located directly behind
113 the TBM. Each station comprised three lubrication ports, trisecting the pipe circumference, and
114 were positioned midway along the length of the pipe. The bentonite system used by these TBMs
115 are volume-controlled, calculated from the TBM advance rate and ground conditions.

116

117 *Ground conditions*

118 The locations of three boreholes (BH1, BH2 and BH3) in relation to the line of Drives A and B are
119 shown on Fig. 1. The ground conditions are summarised in Fig. 2 and comprise made ground (0.4
120 m thickness) underlain by gravelly sand (2.6 m - 4.4 m), peat (1.0 m - 1.7 m), silt (1.2 m - 2.5 m)
121 and silty sand/sand (>5.0 m). Tunnelling occurred predominantly in the silt and silty sand layers.
122 The water table was located 1.2 m below ground level. Uncorrected Standard Penetration Test (N)
123 values are also shown in Fig. 2. An average N1 value (N values corrected for overburden

124 pressure) was used to derive an operational friction angle for the material above the tunnel crown
125 using correlations proposed by Stroud (1989). This exercise yielded a friction angle of
126 approximately 32°. The reader is referred to O’ Dwyer et al. (2018, 2019) for additional details on
127 the project.

128

129 *Monitored results: structure of jacking force data*

130 The output data from the TBM was recorded at 200 mm intervals of jacked distance. Due to a
131 technical issue with the data acquisition system, data for Drive A were only recorded beyond a
132 jacked distance of 62 m. The development of total jacking force with jacked distance is shown in
133 Figs 3(a) and 3(b) for Drives A and B respectively. From both figures, it can be seen that the data
134 contains a number of important ‘features’ that are desirable to capture within a data-driven
135 approach: (a) a global linear trend representing an increase in frictional resistance with jacked
136 distance, (b) occasional, discontinuous and transient peaks representing the influence of
137 stoppages and (c) minor fluctuations arising from miscellaneous site factors such as pipe
138 misalignments and TBM driving style.

139

140 **GAUSSIAN PROCESSES**

141 *Gaussian Process regression*

142 A GP is a stochastic method involving a collection of random variables of which any finite number
143 follow a joint Gaussian distribution (Rasmussen and Williams, 2006). GPs provide a method to
144 perform Bayesian inference about functions in a non-parametric way. One of the key aspects of
145 GPs is the use of covariance functions (also known as ‘kernels’) which encodes prior assumptions
146 about the functions one wishes to learn (in this case the monitored data). This avoids reliance on
147 algebraic mapping between inputs and outputs. The overall aim of the process is to learn a
148 regression model of the form $y = f(x) + \epsilon$, where $f(x)$ is a latent function representing the underlying
149 structure of the data and $\epsilon \sim (0, \sigma^2)$ is a noise term where σ^2 is the variance of the noise. Given
150 training dependent function values $\mathbf{Y} = \{y_1, y_2, \dots, y_n\}$ evaluated at locations $\mathbf{X} = \{x_1, x_2, \dots, x_n\}$, the

151 objective is to obtain the value of the predictand $\mathbf{Y}^* = \{y^*_1, y^*_2, \dots, y^*_m\}$ at known values of $\mathbf{X}^* = \{x^*_1,$
 152 $x^*_2, \dots, x^*_m\}$. A Gaussian distribution can be completely described by a mean vector, $\mu(x)$, and
 153 covariance function $k(x, x')$ of input pairs x and x' to describe an underlying real process $f(x)$ as
 154 follows:

$$\mu(x) = \mathbb{E}[f(x)] \quad (1)$$

$$k(x, x') = \mathbb{E} \left[(f(x) - \mu(x))(f(x') - \mu(x'))^T \right] \quad (2)$$

155 The GP can therefore be defined as:

$$f(x) \sim \mathcal{GP}(\mu(x), k(x, x')) \quad (3)$$

156 where the symbol ' \sim ' means 'distributed according to'. In this study, noise terms are added to the
 157 diagonal of the covariance matrix, to account for noisy observations. This is equivalent to adding a
 158 covariance function of the following form:

$$k(x_i, x_j) = \delta_{i,j} \sigma^2 \quad (4)$$

159 where $\delta_{i,j}$ is the Kronecker delta function. Parameters of the covariance functions, referred to as
 160 hyperparameters, define the exact form of the function and are inferred by training on the observed
 161 monitored data. The likelihood of the observed data can be estimated by marginalising over the
 162 latent function \mathbf{f} :

$$p(\mathbf{Y}|\mathbf{X}) = \int_{\mathbf{f}} p(\mathbf{Y}|\mathbf{f}, \mathbf{X}) p(\mathbf{f}|\mathbf{X}) d\mathbf{f} \quad (5)$$

163 The process of learning hyperparameters, θ , from data is achieved using an empirical Bayes
 164 approach by maximising the log likelihood function:

$$\log p(\mathbf{y}|\mathbf{X}, \theta) = -\frac{1}{2} \log |\mathbf{K}_{\mathbf{x}, \mathbf{x}} + \sigma^2 \mathbf{I}| - \frac{1}{2} \mathbf{Y}^T [\mathbf{K}_{\mathbf{x}, \mathbf{x}} + \sigma^2 \mathbf{I}]^{-1} \mathbf{Y} - \frac{n}{2} \log(2\pi) \quad (6)$$

165 where \mathbf{I} is the identity matrix, n is the number of training cases and $\mathbf{K}_{\mathbf{x}, \mathbf{x}}$ denotes the covariance
 166 matrix. This process incorporates a trade-off between model fit and complexity. A Bayesian
 167 formulation can subsequently be adopted to forecast the function outputs \mathbf{f}^* at inputs \mathbf{X}^* , having

168 observed \mathbf{Y} (a noisy observation of the underlying function \mathbf{f}) corresponding to \mathbf{X} . The joint
 169 probability of \mathbf{Y} and \mathbf{f}^* that is conditional on \mathbf{X} and \mathbf{X}^* can be obtained as follows:

$$p\left(\begin{bmatrix} \mathbf{y} \\ \mathbf{f}^* \end{bmatrix}\right) = N\left(\begin{bmatrix} \mathbf{y} \\ \mathbf{f}^* \end{bmatrix} \middle| \begin{bmatrix} \boldsymbol{\mu} \\ \boldsymbol{\mu}^* \end{bmatrix}, \begin{bmatrix} \mathbf{K} + \sigma^2 \mathbf{I} & \mathbf{K}_{\mathbf{x}, \mathbf{x}^*} \\ \mathbf{K}_{\mathbf{x}, \mathbf{x}^*}^T & \mathbf{K}_{\mathbf{x}^*, \mathbf{x}^*} \end{bmatrix}\right) \quad (7)$$

170 The posterior predictive density of \mathbf{f}^* , conditioned on the observed monitored data, can finally be
 171 defined as:

$$p(\mathbf{f}^* | \mathbf{X}^*, \mathbf{X}, \mathbf{Y}) = N(\mathbf{M}^*, \boldsymbol{\Sigma}^*)$$

$$\mathbf{M}^* = \mathbf{K}_{\mathbf{x}, \mathbf{x}^*}^T [\mathbf{K}_{\mathbf{x}, \mathbf{x}} + \sigma^2 \mathbf{I}]^{-1} \mathbf{Y} \quad (8)$$

$$\boldsymbol{\Sigma}^* = \mathbf{K}_{\mathbf{x}^*, \mathbf{x}^*} - \mathbf{K}_{\mathbf{x}, \mathbf{x}^*}^T [\mathbf{K}_{\mathbf{x}, \mathbf{x}} + \sigma^2 \mathbf{I}]^{-1} \mathbf{K}_{\mathbf{x}, \mathbf{x}^*}$$

172 *Covariance functions*

173 The ‘core’ covariance functions adopted for this study are defined in Table 1 and include linear,
 174 periodic, squared exponential, Matérn 5/2 and Matérn 3/2 functions. The structure of each core
 175 covariance function is illustrated in Fig. 4. The linear covariance function, k_{LIN} , is non-stationary and
 176 can be obtained from linear regression. The periodic covariance function, k_{PER} , is a stationary
 177 covariance function that enables modelling of periodic functions. It is parameterised by a length-
 178 scale l and periodicity parameter, p . The squared exponential covariance function, k_{SE} , (often
 179 referred to as the radial basis function) is a stationary and infinitely differentiable covariance
 180 function parameterised by a length-scale parameter l . Finally, the Matérn class of covariance
 181 functions are stationary and represent a generalisation of k_{SE} (Matérn 1960). These covariance
 182 functions are parameterised by a length-scale parameter l . An additional parameter ν controls the
 183 smoothness of the learned function but is not optimised based on the training data, unlike l . For $\nu =$
 184 ∞ , the covariance function is equivalent to k_{SE} . Popular intermediate values used here are $\nu = 5/2$
 185 (twice differentiable) and $\nu = 3/2$ (once differentiable). The influence of ν on the structure of a
 186 sample drawn from a GP is qualitatively illustrated in Fig. 5.

187 These core covariance functions can be combined (summation, multiplication etc.) to create
 188 customized covariance functions to model complex processes. This is because the direct sum and

189 the tensor product of multiple covariance functions are also covariance functions. For example,
190 while k_{PER} corresponds to an exact periodic structure, $k_{\text{LIN+PER}} = k_{\text{LIN}} + k_{\text{PER}}$ corresponds to a
191 periodic structure with a global linear trend (see Fig. 6). In this study, only covariance function
192 summation is considered as this has been shown to be sufficiently capable of capturing complex
193 data structures (Duvenaud, 2014). By summing covariance functions, the data is modelled as a
194 superposition of independent functions representing different structures present in the data shown
195 in Fig. 3. All possible pairs of the core covariance functions in Table 1 were considered for
196 analysis. Recognising that the summation of two linear covariance functions yields the same result
197 as a single linear covariance function, this leaves a total of 19 combinations to be assessed. For
198 this work, the GP models were developed using Scikit-Learn (Pedregosa et al., 2011) within
199 Python 3.6.

200

201 **GP FORECASTING: IMPLEMENTATION**

202 The implementation of the proposed approach is illustrated in Fig. 7. Filtering feature selection,
203 using the Pearson correlation matrix technique, was adopted to identify the most discriminant
204 parameters recorded by the TBM for the prediction of total jacking force. As a result of this
205 process, TBM records of time and jacked distance are used as the GP model inputs whereas total
206 jacking force represents the model output. During training, the GP model autonomously develops a
207 relationship between jacked distance, time (and tacitly penetration rate, stoppage duration) and
208 total jacking force within a probabilistic framework. Gaussian process training and forecasting is
209 performed using a sliding window approach. The forecast origin is defined as the last point of the
210 known (monitored) value from which the GP forecast is to be performed. The forecast horizon, h , is
211 the number of steps into the future for which the forecasts are to be performed. The GP model is
212 retrained and forecasts are performed by sequentially moving newly-acquired data to the training
213 set, as shown in Fig. 8(a) for a fixed forecast horizon and Fig. 8(b) for 'long-term forecasting'. If the
214 size of the training dataset exceeds a maximum size, r , then the oldest datapoint is discarded.

215 In this work, a $100(1-\alpha)\%$ prediction interval (PI) is adopted:

$$PI_{t+1} = \hat{y}_{t+1} \pm t_{\alpha/2, n-n_p} \times s \times \sqrt{h} \quad (9)$$

216 where \hat{y}_{t+1} denotes the forecast for step $t + 1$ made at step t , $t_{\alpha/2, n-n_p}$ is the $\alpha/2$ quantile of a t -
 217 distribution with $n - n_p$ degrees of freedom, n_p is the number of parameters in the model and s is
 218 the square root of the mean of the squared prediction residuals in the training dataset. In this
 219 paper, a significance level of 1% ($\alpha = 0.01$) is initially adopted as default to ensure all peaks in
 220 jacking force are captured. The root mean squared error (RMSE) is used to define the error
 221 between the mean GP forecast and the monitored data as follows:

$$RMSE = \sqrt{\frac{1}{k} \sum_{i=1}^k (f_i^* - y_i^*)^2} \quad (10)$$

222 where k is the total number of forecasts made. In all cases, the forecast accuracy is computed by
 223 averaging over the test sets.

224

225 **FORECASTING RESULTS: DRIVE A**

226 *Influence of GP covariance function*

227 Fig. 9 shows the results of the GP forecasting, using the RMSE defined in equation (10), for all 19
 228 instances of the covariance function and for four different forecast horizons: $h = 1$ (0.2 m; ‘short-
 229 term’), $h = 12$ and 50 (2.4 m, approximately one pipe length, and 10 m; ‘medium-term’), and long-
 230 term (variable h). The short- and medium-term forecasting was performed using the approach
 231 outlined in Fig. 8(a) whereas the long-term forecasting used the approach outlined in Fig. 8(b). In
 232 these initial analyses, no maximum has been imposed on the size of the training dataset i.e. $r = \infty$.

233 It can be observed that short-term forecasts of the total jacking force determined using the linear
 234 covariance function, k_{LIN} , are the least accurate. This is because the simplified structure of this
 235 covariance function is not capable of capturing the complex relationship between jacked distance,
 236 time and force (henceforth referred to as the ‘distance-time-force relationship’). Conversely, the
 237 best short-term forecast accuracy is achieved using the $k_{MAT3+MAT5}$ covariance function.

238 Interestingly, the performance of the covariance functions appears to be most closely linked to the

function's 'smoothness', controlled by ν , where k_{Mat3} ($\nu = 3/2$) provides the best forecast accuracy, followed by k_{Mat5} ($\nu = 5/2$) and k_{SE} ($\nu = \infty$). This finding is perhaps more obvious when the structure of the monitored data presented in Fig. 3 is compared with those of the covariance functions in Fig. 5.

With the exception of long-term forecasts performed using covariance functions comprising a periodic element, an increase in h causes a deterioration in forecast accuracy. This is because the uncertainty of a forecast increases in proportion to h . For greater forecast horizons, covariance functions comprising k_{LIN} generate the most accurate GP forecasts because of its simple structure and independence of a length-scale parameter, l . In general, it is not possible to accurately extrapolate more than l units away from the origin. As variations in the monitored data occur over short intervals of jacked distance, the optimised values of l are low and therefore forecasts quickly return to the mean of the prior. This leads to a deterioration in the accuracy of forecasts generated using covariance functions comprising a length-scale dependency for greater forecast horizons.

Forecasts of the development of the total jacking force with jacked distance determined using the most accurate GP covariance functions are plotted in Fig. 10 for short- and medium-term forecasting and for $r = \infty$. In these plots, a solid line is used to denote the GP best-estimate whereas a shaded region denotes the 99% PI defined by equation (9). From Fig. 10(a), the structure of the data, particularly stoppage-induced peaks in jacking force, appear to be well-captured by the $k_{\text{MAT3+MAT5}}$ GP where all peaks are encapsulated by the 99% PI. This highlights the ability of the GP model to automatically establish a site-specific probabilistic relationship between stoppage time and jacking force. Similar observations can be drawn from the results presented in Figs. 10(b) and 10(c) using $k_{\text{LIN+SE}}$ and k_{LIN} respectively. In this case, the 99% PI is larger due to forecasting $h = 12$ and 50 steps ahead respectively. While there is a deterioration in the agreement between the GP best-estimates and the monitored data, the 99% PI provides a safe estimate of the maximum total jacking force.

Long-term GP forecasts using the most accurate covariance function (in this case k_{LIN}) is shown in Fig. 11 for three arbitrary instances of the forecast origin. The much greater forecast horizon causes a significant increase in the uncertainty of the forecasts and therefore also the 99% PI.

267 While there is a clear deterioration in the fidelity of the GP's forecast of the distance-time-force
268 relationship, the GP provides excellent forecasts of the linear friction trend in all instances.

269

270 *Influence of maximum training window size*

271 Application of the proposed approach necessitates the inversion of an $n \times n$ matrix which may
272 become computationally demanding for large training datasets i.e. for long drives (c.f. equation
273 (8)). Fig. 12 explores a 'computationally light' implementation of the proposed approach by
274 imposing a maximum size, r , on the training dataset where all four forecast horizons have again
275 been considered. In this case, the RMSE has been normalised by the corresponding $r = \infty$ value
276 (i.e. no maximum has been imposed). Intuitively, a reduction in r causes a gradual increase in
277 forecast error because there is an insufficient amount of data to accurately describe the distance-
278 time-force relationship. The results also suggest that long-term forecasting requires more data to
279 reliably capture the long-term friction trend. By way of example, short- and medium-term forecasts
280 determined using the extreme case of $r = 2.4$ m (approximately one pipe length) are presented in
281 Fig. 13. It can be seen that insufficient training data causes the GP to provide poor predictions of
282 stoppage-induced peaks in jacking force. Nevertheless, the results in Fig. 12 show that the
283 selection of 'intermediate' values of r allows the proposed approach to be optimised for real-time
284 implementation for a modest trade-off in the forecast accuracy; these 'optimal' values are
285 presented in Table 2 and were determined based on computational time and forecast accuracy.

286

287 *Influence of prediction interval*

288 While the previous results highlight the ability of the proposed GP model to provide a 'best-
289 estimate' of the total jacking force, it is more common for a safe 'upper bound' estimate to be used
290 in design. Rather than using a single upper bound estimate, the GP model provides an expedient
291 approach to derive a probabilistic upper bound. To this end, Figs. 14 and 15 plot GP forecasts for
292 various forecast horizons using the optimal parameters presented in Table 2. Three prediction
293 intervals have been considered for these comparisons: 99%, 90% and, as an extreme case, 50%.

It can be seen that for short-term forecasting, the prediction intervals are tightly-banded given the high level of certainty in the forecasts (see Fig. 14(a)). In this case a PI = 99% is necessary to capture all peaks in jacking force. An increase in h to 12 and 50 causes an increase in the range of the prediction intervals as shown in Figs. 14(b) and 14(c) respectively. While a 99% PI provides an appropriate upper bound forecast for $h = 1$ and 12, it provides a conservative estimate of the upper bound in Fig. 14(c); in this instance PI = 90% is sufficient. Similar findings may be deduced from Fig. 15 where it can be seen that the PI = 99% and 90% appear overly-conservative because of the large forecast horizon. The proposed methodology therefore allows the engineer the flexibility to develop an upper bound envelope of the jacking force corresponding to a desired risk level.

303

304 **VALIDATION OF PROPOSED APPROACH: DRIVE B**

305 *Existing jacking force design methods*

To validate the proposed methodology, forecasts of Drive B are compared to predictions determined using existing design guidelines commonly used in industry. The Pipe Jacking Association (PJA 1995) design guidance recommends that the face resistance, F_0 , is taken to be at least the total horizontal stress, σ_h , acting on the cutterhead face:

$$F_0 = \sigma_h \frac{\pi D_c^2}{4} \quad (11)$$

310 The frictional resistance acting on the pipe string in cohesionless soils is defined as follows:

$$F_s = \frac{\pi D_c}{2} (\sigma'_v + \sigma'_h) \tan \delta \cdot L \quad (12)$$

$$\sigma'_v = \frac{\gamma B}{K \tan \phi'} \left(1 - e^{-\frac{K \tan \phi' z_w}{B}} \right) e^{-\frac{K \tan \phi' (H - z_w)}{B}} + \frac{\gamma' B}{K \tan \phi'} \left(1 - e^{-\frac{K \tan \phi' (H - z_w)}{B}} \right) \quad (13)$$

$$\sigma'_h = K(\sigma'_v + 0.5\gamma' D_c) \quad (14)$$

$$B = \frac{D_c}{2} \tan \left(45^\circ - \frac{\phi'}{2} \right) + \frac{D_c}{2 \sin \left(45^\circ + \frac{\phi'}{2} \right)} \quad (15)$$

$$K = \frac{1 - \sin \phi'}{1 + \sin \phi'}$$

311 where σ'_v and σ'_h are the vertical and horizontal effective soil stresses respectively, δ is the pipe-
 312 soil interface friction angle, L is the current drive length, z_w is the depth of the water level below the
 313 ground surface, γ and γ' are the total and effective soil unit weights respectively, K is the coefficient
 314 of lateral earth pressure and H is the cover depth measured from the tunnel crown. The
 315 recommended interface friction angle for a concrete pipe in cohesionless soil is $0.7\phi' < \delta < 0.9\phi'$
 316 (PJA 1995); a value of $\delta = 0.8\phi'$ has therefore been adopted. The influence of stoppages is
 317 accounted for by augmenting the value of F_s determined using equation (12) by 50% (PJA 1995).
 318 More recently, Staheli (2006) proposed an alternative expression for F_s :

$$F_s = \frac{\mu_r \cdot \gamma \cdot D_p \cdot \cos(45^\circ + \frac{\phi'_r}{2})}{2 \cdot \tan \phi'_r} \cdot \pi \cdot D_p \cdot L \quad (16)$$

319 where μ_r and ϕ'_r are the residual interface friction coefficient and residual soil friction angle
 320 respectively. In this case, the widely adopted relationship for μ_r for microtunnelling operations has
 321 been adopted (Japan Microtunnelling Association 2000; Pellet-Beacour and Kastner 2002;
 322 Sofianos et al. 2004; Staheli 2006; Shou et al. 2010):

$$\mu_r = \tan\left(\frac{\phi'}{2}\right) \quad (17)$$

323 Instead of a prescriptive design method, the Concrete Pipe Association of Australasia (CPAA
 324 2013) present typical values for the jacking resistance per unit area of the external surface of the
 325 pipe string, as shown in Table 3. These guidelines also recommend an additional 20-50% to
 326 account for stoppage-induced increases in jacking force (50% has again been adopted here).

327

328 *Application: forecasting Drive B jacking forces*

329 For the GP forecasts of Drive B, the optimal parameters presented in Table 2 have been adopted.
 330 Also superimposed on these plots are the predictions determined using the PJA (1995), Staheli
 331 (2006) and CPAA (2013) design methods. The shaded region associated with the PJA (1995) and

CPAA (2013) predictions represent the recommended additional 50% increase in jacking force to account for stoppage-induced peaks. The results presented in Fig. 16 show that the 99% PI provides a very good upper bound estimate of the maximum jacking forces for all three forecast horizons. Conversely, the jacking forces are significantly over-predicted by the existing prescriptive design methods. This is likely due to an over-prediction of both the coefficient of friction for lubricated interfaces and the normal soil stresses exerted on the pipe string. This reflects the effectiveness of modern lubrication systems in reducing friction during microtunnelling and suggests that the use of historical pipe jacking parameters may provide overly conservative predictions.

Similar conclusions can be drawn from an examination of the long-term forecasting results presented in Fig. 17. In this case, the 99% PI estimate appears overly-conservative and even a 50% prediction interval appears to provide a safe envelope. Nevertheless, all three bounds represent an improvement on the predictions determined using the existing design methods. The traditional design methods correspond to less than a 50% prediction interval during the initial stages of the drive (see Fig. 17(a)) whereas they significantly exceed a 99% prediction interval as the drive progresses (see Fig 17(b) and 17(c). These results highlight one of the key benefits of the GP-based approach, namely its ability to quantify the uncertainty associated with the traditional design profile and its flexibility to define bounds based on the desired risk level.

BENEFITS AND LIMITATIONS OF PROPOSED APPROACH

While significant advances have been made in prediction modelling, uncertainty surrounding the assessment of geotechnical parameters and underground conditions remains the main barrier to accurate prediction of construction behaviour (Jin et al. 2018). The observational method is desirable for its potential to save materials, time and costs relative to conventional design approaches (Spross and Johansson 2017). The proposed approach advances existing prescriptive design approaches for microtunnelling jacking forces by integrating the observational method within a Bayesian framework. Key advantages of this technique are that it provides (a) a robust approach for treating signal artefacts encountered in monitored construction data, (b) incorporates

360 uncertainty explicitly into the predictions and (c) the jacking distance-time-force relationship is
361 allowed to adapt dynamically based on the latest information acquired during the drive. It also
362 offers a means of quantifying the uncertainty associated with the traditional design profile and
363 provides the flexibility of defining a probabilistic design profile based on the desired risk level.
364 Furthermore, the model accounts for site-specific variations in slurry conditions, lubricant
365 composition and delivery, and TBM driving style by influencing the monitored data (i.e. the jacking
366 force-time-distance relationship).

367 It is worth noting that the methodology presented in this paper develops a probabilistic model of
368 ‘normality’ based on the monitored data acquired at the time (i.e. the training data). The proposed
369 approach is therefore not capable of forecasting features which are not present in the training data.
370 For the case of unexpected events, such as sudden changes in ground conditions and drive
371 trajectory, and encountering obstacles, the proposed approach can be used to detect deviations of
372 the monitored data from normal working behaviour (i.e. ‘anomaly detection’; see Sheil et al.
373 (2020b) and Chieh et al. (2020) for additional information). It is also noteworthy that this
374 methodology is applied on a *site-specific* basis; application of this technique *across* various sites is
375 likely to necessitate a higher dimensional input dataset.

376

377 **CONCLUDING REMARKS**

378 This paper has described a probabilistic observational approach to forecast jacking forces during
379 microtunnelling using Gaussian Process regression. The proposed approach was applied to two
380 recent UK microtunnelling monitoring projects: Drive A was used to develop the forecasting
381 methodology while Drive B was used for validation. The main conclusions from the study are as
382 follows:

- 383 (a) Covariance functions were used to encode prior assumptions about the monitored data.
- 384 The accuracy of ‘short-term’ forecasting was shown to be most closely linked to the
- 385 ‘smoothness of the covariance function; the best forecast accuracy was achieved using the
- 386 Matérn 3/2 covariance function, followed by the Matérn 5/2 and squared exponential

- covariance functions. The structure of the data, particularly stoppage-induced peaks in jacking force, was well-captured by the GP where all peaks in jacking force were encapsulated by a 99% prediction interval. This highlights the ability of the GP model to automatically establish a site-specific probabilistic relationship between stoppage time and jacking force.
- (b) For 'long-term' forecasting, the best GP performance was achieved using a linear covariance function due to its simplified structure and its independence of a length-scale parameter. The much greater forecast horizon caused a significant increase in the uncertainty of the forecasts, and therefore the 99% prediction interval. While there is a clear deterioration in the fidelity of the GP's forecast of the distance-time-force relationship, the GP provides excellent forecasts of the linear friction trend in all instances.
- (c) A 'computationally light' implementation of the proposed approach was explored by imposing a maximum size on the training dataset. Intuitively, smaller window sizes caused a gradual increase in error because of an insufficient amount of data to accurately describe the distance-time-force relationship. The results also suggest that long-term forecasting requires more data to reliably capture the long-term friction trend compared to short-term forecasting. Nevertheless, the results showed that the proposed approach can be optimised for real-time implementation for a modest trade-off in forecast accuracy.
- (d) Rather than using a single upper bound estimate, the GP model was shown to provide an expedient means of deriving a probabilistic upper bound. For short-term forecasting, a 99% prediction interval is necessary to capture all jacking force peaks. Due to the increased uncertainty associated with long-term forecasting, it was shown that a 99% prediction interval is overly-conservative and even a 50% prediction interval provides a safe upper bound of the expected jacking forces.
- (e) The proposed GP approach provided vastly improved predictions of monitored data from Drive B compared to design methods currently used in industry. Prescriptive design methods are not capable of capturing subtle site-specific variations in the construction process. These results also highlight one of the key benefits of the GP-based approach,

namely its ability to quantify the uncertainty associated with the traditional design profile and its flexibility to define a probabilistic design profile based on the desired risk level.

(f) The results of this study have revealed an exciting potential for probabilistic data-driven methods to complement existing jacking force design methods. It should also be noted that the results presented in this paper pertain to specific TBM/tunnel geometries and soil/lubrication conditions. Further validation and development of the proposed approach for application to more complex scenarios involving curved drives in mixed ground conditions is clearly desirable.

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Table 1 List of core covariance functions including their specific hyperparameters and formulation

Covariance function	Hyperparameters	Formulation
Linear, k_{LIN}	Output variance, σ^2 , inhomogeneity factor, σ_0^2	$\sigma^2(\sigma_0^2 + \langle x, x' \rangle)$
Periodic, k_{PER}	Output variance, σ^2 , length-scale, l , and period p	$\sigma^2 \exp\left(-2 \frac{\sin^2\left(\frac{\pi}{p} x - x' \right)}{l^2}\right)$
Squared exponential, k_{SE}	Output variance, σ^2 , length-scale, l	$\sigma^2 \exp\left(-\frac{(x - x')^2}{2l^2}\right)$
Matérn 5/2, k_{MAT5}	Output variance, σ^2 , and length-scale, l . Smoothness parameter, $\nu = 5/2$ (fixed)	$\sigma^2 \left(1 + \frac{\sqrt{5}r}{l} + \frac{5r^2}{3l^2}\right) \exp\left(-\frac{\sqrt{5}r}{l}\right)$ where $r = \sqrt{(x - x')^T (x - x')}$
Matérn 3/2, k_{MAT3}	Output variance, σ^2 , and length-scale, l . Smoothness parameter, $\nu = 3/2$ (fixed)	$\sigma^2 \left(1 + \frac{\sqrt{3}r}{l}\right) \exp\left(-\frac{\sqrt{3}r}{l}\right)$

Table 2 Optimal covariance functions and training window size composition for all four levels of forecasting

Forecast horizon	Covariance function structure	Maximum size of training window, r
Short-term; $h = 1$ (0.2 m)	$k_{MAT3+MAT5}$	250 (50 m)
Medium-term; $h = 12$ (2.4 m)	k_{LIN+SE}	250 (50 m)
Medium-term; $h = 50$ (10 m)	k_{LIN}	500 (100 m)
Long-term; variable h	k_{LIN}	500 (100 m)

Table 3 Jacking resistance recommendations according to the CPAA (2013) design guidelines

Ground condition	Jacking resistance per unit surface area (kPa)
Rock	2 – 3
Boulder clay	5 – 18
Firm clay	5 – 20
Wet clay	10 – 15
Silt	5 – 20
Dry loose sand	25 – 45

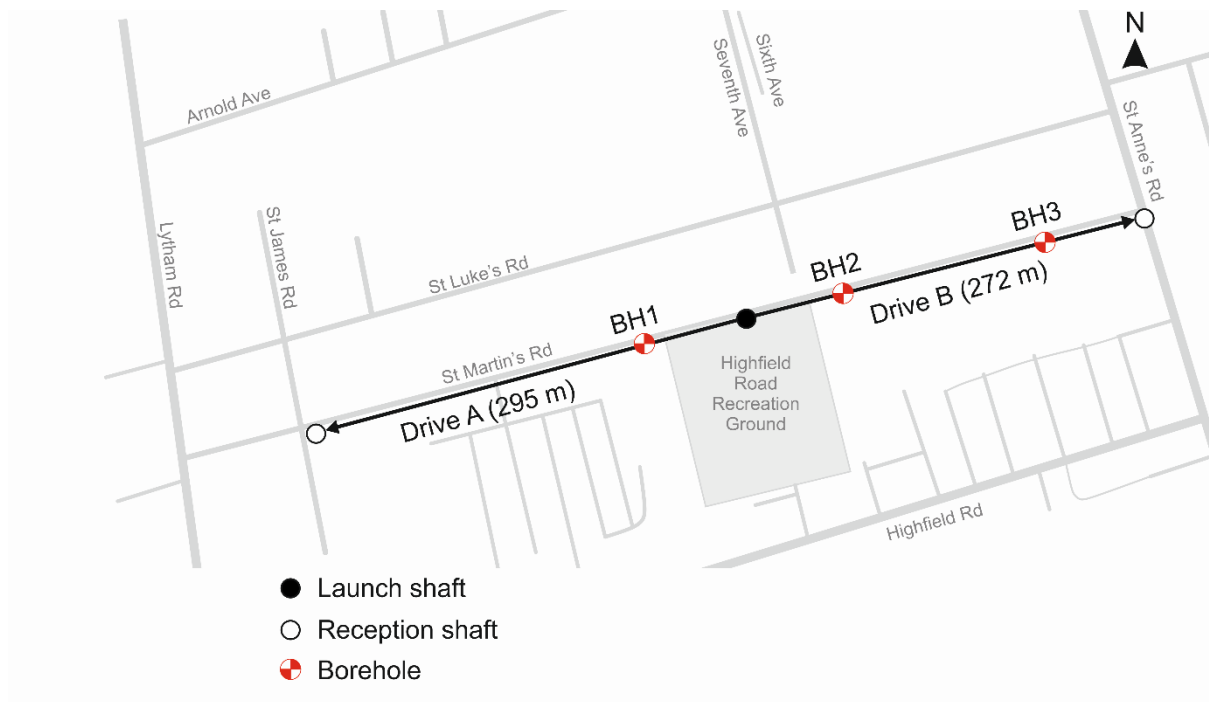


Fig. 1 Location of tunnels and shafts for Drives A and B at the Blackpool site

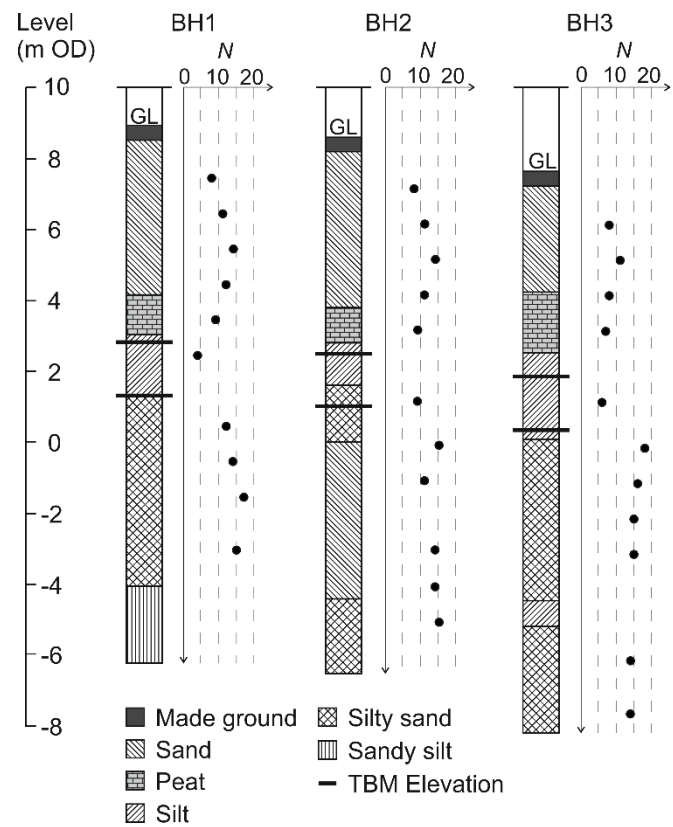


Fig. 2 Stratigraphy at the boreholes along the tunnel drive as well as the associated uncorrected SPT profiles

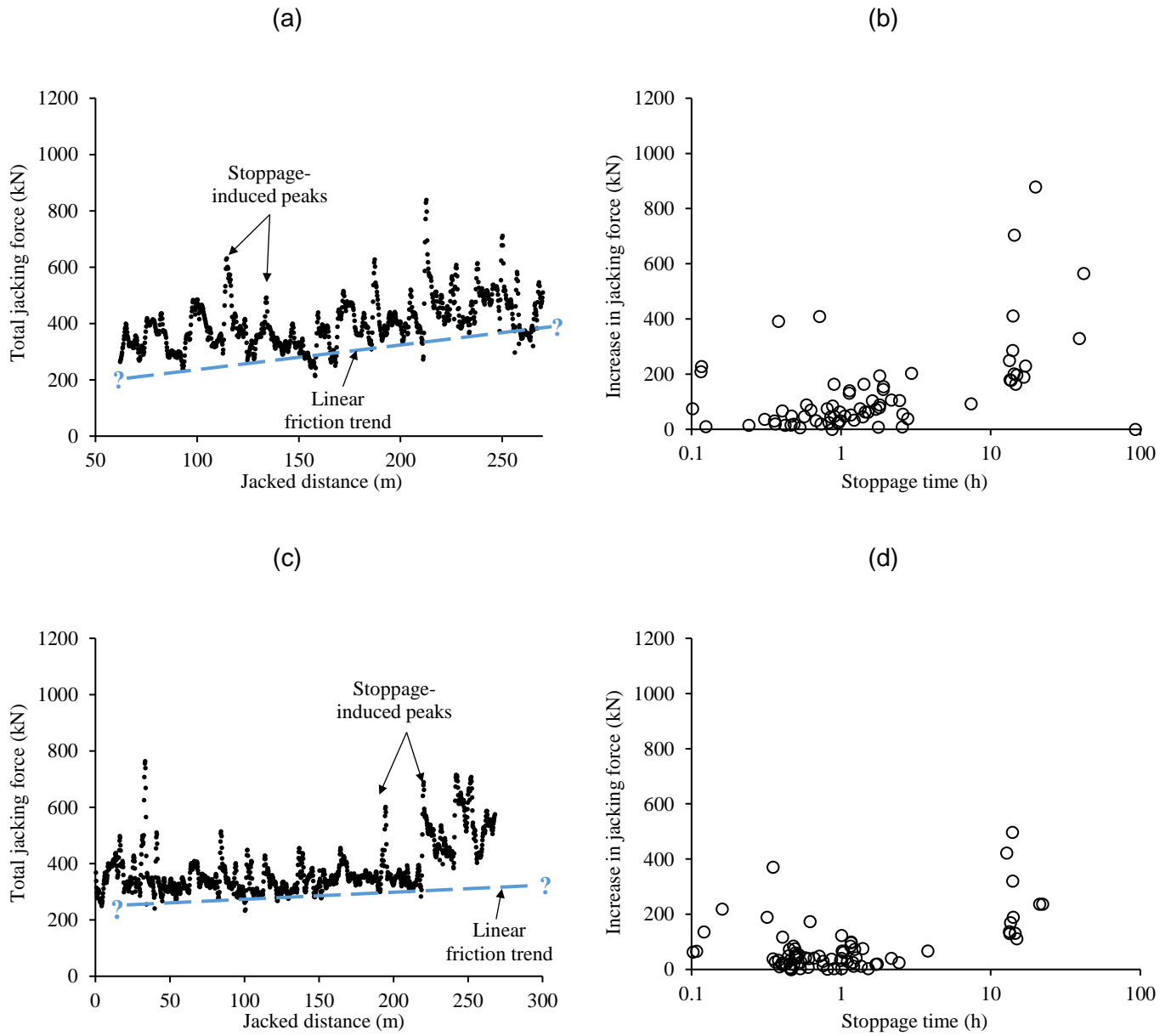


Fig. 3 Monitored data acquired from TBM records showing relationship between (a) total jacking force and jacked distance for Drive A, (b) stoppage time and increase in jacking force for Drive A, (c) total jacking force and jacked distance for Drive B, (d) stoppage time and increase in jacking force for Drive B

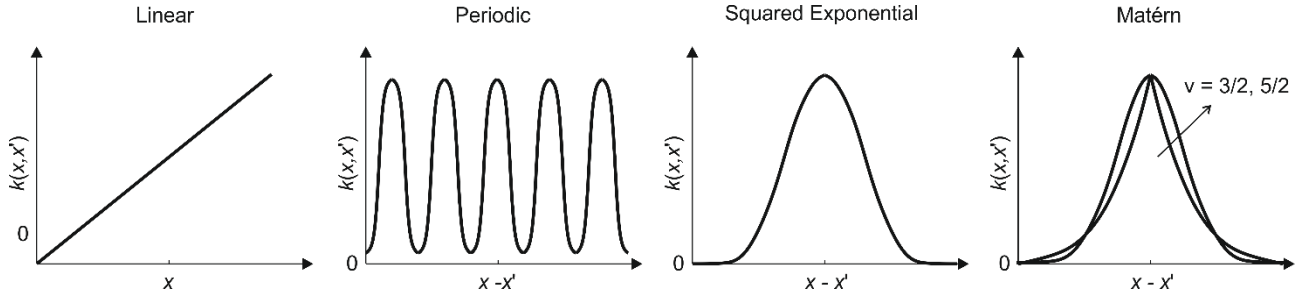


Fig. 4 Illustrations of the structure of the five 'core' covariance functions adopted in this study

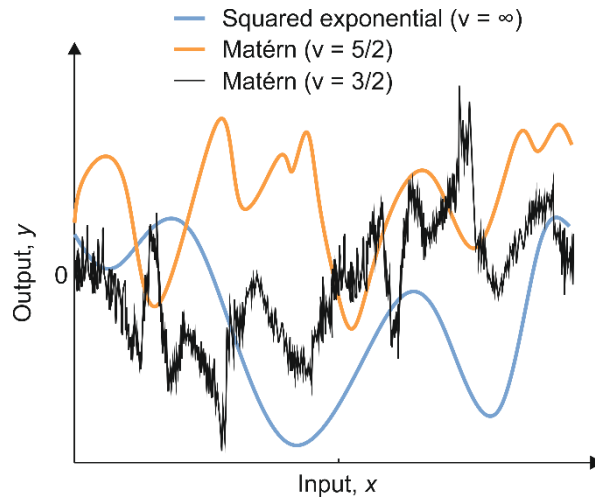


Fig. 5 Illustration of functions randomly drawn from a GP with squared exponential and Matérn covariance functions for different values of v .

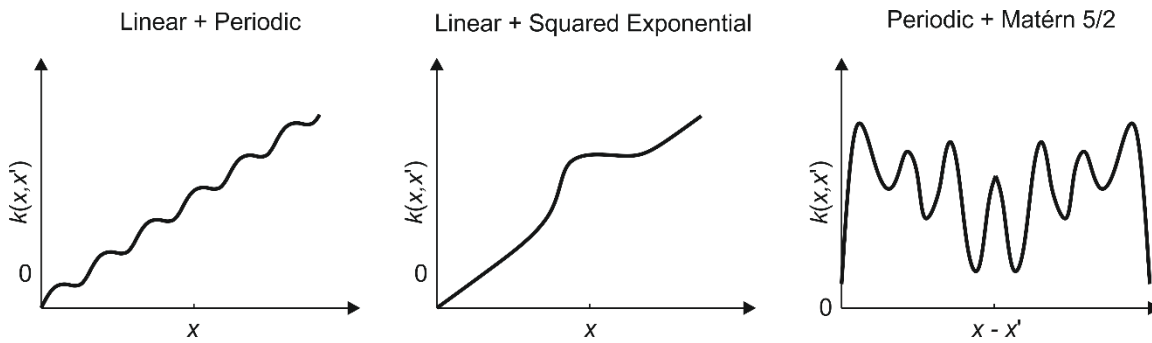


Fig. 6 Illustrations of the structure of covariance functions developed by summing various pairs of the core covariance functions considered in this paper.

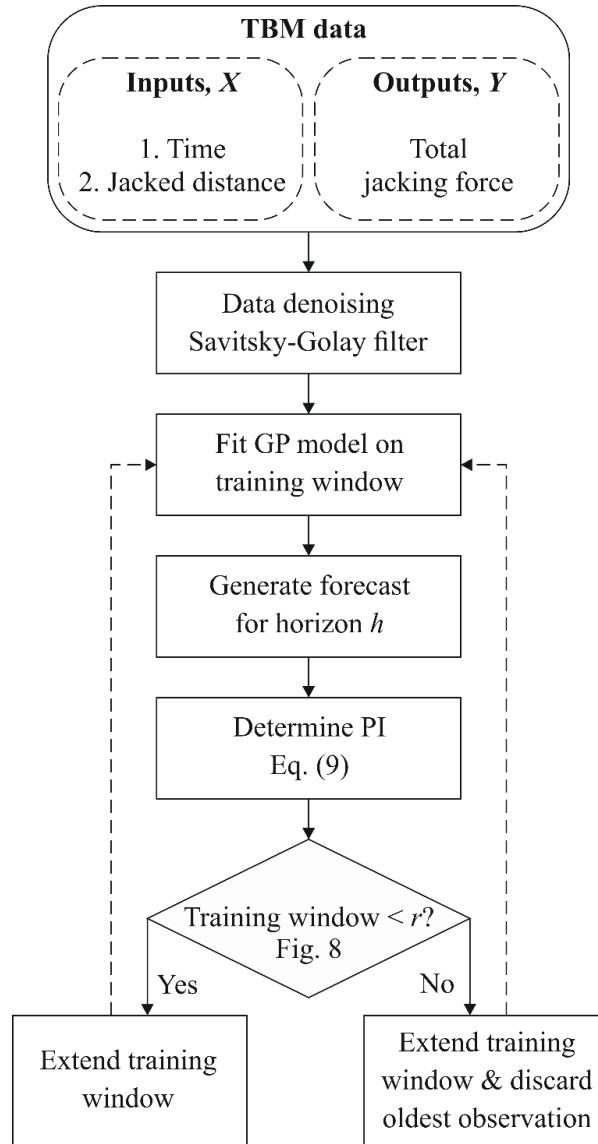


Fig. 7 Implementation of the proposed forecasting strategy

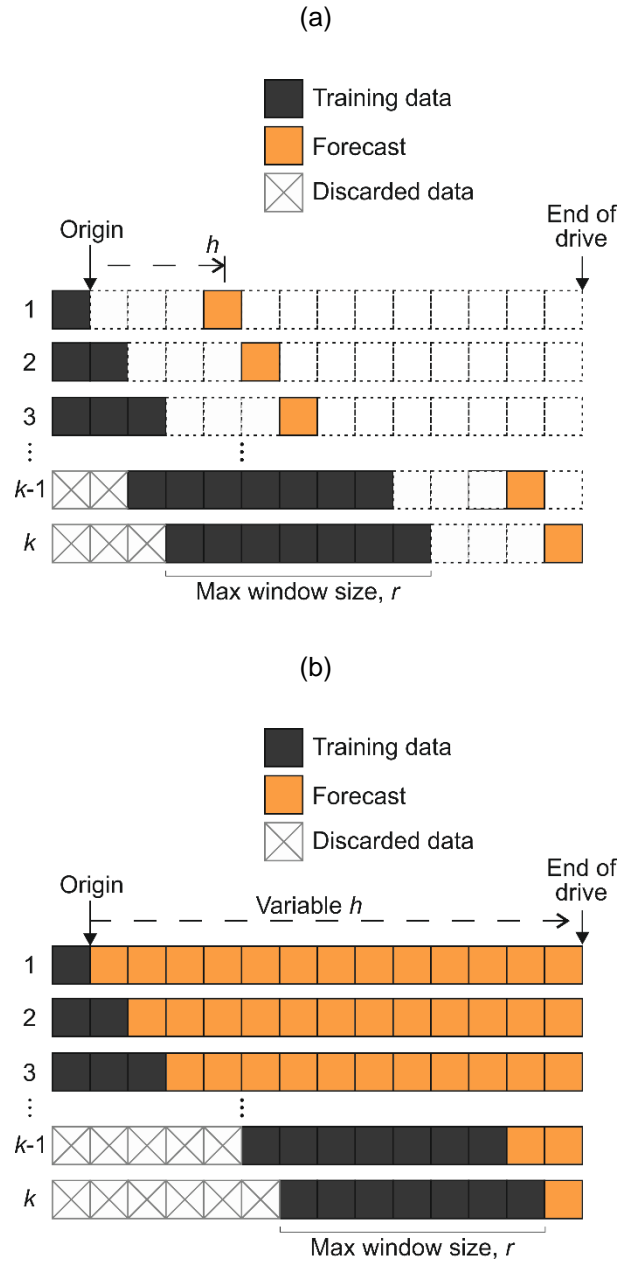


Fig. 8 Illustration of sliding window approach for (a) forecasting h steps ahead and (b) 'long-term' forecasting

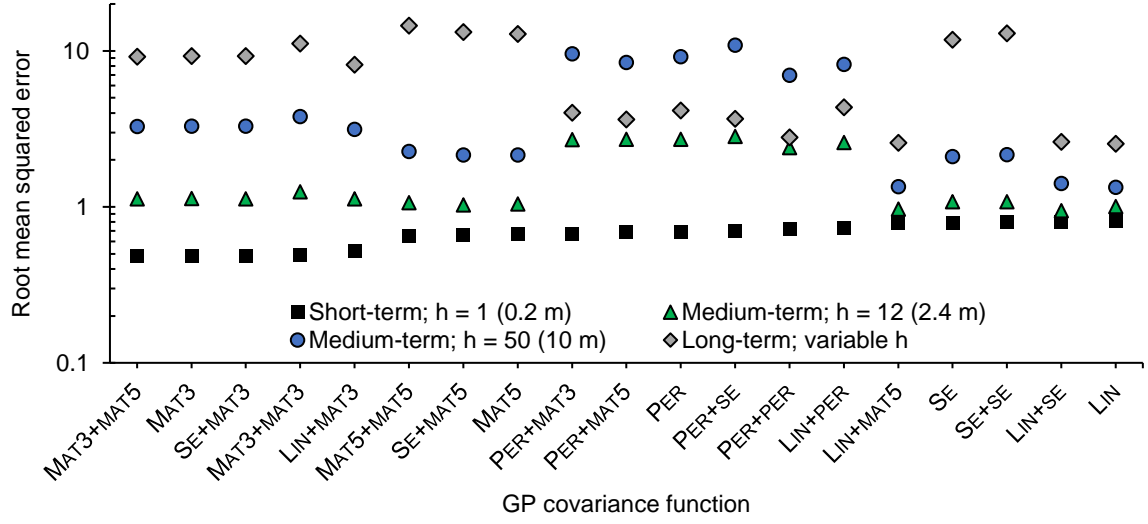


Fig. 9 GP forecasting results using the RMSE defined in equation (10) for all 19 instances of the covariance function and for four different forecast horizons: $h = 1$ (0.2 m; ‘short-term’), $h = 12$ and 50 (2.4 m and 10 m; ‘medium-term’), and long-term (variable h); Drive A, $r = \infty$.

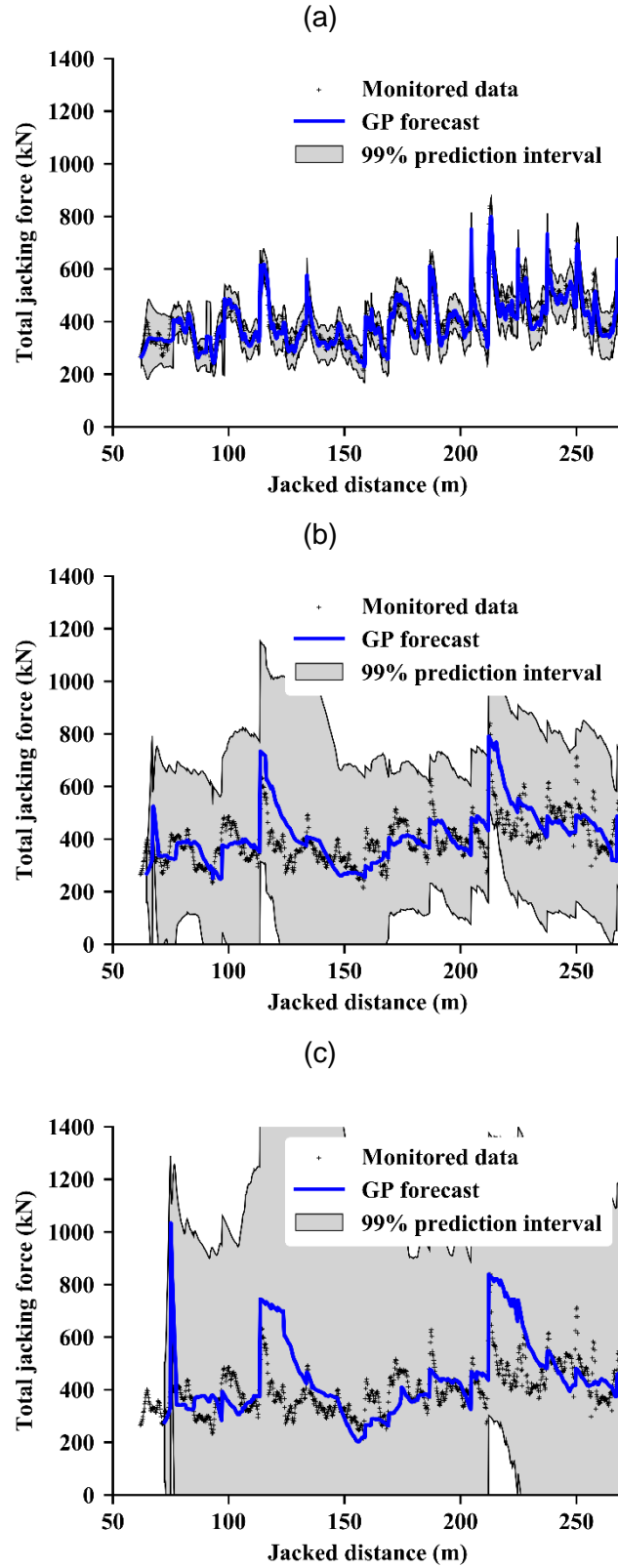


Fig. 10 Short- and medium-term forecasts of the development of total jacking force with jacked distance using the most accurate GP covariance functions compared to the Drive A monitored data: (a) $h = 1$ (0.2 m) using $k_{MAT3+MAT5}$, (b) $h = 12$ (2.4 m) using k_{LIN+SE} , (c) $h = 50$ (10 m) using k_{LIN} ; $r = \infty$

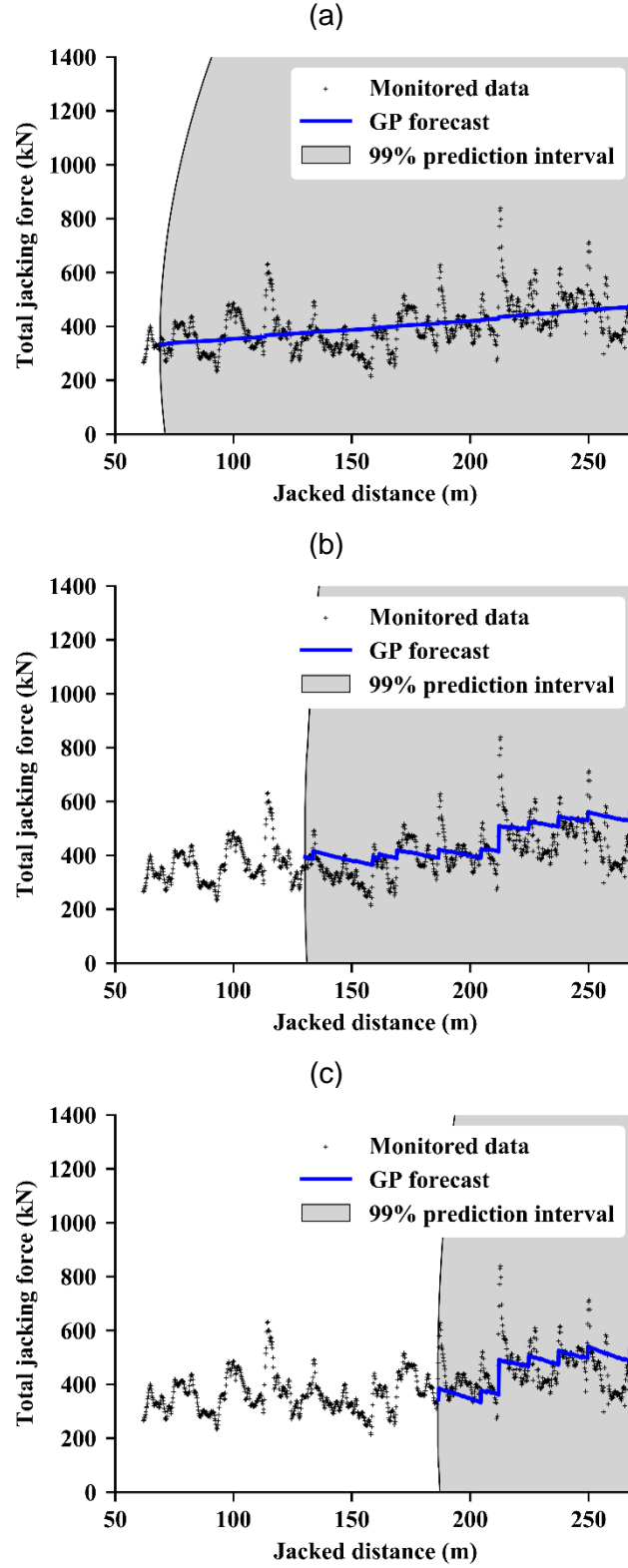


Fig. 11 Long-term forecasts of the development of total jacking force with jacked distance using the best-performing GP covariance function (k_{LIN}) compared to the Drive A monitored data for forecast origins of (a) 69 m ($k = 35$), (b) 130 m ($k = 340$), (c) 192 m ($k = 650$) where k is defined in Fig. 8(b); $r = \infty$

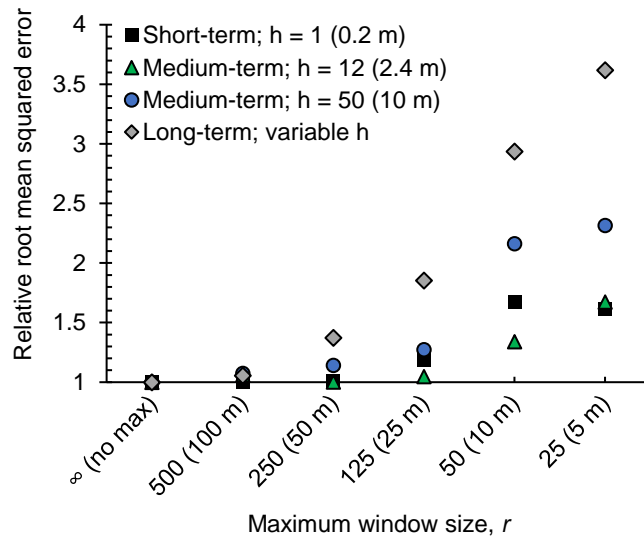


Fig. 12 Influence of the maximum window size, r , on the accuracy of GP forecasts using the RMSE relative to the corresponding $r = \infty$ value for four different forecast horizons; Drive A

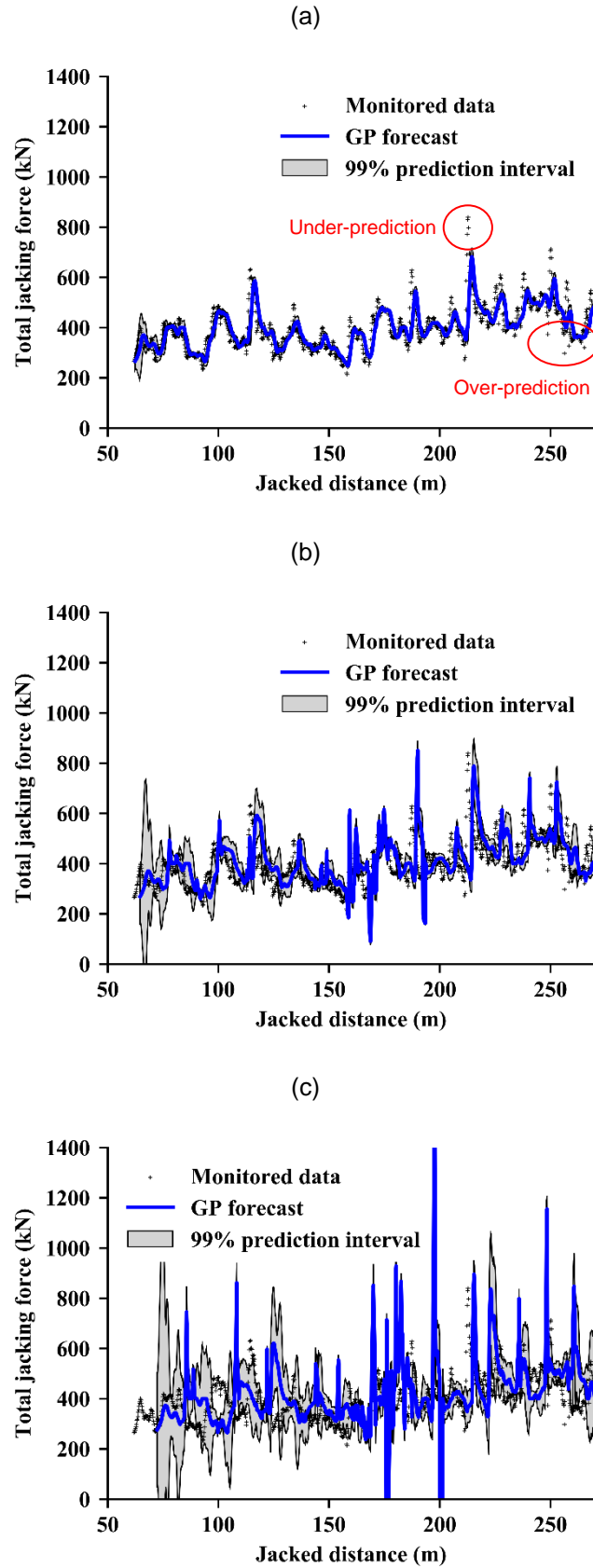


Fig. 13 Short- and medium-term forecasts of the development of total jacking force with jacked distance using the most accurate GP covariance functions with $r = 12$ (2.4 m) compared to the Drive A monitored data: (a) $h = 1$ (0.2 m) using $k_{MAT3+MAT5}$, (b) $h = 12$ (2.4 m) using k_{LIN+SE} , (c) $h = 50$ (10 m) using k_{LIN} .

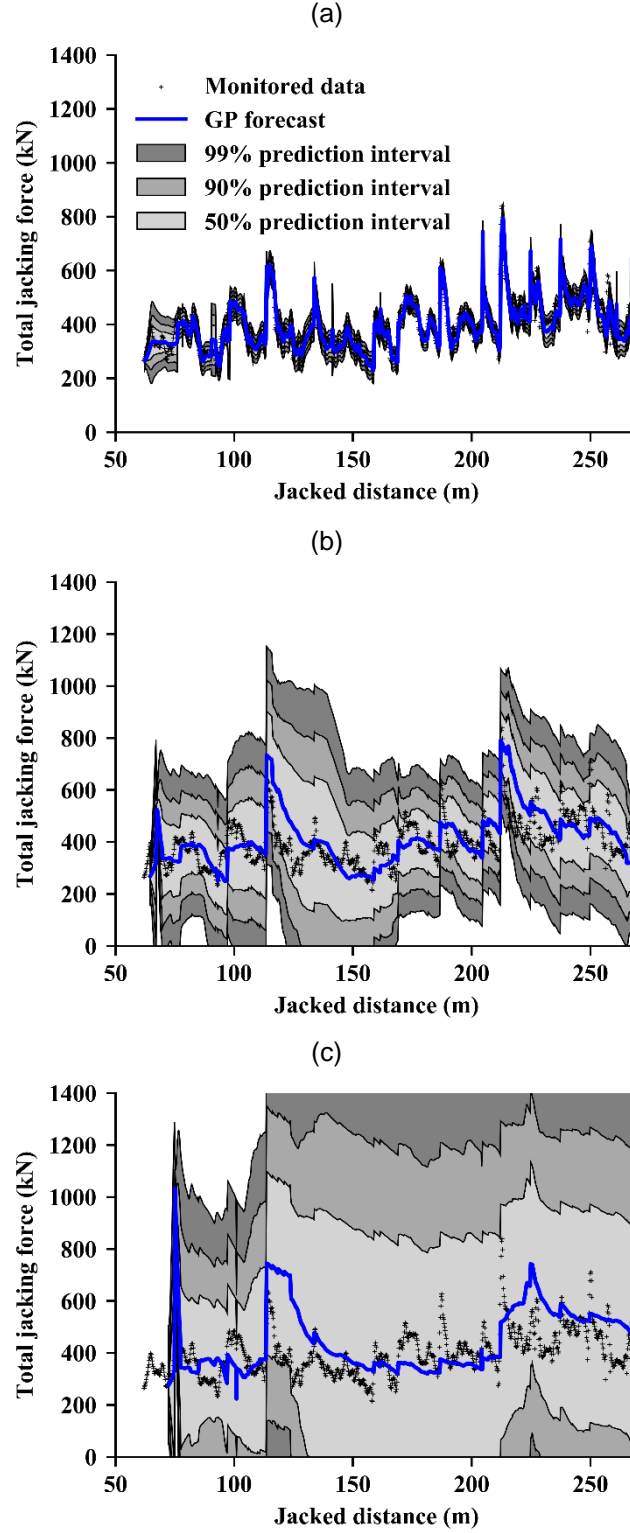


Fig. 14 Influence of prediction interval on short- and medium-term forecasts of maximum jacking forces using the ‘optimal parameters’ presented in Table 2 and compared to the Drive A monitored data: (a) $h = 1$ (0.2 m) using $k_{MAT3+MAT5}$ and $r = 250$, (b) $h = 12$ (2.5 m) using k_{LIN+SE} and $r = 250$, (c) $h = 50$ (10 m) using k_{LIN} and $r =$

500

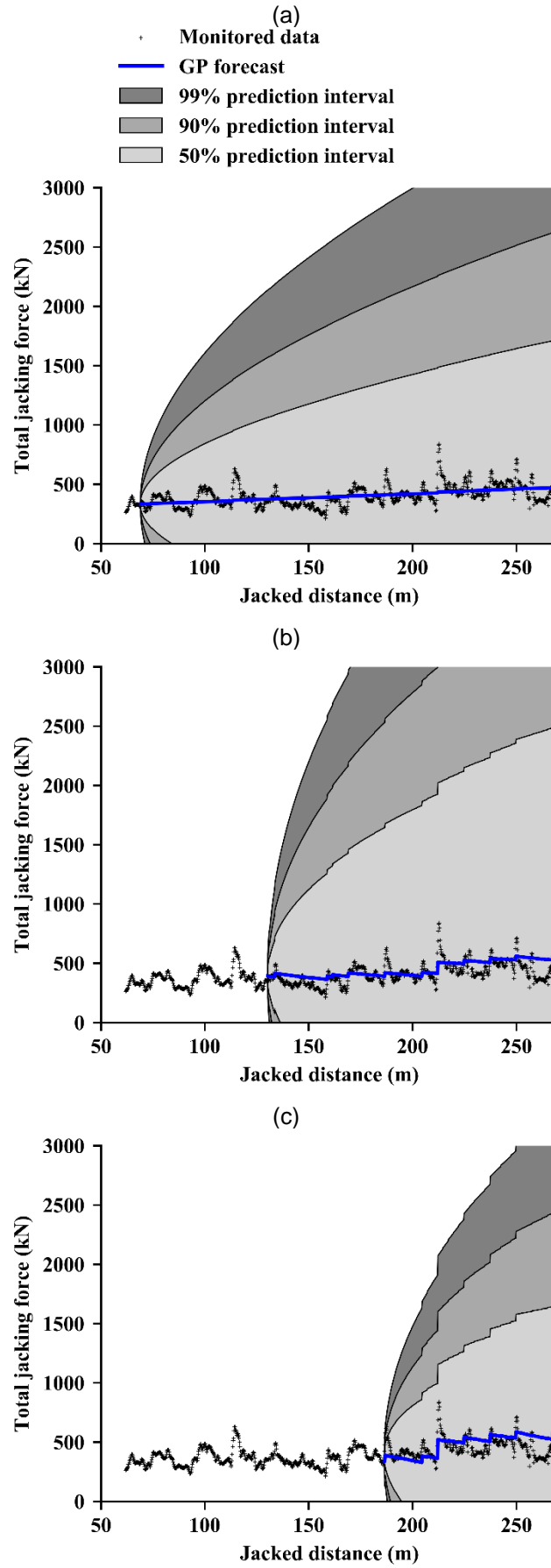


Fig. 15 Long-term forecasts of the development of total jacking force with jacked distance using the best-performing GP covariance function (k_{LIN}) compared to the Drive A monitored data for forecast origins of (a) 69 m ($k = 35$), (b) 130 m ($k = 340$), (c) 192 m ($k = 650$) where k is defined in Fig. 8(b)

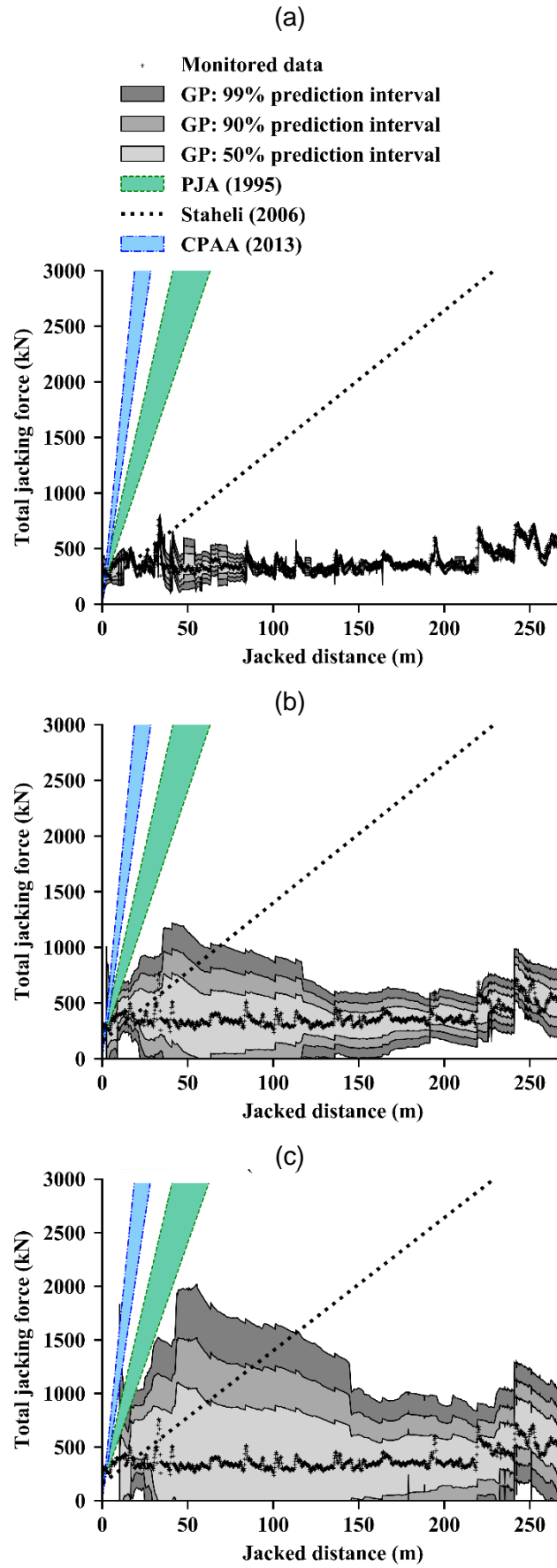


Fig. 16 Comparison of short- and medium-term GP forecasts of Drive B jacking forces with predictions determined using existing design methods: (a) $h = 1$ (0.2 m) using $k_{MAT3+MAT5}$ and $r = 250$, (b) $h = 12$ (2.5 m) using k_{LIN+SE} and $r = 250$, (c) $h = 50$ (10 m) using k_{LIN} and $r = 500$

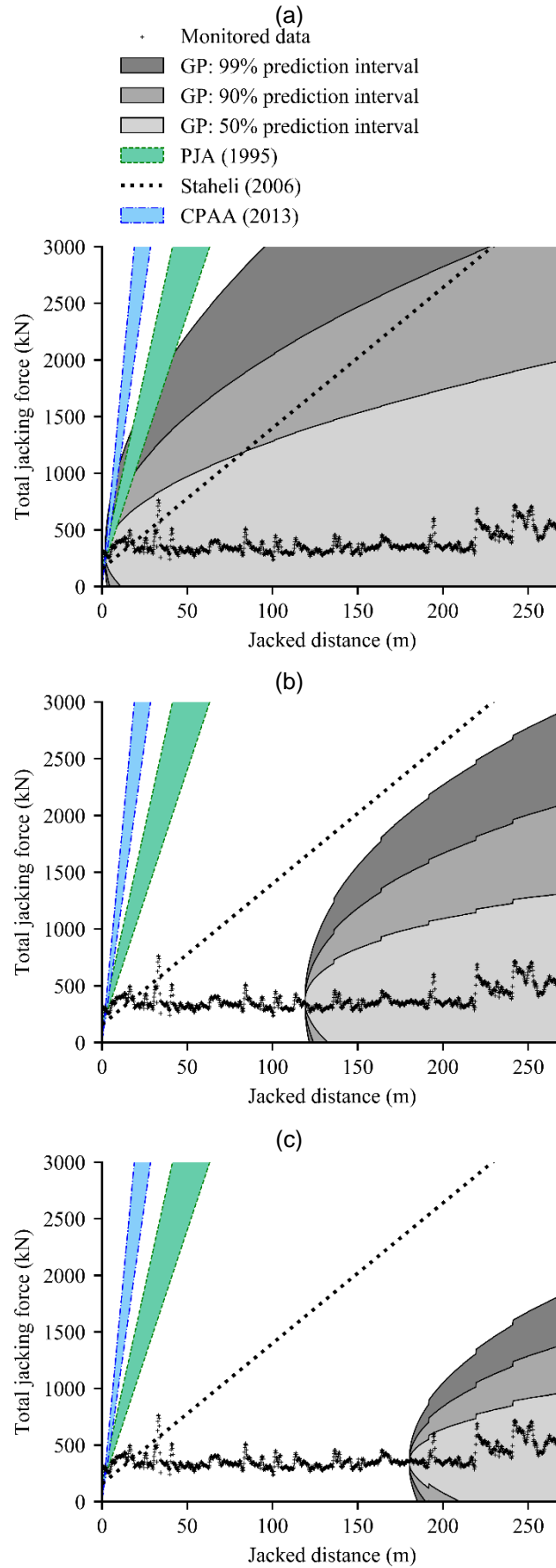


Fig. 17 Comparison of long-term GP forecasts of Drive B jacking forces with predictions determined using existing design guidelines for forecast origins of (a) 2 m ($k = 10$), (b) 117 m ($k = 585$), (c) 177 m ($k = 885$) where k is defined in Fig. 8(b)