



# Rapid pre-explosion increase in dome extrusion rate at La Soufrière, St. Vincent quantified from synthetic aperture radar backscatter

E.W. Dualeh<sup>a,\*</sup>, S.K. Ebmeier<sup>a</sup>, T.J. Wright<sup>a</sup>, M.P. Poland<sup>b</sup>, R. Grandin<sup>c</sup>, A.J. Stinton<sup>d,e</sup>, M. Camejo-Harry<sup>f,e</sup>, B. Esse<sup>g</sup>, M. Burton<sup>g</sup>

<sup>a</sup> COMET, School of Earth and Environment, University of Leeds, Leeds, LS2 9JT, UK

<sup>b</sup> USGS, Yellowstone Volcano Observatory, Vancouver, WA, United States

<sup>c</sup> Université de Paris, Institut de Physique du Globe de Paris, CNRS, Paris, France

<sup>d</sup> Montserrat Volcano Observatory, Flemmings, Montserrat

<sup>e</sup> Department of Earth Sciences, University of Oxford, Oxford, OX1 3AN, UK

<sup>f</sup> The University of the West Indies, Seismic Research Centre, St. Augustine, Trinidad and Tobago

<sup>g</sup> Department of Earth and Environmental Sciences, University of Manchester, Oxford Road, Manchester, M13 9PL, UK

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## ABSTRACT

The extrusion rate of a lava dome is a critical parameter for monitoring silic eruptions and forecasting their development. Satellite radar backscatter can provide unique information about dome growth during a volcanic eruption when other datasets (e.g., optical, thermal, ground-based measurements, etc.) may be limited. Here, we present an approach for estimating volcanic topography from individual backscatter images. Using data from multiple SAR sensors we apply the method to the dome growth during the 2021 eruption at La Soufrière, St. Vincent. We measure an average extrusion rate of  $1.8 \text{ m}^3 \text{ s}^{-1}$  between December 2020 and March 2021 before an acceleration in extrusion rate to  $17.5 \text{ m}^3 \text{ s}^{-1}$  in the 2 days prior to the explosive eruption on 9 April 2021. We estimate a final dome volume of 19.4 million  $\text{m}^3$ , extrapolated from the SAR sensors, with approximately 15% of the total extruded volume emplaced in the last 2 days. A possible explanation for the acceleration in extrusion rate could be the combined emptying of a conduit and reservoir of older material before the ascent of gas-rich magma in April 2021.

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## 1. Introduction

After 41 years of quiet, La Soufrière Volcano, St. Vincent, began a new phase of extrusive dome growth on 27 December 2020. By the beginning of April 2021 the new dome had grown steadily around the southwest section of the 1979 dome (Fig. 1). Starting on 9 April 2021 the eruption suddenly transitioned into an explosive phase that lasted until 22 April 2021, completely reshaping the summit crater (Joseph et al., 2022). Understanding and forecasting such transitions from extrusive to explosive phases of eruptions is critical for hazards assessment and mitigation (Fink and Anderson, 2000; Joseph et al., 2022) and relies on robust monitoring data (e.g., Griffiths and Fink, 1997; Pallister et al., 2013; Scharff et al., 2014).

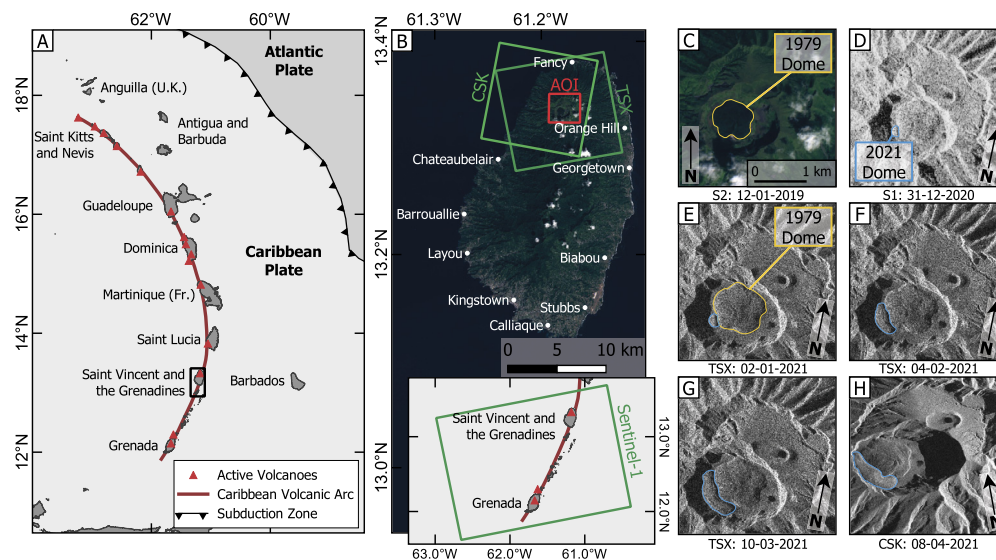
Transition from an effusive to explosive eruption occurs when the overpressure in a conduit exceeds confining pressure and has

been attributed to both shallow changes in a volcano's edifice ('top-down,' depressurisation) and events deeper in the magmatic system ('bottom-up,' increased overpressure). Some top-down triggers of explosive eruption, such as changes in the shallow stress regime caused by dome collapse (e.g., Pallister et al., 2013), high rainfall (e.g., Carn et al., 2004), or changes in extrusion direction (e.g., Watts et al., 2002) are detectable from ground- or satellite-based observations (e.g., Ryan et al., 2010; Pallister et al., 2013). Deeper triggers (Metcalf et al., 2022), such as the crystallisation or degassing of an ascending magma, or an increase in conduit permeability, may not result in diagnostic changes at the surface. However, the resulting increases in magma ascent rate (e.g., Castro et al., 2012; Wang et al., 2015) can be inferred from (1) changes in seismicity (e.g., Nakada et al., 1999; Roman et al., 2016) or (2) increases in extrusion rate, if measurements are sufficiently frequent.

High-temporal-resolution measurements of dome growth are difficult to obtain from the ground, being limited by accessibility, resources, cloud coverage and rapidly changing hazards. Although optical aerial and satellite imagery can have sub-metre pixel resolution (e.g., Pléiades, WorldView), and one can make Digital EL-

\* Corresponding author.

E-mail address: [edna.dualeh@bristol.ac.uk](mailto:edna.dualeh@bristol.ac.uk) (E.W. Dualeh).



**Fig. 1.** Location and overview of La Soufrière. (A) map of the Lesser Antilles arc and the Atlantic and Caribbean plate subduction zone, (B) Sentinel-2 (S2) image (29-12-2019) of the island of St. Vincent with extent of SAR tracks shown in green and the summit of La Soufrière in red, (C) optical and (D-H) SAR images in radar geometry showing the dome growth in La Soufrière crater between December 2020 to April 2021. SAR satellite abbreviation: CSK, COSMO-SkyMed; TSX, TerraSAR-X; S1, Sentinel-1. (For interpretation of the colours in the figure(s), the reader is referred to the web version of this article.)

evaluation Models (DEM) directly with stereo optical imagery, these datasets depend on daylight and low cloud coverage. Similarly, the bistatic approach using TanDEM-X data to calculate measurements of elevation change over time (e.g., Poland, 2014; Albino et al., 2020) require a pair of images acquired at the same time. Historical time series of dome extrusion (e.g., Zharinov and Demyanchuk, 2008; Ryan et al., 2010; Harnett et al., 2019) therefore tend to have large gaps or rely on measurements averaged over weeks to months.

Synthetic Aperture Radar (SAR) sensors have the benefit of being independent of the time of day and meteorological conditions. SAR backscatter has previously been used to observe dome stability and growth (e.g., Pallister et al., 2013; Plank et al., 2019) and to track changing morphology (e.g., Wadge et al., 2011; Walter et al., 2015). Structural information such as dome heights and volumes have been extracted from SAR backscatter through the use of radar shadows (El Reventador, Ecuador, Arnold et al., 2017), feature tracking (Mount Cleveland, Alaska, Wang et al., 2015) and simulating SAR backscatter signals to construct synthetic domes (Shinmoe-dake, Japan, Ozawa and Kozono, 2013). The recent study by Angarita et al. (2022) demonstrates a method similar to that presented here to quantify changes at Shishaldin Volcano.

Here, we present an analysis of the 2021 dome growth at La Soufrière volcano on the island of St. Vincent using radar backscatter from multiple sensors. We describe an approach to extract topographic profiles from SAR backscatter images. Using data from multiple SAR satellite systems (i.e., TerraSAR-X, COSMO-SkyMed and Sentinel-1), we construct a time series of 32 dome volume estimates between December 2020 and April 2021. We show that the extrusion rate remained relatively constant until two days before the explosive eruption on 9 April 2021.

### 1.1. Soufrière St. Vincent

La Soufrière (1,234 m) is the current active volcanic centre on the main island of St. Vincent and is situated in the northern section of the island (Fig. 1). La Soufrière is considered one of the most active volcanoes in the Caribbean, with at least five explosive eruptions since the first recorded eruption in 1718 (Robertson, 1995).

La Soufrière is monitored by the University of the West Indies Seismic Research Centre (UWI-SRC), assisted by the Soufrière Monitoring Unit (SMU) of National Emergency Management Organisation (NEMO) of St. Vincent and the Grenadines. Historical eruptions were characterised by both explosive activity and effusive dome growth.

In December 2020, La Soufrière entered a new period of activity with a new dome growing on the edge of the 1979 dome first observed on 27 December 2020 (Joseph et al., 2022). The Government of St. Vincent raised the volcanic alert level in December to 'Orange' in response to the extrusive activity (NEMO, 2020a). By mid-February 2021 the dome had grown to approximately 90 m in height and had transitioned into an elongated coulee, curling around the southwest edge of the 1979 dome (Fig. 1). During the extrusive phase, 12 measurements of the 2021 lava dome were made by UWI-SRC and SMU through photogrammetry using ground-based (i.e., from the crater rim) and aerial (i.e., UAVs, helicopters and fixed-wing aircrafts) imagery. A volcano-tectonic (VT) earthquake swarm was observed on 23–25 March 2021, marking a change in eruptive style and suggesting movement of magma towards the surface (NEMO, 2020c; Joseph et al., 2022). The rate of earthquakes increased on 5–6 April 2021 with the first banded tremor appearing on the 8 April (Joseph et al., 2022); the volcanic alert level was raised to 'Red' (at 18:00 UTC on 8 April), triggering an evacuation order for sections of the island (NEMO, 2020b; Joseph et al., 2022).

At 12:41 UTC on 9 April 2021 La Soufrière started to erupt explosively, with multiple explosions occurring over the day. Over the following week the volcano continued to erupt, with pyroclastic flows, continuous venting, and ashfall over St. Vincent and on neighbouring Barbados (11 April 2021). The newly emplaced dome that had been growing since the beginning of the year, the 1979 dome, and much of the previously existing crater floor were completely destroyed. These changes were confirmed by the first observations of the volcano summit from SAR images acquired on 10 April 2021 from ICEYE at 02:03 UTC (Fig. S12) and Capella at 14:02 UTC (Joseph et al., 2022). Explosive activity ceased on 22 April 2021 at La Soufrière and the seismicity has remained low since then. The alert level was lowered to 'Orange' on 6 May 2021 (NEMO, 2020b; Joseph et al., 2022) and to 'Green' in March 2022.

**Table 1**

SAR acquisitions used to monitor St. Vincent Dome growth. Images are acquired by three sensors (COSMO-SkyMed, CSK; TerraSAR-X, TSX; Sentinel-1, S1) for five tracks (indicated by subscript).

Acquisition Date	Sensor	Acquisition Date	Sensor	Acquisition Date	Sensor
31 Dec. 2020 22:19	<sup>1</sup> S1	24 Jan. 2021 22:19	TSX <sub>a</sub>	09 Mar. 2021 22:19	TSX <sub>a</sub>
02 Jan. 2021 22:19	<sup>2</sup> TSX <sub>a</sub>	30 Jan. 2021 22:18	S1	13 Mar. 2021 22:18	S1
08 Jan. 2021 22:10	<sup>3</sup> TSX <sub>b</sub>	04 Feb. 2021 22:19	TSX <sub>a</sub>	19 Mar. 2021 22:18	S1
12 Jan. 2021 22:19	S1	05 Feb. 2021 22:19	S1	20 Mar. 2021 22:19	TSX <sub>a</sub>
13 Jan. 2021 22:19	TSX <sub>a</sub>	10 Feb. 2021 22:10	TSX <sub>b</sub>	25 Mar. 2021 22:19	S1
17 Jan. 2021 21:38	<sup>4</sup> CSK <sub>a</sub>	11 Feb. 2021 22:18	S1	31 Mar. 2021 22:18	S1
18 Jan. 2021 21:38	CSK <sub>a</sub>	15 Feb. 2021 22:19	TSX <sub>a</sub>	31 Mar. 2021 22:19	TSX <sub>a</sub>
18 Jan. 2021 22:18	S1	17 Feb. 2021 22:18	S1	06 Apr. 2021 22:19	S1
19 Jan. 2021 22:10	TSX <sub>b</sub>	23 Feb. 2021 22:18	S1	07 Apr. 2021 21:38	CSK <sub>a</sub>
22 Jan. 2021 21:32	<sup>5</sup> CSK <sub>b</sub>	01 Mar. 2021 22:18	S1	08 Apr. 2021 21:38	CSK <sub>a</sub>
24 Jan. 2021 22:19	S1	07 Mar. 2021 22:18	S1		

<sup>1</sup>Sentinel-1 Descending; <sup>2</sup>TerraSAR-X Descending 085; <sup>3</sup>TerraSAR-X Descending 039

<sup>4</sup>COSMO-SkyMed S2\_17 Ascending; <sup>5</sup>COSMO-SkyMed S2\_25 Ascending

## 2. Data and methods

We develop a method that allows us to make measurements of new volcanic topography from single SAR backscatter images on the assumption that relative brightness derived from SAR backscatter range is proportional to the local topographic gradient. We make empirical estimations of the scaling factors and offsets required to map backscatter onto local slope and integrate along range lines to retrieve a relative height for each range pixel. We then apply a triangular mesh interpolation in radar geometry, including a smoothing factor and edge constraints, to estimate the full lava dome shape, before returning to geographic coordinates to calculate the dome volume and extrusion rates.

We exploit 32 SAR images from three sensors (TerraSAR-X, COSMO-SkyMed and Sentinel-1) acquired from January 2021 to April 2021 (Table 1) to observe the dome growth at St. Vincent (Fig. 1). The acquisition of high-resolution X-band data (i.e., CSK and TSX) was coordinated and supported by the CEOS Volcano Demonstrator, and output products were provided to UWI-SRC during the eruption to support monitoring efforts. For each sensor geometry we co-register the image to the first in the dataset and multi-look to give the pixel range dimensions shown in Supplement Table 1. Multi-look reduces the contribution of speckle, which would otherwise introduce noise to our estimations of topography. We use the GAMMA-remote sensing software (Werner et al., 2000) to produce the backscatter images. We use a Digital Elevation Model (DEM) constructed from three 2014 Pleiades images (2 m pixels) and 2018 Copernicus DEM (30 m pixels) (Grandin and Delorme, 2021) to calibrate our estimates of relative brightness and act as reference points for the height profiles extracted from SAR cross sections.

SAR backscatter ( $\sigma_0$ ), describes the radar pulse scattered back towards the sensor by the ground surface and is affected by local gradient, surface roughness and dielectric properties.

Surface scatterers are the main variables that determine the backscatter signal of the ground surface. Slopes facing towards the satellite will appear brighter than ones facing away (due to the effect of differences in local incidence angle), although this contribution can be corrected through radiometric terrain corrections if accurate DEMs are available (Small, 2011; Meyer et al., 2015). The roughness of a surface is dependent on instrument wavelength. Smooth surfaces will demonstrate specular reflection, but as the surface roughness increases, there will be more non-coherent or diffuse scattering, resulting in lower magnitude backscatter. Lastly, the dielectric properties of the ground surface also affect backscatter. However, in many applications moisture content is considered the main influencing factor, with higher moisture content reducing the proportion of the wave that is absorbed and increasing

the measured backscatter (Woodhouse, 2017; Flores-Anderson et al., 2019). The resulting backscatter is therefore controlled by the constructive and destructive interaction among these factors (i.e., surface roughness, local incidence angle and dielectric properties), which can lead to a complex signal that can be difficult to interpret. Further, these surface scatterers are dependent on the satellite instrument properties (e.g., polarisation, wavelength and incidence angle), making direct comparisons among sensors and tracks more challenging. Different polarisation, (e.g., VV or VH) will produce different signals over the same type of surface depending on orientation of the scattering target. For example, cross-polarised sensors are more sensitive to vegetation changes as a result of the depolarising effect from volume scattering (Woodhouse, 2017; Flores-Anderson et al., 2019). Cross-polarisation may therefore better distinguish between different degrees of vegetation coverage than co-polarisation, which can help better distinguish volcanic deposits (Solikhin et al., 2015).

La Soufrière's crater prior to the explosive eruption was dominated by grass and small shrubs, with more rock exposure found on the crater wall and the rougher 1979 dome. The area between the 1979 dome and the crater wall was relatively flat with a small crater lake in the eastern section.

We use calibrated SAR backscatter intensity images ( $\sigma_0$ ), rather than the raw intensity images ( $I_0$ ) in our analysis. These two quantities are related by  $I_0 = k\sigma_0$ , where  $k$  is a calibration constant of the SAR system. For our dataset, we assume that local incidence angle is the dominant contributor to the backscatter signal. Slopes facing towards the satellite are foreshortened, meaning there are more returns per ground unit, whereas slopes facing away are lengthened and have fewer ground returns. When the local incidence angle of slopes (i.e., angle between the normal to the slope and the SAR line-of-sight) is greater than the satellite incidence angle (i.e., angle between the satellite line-of-sight and the normal to the surface of the ellipsoid,  $\theta$  in Fig. S1a), we observe radar shadows for slopes facing away and layovers for slopes facing towards the sensor. In a SAR image a radar shadow appears as a gap in data where no returns are recorded. Regions of layover do return radar signals, but as the sensor will image the top of the slope before the base, each radar unit receives returns from multiple locations at the same radar range, producing a layered image that results in ambiguity in the location of the reflectors.

### 2.1. Topographic change from SAR backscatter

#### 2.1.1. Estimation of relative brightness

SAR backscatter is dependent on sensor parameters that vary between sensors. We therefore estimate scaling factors that describe how relative brightness relates to topography. We estimate

**Table 2**

SAR sensor parameters used to examine the St. Vincent dome growth.

Sensor	Band	Incidence Angle	Polarisation	Multilook Resolution Factor	Range × Azimuth [m]
COSMO-SkyMed	X (3.1 cm)	44.2–44.4	HH	4×4	1.5×2.8
TerraSAR-X	X (3.1 cm)	50.9	HH	4×4	3.6×5.1
Sentinel-1 (Asc)	C (5.5 cm)	43.0	VV & VH	4×1	9.3×14.0
Sentinel-1 (Desc)	C (5.5 cm)	31.0	VV & VH	4×1	9.3×14.0
ALOS-2	L (23.6 cm)	36.3	HH & HV	2×2	4.3×3.8

these factors for each image by comparing an area where topography is unchanged to the simulated backscatter ( $\sigma_s$ ) that we calculated from the pre-eruptive DEM using a Lambertian backscatter model. We consider a ‘stable’ area to be one where there has been no change in topography and minimal change in scattering properties, ideally where the scaling factor is dominantly influenced by the local incidence angle. In the SAR images of St Vincent, we exclude the site surrounding the new dome and the surrounding area of vegetation die-back and alteration (approximately 27% of the St. Vincent crater in the TSX image) from estimation of scaling factors. Using an unstable area will distort the simulated SAR, which will then not correlate well with the real SAR signal and produce inaccurate scaling factors. For most datasets we used the 1979 dome as the ‘stable’ area used to calculate the scaling factors (Fig. 1). However, for the lower-resolution Sentinel-1 we incorporated areas outside the 1979 dome to increase the number of data points used to estimate the scaling factors. We then apply an iteratively reweighted least squares method to determine the best linear scaling factors ( $m$ ,  $c$ ) between the simulated backscatter,  $\sigma_s$ , and the real backscatter values,  $\sigma_0$ . These scaling factors vary among sensors due to different (1) levels of noise present, (2) calibrations of sensors, and (3) satellite geometry and parameters (i.e., wavelength). Finally, we apply the scaling factors to the whole image (including where topography has changed) to estimate a relative backscatter ( $\sigma_r = m\sigma_0 + c$ ).

Although no radiation is scattered back to the sensor from shadows, they still have non-zero  $\sigma_0$  values introduced by thermal noise and residual radiation from sidelobes. We therefore mask out the data gaps caused by radar shadows using a threshold estimated from the maximum backscatter within a known shadow in each SAR dataset (e.g., from La Soufrière crater wall, Table 2).

### 2.1.2. Retrieval of topography along range lines

Based on the assumption that the local incidence angle is the dominant scattering property of the radar backscatter signal, we can express this in terms of the gradient of topography,  $h$ , in radar (slant range) geometry,

$$\sigma_r \propto \frac{dh}{d\delta} \quad (1)$$

where  $\delta$  is the range pixel spacing. A relative brightness of 1 implies flat topography, whereas values  $> 1$  are caused by slopes that face the satellite and  $< 1$  are caused by slopes facing away (Fig. S1).

To calculate  $h$  from  $\sigma_r$  we need to integrate along each range line. Following Taud and Parrot (1995) and Paquerault and Maitre (1998), we calculate relative height ( $\varepsilon_i$ ) with respect to the first point, set to 0, for the  $i^{\text{th}}$  point along a line in range by;

$$\varepsilon_i = \varepsilon_{i-1} + \delta(\sigma_r - 1) \quad (2)$$

This equation is valid provided there is no layover or radar shadows (Supplementary Text). To mitigate the gaps in data caused by radar shadows, we use the width of the shadow in the SAR range line and calculate the corresponding shift in height,  $\Delta_H$ , for each radar shadow present in the cross-section:

$$\Delta_H = W_{\text{range}} \cos \theta \quad (3)$$

where  $W_{\text{range}}$  is the width of the shadow in radar geometry and  $\theta$  the incidence angle, (Fig. S1d). We then apply this correction  $\Delta_H$  to all of the heights following that radar shadow.

Because we apply the summation independently on each range line, inconsistencies between consecutive range lines can give rise to apparent ‘jumps,’ typical of topographic maps derived from radarclinometry methods (Willey, 1986; Guindon, 1990). Differences between the shape of our relative height profile and the true topography can be introduced by layover, inadequate estimate of scaling factors, speckle, or by changes in backscatter caused by differences in roughness or dielectric constant. We therefore estimate a best-fit vertical adjustment by masking out the 2021 dome and comparing the shape of our relative height profile with the pre-eruption DEM along the same line in range. Until this point, we have not made any adjustment for the influence of layovers in our estimated profiles. To accurately calculate the vertical shift, we apply a layover mask constructed from the pre-eruption DEM. We then use the DBSCAN clustering algorithm (Ester et al., 1996) to determine the different clusters between the two profiles and then calculate the linear gradient, such that a value of 1 indicates a perfect match between our estimations and DEM topography. We select the cluster with a linear gradient closest to 1 and use the corresponding y-intercept,  $y$ , to shift our relative height profiles, such that best estimates of the new topography,  $d_{\text{topo}}$ , takes the form  $d_{\text{topo}(i)} = \varepsilon_{i-1} + \delta(\sigma_r - 1) + y$ , neglecting corrections for any shadows (Fig. 2).

### 2.1.3. Inversion for dome shape

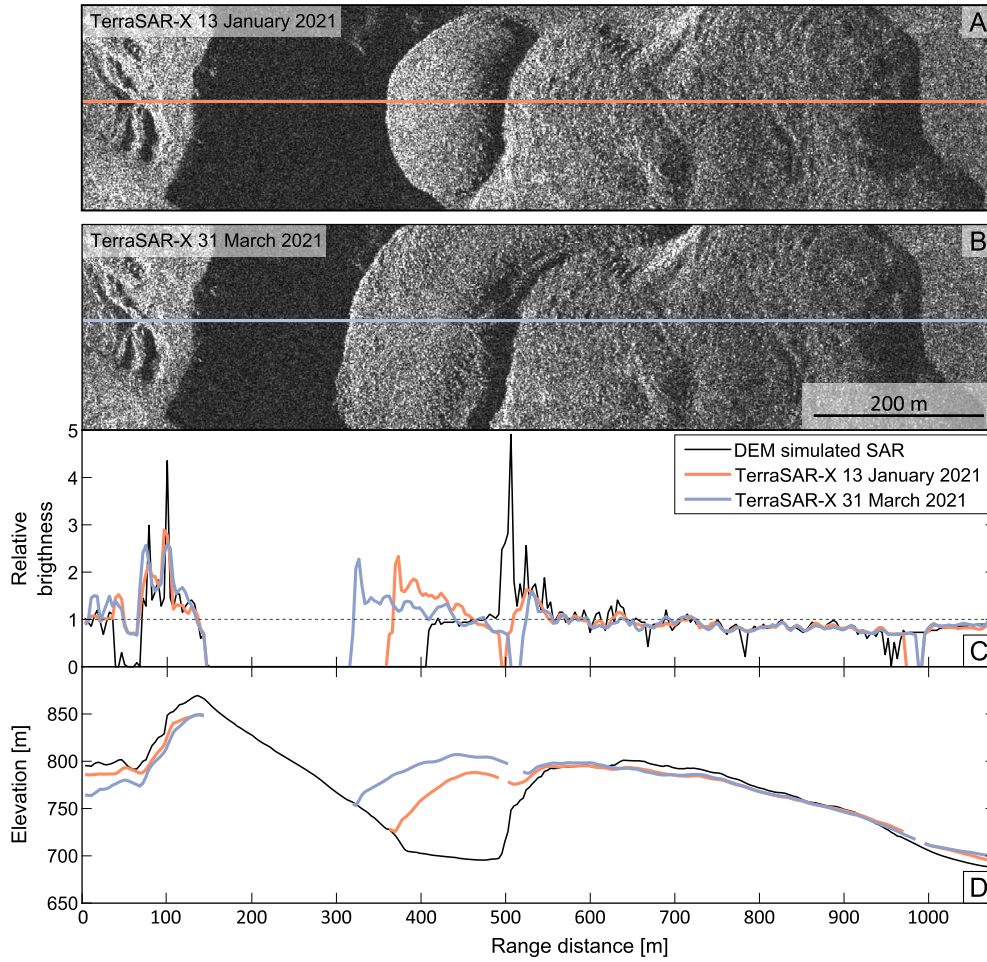
To construct a complete dome surface from the multiple topographic profiles along range lines we divide the outline of the SAR dome into a regular triangular mesh and solve for the height of each node, assuming that the topography changes linearly across each triangle (Fig. 3). The resolution of the constructed mesh is lower than the original heights estimated from the SAR images such that multiple height estimations fall into a single triangle (Table S2). This smooths the small-scale variations originating in backscatter noise and bridges areas where there are gaps in height measurements (e.g., radar shadows). Using the topographic profiles in range,  $d_{\text{topo}}$ , and the DEM height values for the edge of the dome,  $d_{\text{edges}}$ , the system of equations for this model can be written as,

$$[h] = (G^T W^{-1} G)^{-1} G^T W^{-1} d \quad (4)$$

$$G = \begin{bmatrix} G_{\text{sar}} \\ K^2 \nabla^2 \\ G_{\text{edges}} \end{bmatrix} \quad W_{\text{diag}} = [r_1, r_2, \dots, r_n, 0] \quad d = [d_{\text{topo}} \quad 0 \quad d_{\text{edges}}] \quad (5)$$

where  $h$  are the unknown height observations for the triangular vertices;  $G$  is a design matrix constructed from  $G_{\text{sar}}$  (number of SAR points × total number of vertices), the matrix of interpolated kernels representing the shape function (Wang and Wright, 2012) for each height observation (Fig S4);  $\nabla^2$  is the Laplacian smoothing operator (number of interior vertices × total number of vertices) with an umbrella smoothing factor,  $K^2$ ; and  $G_{\text{edges}}$  is the matrix





**Fig. 2.** Topography extracted from radar backscatter range line. TerraSAR-X images (A) 13 January 2021 and (B) 31 March 2021 with cross-section lines over the 2021 dome. The growth of the 2021 dome can be seen in (C) the radar backscatter range line cross-sections with the corresponding simulated Synthetic Aperture Radar (SAR) signal produced from the Digital Elevation Model (black line) and (D) the retrieved topography for all cross-sections shown in (C). Zero values (C) and gaps in data (D) correspond to radar shadow locations.

that contains a weighted edge constraint (number of edge vertices  $\times$  total number of vertices). For the smoothing factor,  $K^2$ , used in the Laplacian operator, we apply a small value ( $K^2 = 0.5$ ) to minimally smooth the structure but remove any large artifacts otherwise introduced over data gaps. Further, to avoid smoothing of the dome beyond where we know its edges to be, we include edge constraints ( $G_{\text{edges}}$ ) that indicate where we are confident about location of the dome edge ( $d_{\text{edges}}$ ), and elevations can be obtained from the DEM in radar geometry. We reduce the contribution from range lines that were particularly distorted by radar layovers, which can cause errors to propagate along the range line (e.g., the negative and positive elevation difference over stable portions of topography, Fig. 3d-f), by applying a weighting matrix ( $W$ ) to our system to reduce the influence from these particular lines.

The weighting values used for our triangular mesh interpolation are the RMSE between each range line and the corresponding pre-existing DEM line (with the new dome masked out). The diagonals of the weighting matrix ( $W_{\text{diag}}$ ), are the respective RMSE values associated with each SAR data point ( $r_1, r_2, \dots, r_n$ ) and we assign additional zeros to the end of the diagonal that corresponds to the total number of vertices to account for the Laplacian ( $K^2 \nabla^2$ ) and edge constraint ( $G_{\text{edges}}$ ) components in the design matrix ( $G$ ). Profiles that deviate from the known topography will produce larger values, which are then accordingly down weighted in Eq. (4).

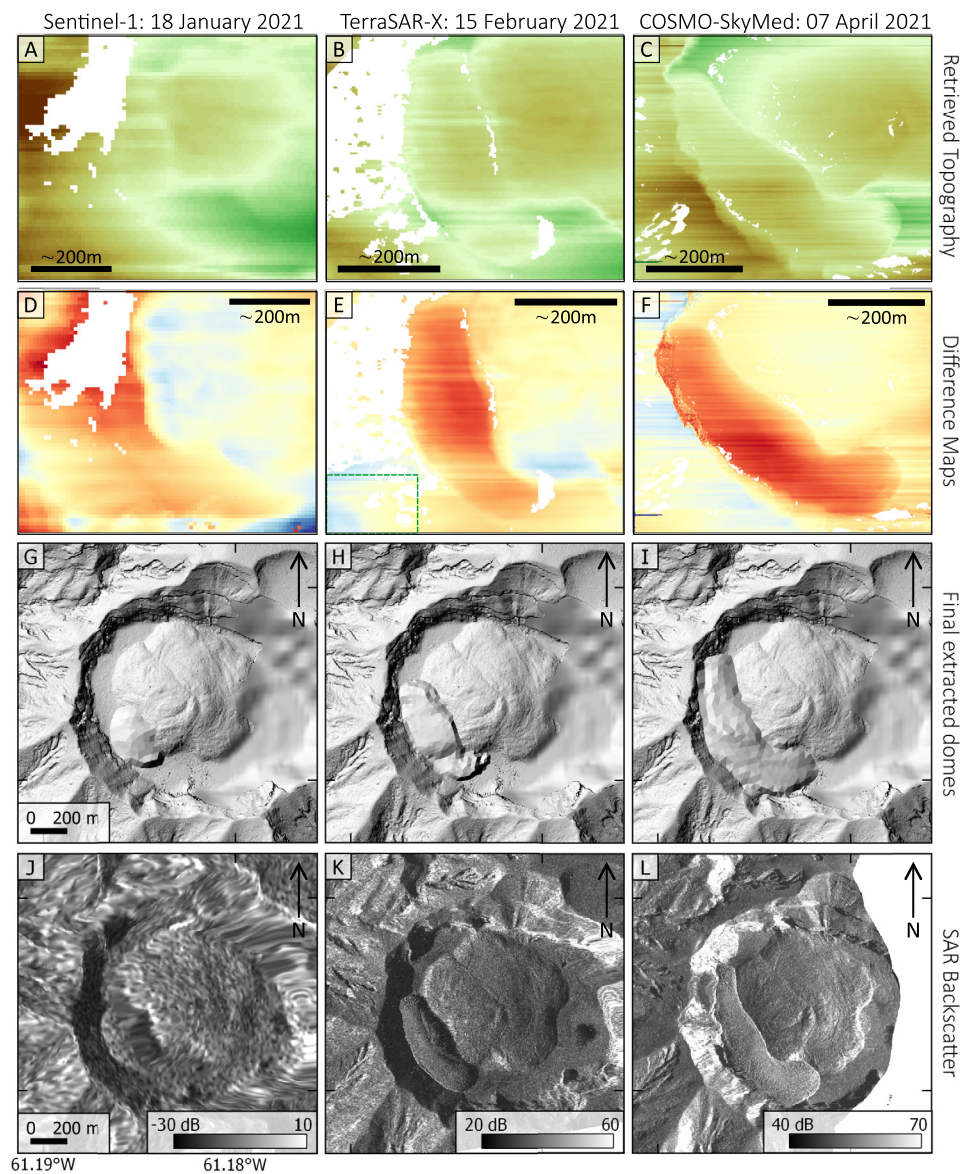
After solving for a smooth continuous mesh of dome heights in radar geometry, we translate our new elevation maps back into

geographic coordinates (Fig. 3g-i). To do this, we return our triangular mesh back into range lines and convert the coordinates of each line into Cartesian geometry (Text S1, Eq.1). We use a look-up table to geographically locate the start and end of each line.

Because we used multi-looked images for the SAR height extractions, when we translate an individual range line back into its geographic coordinates, the translation results in gaps in heights between lines. We apply a second triangular mesh in geographic coordinates to bridge these data gaps and fully construct the dome geometry without any additional weighting, smoothing, or constraints. By comparison to the original pre-eruption DEM, we can then calculate the dome heights and volumes for each SAR image (Fig. 3g-i, S6, 4). For a more complete description of the method see supplementary text and figures S1–S3.

## 2.2. Estimation of extrusion rates and uncertainties

Using our dome volumes estimates, we calculate extrusion rates between pairs of images that have the same geometry. We do this separately for each sensor to avoid introducing uncertainties associated with combining different sensor resolutions and geometries. We consider the largest sources of uncertainty in our estimates to be the systematic effects of radar layover, which introduce distortions to the topographic profiles retrieved, and which vary between satellite geometries. We calculate the volume uncertainties by estimating the percentage of the dome that is affected by layover.



**Fig. 3.** (A) Sentinel-1 (18 January 2021), (B) TerraSAR-X (15 February 2021) and (C) COSMO-SkyMed (07 April 2021) examples of the range line retrieval of topography. (D-F) show the difference between the extracted height from SAR and the pre-eruption DEM. (G-I) show the final dome shapes shown as shaded relief maps. (J-L) show the original SAR backscatter images used to estimate the dome topography. Note (A-F) are in radar geometry and (G-I) are in geographic coordinates. The green outline in E indicates the area used to calculate average difference between SAR topography and the pre-eruption DEM.

This estimate depends on the accuracy and resolution of the pre-eruption DEM, which we need to identify where these distortions occur. We then use these percentage errors to calculate the upper and lower limits for our dome volumes. It is important to note that while our estimations of uncertainties relate solely to the systematic, higher-magnitude errors associated with the satellite geometry, there are other sources of error associated with noise in backscatter (e.g., speckle, changes to surface scatterers). We mitigate the contribution of these sources of noise by multi-looking our data, applying speckle filters, and using the triangular mesh interpolation. However, even after these corrections, some uncertainties remain, especially in areas where the properties of surfaces scatterers vary over time (e.g., crater floor and wall). For example, the differences between TSX-retrieved topography and the DEM for areas where topography is unchanged vary between 10 and 24 m (area used is outlined in green, Fig. 3e).

### 2.3. SAR pixel tracking

We also make pixel-offset tracking estimates of surface displacements in both range (i.e., perpendicular to the satellite track direction) and azimuth (i.e., parallel to the satellite track direction) using pixel-based cross-correlation. Although Interferometric SAR (InSAR) methods are able to measure surface displacements between acquisitions with centimetre accuracy (e.g., Delgado et al., 2017; Moore et al., 2021), they require stable ground surface scatterers, otherwise the data become completely decorrelated. In contrast, pixel-offset tracking can measure larger surface movements (i.e., metre-scale) without the use of SAR phase (e.g., Wang et al., 2015; Schaefer et al., 2017) using pixel-based cross-correlation between the backscatter signals of the two images. The two SAR images used are required to be precisely co-registered, as the accuracy of the pixel-offset measurements is strongly dependent on the image co-registration. This method only works if changes are relatively small.



We apply pixel-offset tracking to two 1-day X-band COSMO-SkyMed (CSK) pairs to detect short-term dome growth during the early phase and immediately before the eruption transitioned from extrusive to explosive. Based on the large perpendicular baseline between our 1-day CSK image pairs (564 m and 2411 m), we apply a co-registration that makes use of a look-up table formed between the SAR images and the DEM in radar geometry based on the primary SAR image. For higher-resolution systems with large baselines, this method has the advantage that it incorporates topography-related offsets in the lookup table and applies them during co-registration. We use a small cross-correlation threshold of 0.05 to remove some of the obvious outliers from the offset results. We found that a large cross-correlation window with steps of about a third of the window size (i.e.,  $100 \times 100$  pixels window and  $32 \times 32$  step size) maximised the spatial coverage of the dome offsets for CSK and returned appropriate offsets across the dome. Nevertheless, measurements were not possible over the centre of the dome, where surface changes were too large. Pixel-offset maps produced from 7 pairs of TerraSAR-X (TSX) images were sparser, with a less-distinct offset pattern (Fig. S11) and higher uncertainties. The difference between the TSX and CSK offset tracking quality results mainly from the longer time intervals for the TSX data (11 days), which capture a longer period of dome growth.

### 3. Results: dome growth

The gradual growth of the 2021 dome, including changes in morphology and surface texture, is observable directly from individual SAR images (Fig. S7-9, 13-16). The 2021 dome gradually changed from uniform central growth to laterally spreading around the 1979 dome. In February 2021 we observe the development of fractures at either end of the 2021 dome (Fig. S7-8, S14) and in April 2021 visible bulging in the center (Fig. S7, S14).

Our analysis has enabled us to estimate dome volumes and extrusion rates from the 32 CSK, TSX and Sentinel-1 SAR images spanning the dome-growth phase (Fig. 4). This allows us to examine patterns in extrusion rates for the dome over 3.5 months in early 2021 before the eruption transitioned from extrusive to explosive on 9 April 2021.

#### 3.1. Lava dome growth

To characterise the main dome-growth phase at La Soufrière from December 2020 to March 2021, we use a total of 29 SAR backscatter images (Fig. 4). The dome at La Soufrière showed steady growth with extrusion rates of  $\sim 0.5\text{--}5 \text{ m}^3\text{s}^{-1}$  from December 2020 to March 2021 (Fig. 4b). Our data indicate that extrusion rate varied over short time scales with shorter timespan image pairs (e.g., CSK 1-day pair dates) recording the highest rates. However, the extrusion rate recorded over intervals  $> 10$  days is remarkably consistent (Fig. 4). Our data are well explained with a constant rate of  $\sim 1.8 \text{ m}^3\text{s}^{-1}$  from the first appearance of the dome until 7 April 2021, two days prior to the eruption. Our independent measurements of extrusion rate are consistent with those presented by Stinton (submitted for publication), who found extrusion rates that varied between 0.95 and  $2.65 \text{ m}^3\text{s}^{-1}$ , with a long term average of  $1.85 \text{ m}^3\text{s}^{-1}$  from 12 sets of photogrammetric measurements made from locations along the rim of the summit crater, UAVs, and helicopter and fixed-wing aircraft overflights.

#### 3.2. Pre-explosive phase increase in extrusion rate

At the beginning of April 2021, the dome continued to grow laterally around the older 1979 dome without any significant change in rate. However, from the SAR data, we observed a major change

in extrusion rate in the days prior to the transition from extrusive to explosive. There was a sudden increase in extrusion rate from  $\sim 1.8$  to  $17.5 \text{ m}^3\text{s}^{-1}$  some time between 21:38 UTC on 7 April and 21:38 UTC on 8 April (Fig. 4a). The rapid increase in extrusion rate is confirmed by images of rapid inflation acquired by a remote camera on the crater rim (Joseph et al., 2022). If we assume this new, higher rate was constant during the few days prior to the onset of explosive activity, then the transition to higher-rate extrusion would have occurred on 7 April 2021, just after the onset of rapid dome inflation as observed by a remote camera (Joseph et al., 2022). Our final dome volume calculated from a CSK image acquired at 21:38 UTC on 8 April, approximately 15h before the first explosions were recorded (12:41 UTC on 9 April 2021), is 18.5 million  $\text{m}^3$ , slightly higher than the estimate of final dome volume of 16 million  $\text{m}^3$  made by Stinton (submitted for publication) by extrapolating a constant extrusion rate of  $1.85 \text{ m}^3\text{s}^{-1}$ . Using the increased extrusion rate from the 8 April CSK image, we extrapolate the dome volume from 8 April to the time of the first explosive eruption (12:41 UTC on 9 April 2021) to estimate a final dome volume of 19.4 million  $\text{m}^3$ . Because, there is no information about the extrusion rate in the hour before the eruption. Thus, we assume that the extrusion rate remained constant, which may not have been the case. The first post-explosion SAR image, acquired on 10 April at 02:03 UTC by ICEYE, showed the complete destruction of the new dome (Fig. S12).

The 1-day CSK pixel-offset tracking over the 2021 dome showed displacements within the dome itself and no significant changes elsewhere in the summit crater (Fig. 5). During the initial dome growth phase from 17-18 January 2021, we observed localised movements (maximum offset of  $\sim 9\text{m}$ ) centred around  $13^\circ 19'56''\text{N}$   $61^\circ 11'08''\text{W}$ , which we estimated to be the location of the vent. The image from 8 April 2021 showed displacements away from the same centre point extending over whole dome (maximum measurable offsets of  $\sim 15\text{m}$ , Fig. 5f). The order-of-magnitude increase in extrusion rate could not be accommodated by continued growth of the dome along the central axis of the coulee (e.g., Fig. S8) but can be seen bulging around the vent location on 7-8 April (Movie S14). Displacement in this area exceeds the threshold measurable with pixel-offset tracking. From our measurements, the dome surface rose by 10 m in its central section during this 24 hour period.

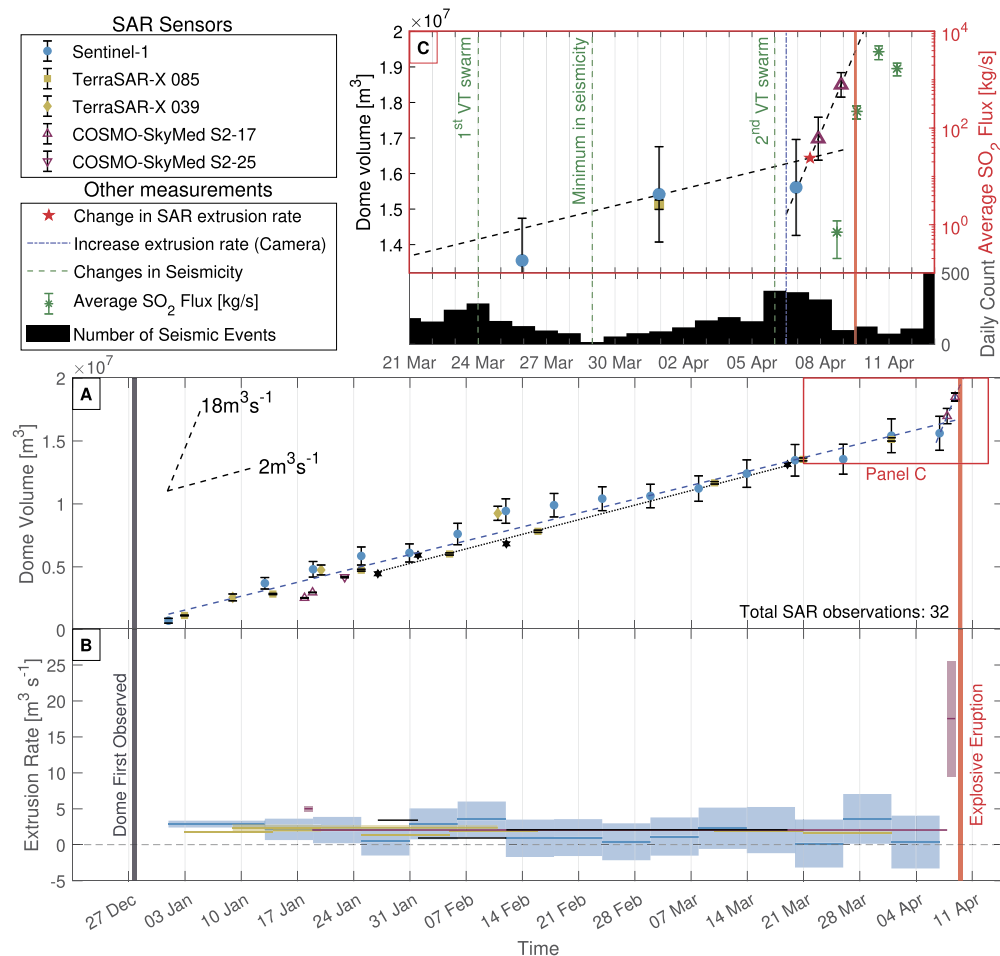
### 4. Discussion

#### 4.1. Transition to explosive eruption at St Vincent 2021

The sudden increase in dome volume and extrusion rate seen at St. Vincent in the days prior to the start of the explosive phase indicates that the transition was driven by changes in the magmatic system (a 'bottom-up' process). We see no evidence in the pre-eruptive SAR imagery of dome collapse up to 15h before the eruption. However, the sudden increase in dome volume between 7 and 8 April 2021 does correlate with other evidence of rapid dome inflation in backscatter images: (1) increased fracturing, (2) surface displacements  $> 15 \text{ m}$ , and (3) a bulge surrounding the vent (Fig. 5).

Independent evidence of a magmatic change that preceded the transition to explosive activity on 9 April includes (1) a change in volcano-tectonic earthquakes beneath the volcano on 5-6 April (Thompson et al., 2022), (2) the first detection of  $\text{SO}_2$  on 8 April from TROPOMI, a coastal traverse made using UV Spectrometer and MultiGAS instruments (e.g., Joseph et al., 2022; Esse et al., in press), (3) banded tremor and incandescence, both first observed on 8 April (Joseph et al., 2022), and (4) ash venting from fractures in the rapidly inflating region on the 2021 dome.

The high volume of extruded material (16.4 million  $\text{m}^3$ , red star in Fig. 4) up to 7 April and constant extrusion rate indicates the



**Fig. 4.** Time series of (A) cumulative volumes and (B) time-averaged extrusion rates of the dome at La Soufrière from December 2020 and April 2021 extracted from SAR backscatter data. The SAR backscatter data extend the photogrammetry observations showing the sudden increase in dome volume and extrusion rate in the days prior to the transition from explosive to explosive eruption. (C) Enlarged time series of the two weeks prior to the eruption, with important changes seen in other datasets (i.e., seismicity, SO<sub>2</sub> emissions, visual observations superposed). SO<sub>2</sub> measurements are time-averaged fluxes over periods of 5–20 hours for the corresponding days (Esse et al., *in press*). Date format is shown as 'Day Month' starting in December 2020 until April 2021. VT = Volcano-Tectonic.

steady removal of older material from a combined conduit and established magma reservoir, where the loss of material does not result in a discernible pressure decay. The subsequent increase in extrusion rate to 17.5 m<sup>3</sup> s<sup>-1</sup> is consistent either with the addition of new magma to the system in April 2021, or, as proposed by Joseph et al. (2022)'s conceptual model, to a gas-rich magma injected earlier in the eruption (between December 2021 and April 2021) that had been slowly pushing up older material intruded in 1979. The increase in extrusion rate may have started as a gradual response to a decreasing overburden of older, degassed magma and a corresponding increase in gas exsolution rate. An alternative may be that a sudden increase in gas pressure was caused by internal processes within the reservoir, allowing gas-rich magma to break through a remaining degassed cap.

By 7 April 2021 we observed changes in the SAR backscatter that indicated a sudden increase in dome volume as the last of the old, degassed material (we estimate 3 million m<sup>3</sup> between the 7–9 April, 15% of the total extruded volume) was erupted. Shortly after, the detection of increased SO<sub>2</sub> on 8 April (Esse et al., *in press*) indicated that SO<sub>2</sub> reached a critical threshold to force its way to the surface, ultimately triggering the 9 April eruption. The timing of the increase in extrusion rate estimated from SAR backscatter measurements (7 April) is consistent with the detectable increase in SO<sub>2</sub> emissions early on 8 April (Esse et al., *in press*). SO<sub>2</sub> emissions were reported beginning 1 February 2021 through MultiGAS measurements. However, they remained below the detection threshold

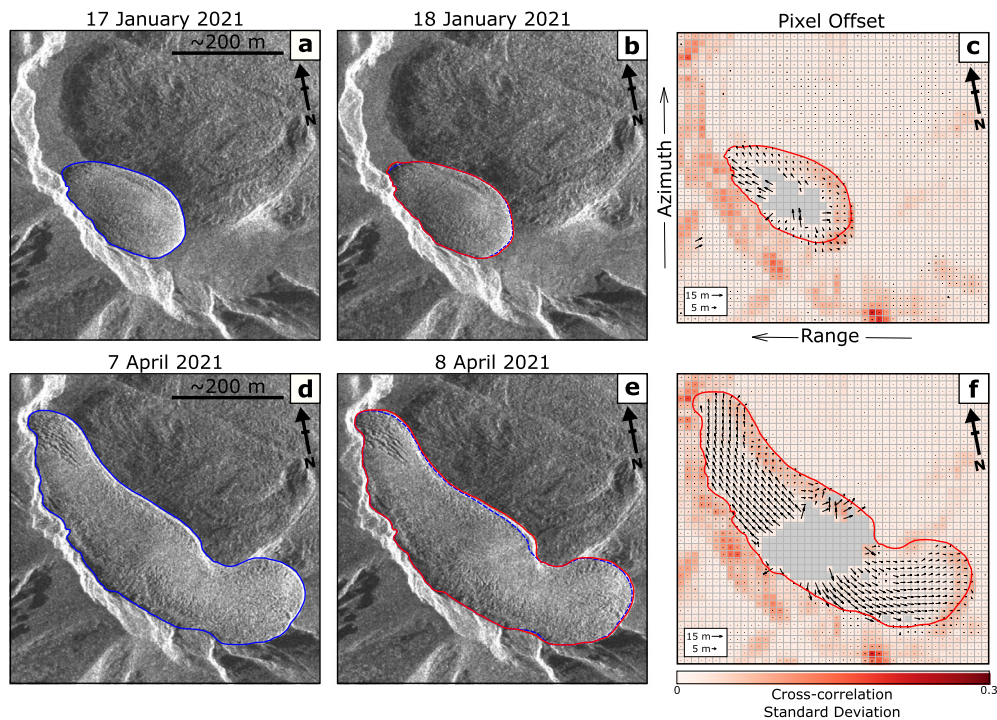
for TROPOMI and DOAS until the increase on the 8 April (Esse et al., *in press*).

#### 4.2. Potential for application to future eruptions

Our method for extracting topographic profiles and thus extrusion rates from SAR backscatter has potential to be a powerful monitoring tool. Extrusion rate is typically one of most challenging geophysical parameters to obtain safely during an eruption, requiring either in-situ measurements near vents or clear conditions for overflights. Volume estimates made from radar satellites have potential to increase the temporal resolution of an extrusion-rate time series, with photogrammetry augmenting when conditions allow (as for the 2021 St Vincent eruption). Photogrammetry measurements shown in Fig. 4a were reported during the progression of the eruption and were based on simplifying assumptions to obtain rapid estimations of dome height, area and volume. We assume that the discrepancies between the photogrammetry and SAR dome volumes are related to the assumptions of both methods.

The usefulness of SAR-retrieved topography depends on (1) the accuracy of our underlying assumption that  $\sigma_0$  is primarily controlled by topography, (2) satellite radar image resolution and geometry relative to the new volcanic topography, and (3) the quality and resolution of the pre-eruption DEM used to identify areas of shadow and layover.





**Fig. 5.** COSMO-SkyMed (CSK) pixel tracking maps. Radar backscatter images from (a) 17 January, (b) 18 January, (d) 7 April and (e) 8 April with dome outlines in blue (1<sup>st</sup> date) and red (2<sup>nd</sup> date). (c) and (f) Pixel tracking maps for (c) January and (f) April overlain on cross-correlation standard deviations. Arrows show the direction of surface displacement in range and azimuth direction, and grid represents the step window used (CSK, 32 × 32). Location of images is shown in Fig. 1H.

Our assumption that local topographic gradient is the primary control on backscatter is justified only where surface roughness and dielectric properties are relatively steady. We can correct for these effects where variations are uniform across the structure. For the lava dome at La Soufrière, based on ground and satellite imagery, we could confidently assume that the surface roughness of the new dome was uniform across the dome and through time; however, this was not the case for other parts of La Soufrière's crater, or other domes elsewhere. For example, we observed that  $\sigma_0$  on sections of the 1979 dome adjacent to the 2021 dome decreased over the course of the eruption, a change that we attribute to the removal of vegetation caused by the emission of gases from the growing dome (Fig. S10).

To explore the accuracy of our method, we use synthetic topographic cross-sections to test the impact of varying incidence angle and the local incidence angle (Fig S2). We found that radar layovers had a greater impact on the accuracy of the retrieved topography than radar shadows, which can be easily identified from backscatter images. The edges of regions of layover are harder to identify in backscatter, and since topographic change is unknown for real data, cannot be reliably predicted. In the synthetic models, a single section of radar layover would skew the final profile shape, but our correlations meant that the overall height estimations were similar to the original profile. When a layover interacted with a radar shadow, the estimated topography contained distortions and differ significantly from the original synthetic cross-section (Fig. S2). The distortion introduced by the layovers in our estimations of topography is under-constrained and cannot be corrected. In this dataset, layovers are most significant during the early period of dome growth, when the edges are relatively steep and not constrained by the surrounding topography. Lower incidence angles produced larger areas affected by radar layovers, and we found that an ALOS-2 ascending track and the Sentinel-1 descending track (that ultimately did not contribute to our results) were less successful in retrieving the dome heights because of smaller incidence angles, 37° and 31° respectively (Table 2). We consider

layover to be the largest source of uncertainty in our results, especially for the descending tracks as the 2021 dome grew into the layover of the crater wall, concealing the backscatter signal from the dome (Fig. S3).

#### 4.3. Optimising SAR acquisitions

The different SAR datasets covering the 2021 dome growth at St Vincent allowed us to test how different sensor polarisations and resolutions affected our estimates of topography. We found that unmitigated speckle greatly increased the noise in our retrievals of topography. Higher-resolution sensors allowed us to multi-look and apply speckle corrections to the images while retaining high spatial resolution (CSK 1.5 × 2.8 m pixels at 4 × 4 looks, range by azimuth and TSX 3.6 × 5.1 m at 4 × 4 looks, range by azimuth). Although the multi-looked Sentinel-1 images (9.3 × 14.0 m at 4 × 1 looks, range by azimuth) were much lower resolution, their frequent acquisitions and multiple tracks covering the dome-growth period provided a denser temporal spacing for extrusion rate estimates and allowed a much denser time series than possible from X-band alone. We also found that the Sentinel-1 cross-polarisation images (i.e., VH) produced less accurate topographic estimates, presumably due to their greater sensitivity to volume scattering and vegetation (Patel et al., 2006).

Based on this, we found the ideal SAR imagery for estimating topography from backscatter has the following characteristics: (1) co-polarization, (2) a geometry that minimises shadow and layover, and (3) is acquired as frequently as possible. In practice, these characteristics are most likely to be achieved for any individual eruption by analysis of a constellation of different SAR instruments. The most appropriate geometry for tasking is especially hard to predict in advance of an eruption, as the shape of new topography determines the locations of shadow and layover. Volcanic craters, domes with steep sides, and flows that fill steep valleys are all likely to be bounded by zones of shadow and layover. Al-

though this source of uncertainty can be minimised by choice of geometry, it is unlikely to be eliminated.

## 5. Conclusions

We successfully estimated topography from 32 SAR backscatter for the 2020–2021 eruption of La Soufrière, St. Vincent volcano using five different geometries from three sensors (TerraSAR-X, TSX; COSMO-SkyMed, CSK; and Sentinel-1). The topographic estimates allowed us to estimate a time series of dome volume and thus extrusion rate. The processing timeframe from raw SAR data to final retrieved topography was about done within a day, and depending on the resolution of the data and size of the target feature. We found that high-resolution, co-polarisation imagery with small areas affected by layover (i.e., larger incidence angles) resulted in the most reliable dome-volume estimates.

Extrusion rate at La Soufrière was relatively stable between December 2020 and March 2021, with an average rate of  $1.8 \text{ m}^3 \text{ s}^{-1}$ . By 7 April 2021, extrusion rate increased by an order of magnitude to  $17.5 \text{ m}^3 \text{ s}^{-1}$ , before the explosive phase on 9 April 2021, 15 hours after our last SAR measurement. The final dome volume measured from SAR data was 18.5 million  $\text{m}^3$  with a maximum height of  $\sim 140 \text{ m}$ . This increase in extrusion rate is consistent with an incursion of gas-rich magma into the conduit, which then led to the explosive phase of the eruption.

## CRediT authorship contribution statement

**E.W. Dualeh:** Conceptualization, Investigation, Methodology, Writing – original draft. **S.K. Ebmeier:** Conceptualization, Funding acquisition, Methodology, Supervision, Writing – review & editing. **T.J. Wright:** Conceptualization, Methodology, Supervision, Writing – review & editing. **M.P. Poland:** Conceptualization, Writing – review & editing. **R. Grandin:** Resources, Writing – review & editing. **A.J. Stinton:** Resources, Writing – review & editing. **M. Camejo-Harry:** Conceptualization, Resources, Writing – review & editing. **B. Esse:** Resources, Writing – review & editing. **M. Burton:** Resources.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Data availability

Data will be made available on request.

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## Appendix A. Supplementary material

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.epsl.2022.117980>.

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