

Detectability of Supernova remnants with the Southern Wide-field Gamma-ray Observatory

N. Scharrer,^a S.T. Spencer ,^{a,b} V. Joshi ^a and A.M.W. Mitchell ^a

^aErlangen Centre for Astroparticle Physics, Friedrich-Alexander-Universität Erlangen-Nürnberg, Nikolaus-Fiebiger-Str. 2, 91058 Erlangen, Germany

^bDepartment of Physics, Clarendon Laboratory, Parks Road, Oxford, OX1 3PU, U.K.

E-mail: nick.scharrer@fau.de, samuel.spencer@physics.ox.ac.uk,
vikas.joshi@fau.de, alison.mw.mitchell@fau.de

ABSTRACT: Supernova remnants (SNRs) are likely sources of hadronic particle acceleration within our galaxy, contributing to the galactic cosmic ray flux. Next-generation instruments, such as the Southern Wide-field Gamma-ray Observatory (SWGGO), will be of crucial importance in identifying new candidate SNRs. SWGGO will observe two-thirds of the gamma-ray sky, covering the energy range between a few hundreds of GeV and a PeV. In this work, we apply a model of SNR evolution to a catalogue of SNRs in order to predict their gamma-ray spectra, explore the SNR emission phase space, and quantify detection prospects for SWGGO. Finally, we validate our model for sources observed with current-generation instruments, fitting it using a Monte-Carlo Markov Chain technique to the observed gamma-ray emission from four SNRs. We anticipate that at least 6, and potentially as many as 11 SNRs will be detected by SWGGO within 1 year.

KEYWORDS: gamma ray experiments, supernova remnants

ARXIV EPRINT: [2410.15741](https://arxiv.org/abs/2410.15741)

Contents

1	Introduction	1
2	Model description	2
2.1	SNR evolution	2
2.2	Particle acceleration	3
2.3	Gamma-ray production	5
3	Model characteristics	5
4	SNR selection	8
5	Results for known SNRs	9
5.1	RX J1713.7-3946	11
5.2	Vela Junior	11
5.3	RCW 86	11
5.4	Puppis A	12
6	Discussion and conclusions	12
A	Flux predictions for SNRs	15
B	Details of MCMC fitting	16

1 Introduction

The Southern Wide-field Gamma-ray Observatory (SWGGO) is proposed to be the next generation ground-based water-Cherenkov detector array to be built in South America. SWGGO will be at an altitude of 4770 m above sea level, making it an ideal ground-based gamma-ray sky survey observatory in an energy range from a few hundred GeV to a PeV. Astrophysical gamma-rays in this energy range can have either a leptonic or hadronic origin. Under the leptonic scenario, inverse Compton scattering of energetic electrons boost photons from background radiation fields into the gamma-ray regime. Under the hadronic scenario, proton-proton interactions generate charged and neutral pions, that rapidly decay producing muons, neutrinos and gamma-ray photons (the latter two both being neutral messengers). Several known source classes can host the environment to produce gamma-rays of these energies [1]. One of these source classes, Supernova-Remnants (SNRs), are likely to contribute to the acceleration of hadronic Cosmic Rays, although the maximum energy to which this is possible is still a matter of debate [2, 3]. The gamma-ray emission from SNRs observable above 10 TeV is likely to be hadronic rather than leptonic in nature [4].

SWGGO will survey the southern gamma-ray sky in a declination range of approximately -70° to $+20^\circ$ deg, encompassing most of the galactic plane. This will allow for observations

of known southern sky SNRs at higher energies, and for detecting previously unknown SNRs. In this work, we aim to determine which of the catalogued SNRs will be detectable by SWGO. To achieve this, we use an SNR evolution and gamma-ray emission model to predict the gamma-ray spectrum emitted by different SNRs. We compare the predicted SNR spectra to the SWGO target sensitivity range [5], and then validate our model with well-known SNRs to verify its robustness. This work therefore provides useful input to the SWGO planning for the science cases pertaining to SNRs.

2 Model description

In this section we will introduce the model we use to predict the gamma-ray emission from SNRs. Firstly, we consider the SNRs' evolution to determine their properties such as their size and age, which are in turn of crucial importance to determine the particle spectrum they produce. We will then describe how we use the GAMERA software package [6, 7] to estimate the resulting gamma-ray emission produced by these particles.

2.1 SNR evolution

The evolution of an SNR is divided into four phases distinguished by their expansion velocity [8]. SNRs begin their life with a so-called *ejecta-dominated phase*. The rate of expansion depends on the type of predecessor supernova type, ranging from 5000 km/s for core-collapse supernovae to 10^4 km/s for type Ia supernovae. We only consider core-collapse supernovae in this work. For these we adopt the model of [9] to characterise the SNR's early evolution.

During the ejecta dominated phase for a core collapse supernova, the SNR expands into the wind of the progenitor star. When the SNR has swept up as much mass from the interstellar medium (ISM) as the initially ejected mass M_{ej} a state of equilibrium is reached, beginning the *Sedov-Taylor or energy conservation phase*. For a SNR expanding into the wind of its progenitor red giant, the corresponding radius at which this occurs is

$$R_0 = \frac{M_{\text{ej}} V_w}{\dot{M}} \approx 1 \left(\frac{M_{\text{ej}}}{M_{\odot}} \right) \left(\frac{V_w}{10 \text{ km s}^{-1}} \right) \left(\frac{\dot{M}}{10^{-5} M_{\odot} \text{ yr}^{-1}} \right) \text{ pc} \quad (2.1)$$

[9] which is reached at the so-called Sedov time

$$t_{\text{sed}} = \left[\left(\frac{B}{A} \right)^{1/(k-m)} \right]^{\frac{k-m}{k-3}}, \quad (2.2)$$

where $k = 9$ and $m = 2$ for type II supernovae [9]. The normalisation factor A is given by

$$A = \frac{1}{4\pi k} \frac{[3(k-3)M_{\text{ej}}]^{5/2}}{[10(k-5)E_{\text{ej}}]^{3/2}} \left[\frac{10(k-5)E_{\text{ej}}}{3(k-3)M_{\text{ej}}} \right]^{k/2}, \quad (2.3)$$

where A arises from assuming self-similarity for the time evolution of the shock [10], and $B = \dot{M}/4\pi V_w$, which arises from the condition that the density of the wind and ejecta are

equal at the SNR forward shock [9]. The development of the shock radius in both the ejecta dominated and Sedov-Taylor phases is then given by [9]

$$R_{\text{sh}}(t) = R_0 \left(\left(\frac{t}{t_{\text{sed}}} \right)^{a\lambda_{\text{ED}}} + \left(\frac{t}{t_{\text{sed}}} \right)^{a\lambda_{\text{ST}}} \right)^{1/a}, \quad (2.4)$$

with $\lambda_{\text{ED}} = (k - 3)/(k - m)$, $\lambda_{\text{ST}} = 2/(5 - m)$ and the smoothing parameter that models the transition between the two phases $a = -5$. The shock velocity during these phases is then given by

$$v_{\text{sh}}(t) = \frac{R_0}{t_{\text{sed}}} \left(\frac{R}{R_0} \right)^{1-a} \left[\lambda_{\text{ED}} \left(\frac{t}{t_{\text{sed}}} \right)^{a\lambda_{\text{ED}}-1} + \lambda_{\text{ST}} \left(\frac{t}{t_{\text{sed}}} \right)^{a\lambda_{\text{ST}}-1} \right]. \quad (2.5)$$

Until now, the energy of the system has only been distributed in thermal and kinetic energy. However, this is no longer true towards the end of the Sedov-Taylor phase. Because the radiative losses start to become non-negligible, the next stage of the SNR evolution is defined as the *snow-plough*, *pressure-driven phase* or *radiative phase*. The corresponding timescale can be defined as [11]

$$t_{\text{rad}} = 1.4 \cdot 10^{12} \left(\frac{E_{51}}{\rho_0} \right)^{\frac{1}{3}} \text{ s} \approx 44600 \left(\frac{E_{51}}{\rho_0} \right)^{\frac{1}{3}} \text{ yr}. \quad (2.6)$$

For typical values $t_{\text{rad}} \approx 100$ kyr. Nevertheless, the momentum of the system is still conserved, and the radius dependency on time decreases to $R(t) \propto t^{\frac{1}{4}}$.

Lastly, in about 10 million years, the velocity of the ejecta shell drops down to the sound speed in the ISM. This results in a constant radius ≈ 100 pc which marks the end of the SNR's evolution, known as the *merging phase*.

2.2 Particle acceleration

In an SNR shock wave, particle acceleration is believed to be driven by first-order Fermi acceleration, also known as diffusive shock acceleration [12]. In this mechanism, particles are repeatedly scattered across the shock front due to turbulent magnetic fields, gradually increasing their energy. This process results in the observed power-law spectra. Their maximum energy is dependent on the magnetic field strength B and the shock velocity v_{sh} . This energy can be approximated following [13] as

$$E_{\text{max}} \approx 3 \times 10^5 \text{ GeV } B_{100} \left(\frac{t_{\text{sed}}}{300 \text{ yr}} \right) \left(\frac{v_{\text{sh}}}{1000 \text{ km s}^{-1}} \right)^2, \quad (2.7)$$

where B_{100} is the magnetic field strength in units of $100 \mu\text{G}$. This equation assumes the maximum energy reached by diffusive shock acceleration, with magnetic field amplification upstream of the shock and Bohm-type diffusion, is highest at the end of the ejecta dominated phase (as this is the time at which the shock velocity is highest). It is obtained by comparing the acceleration timescale to the age of the SNR. Figure 1 shows how the estimated E_{max} of SNRs changes with B . The median value increases from 0.15 TeV to 5.16 TeV with increasing magnetic field and the number of SNRs exceeding 1 PeV is 0, 0 and 3 for magnetic field strengths of 3, 10 and $100 \mu\text{G}$ respectively.

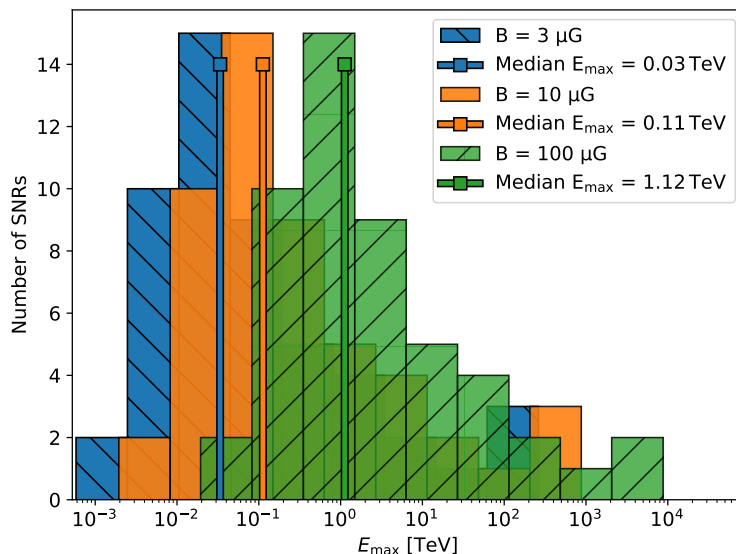


Figure 1. Change of the distribution of maximum particle energies for SNRs with the magnetic field strength.

For the energy spectrum of the protons, we use a power-law with a cut-off [14]

$$J_p \equiv \frac{dN_p}{dE_p dV} = K_p E_p^{-\alpha_p} \exp\left(-\left(\frac{E_p}{E_{0,p}}\right)^{\beta_p}\right), \quad (2.8)$$

setting the exponents to their typically used values of $\alpha_p = 2$ and $\beta_p = 1$ [14]. The normalisation constant K_p is derived from the energy density above 100 GeV

$$w_p = \int_{100 \text{ GeV}}^{\infty} E_p J_p(E_p) dE_p = 1 \text{ erg cm}^{-3}. \quad (2.9)$$

The maximum energy $E_{0,p}$ at the current age is determined by equation (2.7) at $t = t_{\text{sed}}$, where the particles of highest energy p_M can escape the acceleration region

$$p_{\text{max},0}(t) = p_M \left(\frac{t}{t_{\text{sed}}}\right)^{-\delta} \equiv E_{0,p}, \quad (2.10)$$

δ is a free parameter of the model that characterises the change in maximum energy over time at $t > t_{\text{sed}}$ [15]. This parameterisation of $p_{\text{max},0}(t)$ is a commonly used phenomenological approach to account for uncertainties associated with the magnetic turbulence generated by the accelerated particles themselves [15, 16]. We assume that magnetic turbulence amplification takes place upstream of the shock, increasing the magnitude of the time-dependence δ , for which we adopt $\delta = 3$ as a baseline value. Using this value, it is possible to replicate the observed very-high-energy gamma-ray emission for certain SNRs [15]. Assuming a power-law time dependence in this manner results in a power-law distribution of escaped particles that can come close to replicating the observed cosmic ray spectrum below the knee [16]. However, the value of δ is not well constrained [15], and we explore the phase space for δ in section 3.

2.3 Gamma-ray production

Proton-proton (p-p) interactions are believed to be the dominant process yielding gamma-ray emission from SNRs in the energy range relevant to SWGO [4]. Energetic protons accelerated in the SNR shock environment have a spectrum (equation (2.8)), and interact with target material in the surrounding medium. These interactions generate energetic pions as by-products, that rapidly decay into either electrons / positrons and neutrinos in the case of charged pions or into two gamma-ray photons in the case of neutral pions. To calculate the resulting Spectral Energy Distributions (SEDs) we use GAMERA, a library for particle and gamma-ray modeling of astrophysical sources [6, 7]. GAMERA incorporates gamma-ray emission arising from p-p interactions following the treatment of [17], which utilises parameterised approximations to the inelastic scattering cross-section $\sigma_{\text{inel}}(E_p)$. The flux of gamma-ray photons with energy E_γ produced at the source location due to p-p interactions can be written:

$$\Phi(E_\gamma) = 4\pi n_H \int \frac{d\sigma}{dE_\gamma}(E_p, E_\gamma) J(E_p) dE_p, \quad (2.11)$$

where n_H is the density of the target material with which the interactions occur, and $J_p(E_p)$ is the proton energy spectrum.

3 Model characteristics

In this section, we explore how free parameters of the model for SNR evolution and particle acceleration influence the resulting gamma-ray SED curves. We compare this to the target SWGO sensitivity band, for which we use public estimates from [5] throughout this work. The upper bound of this sensitivity band corresponds to the baseline anticipated sensitivity of SWGO in a 1 year exposure. As development of detector technologies and array layout optimisation for SWGO is ongoing, a range of lower sensitivities are possible. In particular, improvements at low energies ($\lesssim 1$ TeV) and at high energies ($\gtrsim 50$ TeV) can be achieved with compact and sparse large area array layouts respectively. Improvements in the core energy range could be achieved with improved PSF and background rejection efficiencies, through either detector technology or analysis algorithms. Table 1 summarises the default values for free parameters of our model, with the exception of the SNR age and distance, which are adapted for each individual SNR we consider.

Firstly, we note that with increasing SNR age, the cut-off energy decreases, as shown in figure 2. Equation (2.10) describes how the maximum energy of trapped particles decreases with age for SNR evolution during the Sedov-Taylor phase, i.e. at times $t_{\text{rad}} \geq t \geq t_{\text{sed}}$, as high energy particles escape.

Secondly, the magnetic field strength within the SNR is treated as affecting the maximum energy achieved via equation (2.7). Hence increasing the magnetic field strength also increases the maximum energy of the particle spectrum and the cut-off energy of the gamma-ray spectrum, as shown in figure 3. The normalisation of the gamma-ray flux due to p-p interactions can be seen to remain at a near constant flux level below $\simeq 0.1$ TeV.

Parameter	Assumed Value	Possible Range	Reference
B	$100 \mu\text{G}$	$50\text{--}200 \mu\text{G}$	[18]
M_{ej}	$3 M_{\odot}$	$1\text{--}10 M_{\odot}$	[19]
ρ_0	$1 m_{\text{p}} \text{cm}^{-3}$	$0.1\text{--}100 m_{\text{p}} \text{cm}^{-3}$	[18]
δ	3	Poorly Constrained	[15]
E_{ej}	10^{51}erg	$\sim 0.1\text{--}10 \times 10^{51} \text{erg}$	[11, 20]
α_{p}	2	Common Assumption	[14]
β	1	Common Assumption	[14]

Table 1. Values adopted for free parameters of our SNR evolutionary model, unless otherwise specified. For the proton spectrum, we use an exponential cut-off power law model with index α_{p} (equation (2.8)).

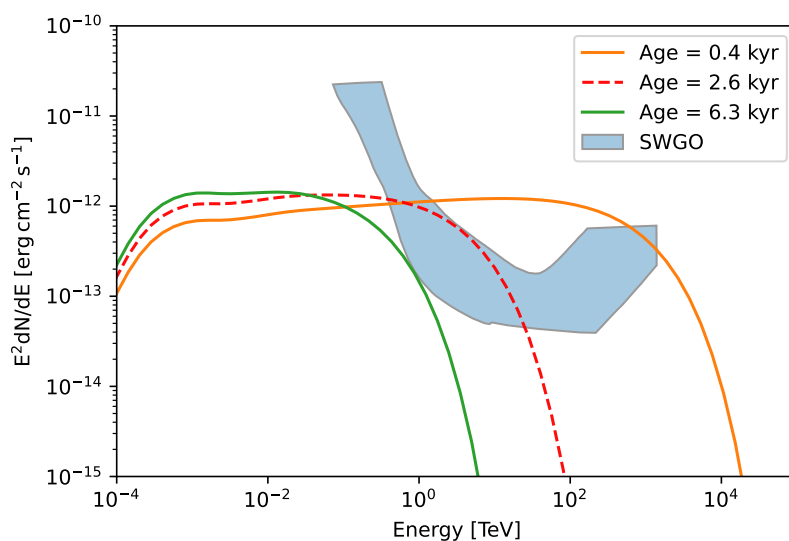


Figure 2. The influence of the SNR age on the SED, the dashed red line is for the median age of the SNRs in the sample that are detectable, the orange line for the 5th and the green line for the 95th percentile of these SNRs [21]. We assume here a distance of 3.7 kpc, which is the mean value for the sources in the SNR sample that exceed the SWGO sensitivity. We take the SWGO sensitivity band from [5] for comparison.

Figure 3 (top) also shows the influence of the ISM density ρ_0 . This does not affect the energy reached, but rather simply number of interactions that protons undergo and hence the flux normalisation.

The parameter δ is relevant to equation (2.10) describing the evolution of the particle escape in the Sedov-Taylor phase. With increasing δ values, the dependence on time is stronger, such that for the same SNR age, the maximum energy of trapped particles is decreased with increasing δ . This decreases the cut-off energy of the gamma-ray spectrum as shown in figure 3; changing δ from 1 to 4 reduces the maximum energy from 1500 TeV to 7 TeV.

With increasing ejecta mass, the Sedov time increases (equation (2.2)), and the maximum energy at a given age also increases. However, with increasing ejecta energy, the Sedov time

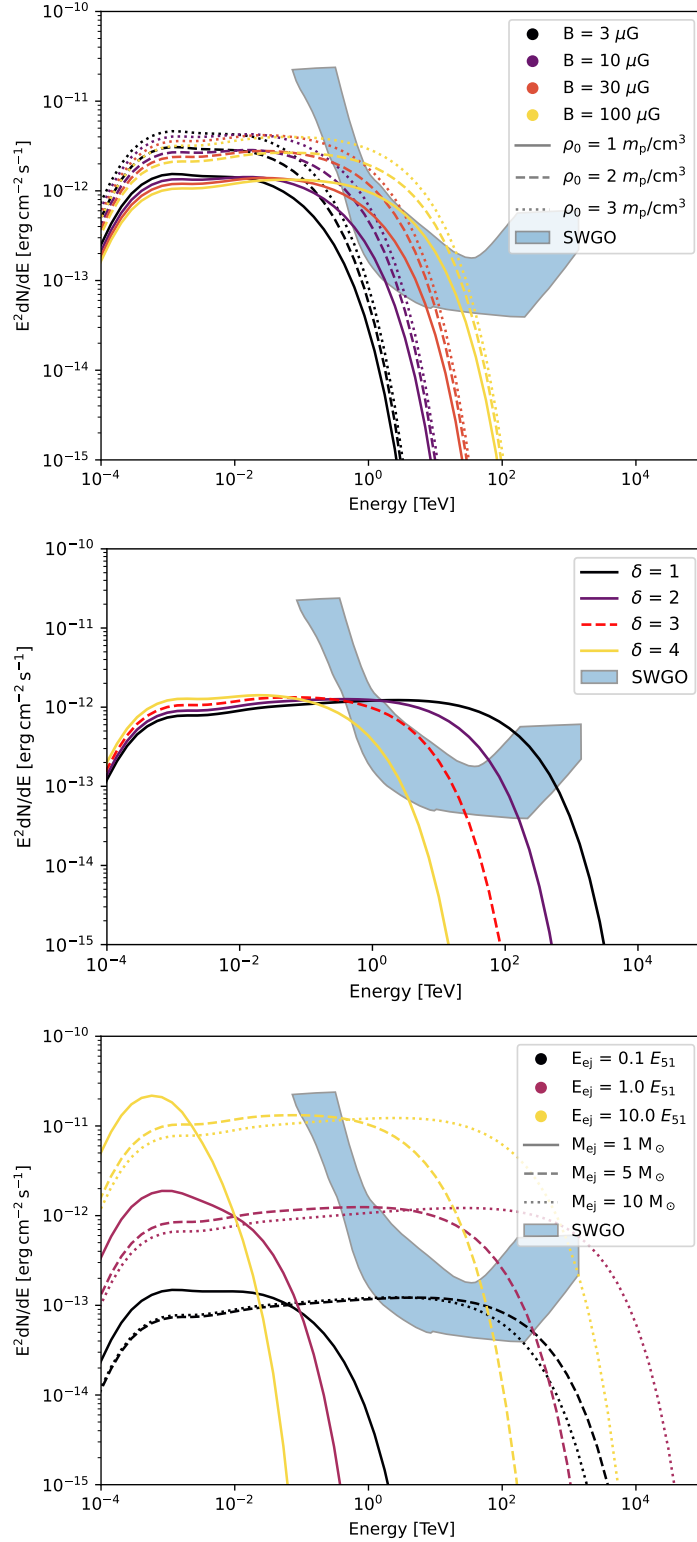


Figure 3. Influence of various model parameters on the gamma-ray SED, shown for an SNR age of 2.8 kyr and a distance of 3.7 kpc corresponding to the mean age and distance of the SNRs from the sample which exceed SWGO sensitivity. We take the target SWGO sensitivity band from [5] for comparison. Top: influence of magnetic field strength and ISM density on the SED. Middle: influence of δ , see equation (2.10). Bottom: influence of the SN ejecta energy E_{ej} and mass M_{ej} on the SED.

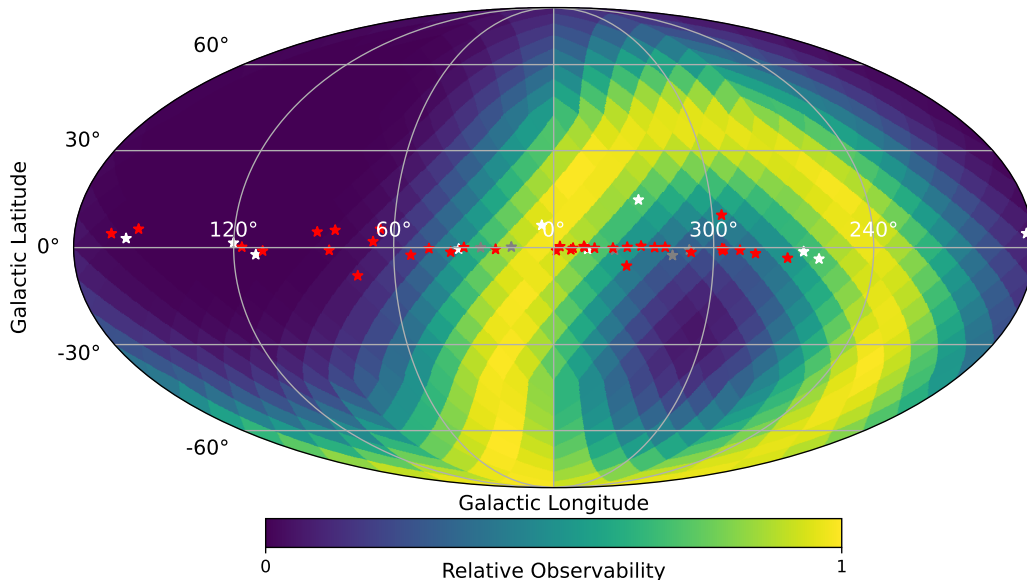


Figure 4. SNRs we consider in this work. Those for which we predict a gamma-ray flux above the upper limits of the 1 year SWGO sensitivity curve shown in white, those within the band that may be detectable depending on the array configuration and analysis improvements are shown in grey, and the remaining SNRs in our selection are shown in red. Possible observability from the SWGO site relative to maximum is also shown [21].

decreases as in equation (2.2), and for fixed age the maximum energy decreases (see figure 3). This is a consequence of higher energy particles escaping from the remnant at earlier times.

4 SNR selection

We obtain our set of SNRs from the public catalogue *SNRcat* [21], which contains 383 entries of SNRs and SNR candidates. To ensure our set only contains true SNRs we exclude all entries of doubtful SNR association, such as plerionic composites and those where it is unclear whether ejecta remains. We also exclude those where information on the distance or age is not available, and restrict the age range to be $300 \text{ yr} \leq \text{age} \leq 95000 \text{ yr}$ such that the selected SNRs are at least on the verge of the Sedov-Taylor phase. The SNRs we consider are shown in figure 4, with the observability calculated for the SWGO site at Pampa La Bola, located at $22^\circ 56' 41.30'' \text{ S}$, $67^\circ 40' 39.09'' \text{ W}$ (altitude 4770 m). A maximum observing zenith angle of 45° was assumed. Based on the reported age and radius of each SNR provided, we estimated the ejecta energy from equation (2.4). To down-select for SNRs that can be reasonably described by our model, we restrict the implied ejecta energy to be $0.1 E_{51} \leq E_{\text{ej}} \leq 10 E_{51}$. With these conditions we obtain the set of 51 SNRs shown in figure 5. SNRs for which the measured radius and reported age lie outside of the shaded band cannot be reasonably approximated as following the Sedov-Taylor evolution described by our model.

Using equation (2.8) we calculate proton spectra assuming the same conditions for each SNR, and using the GAMERA modelling package we obtain the gamma-ray curves shown in figure 6. The 6 SNRs that are located within the observable sky to SWGO and exceed

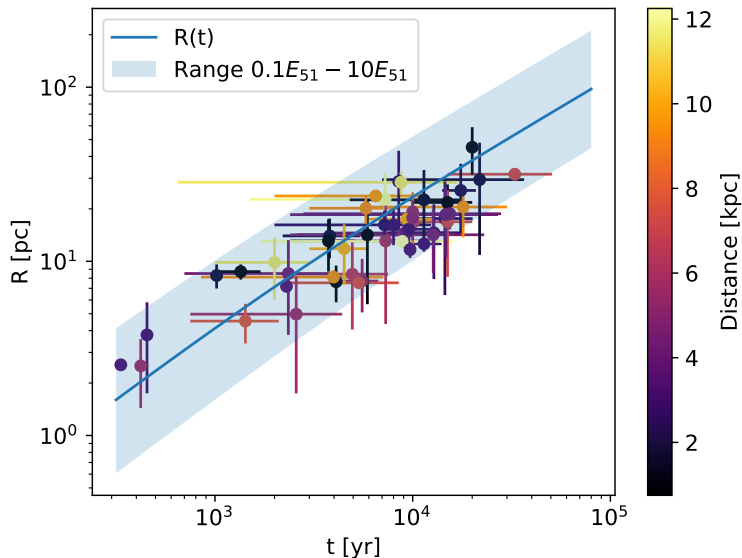


Figure 5. Properties of the 55 SNRs fulfilling our selection criteria. The relation between ejecta energy E_{ej} , age and SNR radius as described by equation (2.4) is indicated by the linear relation, with the shaded region indicating variation in ejecta energy of a factor 10.

the baseline SWGO sensitivity, and thus will certainly be detectable, are highlighted with solid lines in figure 6. Those SNRs that (according to our model) cannot be detected within 1 year by the baseline configuration of SWGO on account of their gamma-ray flux, but that could be detected with the best possible SWGO sensitivity, are shown with dot-dashed lines in figure 6. We note that should improvements in the core energy range achieve the lower bound of the anticipated sensitivity band, then a further 5 SNRs are potentially detectable by SWGO in 1 year. Improvements at high energies (such as due to a sparse array layout) do not lead to a larger number of detected SNRs, as few SNRs have a $E_{max} \gtrsim 1$ TeV using our model. These 11 SNRs that could potentially be detected by SWGO are listed in table 2, the other SNRs in the sample are shown in grey in figure 6 and listed in table 4.

5 Results for known SNRs

To validate our simple model with existing observations, we used a Markov Chain Monte Carlo (MCMC) fitting approach for four SNRs. We fit our model to SNRs that have already been detected at gamma-ray energies, and that should also be visible from the SWGO site. From table 2 (which also shows the SNRs' properties) and figure 6, the certainly detectable SNRs are RX J1713.7-3946, SN1006, Vela Jr, the Kepler SNR, Puppis A and G035.6-00.4, and the SNRs detectable dependent on the final array configuration and analysis pipeline are G309.2-00.6, Kes 73, G337.2-00.7 and G015.9+00.2. RCW 86 is a borderline case which we will consider potentially detectable for the remainder of this paper. Of these, we choose four SNRs as exemplars to test the validity of our model. It should however be noted that our model is simplistic in order to maintain its predictive power, and so for interpretation of the physics of these systems in greater depth we refer the reader to the works referenced in this section.

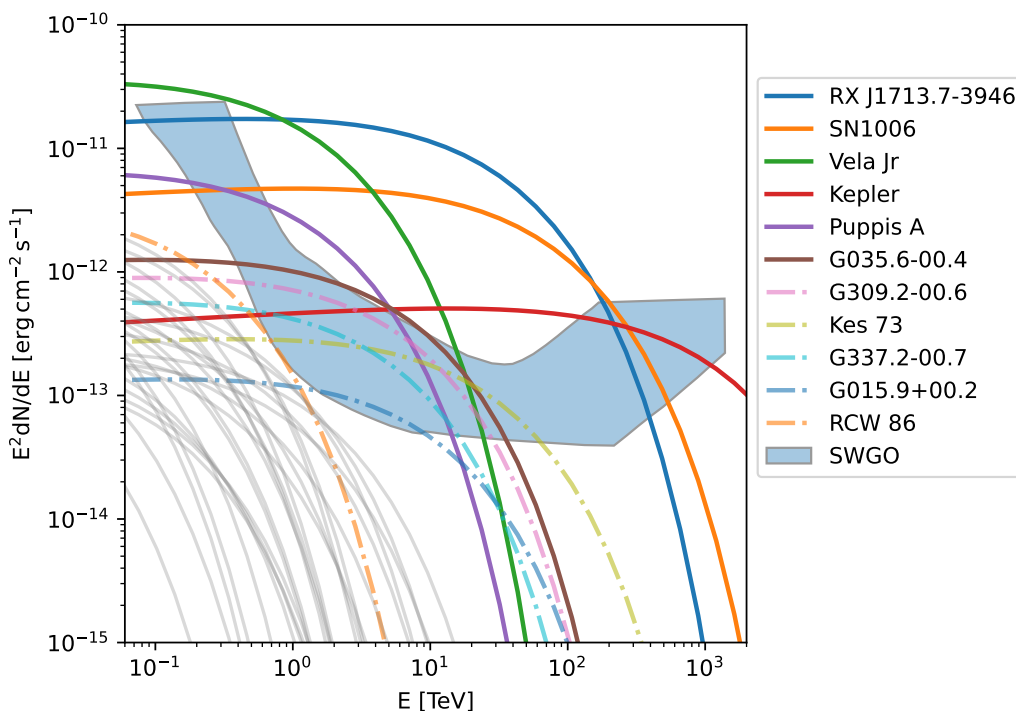


Figure 6. SEDs resulting from our model for the SNRs located in the southern sky compared to the target SWGO sensitivity curve which we take from [5] for comparison. The potentially detectable SNRs are highlighted, with solid lines indicating that the SNR will be detectable regardless of array configuration and analysis method, and dot-dashed lines showing those that will be detectable in the most favorable scenario. As RCW 86 is a borderline case we will consider it potentially detectable in this work.

Source	Age [kyr] [min, max]	Dist. [kpc] [min, max]	Size [arcmin]	Flux $E > 1$ TeV [TeV cm ⁻² s ⁻¹]	Flux $E > 10$ TeV [TeV cm ⁻² s ⁻¹]
RX J1713.7-3946	[1.0,1.7]	[0.9,1.1]	60	3e-11	7.99e-12
SN1006	1.019	[1.6,2.2]	30	1.07e-11	3.93e-12
Vela Jr	[2.4,5.1]	[0.5,1.0]	120	8.61e-12	8.81e-14
Kepler	0.421	[3.3,8.2]	3	1.98e-12	1.23e-12
Puppis A	[2.2,5.4]	[1.3,2.2]	55	1.52e-12	1.42e-14
G035.6-00.4	≤2.3	[3.5,4.1]	13	1.03e-12	9.19e-14
G309.2-00.6	[0.7,4.0]	[2.0,7.0]	13	7.08e-13	5.92e-14
Kes 73	[0.75,2.1]	[5.8,9.8]	4	4.67e-13	1.15e-13
G337.2-00.7	[0.75,4.4]	[2.0,9.4]	6	3.73e-13	2.31e-14
G015.9+00.2	[1.0,3.0]	[7.0,16.0]	5.9	1.41e-13	1.82e-14
RCW 86	[2.0,12.4]	[2.1,3.2]	42	2.98e-14	—

Table 2. List of SNRs that will be potentially detectable by SWGO within 1 year according to figure 6. The values for the ages, distances and sizes are taken from *SNRcat* [21].

5.1 RX J1713.7-3946

For RX J1713.7-3946 the single power law (PL) from equation (2.8) proved to not be able to sufficiently represent the data, therefore we adopted a broken power law (BPL)

$$J_p = \begin{cases} \left(\frac{E}{1 \text{ TeV}}\right)^{-\alpha_0} & E < E_{\text{break}} \\ \left(\frac{E}{E_{\text{break}}}\right)^{-(\alpha-\alpha_0)} E^{-\alpha} \exp\left(-\frac{E}{E_{0,p}}\right) & E \geq E_{\text{break}} \end{cases} \quad (5.1)$$

as used in [22]. Figure 7 shows the results of an MCMC fit to existing gamma-ray data on this SNR, with best fit parameters reported in table 3.

In our model, the ambient density and the ejecta energy have a similar effect on the spectrum (see figure 3) and are therefore not constrained in the MCMC results. However, during the Sedov-Taylor phase they describe the SNR's radius via equation (2.4). Therefore, we added a condition to our prior for the MCMC fitting that checks whether the radius lies within the range of the size derived from the parameters in *SNRcat* if the age of the SNR is larger than t_{sed} . A detailed description is given in appendix B. A similar degeneracy exists between the magnetic field and the mass in our model. Here we used evidence that the magnetic field should be at the order of $100 \mu\text{G}$ to explain the measured flux [23], and set the prior for B to a Gaussian with $\mu = 100 \mu\text{G}$ and $\sigma = 20 \mu\text{G}$. For SNRs with an age of a few kyr, the influence of δ on the resulting spectrum is still weak. Therefore we set a Gaussian prior for δ as well, with $\mu = 3$ and $\sigma = 0.5$.

The spectral best-fit parameters differ slightly from those reported in [22], which obtained an $E_{\text{break}} = 1.4_{-0.4}^{+0.7} \text{ TeV}$ and $\alpha = 1.94 \pm 0.05$ above the break energy, although the low index of 1.53 ± 0.09 is compatible with our $\alpha_0 = 1.42_{-0.14}^{+0.11}$. In terms of physical properties, we obtained an ejecta energy of $2.75_{-0.13}^{+0.12} \times 10^{51} \text{ erg}$ for an underdense medium of $0.38 \pm 0.02 \text{ cm}^{-3}$. The total energy in particles can be obtained from ejecta energy via $W_p = \varepsilon_{\text{cr}} E_{\text{ej}} \left(\frac{n}{1 \text{ cm}^{-3}}\right)$ [22, 24]. For a fixed conversion efficiency ε_{cr} of 10% (which we assume throughout this work), this corresponds to $\sim (1.05 \pm 0.07) \times 10^{50} \text{ erg}$, a factor 10 higher than the 10^{49} erg reported in [22].

Using equations (2.10) and (2.2), the cut-off energy $E_{0,p}$ of the particle spectrum can be derived from our best-fit parameters in table 3, yielding 60_{-8}^{+9} TeV .

5.2 Vela Junior

For Vela Jr, the spectral model used for the particle spectrum was equation (2.8) (consistent with that used by H.E.S.S. [24]), where an index α_p of 1.81 ± 0.08 was fit. This is compatible with our MCMC results.

We obtained an ejecta energy for the progenitor supernova explosion of $1.18_{-0.19}^{+0.22} \times 10^{51} \text{ erg}$. For our obtained density of $0.71_{-0.12}^{+0.14} \text{ cm}^{-3}$ this corresponds to an energy in particles of $\sim (8.4 \pm 2.0) \times 10^{49} \text{ erg}$, of the same order of magnitude as the $(7.1 \pm 0.3) \times 10^{49} \text{ erg}$ reported by [24].

5.3 RCW 86

From our power law spectral model for the proton population, we obtain an index $\alpha_p = 1.57_{-0.15}^{+0.13}$, compatible with the spectral index value of 1.7 obtained by H.E.S.S. [25]. For RCW 86, the corresponding cut-off energy derived from our MCMC results in table 3 is

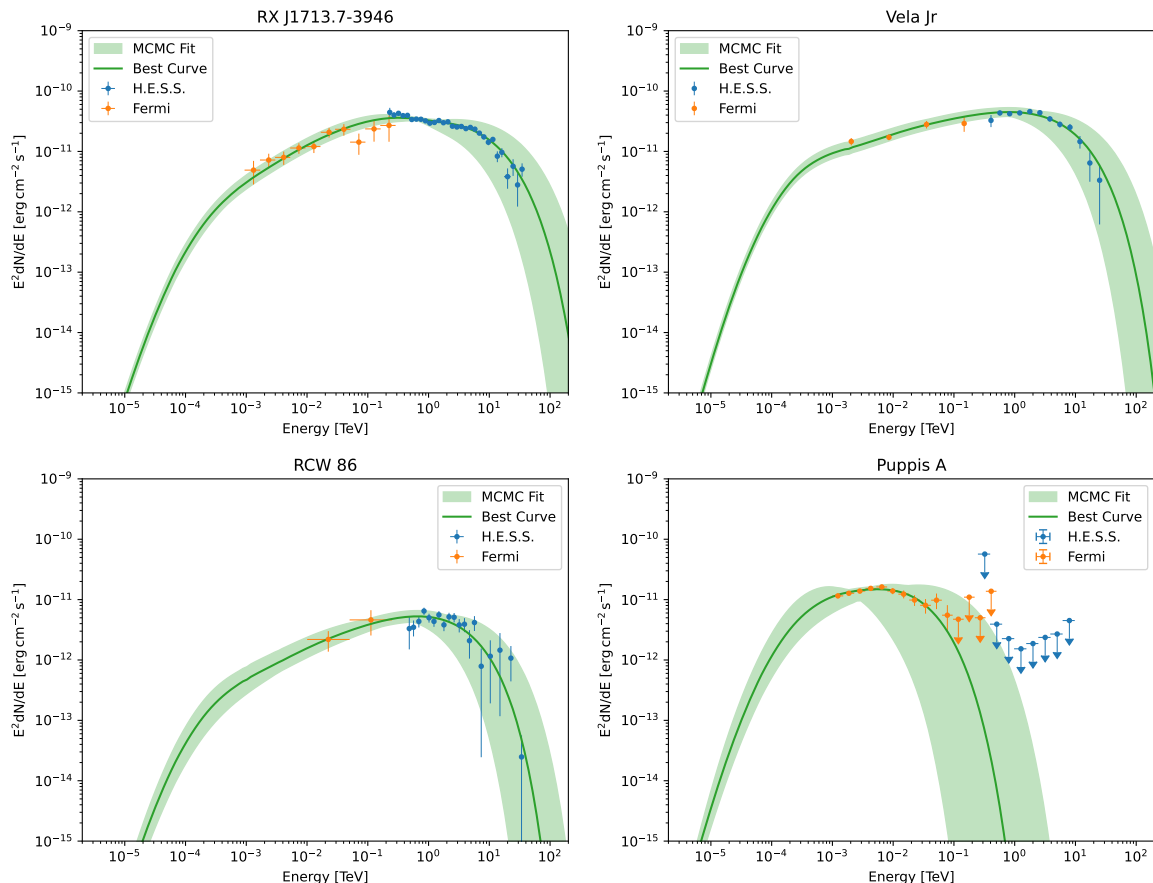


Figure 7. Best fit results of MCMC fitting of our model to gamma-ray data for the detected SNRs. The shaded band indicates the region allowed by variation within the 16th and 84th quantiles of the sample distribution.

30_{-7}^{+8} TeV. We obtain a magnetic field strength of $100_{-20}^{+21} \mu\text{G}$, compatible with the $\sim 100 \mu\text{G}$ used for the hadronic model of [25]. We also obtain a total energy in particles of $(9.5_{-2.6}^{+3.2}) \times 10^{49}$ erg using our best-fit density value and a 10% conversion efficiency from the SN ejecta energy into protons, comparable with the $\sim 7 \times 10^{49}$ erg from [25, 26].

5.4 Puppis A

Despite a reasonably bright detection with Fermi-LAT, observations with H.E.S.S. found no significant emission, placing constraining upper limits on the region [27]. We apply an MCMC fit to the Fermi-LAT and H.E.S.S. data with our model, finding a slightly lower ejecta mass $M_{\text{ej}} = 1.4_{-0.5}^{+0.6} M_{\odot}$ than for the other SNRs modelled. The cut-off energy $E_{0,p}$ for the proton spectrum is however considerably lower than for the other three SNRs, which is necessary in this model to account for the lack of TeV emission from Puppis A.

6 Discussion and conclusions

In this study, we implemented a simple evolutionary model to describe SNRs in the Sedov phase, during which it is most likely that gamma-ray emission can be anticipated. Using *SNR*-

	RX J1713.7-3946	Vela Jr	RCW 86	Puppis A
J_p	BPL	PL	PL	PL
B (μG)	100 ± 20	99^{+20}_{-21}	100^{+21}_{-20}	99 ± 20
M_{ej} (M_{\odot})	$2.7^{+0.5}_{-0.6}$	$4.3^{+0.8}_{-0.9}$	$4.8^{+1.0}_{-1.1}$	$1.4^{+0.6}_{-0.5}$
ρ ($m_p \text{cm}^{-3}$)	0.38 ± 0.02	$0.71^{+0.14}_{-0.12}$	$1.44^{+0.40}_{-0.29}$	$1.12^{+0.12}_{-0.11}$
δ	3.0 ± 0.5	3.0 ± 0.5	3.0 ± 0.5	3.1 ± 0.5
E_{ej} (E_{51})	$2.75^{+0.12}_{-0.13}$	$1.18^{+0.22}_{-0.19}$	$0.66^{+0.13}_{-0.12}$	$1.36^{+0.10}_{-0.09}$
α_p	—	1.78 ± 0.03	$1.57^{+0.13}_{-0.15}$	$1.42^{+0.23}_{-0.40}$
β_p	—	$1.25^{+0.22}_{0.21}$	$1.27^{+0.21}_{-0.20}$	$0.95^{+0.26}_{-0.25}$
α	$1.54^{+0.3}_{-0.4}$	—	—	—
α_0	$1.42^{+0.11}_{-0.14}$	—	—	—
E_{break} (TeV)	$3.2^{+0.9}_{-0.7}$	—	—	—
$E_{0,p}$ (TeV)	61^{+150}_{-21}	66^{+160}_{-23}	28^{+80}_{-9}	$0.132^{+0.700}_{-0.016}$

Table 3. Best fit values from the MCMC, the values correspond to the 16th, 50th and 84th quantile of the sample distribution. Corner and convergence plots are shown in appendix B.

cat [21], we selected SNRs that will be observable by the forthcoming SWGO. Implementing the baseline scenario for our model (representative values) for each SNR, and adapting the age and distance as appropriate, we are able to predict an expected gamma-ray flux level. A total of at least six and possibly as many as eleven SNRs have predicted gamma-ray fluxes that should be detectable by SWGO within one year of operation.

For four of these SNRs that have already been detected at gamma-ray energies, RX J1713.7-3946, Vela Jr, RCW 86 and Puppis A, we proceeded to run an MCMC analysis using our model to constrain the properties of the supernova remnant and its environment. These converged to values that are comparable to those in the literature, as discussion in the previous section.

This broad consistency with values obtained in previous works helps to validate our simple model and predictions for SNR observations with SWGO. Given that WCD facilities such as SWGO have a wide field-of-view, observations may be able to detect a halo of particles escaped from the SNR shock, as predicted by [28], that may extend over large angular scales. Detailed studies of large-scale gamma-ray emission around SNRs could constrain particle transport and the diffusion coefficient of CRs in the vicinity of SNR shocks, as well as the contribution of escaping particles to the galactic CR sea.

Although we do not fit SN 1006 with our model in this study, observations of the SNR will nevertheless be interesting on account of its dual lobe morphology. It has been suggested that this feature is due to polarisation of the magnetic field in this SNR, such that particles are preferentially transported in one direction along the magnetic field lines, as opposed to perpendicular to them (where less emission is observed) [29]. Observations with SWGO could further help to corroborate this hypothesis, by improving the sensitivity across the entire region and on larger angular scales, indicating to what extent the nonthermal emission in the region continues to show preferential orientation.

SWGGO will have an angular resolution improving with energy from $\sim 1^\circ$ at threshold to $\lesssim 0.4^\circ$ at energies > 1 TeV, potentially reaching $\sim 0.1^\circ$ [30]. From table 2, this should be sufficient to resolve shell-like structure in at least half of the potentially detectable SNRs. Asymmetries to the emission could hence be detected by SWGGO, although these are not accounted for in our work.

The model presented here can be similarly applied to SNRs located in the Northern hemisphere, and potentially compared to Northern observations by facilities such as HAWC, LHAASO, the ASTRI Mini-Array or the forthcoming CTAO [31–34]. However, to gain a better handle on the magnetic field strength or ambient density, multiwavelength observations are required. Given the large angular size of some of these supernova remnants, sky scanning facilities such as eROSITA [35] or MeerKAT [36] provide ideal complements to the SWGGO survey view at TeV energies.

Recent results from HAWC and LHAASO revealed a new population of ultra high energy ($E_\gamma > 100$ TeV) sources along the Northern galactic plane [37–39]. We anticipate that a number of ultra high energy sources remain to be discovered in the Southern sky by SWGGO. Whether or not SNRs are among these ultra high energy sources remains to be determined.

As we assumed a hadronic scenario in all cases, constraining the model parameters (for both the SN energetics and proton spectrum) yields insights as to the likely contributions of the SNRs towards the origins of galactic Cosmic Rays. It should also be noted that SWGGO will also have a high degree of complementarity with the upcoming Cherenkov Telescope Array Observatory (CTAO); new SNRs detected by SWGGO given its wide field of view could be the subject of follow-up observations by CTAO with its enhanced angular resolution. This would help to reduce source confusion. But SWGGO may be sensitive to larger angular structures, and will have a larger effective area at the highest energies, therefore constraining the maximum energies reached.

Acknowledgments

NS, STS and AMWM are supported by the Deutsche Forschungsgemeinschaft (DFG) project number 452934793.

A Flux predictions for SNRs

Source	Observable	Age [kyr] [min, max]	Dist. [kpc] [min, max]	Size (arcmin)	Flux	
					$E > 1$ TeV [TeV cm ⁻² s ⁻¹]	$E > 10$ TeV [TeV cm ⁻² s ⁻¹]
Tycho	—	0.453	[1.5,5.0]	8	6.02e-12	3.66e-12
Cassiopeia A	—	[0.316,0.352]	[3.3,3.7]	5	5.13e-12	3.09e-12
G182.4+04.3	—	[3.8,4.4]	[0.8,1.3]	50	3.3e-12	1.81e-14
HB9	—	[2.6,9.2]	[0.3,1.2]	130	1.33e-12	1.39e-16
Circinus X-1	✓	[0.85,7.1]	[8.4,10.2]	6	4.66e-14	3.21e-16
G308.3-01.4	✓	[2.4,7.5]	[3.1,9.8]	9	4.25e-14	4.24e-17
Kes 79	✓	[4.4,6.7]	[3.5,7.1]	10	3.68e-14	9.29e-18
G344.7-00.1	✓	[3.0,6.0]	[6.3,14.0]	8	2.53e-14	6.43e-17
G352.7-00.1	✓	[2.2,8.5]	[7.0,8.0]	6.9	2.2e-14	8.94e-18
G318.2+00.1	✓	≤8.0	[2.3,3.71]	37	9.97e-15	—
Kes 32	✓	[3.0,8.6]	[7.5,11.0]	15	9.59e-15	1.3e-18
PKS 1209-51/52	✓	[7.0,10.0]	[1.3,3.9]	76	7.67e-15	—
G272.2-03.2	✓	[3.6,11.0]	[2.0,10.0]	15	5.25e-15	—
1156-62	✓	[2.0,11.0]	[9.0,10.2]	17	4.58e-15	—
G332.5-05.6	✓	[7.0,12.1]	[2.2,3.8]	35	1.7e-15	—
G067.7+01.8	—	[1.5,13.0]	[7.0,17.0]	13	1.38e-15	—
G038.7-01.3	✓	[3.8,14.7]	[4.0,4.0]	25	1.37e-15	—
Kes 69	✓	[8.8,9.2]	[4.1,5.8]	20	1.2e-15	—
G359.0-00.9	✓	≤9.7	[3.13,3.85]	23	1.05e-15	—
HB21	—	[4.8,18.0]	[0.8,2.3]	100	5.91e-16	—
the Square	✓	≤10.0	[3.79,6.4]	24	3.39e-16	—
CTB 37B	✓	[0.65,16.8]	[9.8,13.2]	17	3.04e-16	—
MSH 10-53	✓	≤10.0	[4.8,6.2]	24	2.91e-16	—
Kes 41	✓	[1.7,16.0]	[12.2,12.3]	7.3	2.32e-16	—
G084.2-00.8	—	[8.4,11.7]	[5.8,7.0]	18	2.02e-16	—
G296.7-00.9	✓	[5.8,12.9]	[9.1,10.9]	12	1.94e-16	—
CTB 109	—	[8.8,14.0]	[2.79,3.4]	28	1.48e-16	—
HC30	✓	≤10.0	[5.7,11.4]	15	1.2e-16	—
CTB 1	—	[7.5,18.1]	[1.6,4.3]	34	2.14e-17	—
Kes 27	✓	[2.4,23.0]	[2.8,6.5]	21	1e-17	—
Cygnus Loop	—	[10.0,20.0]	[0.576,1.0]	190	8.08e-18	—
VRO 42.05.01	—	[9.0,20.1]	[1.0,4.5]	44	1.46e-18	—
J1731-347	✓	[2.4,27.0]	[2.4,6.1]	30	4.71e-19	—
G296.1-00.5	✓	[2.8,28.0]	[3.5,5.1]	30	1.32e-19	—
MSH 11-61A	✓	[10.0,20.0]	[3.5,11.0]	16	—	—
CTB 37A	✓	[6.0,30.0]	[6.3,12.5]	15	—	—
3C400.2	✓	[15.0,50.7]	[6.7,7.8]	30	—	—
W63	—	[14.1,20.9]	[1.3,3.2]	78	—	—
G065.3+05.7	—	≤20.0	[0.8,1.5]	270	—	—
G156.2+05.7	—	[7.0,36.6]	[0.68,3.0]	110	—	—

Table 4. All SNRs from the set that will not be detectable. The second column indicates whether they will be physically observable from the SWGO site. Fluxes below 1e-19 TeV cm⁻² s⁻¹ are omitted.

parameter	RX J1713.7-3946	Vela Jr	RCW 86	Puppis A
B (μG)	$\mu = 100, \sigma = 20$	$\mu = 100, \sigma = 20$	$\mu = 100, \sigma = 20$	$\mu = 100, \sigma = 20$
M_{ej} (M_{\odot})	RP: $a = 2$	RP: $a = 1$	RP: $a = 3$	RP: $a = 1.25$
ρ ($m_{\text{p}}\text{cm}^{-3}$)	[0, 10]	[0, 6]	[0, 3]	[0, 5]
δ	$\mu = 3, \sigma = 0.5$	$\mu = 3, \sigma = 0.5$	$\mu = 3, \sigma = 0.5$	$\mu = 3, \sigma = 0.5$
E_{ej} (E_{51})	RP	RP	RP	RP
α_{p}	—	[1.6, 2.2]	$\mu = 2, \sigma = 0.25$	[0, 5]
β_{p}	—	$\mu = 1, \sigma = 0.25$	$\mu = 1, \sigma = 0.25$	$\mu = 1, \sigma = 0.25$
α	[1.35, 4.00]	—	—	—
α_0	[1, 5]	—	—	—
E_{break} (TeV)	[0, 6]	—	—	—

Table 5. The priors used for each parameter. The intervals stand for uniform priors, μ/σ for gaussian priors. RP stands for “radius prior” and is described separately.

B Details of MCMC fitting

MCMC algorithms are a class of techniques to sample probability distributions, and are therefore highly useful for fitting multi-parameter functions to data. Through sampling the posterior probability distributions of these variables around their determined optimum value, they allow one to provide robust uncertainties and to explore covariances between parameters [40]. To perform the MCMC fitting, we follow the recommendation of [40] and use the *scipy* package [41] to find the best starting position in the multi-dimensional parameter space for the MCMC sampler, for which we use the *emcee* package [42] to obtain posterior distributions. These are obtained by having a number of ‘walkers’ performing random steps around the parameter space in order to find the best possible fit to the data. In order to help the MCMC sampler find this optimal fit, it is useful to specify a prior that describes the likely range and distribution of the fitted variables. We detail the priors we use in this work in table 5. In this appendix, we also display corner plots for the three sources we consider (figures 8, 9, 10 and 11); these show the 1 and 2-dimensional projections of the posterior parameter distributions, and can be used to visualise covariances between parameters. We also show convergence plots based on the autocorrelation metric described in detail in [40] (figures 12, 13, 14 and 15) to investigate whether the walkers have had sufficient time to robustly explore the parameter space. All four fits show good evidence for convergence.

Radius prior. Since the shock radius is described via equation (2.4), which depends on M_{ej} and E_{ej} , we can define a prior that constrains the modelled radius to be within the range derived from the given angular size and distance, i.e. we check whether the radius for given M_{ej} and E_{ej} estimated at the youngest age is larger than the lower limit of the radius and vice versa at the upper limit. However, since for some SNRs the range of possible ages is quite large, the possible values for M_{ej} and E_{ej} are quite restricted. So to let the sampler explore the parameter space we took as a uniform prior the radius range $\bar{R} \pm \Delta R * a$, where a is the factor by which we increase the allowed radius.

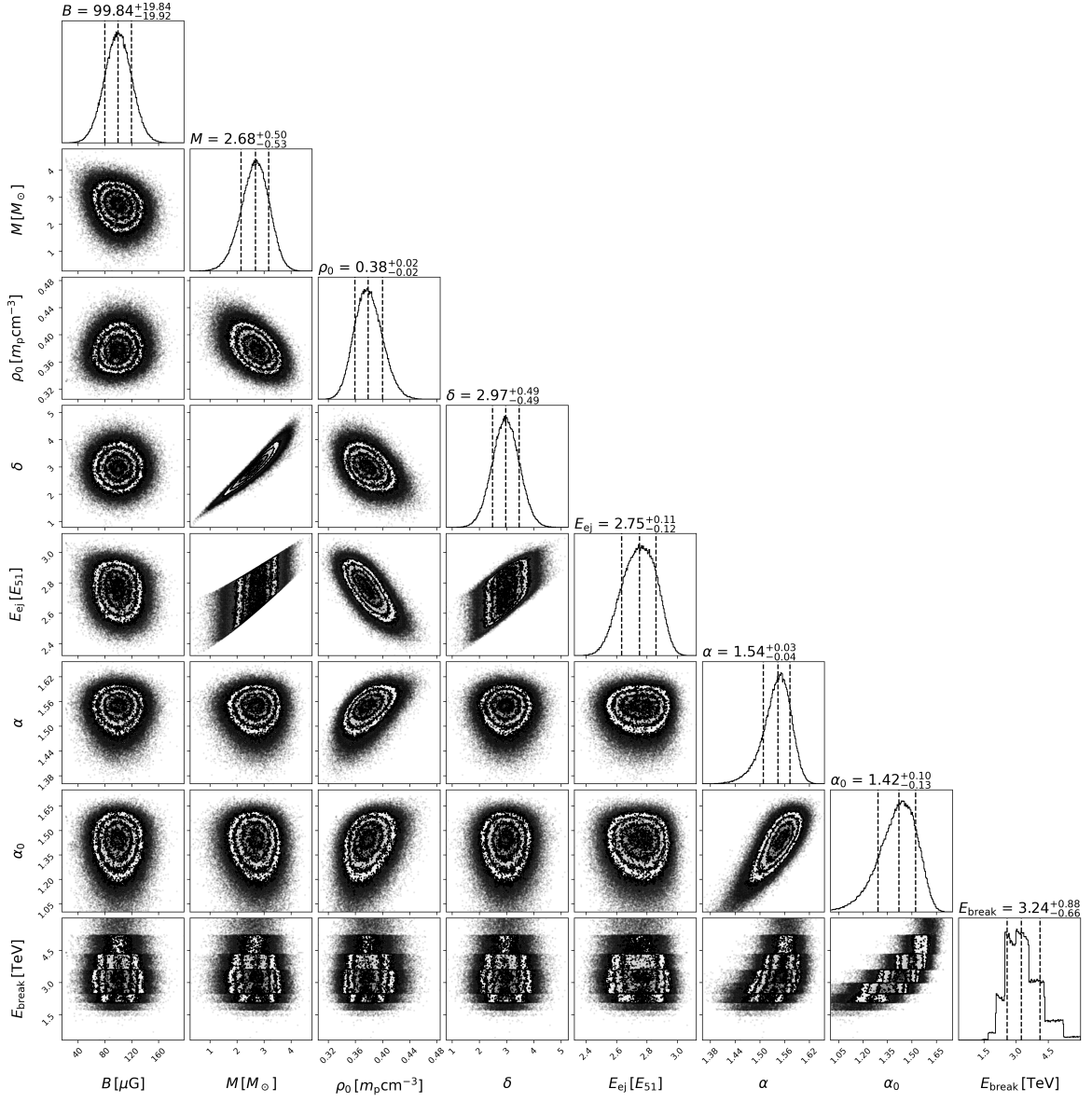


Figure 8. MCMC results for RX J1713.7-3946.

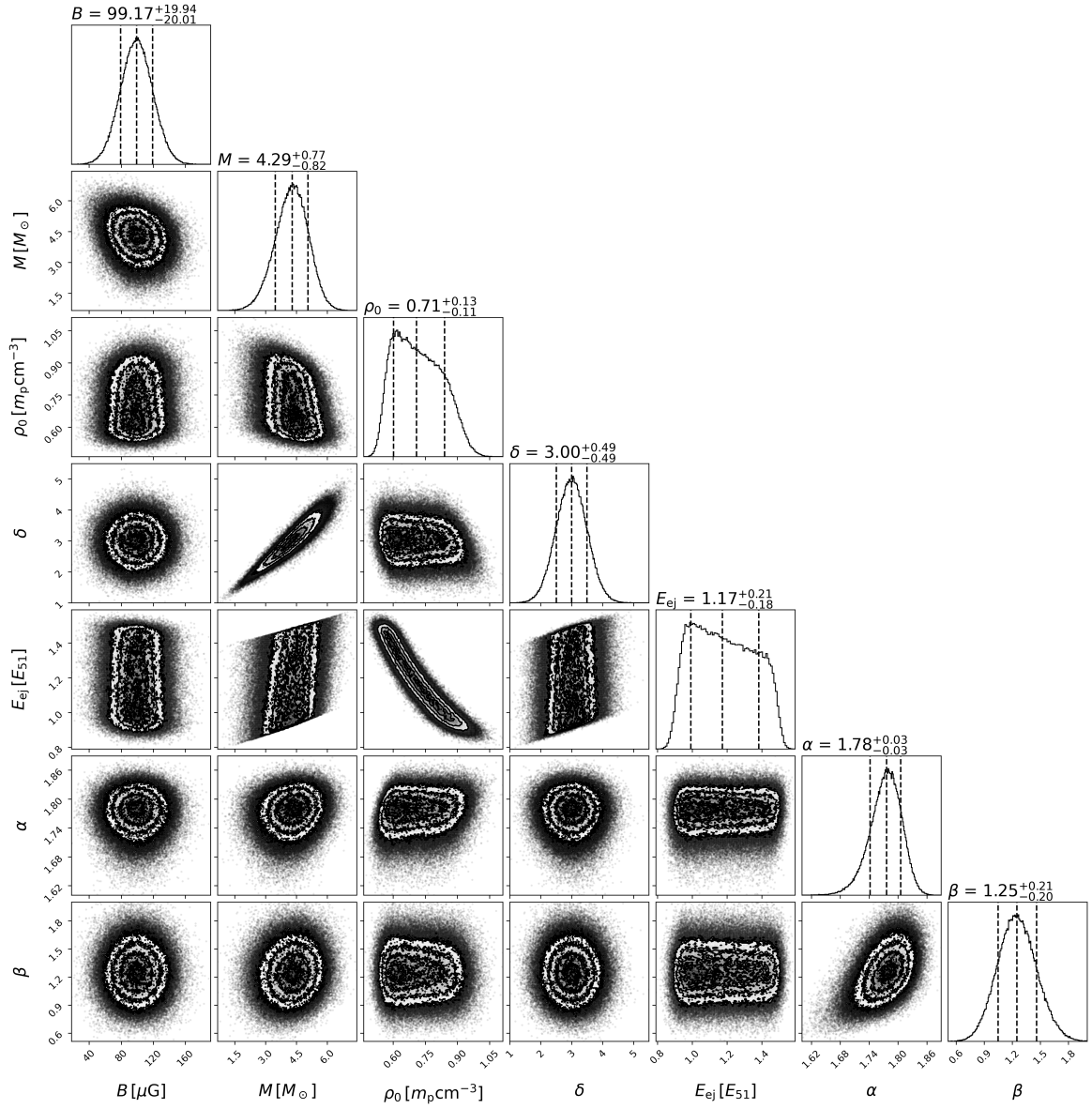


Figure 9. MCMC results for Vela Jr.

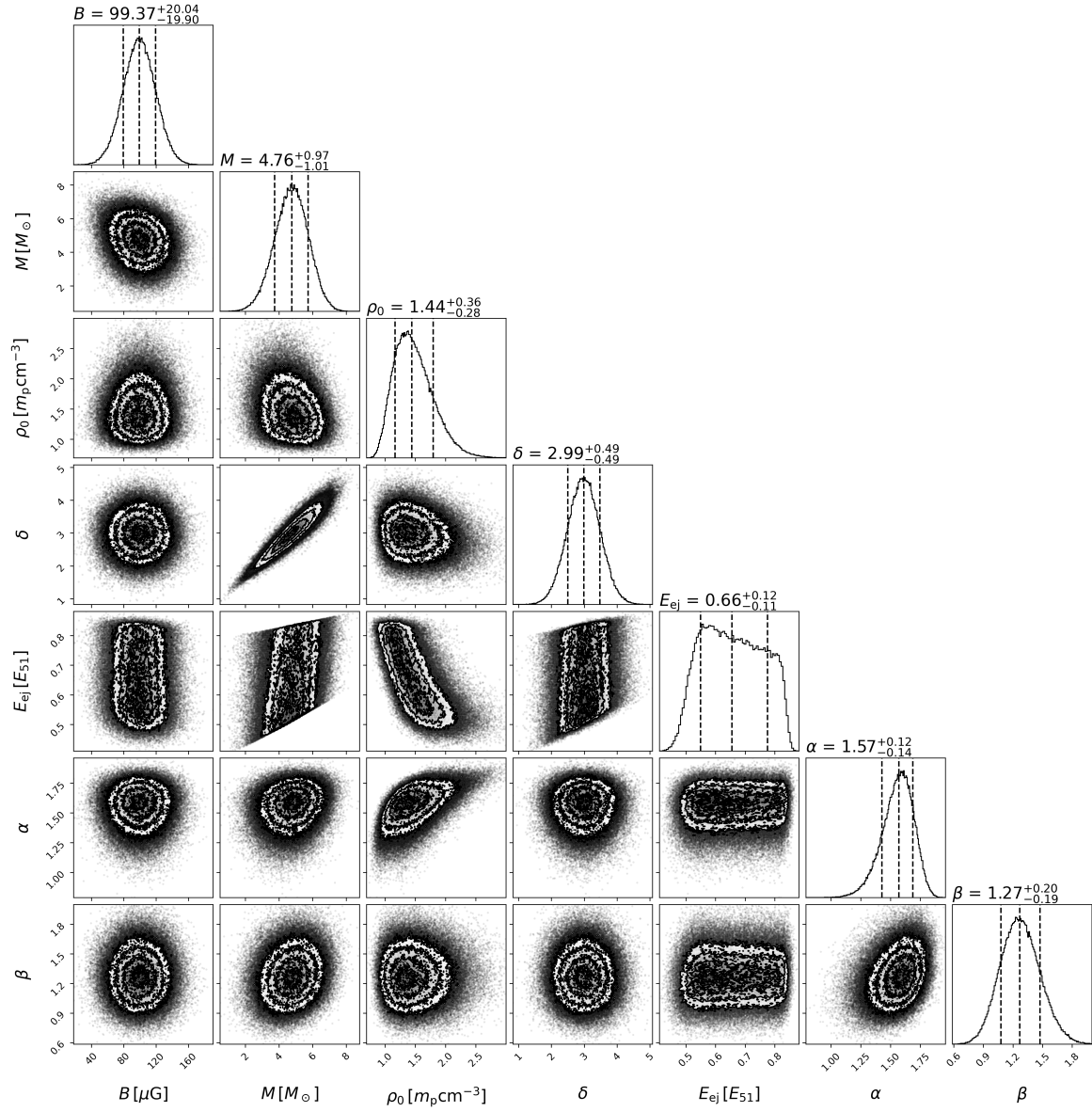


Figure 10. MCMC results for RCW 86.

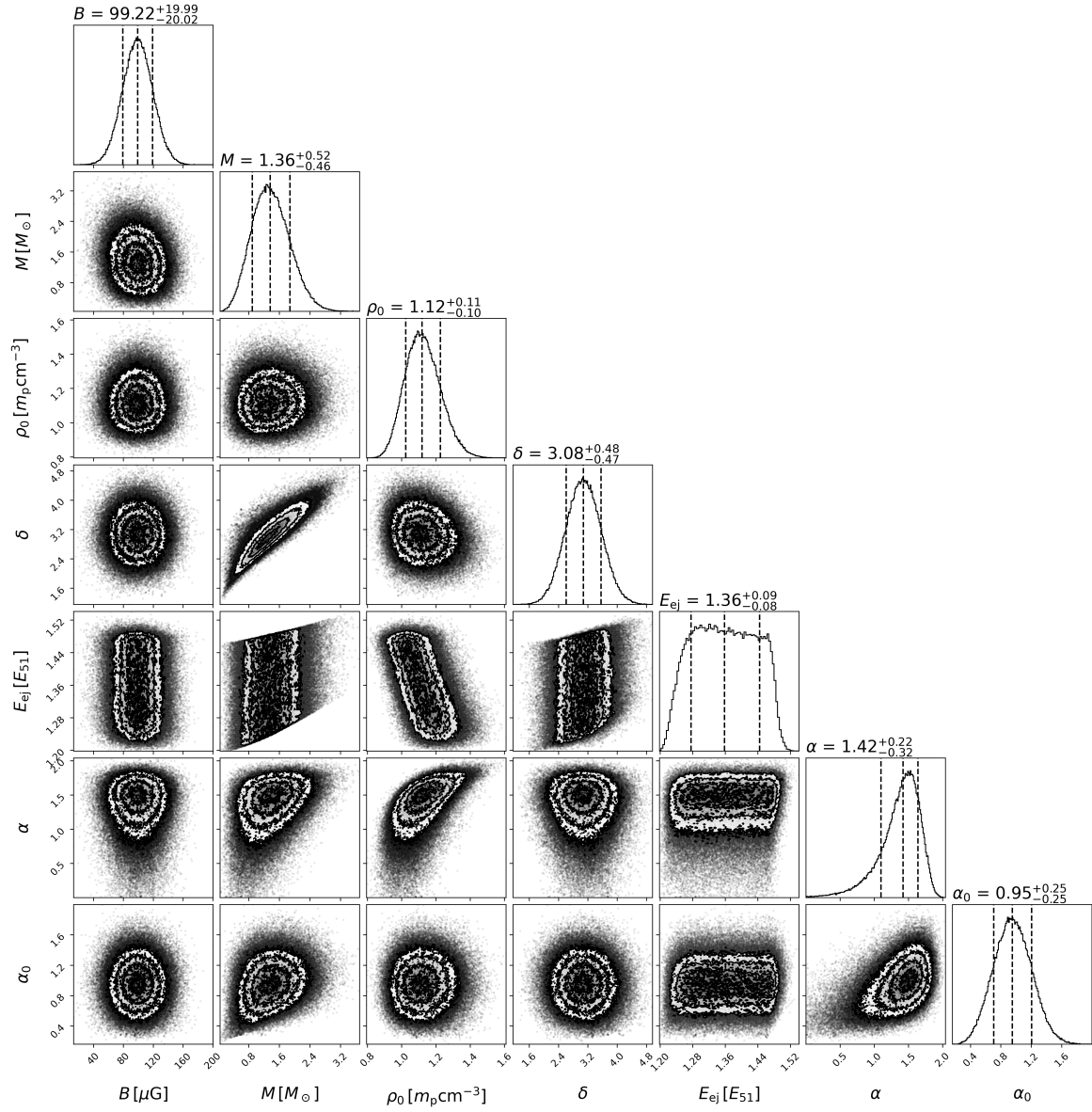


Figure 11. MCMC results for Puppis A.

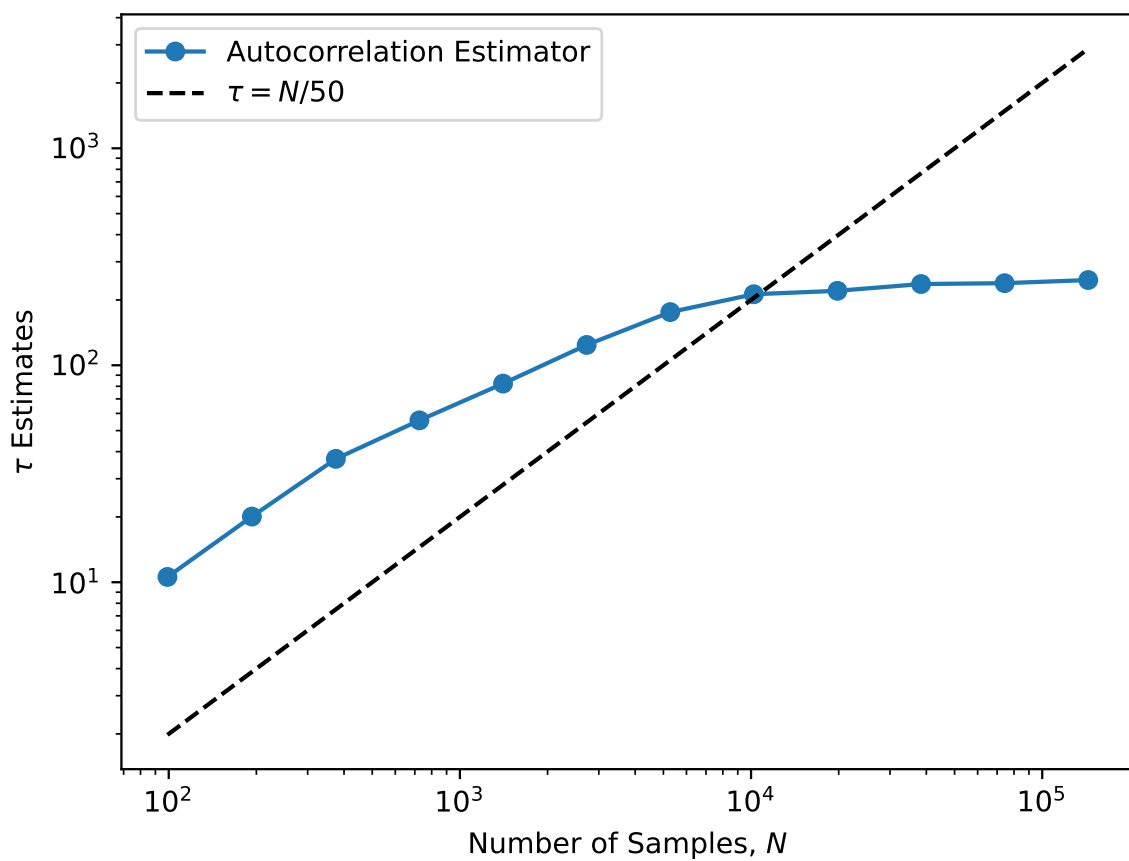


Figure 12. MCMC convergence for RX J1713.7-3946.

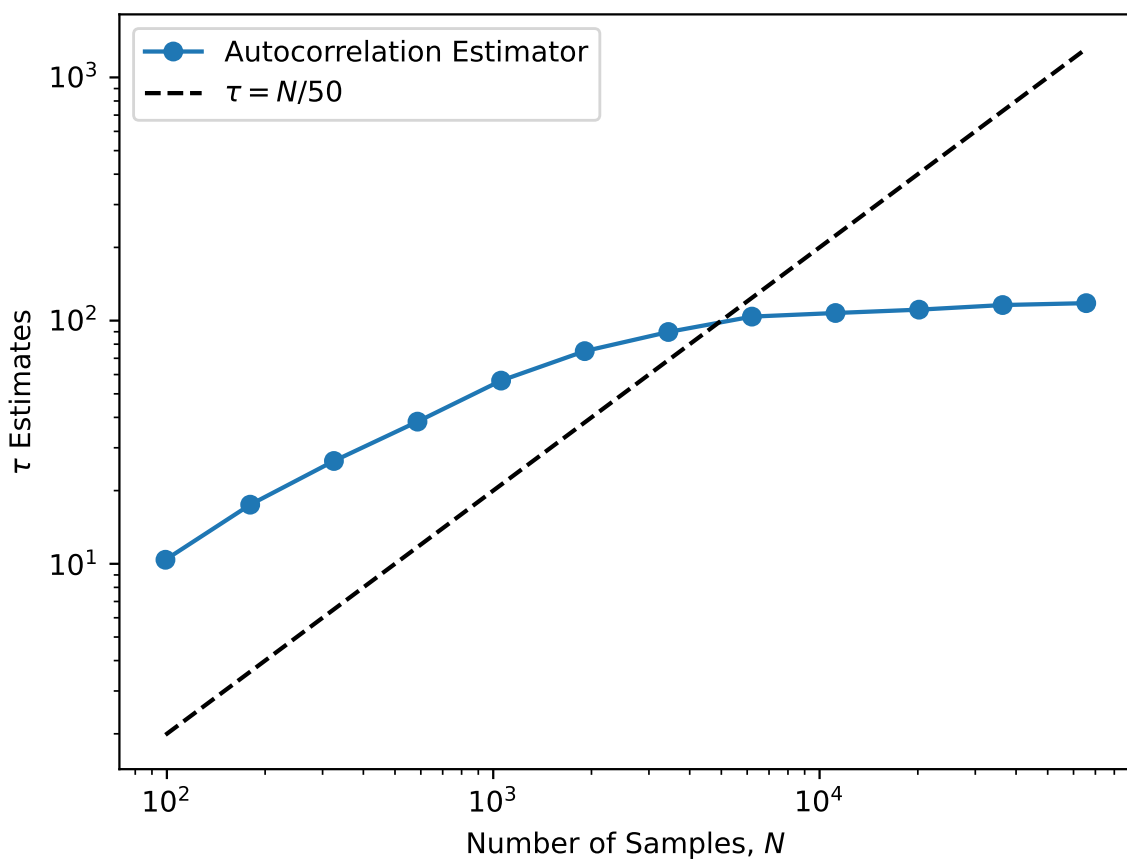


Figure 13. MCMC convergence for Vela Jr.

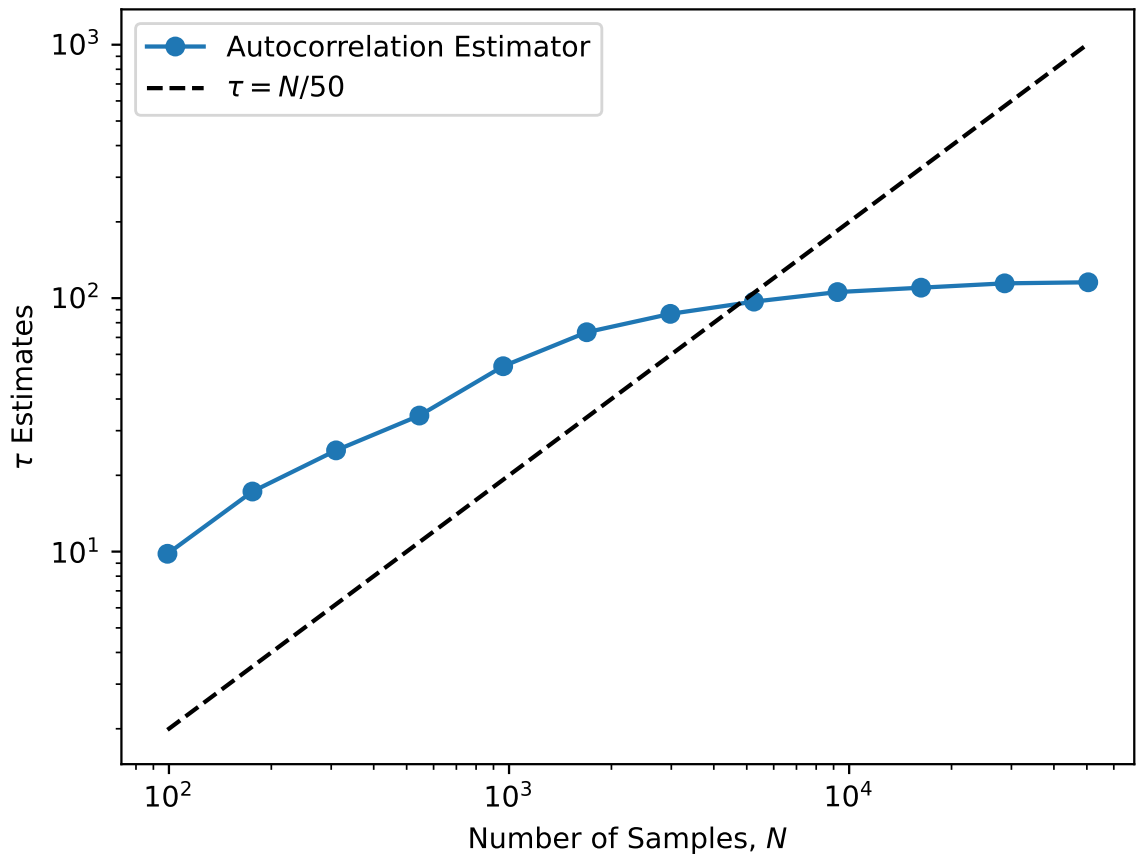


Figure 14. MCMC convergence for RCW 86.

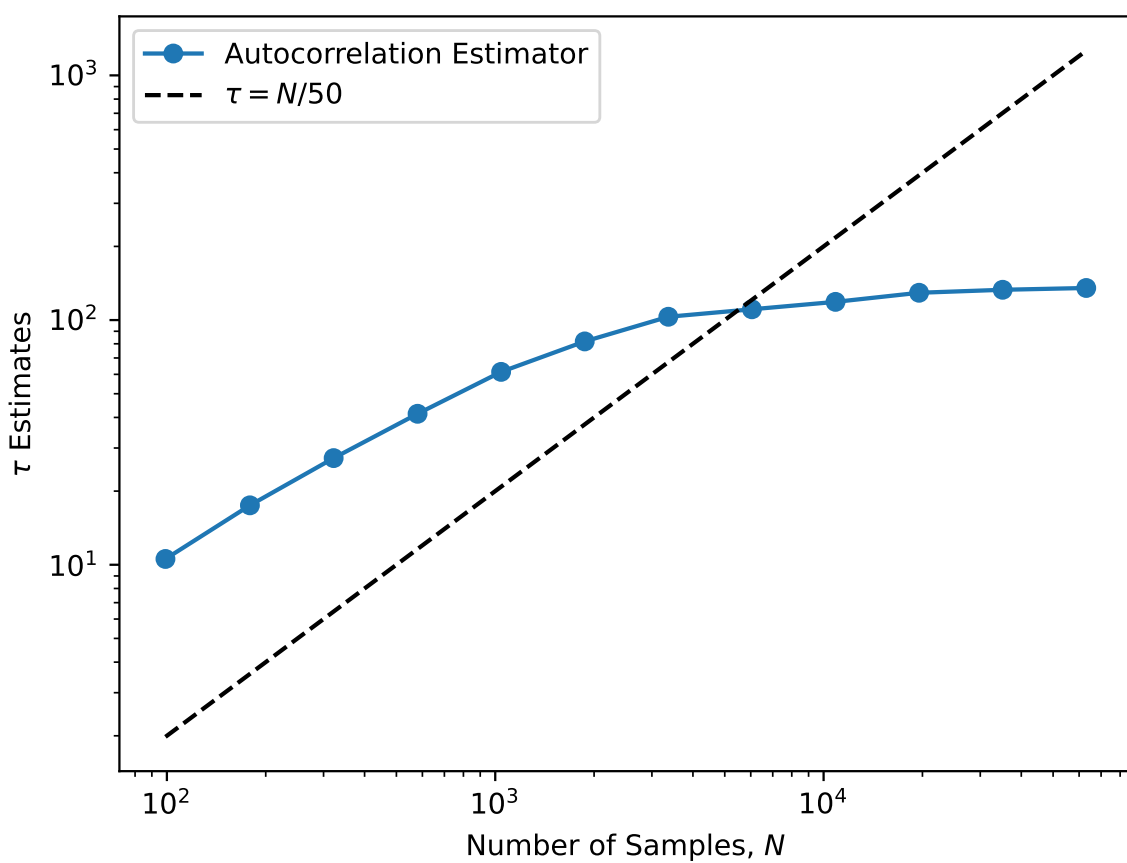


Figure 15. MCMC convergence for Puppis A.

References

- [1] J.A. Hinton and W. Hofmann, *Teraelectronvolt astronomy*, *Ann. Rev. Astron. Astrophys.* **47** (2009) 523 [[arXiv:1006.5210](#)] [[INSPIRE](#)].
- [2] R. Diesing, *The Maximum Energy of Shock-accelerated Cosmic Rays*, *Astrophys. J.* **958** (2023) 3 [[arXiv:2305.07697](#)] [[INSPIRE](#)].
- [3] P. Cristofari, P. Blasi and D. Caprioli, *Cosmic ray protons and electrons from supernova remnants*, *Astron. Astrophys.* **650** (2021) A62 [[arXiv:2103.02375](#)] [[INSPIRE](#)].
- [4] F.A. Aharonian, *Gamma rays from supernova remnants*, *Astropart. Phys.* **43** (2013) 71 [[INSPIRE](#)].
- [5] R. Conceição, *The Southern Wide-field Gamma-ray Observatory*, *PoS ICRC2023* (2023) 963 [[arXiv:2309.04577](#)] [[INSPIRE](#)].
- [6] J. Hahn, *GAMERA — a new modeling package for non-thermal spectral modeling*, *PoS ICRC2015* (2016) 917 [[INSPIRE](#)].
- [7] J. Hahn, C. Romoli and M. Breuhaus, *GAMERA: Source modeling in gamma astronomy*, *Astrophysics Source Code Library*, [ascl:2203.007](#) (2022).
- [8] L. Woltjer, *Supernova remnants*, *Ann. Rev. Astron. Astrophys.* **10** (1972) 129 [[INSPIRE](#)].
- [9] M. Cardillo, E. Amato and P. Blasi, *On the cosmic ray spectrum from type II Supernovae expanding in their red giant presupernova wind*, *Astropart. Phys.* **69** (2015) 1 [[arXiv:1503.03001](#)] [[INSPIRE](#)].
- [10] J.K. Truelove and C.F. McKee, *Evolution of Nonradiative Supernova Remnants*, *Astrophys. J. Suppl.* **120** (1999) 299.
- [11] J. Vink, *Physics and evolution of supernova remnants*, Springer (2020) [[DOI:10.1007/978-3-030-55231-2](#)].
- [12] A.R. Bell, *The acceleration of cosmic rays in shock fronts — I*, *Mon. Not. Roy. Astron. Soc.* **182** (1978) 147 [[INSPIRE](#)].
- [13] P. Blasi, *The Origin of Galactic Cosmic Rays*, *Astron. Astrophys. Rev.* **21** (2013) 70 [[arXiv:1311.7346](#)] [[INSPIRE](#)].
- [14] S. Celli, F. Aharonian and S. Gabici, *Spectral signatures of PeVatrons*, *Astrophys. J.* **903** (2020) 61 [[arXiv:2009.05999](#)] [[INSPIRE](#)].
- [15] S. Celli, *Gamma-ray and Neutrino Signatures of Galactic Cosmic-ray Accelerators*, Springer (2019) [[DOI:10.1007/978-3-030-33124-5](#)].
- [16] S. Gabici, F.A. Aharonian and S. Casanova, *Broad-band nonthermal emission from molecular clouds illuminated by cosmic rays from nearby supernova remnants*, *Mon. Not. Roy. Astron. Soc.* **396** (2009) 1629 [[arXiv:0901.4549](#)] [[INSPIRE](#)].
- [17] E. Kafexhiu, F. Aharonian, A.M. Taylor and G.S. Vila, *Parametrization of gamma-ray production cross-sections for pp interactions in a broad proton energy range from the kinematic threshold to PeV energies*, *Phys. Rev. D* **90** (2014) 123014 [[arXiv:1406.7369](#)] [[INSPIRE](#)].
- [18] S.P. Reynolds, *Supernova Remnants at High Energy*, *Ann. Rev. Astron. Astrophys.* **46** (2008) 89.
- [19] A. Bamba and B.J. Williams, *Supernova remnants: Types and evolution*, [arXiv:2211.02217](#) [[DOI:10.1007/978-981-16-4544-0_88-1](#)] [[INSPIRE](#)].
- [20] R. Diesing et al., *Nonthermal Signatures of Radiative Supernova Remnants*, *Astrophys. J.* **974** (2024) 201 [[arXiv:2404.15396](#)] [[INSPIRE](#)].
- [21] G. Ferrand and S. Safi-Harb, *A Census of High-Energy Observations of Galactic Supernova Remnants*, *Adv. Space Res.* **49** (2012) 1313 [[arXiv:1202.0245](#)] [[INSPIRE](#)].

- [22] H.E.S.S. collaboration, *H.E.S.S. observations of RX J1713.7-3946 with improved angular and spectral resolution: Evidence for gamma-ray emission extending beyond the X-ray emitting shell*, *Astron. Astrophys.* **612** (2018) A6 [[arXiv:1609.08671](#)] [[INSPIRE](#)].
- [23] S. Gabici and F.A. Aharonian, *Hadronic gamma-rays from RX J1713.7-3946?*, *Mon. Not. Roy. Astron. Soc.* **445** (2014) 70 [[arXiv:1406.2322](#)] [[INSPIRE](#)].
- [24] H.E.S.S. collaboration, *Deeper H.E.S.S. observations of Vela Junior (RX J0852.0-4622): Morphology studies and resolved spectroscopy*, *Astron. Astrophys.* **612** (2018) A7 [[arXiv:1611.01863](#)] [[INSPIRE](#)].
- [25] H.E.S.S. collaboration, *Detailed spectral and morphological analysis of the shell type supernova remnant RCW 86*, *Astron. Astrophys.* **612** (2018) A4 [[arXiv:1601.04461](#)] [[INSPIRE](#)].
- [26] H.E.S.S. collaboration, *Discovery of gamma-ray emission from the shell-type supernova remnant RCW 86 with H.E.S.S.*, *Astrophys. J.* **692** (2009) 1500 [[arXiv:0810.2689](#)] [[INSPIRE](#)].
- [27] H.E.S.S. collaboration, *H.E.S.S. reveals a lack of TeV emission from the supernova remnant Puppis A*, *Astron. Astrophys.* **575** (2015) A81 [[arXiv:1412.6997](#)] [[INSPIRE](#)].
- [28] R. Brose, M. Pohl and I. Sushch, *Morphology of supernova remnants and their halos*, *Astron. Astrophys.* **654** (2021) A139 [[arXiv:2108.10773](#)] [[INSPIRE](#)].
- [29] P. Zhou et al., *Magnetic Structures and Turbulence in SN 1006 Revealed with Imaging X-Ray Polarimetry*, *Astrophys. J.* **957** (2023) 55 [[arXiv:2309.01879](#)] [[INSPIRE](#)].
- [30] A. Albert et al., *Science Case for a Wide Field-of-View Very-High-Energy Gamma-Ray Observatory in the Southern Hemisphere*, [arXiv:1902.08429](#) [[INSPIRE](#)].
- [31] A.U. Abeysekera et al., *Observation of the Crab Nebula with the HAWC Gamma-Ray Observatory*, *Astrophys. J.* **843** (2017) 39 [[arXiv:1701.01778](#)] [[INSPIRE](#)].
- [32] LHAASO collaboration, *Peta-electron volt gamma-ray emission from the Crab Nebula*, *Science* **373** (2021) 425 [[arXiv:2111.06545](#)] [[INSPIRE](#)].
- [33] S. Scuderi et al., *The ASTRI Mini-Array of Cherenkov telescopes at the Observatorio del Teide*, *JHEAp* **35** (2022) 52 [[arXiv:2208.04571](#)] [[INSPIRE](#)].
- [34] CTA CONSORTIUM collaboration, *Science with the Cherenkov Telescope Array*, World Scientific (2018) [[DOI:10.1142/10986](#)] [[INSPIRE](#)].
- [35] EROSITA collaboration, *The eROSITA X-ray telescope on SRG*, *Astron. Astrophys.* **647** (2021) A1 [[arXiv:2010.03477](#)] [[INSPIRE](#)].
- [36] S. Goedhart et al., *The SRAO MeerKAT 1.3 GHz Galactic Plane Survey*, [arXiv:2312.07275](#).
- [37] HAWC collaboration, *Multiple Galactic Sources with Emission Above 56 TeV Detected by HAWC*, *Phys. Rev. Lett.* **124** (2020) 021102 [[arXiv:1909.08609](#)] [[INSPIRE](#)].
- [38] LHAASO collaboration, *Ultrahigh-energy photons up to 1.4 petaelectronvolts from 12 γ -ray Galactic sources*, *Nature* **594** (2021) 33 [[INSPIRE](#)].
- [39] LHAASO collaboration, *The First LHAASO Catalog of Gamma-Ray Sources*, *Astrophys. J. Suppl.* **271** (2024) 25 [[arXiv:2305.17030](#)] [[INSPIRE](#)].
- [40] D.W. Hogg and D. Foreman-Mackey, *Data analysis recipes: Using Markov Chain Monte Carlo*, *Astrophys. J. Suppl.* **236** (2018) 11 [[arXiv:1710.06068](#)] [[INSPIRE](#)].
- [41] P. Virtanen et al., *SciPy 1.0 — Fundamental Algorithms for Scientific Computing in Python*, *Nature Meth.* **17** (2020) 261 [[arXiv:1907.10121](#)] [[INSPIRE](#)].
- [42] D. Foreman-Mackey, D.W. Hogg, D. Lang and J. Goodman, *emcee: The MCMC Hammer*, *Publ. Astron. Soc. Pac.* **125** (2013) 306 [[arXiv:1202.3665](#)] [[INSPIRE](#)].