

# Low field spin dynamics of Cr<sub>7</sub>Ni and Cr<sub>7</sub>Ni-Cu-Cr<sub>7</sub>Ni molecular rings as detected by $\mu$ SR

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Muon Spin Rotation ( $\mu^+$ SR) measurements were used to investigate the spin dynamics of heterometallic Cr<sub>7</sub>Ni and Cr<sub>7</sub>Ni-Cu-Cr<sub>7</sub>Ni molecular clusters. In Cr<sub>7</sub>Ni the magnetic ions are arranged in a quasi-planar ring and interact via an antiferromagnetic exchange coupling constant  $J$ , while Cr<sub>7</sub>Ni-Cu-Cr<sub>7</sub>Ni is composed of two Cr<sub>7</sub>Ni linked by a bridging moiety containing one Cu ion, that induces an inter-ring ferromagnetic interaction  $J' \ll J$ . The longitudinal muon relaxation rate  $\lambda$  collected at low magnetic fields  $\mu_0 H < 0.15$  Tesla, shows that the two systems present differences in spin dynamics vs temperature. While both samples exhibit a main peak in the muon relaxation rate vs temperature, at  $T \sim 10$  K for Cr<sub>7</sub>Ni and  $T \sim 8$  K for Cr<sub>7</sub>Ni-Cu-Cr<sub>7</sub>Ni, the two compounds have distinct additional features: Cr<sub>7</sub>Ni shows a shoulder in  $\lambda(T)$  for  $T < 8$  K, and Cr<sub>7</sub>Ni-Cu-Cr<sub>7</sub>Ni shows a flattening of  $\lambda(T)$  for  $T < 2$  K down to temperatures as low as  $T = 20$  mK. The main peak of both systems is explained by a BPP-like heuristic fitting model that takes into account of a distribution of electronic spin correlation times for  $T > 5$  K, while the shoulder presented by Cr<sub>7</sub>Ni can be reproduced by a Bloembergen-Purcell-Pound (BPP) function that incorporates a single electronic correlation time theoretically predicted to dominate for  $T < 5$  K. The flattening of  $\lambda(T)$  in Cr<sub>7</sub>Ni-Cu-Cr<sub>7</sub>Ni occurring at very low temperature can be tentatively attributed to field-dependent quantum effects and/or to an inelastic term in the spectral density of the electronic spin fluctuations.

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## I. INTRODUCTION

It was the late 1980s when molecular magnets started to receive a progressively increasing attention due to their possible applications in several fields, the first recognized to be memory storage<sup>1</sup>. Since then, their potential uses have been extended to the fields of quantum information processing (QIP)<sup>2</sup> and, more recently, spintronics<sup>3</sup>. Particularly, in the last 10 years suitable systems for QIP were identified in antiferromagnetic (AFM) heterometallic wheels<sup>4</sup>, a particular class of molecules composed of a finite number of transition metal ions arranged in a planar or quasi-planar regular ring. In all molecular magnets, each molecule is magnetically quasi-isolated from the others, thus allowing to study the single unit properties by investigating a bulk system. In AFM wheels, inside the single molecule each ion is coupled with its neighbour via a strong antiferromagnetic exchange interaction  $J$  and, depending on the magnitude of  $J$  and of the different intra-molecular anisotropies, the electronic dominating correlation time could become enough long to allow for instance QIP, the main limitation being the very low temperature where this occurs. As a consequence, the experimental investigation of the magnetic properties and, particularly, of the spin dynamics of AFM rings is relevant for a complete understanding of

the mechanisms affecting quantum coherence and decoherence. Muon Spin Rotation ( $\mu$ SR), Nuclear Magnetic Resonance (NMR) and Electron Spin Resonance (ESR) are excellent choices for probing the local dynamics and have been proved useful in understanding the static and dynamic magnetic properties of a significant number of molecular magnets<sup>5-14</sup>. Particularly  $\mu$ SR has the advantage to use very low or zero applied magnetic field, a situation where in most cases the zero-field energy levels and the magnetic dynamics of the system are slightly perturbed.

A specific example of molecular magnet possibly useful for applications where the typical correlation times are important, is given by the so-called Cr<sub>7</sub>Ni AFM ring<sup>2,15,16</sup>, whose magnetic core consists of seven  $s=3/2$  Cr<sup>3+</sup> ions and one  $s=1$  Ni<sup>2+</sup> ion (which breaks the spin lattice symmetry) forming an octagonal planar ring. The total ground state spin of the Cr<sub>7</sub>Ni molecule is  $S_T=1/2$ , resulting from the AFM couplings Cr<sup>3+</sup>-Ni<sup>2+</sup> and Cr<sup>3+</sup>-Cr<sup>3+</sup> among the magnetic ions. The Cr<sub>7</sub>Ni system has been demonstrated to have long electronic correlation times  $\tau_c \sim 3\mu\text{s}$  at  $T < 5\text{K}$  by pulsed ESR echo experiments<sup>16</sup>, subsequently confirmed by <sup>1</sup>H NMR nuclear spin-lattice (longitudinal) relaxation rate  $1/T_1$  measurements<sup>17</sup>. On the other hand Timco et al.<sup>2</sup> demonstrated that when two Cr<sub>7</sub>Ni molecules are joined

together by a metallic  $\text{Cu}^{2+}$ -based linker, the resulting  $\text{Cr}_7\text{Ni-Cu-Cr}_7\text{Ni}$  system exhibits quantum spin entanglement at low temperature emerging from the magnetic coupling of the two spin-1/2  $\text{Cr}_7\text{Ni}$  rings with the spin-1/2 of the  $\text{Cu}^{2+}$  ion, an occurrence suggesting that this system can be used to implement quantum gates.

$^1\text{H}$  NMR measurements of  $1/T_1$  vs temperature showed that for magnetic fields chosen in the range  $0.47 < \mu_0 H < 1.7$  Tesla,  $\text{Cr}_7\text{Ni}$  and  $\text{Cr}_7\text{Ni-Cu-Cr}_7\text{Ni}$  (in short  $\text{Cr}_7\text{Ni-ent}$ ) have the same spin dynamics at intermediate temperatures  $T > 5 - 10\text{K}$ , while down to temperatures as low as 80 mK the data are inconclusive<sup>18</sup>, although the presence of spin freezing is demonstrated.

In this paper, we present a  $\mu\text{SR}$  investigation of the heterometallic  $\text{Cr}_7\text{Ni}$  and  $\text{Cr}_7\text{Ni-ent}$  rings in longitudinal field, aimed at highlighting the difference in the spin dynamics among the two systems at low magnetic fields, possibly caused by the inter-molecular coupling occurring via the Cu bridge in  $\text{Cr}_7\text{Ni-ent}$ . In fact, the longitudinal muon relaxation rate  $\lambda$  behaviour as a function of temperature at constant low magnetic fields  $\mu_0 H < 0.15$  Tesla, presents some differences in the two systems. At intermediate temperature  $5 < T < 60$  K, we show that both samples present a main peak of  $\lambda(T)$  at constant H occurring at  $T \sim 10 \pm 1\text{K}$  for  $\text{Cr}_7\text{Ni}$  and  $T \sim 8 \pm 1\text{K}$  for  $\text{Cr}_7\text{Ni-ent}$ , but  $\text{Cr}_7\text{Ni}$  shows also a shoulder in  $\lambda(T)$  for  $T < 8$  K. The main peak of both systems is explained in terms of a heuristic Bloembergen-Purcell-Pound (BPP)-like fitting model that takes into account a distribution of electronic spin correlation times for  $T > 5$  K (see also Ref. 18 for a comparison with NMR data). The shoulder presented by  $\text{Cr}_7\text{Ni}$  can be reproduced by a BPP curve dominated by a single electronic correlation time as theoretically predicted by A. Bianchi et al.<sup>17</sup>. On the other hand, in the  $\text{Cr}_7\text{Ni-ent}$  compound  $\lambda(T)$  for  $T < 2$  K flattens to a value that decreases by increasing the field. This flattening could possibly have quantum origin or could originate from inelastic terms contributing to  $\lambda$ .

## II. EXPERIMENTAL DETAILS

Two polycrystalline samples of antiferromagnetic heterometallic rings have been prepared following Refs.2 and 15; their structures are shown in Fig. 1. In the first sample,  $[\text{Me}_2\text{H}_2\text{Cr}_7\text{NiF}_8(\text{OCCMe}_3)_{16}]$  (in short  $\text{Cr}_7\text{Ni}$ ), the magnetic core is composed by a single ring of seven  $\text{Cr}^{3+}$ ,  $s=3/2$ , ions and one  $\text{Ni}^{2+}$ ,  $s=1$ , ion interacting via two slightly different exchange antiferromagnetic (AF) coupling constants Cr-Cr ( $J_{\text{Cr-Cr}}/k_B$ ) and Cr-Ni ( $J_{\text{Cr-Ni}}/k_B$ ). Thus, the resulting AF ground state has total spin  $S_T=1/2$ , with  $J_{\text{Cr-Cr}}/k_B \sim 16.9$  K and  $J_{\text{Cr-Ni}}/k_B \sim 19.6$  K<sup>20</sup>. The second sample, namely  $[\text{NH}_2\text{Pr}_2][\text{Cr}_7\text{NiF}_8(\text{O}_2\text{CCMe}_3)_{15}(\text{O}_2\text{CC}_5\text{H}_4\text{N})]_2[\text{Cu}(\text{NO}_3)_2(\text{OH}_2)]$  (in short  $\text{Cr}_7\text{Ni-ent}$ ), is composed of two single  $\text{Cr}_7\text{Ni}$  rings interacting through an organic bridge including a  $\text{Cu}^{2+}$  ion, thereby giving rise to the phenomenon of "quantum entanglement", as previously

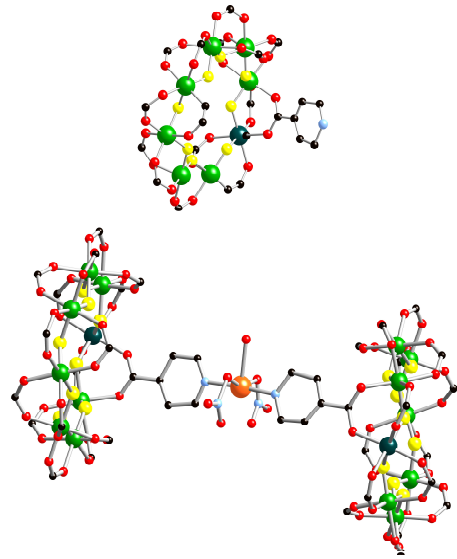


FIG. 1. (Color online) Structure of the single molecule of  $\text{Cr}_7\text{Ni}$  (top) and  $\text{Cr}_7\text{Ni-ent}$  (bottom). Light green : Cr, dark green : Ni, F: yellow, O :red, C : black, light blue : nitrogen.

remarked. Theoretical calculation, specific heat and EPR characterization measurements<sup>2,19</sup> indicates that this Cu bridge promotes a weak additional ferromagnetic exchange interaction coupling,  $J' \sim 1$  K, which entangles the respective single molecule wave-functions at the first excited state.

To have magnetic data for  $\mu\text{SR}$  analysis, DC magnetization measurements have been performed by a commercial superconducting quantum interferometer device (SQUID) MPMS-XL7 by Quantum Design. All collected data resulted in agreement with previous results<sup>2,17</sup>. Field-cooled (FC) measurements of magnetic susceptibility  $\chi(T) \simeq M/H$  have been performed on  $\text{Cr}_7\text{Ni}$  and  $\text{Cr}_7\text{Ni-ent}$  powders, in the temperature range  $2 < T < 300$  K under an applied DC field  $\mu_0 H = 0.1$  Tesla (Fig.2, main graph). M vs H curves have been collected at  $T = 2\text{K}$  on both systems in the range  $0 - 7$  Tesla (Fig.2, insets).

Positive muon spin relaxation ( $\mu\text{SR}$ ) measurements were performed on samples in powder, in longitudinal (i.e. parallel to the muon beam) applied magnetic fields (LF) fields  $\mu_0 H=80, 148$  mTesla for  $\text{Cr}_7\text{Ni}$  in the temperature range  $1.5 < T < 70$  K, and in LF fields  $\mu_0 H=20, 60, 80, 148$  mTesla for  $\text{Cr}_7\text{Ni-ent}$ , in the temperature

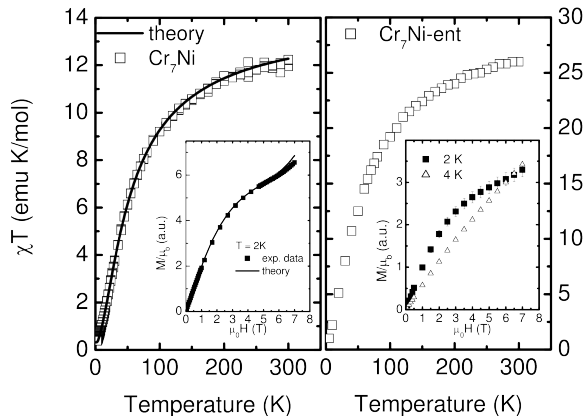


FIG. 2. Temperature evolution of  $\chi \cdot T$  of  $\text{Cr}_7\text{Ni}$  (left) and  $\text{Cr}_7\text{Ni-ent}$  (right) in an applied magnetic field  $\mu_0 H = 0.1$  Tesla in field cooling conditions. Insets: magnetic moment as a function of the magnetic field (for  $\text{Cr}_7\text{Ni-ent}$  at two different temperatures).

range  $0.02 < T < 70$  K. Experiments were run at the continuous muon source of the Paul Scherrer Institute with the GPS (for  $1.6 \text{ K} < T < 200 \text{ K}$ ) and LTF (for temperatures down to 80 mK) spectrometers. In  $\mu\text{SR}$ , 100%-spin-polarized positive muons directed antiparallel to the beam momentum are implanted in the sample, and the time-dependent response of the  $s=1/2$  muon spin interaction with the local magnetic environment is monitored via the positrons emitted by millions of muon decay events. From the collection of the emitted positrons, it is possible to extract the muon asymmetry  $A(t) = [N_F(t) - N_B(t)] / [N_F(t) + N_B(t)]$ , being  $N_{F/B}$  the sum of the decay positrons recorded by a set of counters placed forward/backward to the sample with respect to the initial polarization of the muon beam. This time-differential signal is proportional to the muon spin or depolarization function  $G(t)$  which results from static or quasi-static (for example, the spatial disorder present in the local magnetic field) and dynamic (such as local field fluctuations) processes.

### III. RESULTS AND DISCUSSION

The magnetic behavior shows an antiferromagnetic ground state for both  $\text{Cr}_7\text{Ni}$  and  $\text{Cr}_7\text{Ni-ent}$  samples (Fig. 2). The results are in good agreement with previous studies<sup>2,15</sup>.

The  $\text{Cr}_7\text{Ni-ent}$  supramolecular compound can be described by the following spin Hamiltonian:

$$H = H_{ring}(1) + H_{ring}(2) + H_{Cu} + H_{int}(1) + H_{int}(2), \quad (1)$$

where the subsystems 1 and 2 correspond to the two  $\text{Cr}_7\text{Ni}$  rings, described by the Hamiltonians  $H_{ring}$ ,  $H_{Cu}$

is the single Cu ion linker term and  $H_{int}$  accounts for the ring-linker interactions.

The Hamiltonian for each  $\text{Cr}_7\text{Ni}$  molecule can be written as:

$$H_{ring} = \sum_{i=1}^N J_i \mathbf{s}_i \cdot \mathbf{s}_{i+1} + \sum_{i=1}^N d_i s_{z,i}^2 + \sum_{i>j=1}^N D_{ij} [2s_{z,i}s_{z,j} - s_{x,i}s_{x,j} - s_{y,i}s_{y,j}] - \mu_B \sum_{i=1}^N g_i \mathbf{B} \cdot \mathbf{s}_i \quad (2)$$

(where  $s = 3/2$  for  $\text{Cr}^{3+}$ ,  $s = 1$  for  $\text{Ni}^{2+}$  and  $N = 8$  is the number of magnetic ions in the molecule, with the usual cyclic boundary condition  $N + 1 = 1$ , assuming Ni on site 8). The first term corresponds to the dominant antiferromagnetic isotropic exchange interaction. The second term describes the axial single-ion zero-field-splitting terms (with  $d_{\text{Cr}} = -0.35 \text{ K}$ ,  $d_{\text{Ni}} = -4 \text{ K}$  and the  $z$  axis perpendicular to the ring)<sup>20</sup>, while the third term is the axial contribution to the dipolar anisotropic intracenter spin-spin interaction, where  $D_{ij}$  is evaluated within the point-dipole approximation. The last term represents the Zeeman coupling with an external field  $\mathbf{H}$  (with  $g_{\text{Cr}} = 1.98$  and  $g_{\text{Ni}} = 2.2$ ).

The linker consists of a single  $\text{Cu}^{2+}$  ion:

$$H_{Cu} = -\mu_B \mathbf{B} \cdot \mathbf{g}_{Cu} \cdot \mathbf{s}_{Cu} \quad (3)$$

(with  $\mathbf{g}_{Cu}$  as in Ref.2), and the Hamiltonian describing the coupling between each ring and the linker is:

$$H_{int} = J' \mathbf{s}_{Cu} \cdot [\mathbf{s}_{Cr} + \mathbf{s}_{Ni}], \quad (4)$$

where  $J' = -1 \text{ K}$  and  $\mathbf{s}_{Cr}$  and  $\mathbf{s}_{Ni}$  correspond to  $\mathbf{s}_1$  and  $\mathbf{s}_8$  in their respective rings.

Following the Hamiltonian in Eq. (2), in zero applied magnetic field, the energy levels structure of  $\text{Cr}_7\text{Ni}$  features a doubly degenerate  $S_T=1/2$  ground state, separated by an energy gap  $\Delta E \simeq 13.7 \text{ K}$  from the first excited state, an  $S_T=3/2$  state. On the other hand,  $\text{Cr}_7\text{Ni-ent}$  displays a more complex configuration of the lowest levels: due to the magnetic coupling between the two  $\text{Cr}_7\text{Ni}$  units and the  $\text{Cu}^{2+}$  ion, the magnetic ground state of the molecule has a total spin  $S_T=3/2$  state split by the zero field splitting anisotropy into two doublets,  $|3/2, \pm 3/2\rangle$  and  $|3/2, \pm 1/2\rangle$ . Two additional  $S_T=1/2$  excited states are separated by energies within 1K from the ground state and spin entanglement effects in  $\text{Cr}_7\text{Ni-ent}$  can be observed on this small energy scale<sup>2</sup>.

The time evolution of the  $\mu\text{SR}$  asymmetry is displayed in Fig. 3 for some representative temperatures with longitudinal applied fields  $\mu_0 H = 80$  and 148 mTesla. As in previous  $\mu\text{SR}$  studies of nanomagnets,<sup>9,10</sup> a single exponential term does not adequately account for the relaxation, and the best fitting of the total relaxing asymmetry requires the following function:

$$A(t) = a_f \exp(\lambda_f t)^{1/2} + a_s \exp(\lambda_s t) + a_{bg} \quad (5)$$

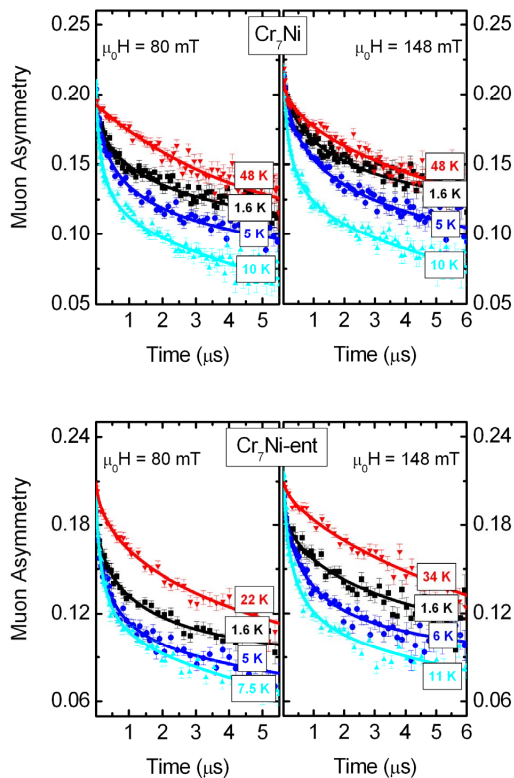


FIG. 3. (Color online) Time evolution of the  $\mu$ SR asymmetry for the  $\text{Cr}_7\text{Ni}$  (top) and  $\text{Cr}_7\text{Ni-ent}$  (bottom) samples at representative temperatures with a longitudinal applied field  $\mu_0 H = 80$  and  $148$  mT (left and right panels respectively). The solid line is the best fit to Eq. 5.

where  $a_f = 0.1(0.005)$  and  $a_s = 0.11(0.005)$  are the amplitudes of two relaxation components and  $\lambda_f$  and  $\lambda_s$  their corresponding relaxation rates;  $a_{bg} = 0$  for GPS beamline and  $a_{bg} = 0.02$  for LTF, is a background component. The first term in Eq.(5) is a root exponential with a faster decay rate ( $\lambda_f \sim 1 - 4 \mu\text{s}^{-1}$ ), which reflects a broad distribution of couplings of the muon to the magnetic moment, due to the multiplicity of possible muon stopping sites in each molecule implanted around the magnetic ions. The second term with a slower decay rate ( $\lambda_s \sim 0.1 - 1 \mu\text{s}^{-1}$ ) indicates the presence of a muon site farther away from the magnetic molecular core. For the rest of the paper we'll focus on the slow rate  $\lambda_s(T, H) \equiv \lambda(T, H)$ ; it is worth to remark that the behaviour of  $\lambda_f$  vs  $T$  and  $H$  is very similar to the one of  $\lambda_s$ .

The temperature behavior of the muon relaxation rate probes the phonon-induced molecular spin relaxation dynamics<sup>22</sup> that cause the muon spin depolarization. In

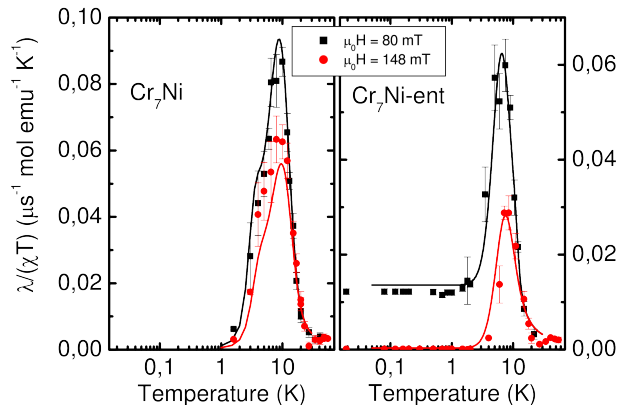


FIG. 4. (Color online) Temperature dependence of  $\lambda_s/(\chi T)$  for both the  $\text{Cr}_7\text{Ni}$  (left) and  $\text{Cr}_7\text{Ni-ent}$  (right) samples in longitudinal applied field  $\mu_0 H = 80$  and  $148$  mT. The solid lines are the best fit to Eq. 7 and 9 for  $\text{Cr}_7\text{Ni}$  (left) and  $\text{Cr}_7\text{Ni-ent}$  respectively.

most  $\mu$ SR and NMR cases<sup>8</sup> concerning molecular nanomagnets it was observed that for a single dominating correlation time  $\tau_c$  the muon spin-lattice relaxation rate  $\lambda$  ( $\equiv 1/T_1$ ) versus temperature at different applied magnetic fields follows the universal BPP-like law:

$$\lambda = K \chi T \frac{\tau_c}{1 + \omega_L^2 \tau_c^2} \quad (6)$$

where  $K$  is a constant and  $\omega_L$  is the Larmor frequency.

Thermal fluctuations of the electronic spins generate fluctuations of the local fields at the muon site. Indeed, the characteristic time  $\tau_c$  in Eq.6 is related to the phonon-induced decay of the electronic spins fluctuations, which in this case takes place through one single dominating process. Thus, the spectral density  $J(\omega)$ , i.e. the Fourier transform of the spin fluctuations correlation function, reduces to a single lorentzian of width  $\tau_c$ .  $\tau_c$  is generally temperature dependent and it may follow, according to different theoretical frameworks, a power law<sup>21</sup> or a thermally activated behavior described by the Arrhenius law<sup>22</sup>. A peak of  $1/T_1$  is observed when  $1/\tau_c = \omega_L$ , i.e. when the frequency of the electronic spin fluctuations equals the Larmor frequency. Fig. 4 displays the behavior of  $\lambda/(\chi T)$  as a function of temperature for both  $\text{Cr}_7\text{Ni}$  and  $\text{Cr}_7\text{Ni-ent}$  at the two different applied fields  $\mu_0 H = 80$  and  $148$  mTesla. Both samples display a peaked behavior around  $10$  K for all the applied fields, in qualitative agreement with previous NMR measurements on  $\text{Cr}_7\text{Ni}$ .<sup>17</sup>  $\text{Cr}_7\text{Ni}$  displays also a shoulder in  $\lambda(T)$  for  $T < 8$  K while the  $\text{Cr}_7\text{Ni-ent}$  compound for  $\mu_0 H = 80$  mTesla and  $T < 2$  K clearly shows a flattening to a non-zero  $\lambda$  value down to  $80$  mK. This flattening, observed also in other molecular clusters<sup>6,14</sup>, indicates the presence of a residual spin-lattice relaxation channel down to the low-

est temperature. This effect has been studied as a function of the field and will be discussed below.

The Eq. 6 with a single dominant correlation time  $\tau_c$  failed to reproduce the experimental data for both samples.

For the Cr<sub>7</sub>Ni compound, a sum of two BPP-like terms is required to fit the experimental data:

$$\frac{\lambda}{\chi T} = K_1 \frac{\tau_{c1}}{1 + \omega_0^2 \tau_{c1}^2} + K_2 \int_0^\infty \frac{f(E) \tau_{c2}(E)}{1 + \omega_0^2 \tau_{c2}^2(E)} dE \quad (7)$$

with  $\tau_{ci}(E) = \tau_{0i} e^{E_i/kT}$ ,  $i = 1, 2$  and

$$f(E) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{(E - \mu)^2}{2\sigma^2}\right]. \quad (8)$$

The first term fits the shoulder shown by  $\lambda/(\chi T)$  data of Cr<sub>7</sub>Ni at low temperatures ( $T \sim 3$  K, Fig. 4left) and yields  $\tau_{01} = 33 \pm 9$  ns and  $E_1/k_B = 12.0 \pm 3.2$  K, in agreement with previous calculations<sup>17</sup> that predicted a single dominating correlation time for temperatures  $T < 5$  K. It should be noted that more refined theoretical calculation of the correlation times entering the spectral density, would be required at the magnetic field ( $\mu_0 H = 80$  mTesla) used in the current experiments. The second term fits the data for  $T > 5$  K and reproduces the muon peak occurring at  $T \simeq 10$ K, by assuming a distribution of correlation times which leads to a distribution of energy barriers  $E$ , described for simplicity with a gaussian distribution represented in Eq. 8. The fit results yields  $\tau_{02} = 0.65 \pm 0.14$  ns and an average energy barrier  $E_2/k_B = 58.6 \pm 4.1$  K with a distribution width  $\sigma = 22.1 \pm 5.1$  K. The presence of the Gaussian distribution in the second term of Eq.(7), necessary to fit the main  $\lambda$ -peak, reflects the existence of more than one phonon-induced relaxation channel, in the region  $T > 5 - 8$  K (in agreement with theory<sup>17</sup>).

As concerns the data fitting of Cr<sub>7</sub>Ni-ent compound the following function is required:

$$\frac{\lambda}{\chi T} = const \cdot (1 - \tanh(T)) + K_3 \int_0^\infty \frac{f(E) \tau_{c3}(E)}{1 + \omega_0^2 \tau_{c3}^2(E)} dE \quad (9)$$

where the first term mimics the flattening at low  $T$  and the second term is similar to the second contribution to  $\lambda$  in Eq. 7. The fit yields  $\tau_{03} = 4.1 \pm 0.3$  ns and an average energy barrier  $E_3/k_B = 34.3 \pm 0.8$  K with a width  $\sigma = 11.2 \pm 0.3$  K. Also in the case of Cr<sub>7</sub>Ni-ent, the presence of the second term in Eq.(9) is due to a distribution of electronic correlation times.

In order to go into deeper details of the very low temperature ( $T \leq 1.5$  K) spin dynamics of Cr<sub>7</sub>Ni-ent we investigated the field dependence of the muon longitudinal relaxation rate as a function of the LF at constant low temperature, where the flattening of  $\lambda$  does occur (inset in Fig. 5). The main panel of Fig. 5 shows at  $T=80$  mK a

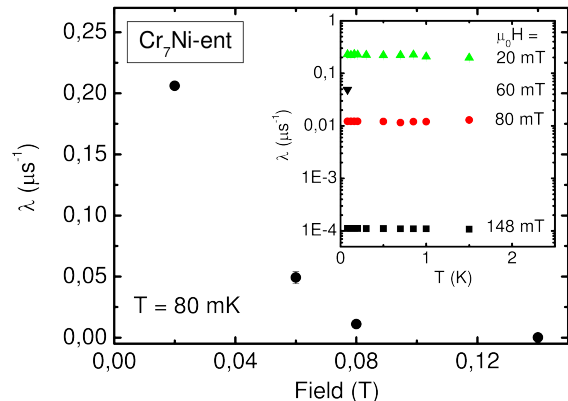


FIG. 5. (Color online) Relaxation rate  $\lambda_s$  from the muon asymmetry fitting by Eq. 5 for Cr<sub>7</sub>Ni-ent as a function of the longitudinal applied field  $\mu_0 H$ . Inset: temperature dependence of  $\lambda_s$  for different applied fields in the regime of very low temperatures.

fast reduction of  $\lambda$  as a function of the field in the range 20-148 mTesla here investigated. This  $\lambda(H)$  behaviour at constant  $T$  persists until  $T=1.5$  K, as can be evinced from the inset of Fig.5, where  $\lambda$  appears constant in the range  $20 \text{ mK} < T \leq 1.5$  K for all applied magnetic fields. In particular, for  $\mu_0 H = 148$  mTesla the value of  $\lambda$  is very near to zero, i.e. the muon polarization does not relax anymore.

The flattening of  $\lambda$  vs  $T$  at constant applied LF was already observed in other molecular magnets<sup>9-12,14</sup> at zero or low applied fields. Though this phenomenon could possibly have a quantum origin, it has to be noticed that also inelastic terms in the spectral density  $J(\omega)$  contributing to  $\lambda$  can give similar effects<sup>23</sup>. In any event, a relaxation channel still active at these extremely low temperatures has to be found and the explanation of the experimental data remains a matter of debate.

#### IV. CONCLUSIONS

We have investigated the molecular magnetic ring Cr<sub>7</sub>Ni vs the Cr<sub>7</sub>Ni-ent system constituted by two Cr<sub>7</sub>Ni units interacting via a Cu(II)-based bridging moiety, with the aim of investigating the spin dynamics at low magnetic fields by  $\mu^+$ SR. We showed that the muon longitudinal relaxation rate  $\lambda$  behaviour, as a function of temperature and field displays a main peak at intermediate temperatures of the order of 10K for both systems (see also Ref. 18 for higher field NMR data), explained by assuming a distribution of correlation times related to more than one electronic transition and phonon-induced relaxation paths. For  $T < 5$  K, the Cr<sub>7</sub>Ni compound reveals a dynamic behaviour guided by a single correlation time, as evinced by a shoulder present in  $\lambda(T)$ . On the other

hand, until extremely low temperature  $T \sim 20\text{mK}$ ,  $\lambda(T)$  for Cr<sub>7</sub>Ni-ent flattens to a value which is field-dependent. The physical origin of this flattening has still to be understood although, due to very low temperature and the independence on  $T$ , one could guess an active channel of relaxation of quantum origin and/or a contribution to  $\lambda$  coming from inelastic terms in the spectral density of the electronic spin fluctuations.

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