

Dissipation-induced correlations in one-dimensional bosonic systems

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New Journal of Physics **13** (2011) 053027 (13pp)

Received 21 December 2010

Published 16 May 2011

Online at <http://www.njp.org/>

doi:10.1088/1367-2630/13/5/053027

Abstract. The quantum dynamics of interacting bosons in a one-dimensional (1D) system is investigated numerically. We consider dissipative and conservative two-particle interactions, and integrate the master equation describing the system dynamics via a time-evolving block-decimation (TEBD) algorithm. Our numerical simulations directly apply to stationary-light polaritons in systems where atoms and photons are confined to the hollow core of a photonic crystal fibre. We show that a two-particle loss term can drive an initially uncorrelated state into a regime where correlations effectively inhibit the dissipation of particles. The correlations induced by two-particle losses are compared with those generated by an elastic repulsion. For the considered time range, we find a similar behaviour in local density–density correlations but we find differences in non-local correlations.

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1. Introduction

The preparation of quantum systems in entangled many-body states is an indispensable resource for quantum information science [1] and allows one to access the rich physics of strongly correlated many-body systems [2]. Despite its reputation as the main adversary of quantum information schemes, dissipation was recognized recently as a versatile tool for the generation of specific many-body states [3]–[5].

The preparation of correlated quantum states via dissipation requires that the target state itself is metastable. An intriguing experiment [6] with cold molecules showed that a dissipative two-particle interaction between bosons in one dimension gives rise to correlations that inhibit the loss of particles. The formal analysis of this effect is based on a generalized Lieb–Liniger model [7]–[9] and suggests that the two-particle loss term effectively results in a repulsion such that inelastic collisions between particles are avoided. In the limit of strong interactions [8], the two-particle losses give rise to a Tonks–Girardeau gas [10], where bosons behave with respect to many observables as if they were fermions.

Recently, it was shown that one-dimensional (1D) systems of interacting bosons can be realized via dark-state polaritons that arise in light–matter interactions under conditions of electromagnetically induced transparency [11]–[15]. A possible experimental realization of the polariton schemes is the setup described in [16, 17], where photons and atoms are simultaneously confined to the hollow core of a photonic-crystal fibre (see figure 1). Another approach comprises the experimental set-up in [18], where atoms are trapped near the surface of an optical nanofibre using evanescent waves. The nature of the polariton–polariton interaction in these approaches can be tuned by external parameters and can be elastic [13] or dissipative [14, 15], and the interaction strength is maximal for a purely dissipative interaction [14]. Polariton schemes ([13]–[15], [19]–[21]) are extremely promising candidates for the realization of strongly correlated photon states.

Here we consider bosons in one dimension and investigate the quantum dynamics after a sudden switch-on of elastic and inelastic interactions via time-dependent density matrix renormalization group techniques. The master equation of the system and the uncorrelated initial state are chosen such that our simulations directly apply to polariton systems [13]–[15]. All details of our model are discussed in section 2, and numerical results are presented in

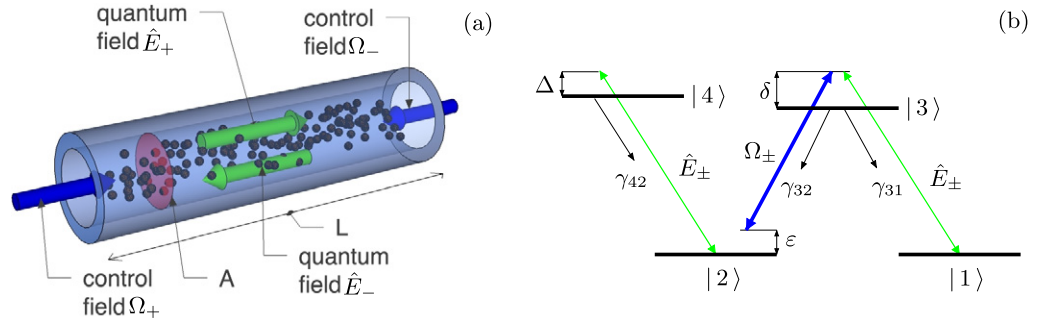


Figure 1. (a) Considered set-up of N_a atoms confined to an interaction volume of length L and transverse area A . Ω_{\pm} are the Rabi frequencies of the classical control fields, and \hat{E}_{\pm} are the quantum probe fields. (b) Atomic level scheme. γ_{ij} is the full decay rate on the $|i\rangle \leftrightarrow |j\rangle$ transition, δ and Δ label the detuning of the probe fields with states $|3\rangle$ and $|4\rangle$, respectively, and ε is the two-photon detuning.

section 3. In particular, we are interested in the preparation of a correlated, non-decaying state via dissipative two-particle interactions that we discuss in section 3.1. Non-local correlations are investigated in section 3.2, where we show that dissipation and repulsion give rise to different results. Finally, a summary is provided in section 4.

2. Model

We consider bosons of mass m in a 1D system of length L that experience a two-particle contact interaction that can be conservative, dissipative or a mixture of both. Firstly, we describe the full master equation governing the time evolution of the system in section 2.1. A physical realization of this model via interacting dark-state polaritons [14, 15] is introduced in section 2.2. Finally, we discuss the discretized model of the master equation in section 2.1 that allows us to perform numerical simulations in section 2.3.

2.1. The master equation

The dynamics of bosons in our 1D system is described by the master equation

$$\hbar \partial_t \varrho = -i H_{\text{eff}} \varrho + i \varrho H_{\text{eff}}^{\dagger} + \mathcal{I} \varrho + \hbar \mathcal{L}_{\text{D}} \varrho, \quad (1)$$

where H_{eff} is a non-Hermitian Hamiltonian,

$$H_{\text{eff}} = \frac{\hbar^2}{2m} \int_0^L dz \partial_z \psi^{\dagger} \partial_z \psi + \frac{\tilde{g}}{2} \int_0^L dz \psi^{\dagger 2} \psi^2. \quad (2)$$

Here, $\psi(z)$ is the field operator obeying bosonic commutation relations

$$[\psi(z), \psi^{\dagger}(z')] = \delta(z - z'), \quad (3)$$

and the first term in equation (2) describes the kinetic energy. The parameter \tilde{g} is the complex coupling constant and its real part gives rise to a Hermitian contribution to H_{eff} in equation (2) that accounts for elastic two-particle collisions. On the other hand, the imaginary part of \tilde{g}

together with the term

$$\mathcal{I}_Q = -\text{Im}(\tilde{g}) \int_0^L dz \psi^2 Q \psi^{\dagger 2} \quad (4)$$

in equation (1) constitutes a two-particle loss term that can be written in Lindblad form [22] as $\text{Im}(\tilde{g}/2)\mathcal{D}[\psi^2]$, where $\mathcal{D}[\hat{X}] = \int_0^L dz (\hat{X}^\dagger \hat{X} Q + Q \hat{X}^\dagger \hat{X} - 2\hat{X} Q \hat{X}^\dagger)$. The last term in equation (1) is defined as

$$\mathcal{L}_{DQ} = -\frac{D}{2} \int_0^L dz \mathcal{D}[\partial_z \psi] \quad (5)$$

and causes diffusion of the field ψ . Throughout this paper we choose

$$D = |\hbar/m|/10, \quad (6)$$

such that the losses associated with the diffusion term are small on a timescale set by the kinetic energy term in equation (2).

The master equation (1) without the last term \mathcal{L}_{DQ} defined in equation (5) can be identified with the dissipative Lieb–Liniger model [8]. For a fixed number of particles N_{ph} , essential features of the system are described by the complex Lieb–Liniger parameter,

$$G = \frac{m\tilde{g}}{\hbar^2 N_{\text{ph}}/L}. \quad (7)$$

The spectrum of the effective Hamiltonian in equation (2) was analysed in [8] via the Bethe–Ansatz. It was found that the ground state of the so-called gaseous states (all momenta converge to finite values for $|G| \rightarrow \infty$) approaches the Tonks–Girardeau gas in the limit $|G| \rightarrow \infty$. This state is metastable since in the Tonks–Girardeau gas limit two particles never occupy the same position in space, and hence the two-particle contact interaction does not contribute to the dissipation of particles.

This feature can be formally derived from the master equation (1). The two-particle loss term $\text{Im}(\tilde{g}/2)\mathcal{D}[\psi^2]$ in equation (1) causes a time dependence of the density of particles according to

$$\partial_t \langle \hat{n}(z) \rangle = \frac{2}{\hbar} \text{Im}(\tilde{g}) g^{(2)}(z, z) \langle \hat{n}(z) \rangle^2, \quad (8)$$

where $\hat{n}(z) = \psi^\dagger(z)\psi(z)$ is the particle density operator and

$$g^{(2)}(z, z') = \frac{\langle \psi^\dagger(z)\psi^\dagger(z')\psi(z)\psi(z') \rangle}{\langle \hat{n}(z) \rangle \langle \hat{n}(z') \rangle} \quad (9)$$

is the second-order correlation function. Note that the kinetic energy and the diffusion term \mathcal{L}_{DQ} in equation (1) will, in general, induce an additional time dependence of $\langle \hat{n}(z) \rangle$. The kinetic energy term conserves the total number of particles but gives rise to polariton fluxes from and to position z that would redistribute the polariton density. In regions where the system and the particle density are homogeneous, these fluxes can safely be neglected. The impact of the diffusion term \mathcal{L}_{DQ} is negligible for the considered timescales since we chose a small value for the parameter D in equation (6). In the strongly correlated regime and for a homogeneous system, the gaseous ground state of H_{eff} obeys [8]

$$g^{(2)}(z, z) = (1 - 1/N_{\text{ph}}^2) 4\pi^2 / (3|G|^2), \quad (10)$$

and hence $g^{(2)}(z, z) \ll 1$ for $|G|$ that is sufficiently large. The combination of equations (8) and (10) implies that a purely dissipative interaction term supports metastable states.

2.2. Physical realization

An example for a physical system that is described by the master equation (1) is shown in figure 1(a), where photons and atoms are simultaneously confined to the hollow core of a photonic-crystal fibre. Since the light-guiding core of the optical fibre is of the same order of magnitude as the optical wavelength, the fibre represents a 1D waveguide for the optical fields. The level scheme of each atom inside the fibre is shown in figure 1(b). The dynamics of the system can be described in terms of dark-state polaritons [23] representing bosonic quasi-particles that arise in light-matter interactions under conditions of electromagnetically induced transparency [24]. The two counter-propagating control fields Ω_{\pm} (see figure 1(a)) of equal intensity give rise to stationary light [25, 26] where the polaritons experience a quadratic dispersion relation like bosons in free space. Moreover, the coupling of the probe fields to the transition $|2\rangle \leftrightarrow |4\rangle$ induces a two-particle contact interaction between the polaritons that can be conservative [11, 13], dissipative or a mixture of both [14, 15]. It can be shown [14, 15] that the dark-state polariton dynamics can be described by the master equation (1), where the effective mass m and the complex coupling constant \tilde{g} depend on the detunings δ , Δ (see figure 1(b)) and the intensity of the control fields. In particular, we point out that a proper adjustment of the detuning δ allows one to fulfil equation (6), and the choice of the detuning Δ determines the relative contribution of elastic and inelastic processes to the two-particle interaction.

In an experiment, the evolution of the polaritons under equation (1) has to be preceded by a loading process that could be realized as follows [13]. Initially, the probe field modes are empty and only the control field Ω_+ is switched on. Then a probe pulse copropagating with Ω_+ enters the fibre under conditions of electromagnetically induced transparency. Here we assume that the transition $|4\rangle \leftrightarrow |2\rangle$ is far off-resonant during the loading process such that its influence is negligible. The dynamics of the probe field inside the medium can be described concisely in terms of dark-state polaritons [23]. As compared to the pulse propagating in vacuum, the polariton pulse inside the medium is spatially compressed and travels with a reduced group velocity $v_g \propto \Omega_+^2$. Once the pulse is entirely inside the fibre, the group velocity of the polariton pulse is reduced to zero by an adiabatic switch-off of the control field Ω_+ . The latter process maps the polaritons into a stationary spin coherence, and all probe field modes are empty. Eventually, both control fields are switched on adiabatically and with equal intensity, $\Omega_{\pm} = \Omega_0$. The time evolution of the corresponding dark-state polaritons is then determined by the master equation (1) [14, 15]. Note that the adiabatic switch-on can be much faster than all typical timescales in the master equation (1). At this stage, the detuning Δ of the probe field with the $|4\rangle \leftrightarrow |2\rangle$ transition can be adjusted by a proper choice of the frequency of the counter-propagating control fields. This frequency can be different from the one used for the single control field during the loading process.

The correlations that are built up under the evolution of the master equation (1) can be measured if the intensity of the control field Ω_- is reduced. The latter process converts the stationary polaritons into a propagating pulse with controllable group velocity. This procedure maps spatial correlations of the trapped pulse into temporal correlations of the output light that can be detected via standard quantum optical techniques.

2.3. The discretized model

The dynamics of the system are studied via the time-evolving block-decimation (TEBD) algorithm [27]–[29] for density operators. The discretized version [30] of equation (1) is given

by a generalized Bose–Hubbard model augmented by loss terms,

$$\dot{\varrho} = -\frac{i}{\hbar}[H_1 + H_2, \varrho] + \mathcal{L}_1\varrho + \mathcal{L}_2\varrho. \quad (11)$$

Here, H_1 and H_2 correspond to the kinetic energy term and the conservative contribution to the two-particle interaction, respectively,

$$H_1 = 2J \sum_l \hat{a}_l^\dagger \hat{a}_l - J \sum_l (\hat{a}_l \hat{a}_{l+1}^\dagger + \hat{a}_{l+1} \hat{a}_l^\dagger), \quad H_2 = \frac{U}{2} \sum_l \hat{a}_l^{\dagger 2} \hat{a}_l^2, \quad (12)$$

and J and U are defined as

$$J = \frac{\hbar^2}{2m} \frac{1}{\Delta z^2}, \quad U = \text{Re}(\tilde{g}) \frac{1}{\Delta z}. \quad (13)$$

The parameter Δz is the lattice constant of the discretization grid. The terms $\mathcal{L}_1\varrho$ and $\mathcal{L}_2\varrho$ in equation (1) are the discretized versions of the diffusion term in equation (5) and the dissipative contribution to the two-particle interaction, respectively,

$$\begin{aligned} \mathcal{L}_1\varrho = & -\Gamma_1 \sum_l (\hat{a}_l^\dagger \hat{a}_l \varrho + \varrho \hat{a}_l^\dagger \hat{a}_l - 2\hat{a}_l \varrho \hat{a}_l^\dagger) + \frac{\Gamma_1}{2} \sum_l (\hat{a}_l^\dagger \hat{a}_{l+1} \varrho + \varrho \hat{a}_l^\dagger \hat{a}_{l+1} - 2\hat{a}_{l+1} \varrho \hat{a}_l^\dagger) \\ & + \frac{\Gamma_1}{2} \sum_l (\hat{a}_l \hat{a}_{l+1}^\dagger \varrho + \varrho \hat{a}_l \hat{a}_{l+1}^\dagger - 2\hat{a}_l \varrho \hat{a}_{l+1}^\dagger), \end{aligned} \quad (14)$$

$$\mathcal{L}_2\varrho = -\frac{\Gamma_2}{2} \sum_l (\hat{a}_l^{\dagger 2} \hat{a}_l^2 \varrho + \varrho \hat{a}_l^{\dagger 2} \hat{a}_l^2 - 2\hat{a}_l^2 \varrho \hat{a}_l^{\dagger 2}), \quad (15)$$

and

$$\Gamma_1 = D \frac{1}{\Delta z^2}, \quad \Gamma_2 = -\text{Im}(\tilde{g}/\hbar) \frac{1}{\Delta z}. \quad (16)$$

The discretized version equation (11) is a good approximation of the continuous master equation (1) if the smallest wavelength λ_{\min} involved is much larger than the grid spacing Δz . Initially, λ_{\min} is determined by the momentum components of the initial state, but the evolution under equation (11) will change the momentum distribution of the sample. In particular, the suddenly switched-on two-particle repulsion term leads (among other processes) to a population of higher momentum states. It was found [31] that the lattice model is a good approximation provided that $U/J \ll 1$. If the latter inequality is violated, lattice artefacts occur. We find that these effects do not occur for a purely dissipative two-particle interaction ($U = 0$) even if $\hbar\Gamma_2/J \approx 1$.

For all numerical simulations, we consider a grid with $N_s = 500$ sites, and the physical state space at each site l is spanned by the four Fock states $\{|0\rangle_l, |1\rangle_l, |2\rangle_l, |3\rangle_l\}$, allowing for a maximum occupation of three particles at each site. We verified the convergence of our algorithm by varying the bond dimension χ of the matrix product state. In our simulations, the truncation errors ϵ_{trunc} are bounded by $\epsilon_{\text{trunc}} \leq 10^{-4}$ for $\chi = 100$.

The choice of the initial state for the numerical integration is motivated by the loading process of an optical pulse into the fibre, as described in section 2.2. We consider an initial state with a mean number of $\langle \hat{N} \rangle_0 = 5$ particles and a spatial density distribution, as shown in figure 2. Here we neglect distortions and correlations due to the optical nonlinearity that may build up during the loading process. The initial shape of the polariton pulse is then determined

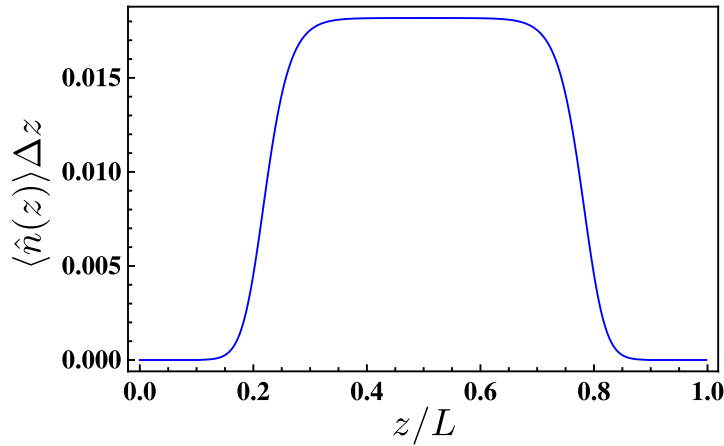


Figure 2. Spatial density distribution $\langle \hat{n}(z) \rangle$ of the initial state in equation (17).

by the slowly varying envelope of the probe pulse entering the system [23]. Furthermore, we assume that the initial polariton pulse is derived from laser light and thus described by a product of coherent states. In the discretized model, we thus model the initial state by a coherent state at each site,

$$|\psi\rangle_0 = \prod_l \exp(-|c_l|^2/2) \exp(c_l a_l^\dagger) |0\rangle, \quad (17)$$

where $\sum_l |c_l|^2 = 5$ and $|c_l|^2 = \Delta z \langle \hat{n}(z_l) \rangle$ with $z_l = l \Delta z$. We point out that $|\psi\rangle_0$ in equation (17) is an uncorrelated state with $g^{(2)}(z, z') = 1$ for all values of z, z' in the sample.

3. Numerical results

Next, we describe the results of the numerical integration of the master equation (11). Starting from the initial state in equation (17), the interaction is suddenly switched on at $t = 0$. We consider various scenarios where the interaction is purely dissipative or predominantly conservative.

In section 3.1, we discuss whether two-particle losses alone are able to drive the system into a correlated regime where the dissipation of particles is suppressed. As discussed in section 2.1, the inhibition of two-particle losses is linked to local correlations in the sample. Section 3.2 is concerned with non-local correlations. In particular, we compare non-local correlations created by a purely dissipative and a predominantly conservative interaction.

3.1. Inhibition of two-particle losses

The two-particle decay term in equation (1) in general leads to a loss of particles from the system. The rate at which the particle density diminishes is determined by equation (8) and depends crucially on the local correlations $g^{(2)}(z, z)$ of the system. Figure 3 shows the temporal evolution of $g^{(2)}(z_0, z_0)$ at the centre $z_0 = L/2$ of the sample for different values of the Lieb–Liniger parameter $|G|$ according to the numerical integration of equation (11). The values of $|G|$ correspond to the mean particle number $\langle \hat{N} \rangle_0 = 5$ of the initial state (see equation (17)). All solid lined lines in figure 3 belong to a purely dissipative two-particle

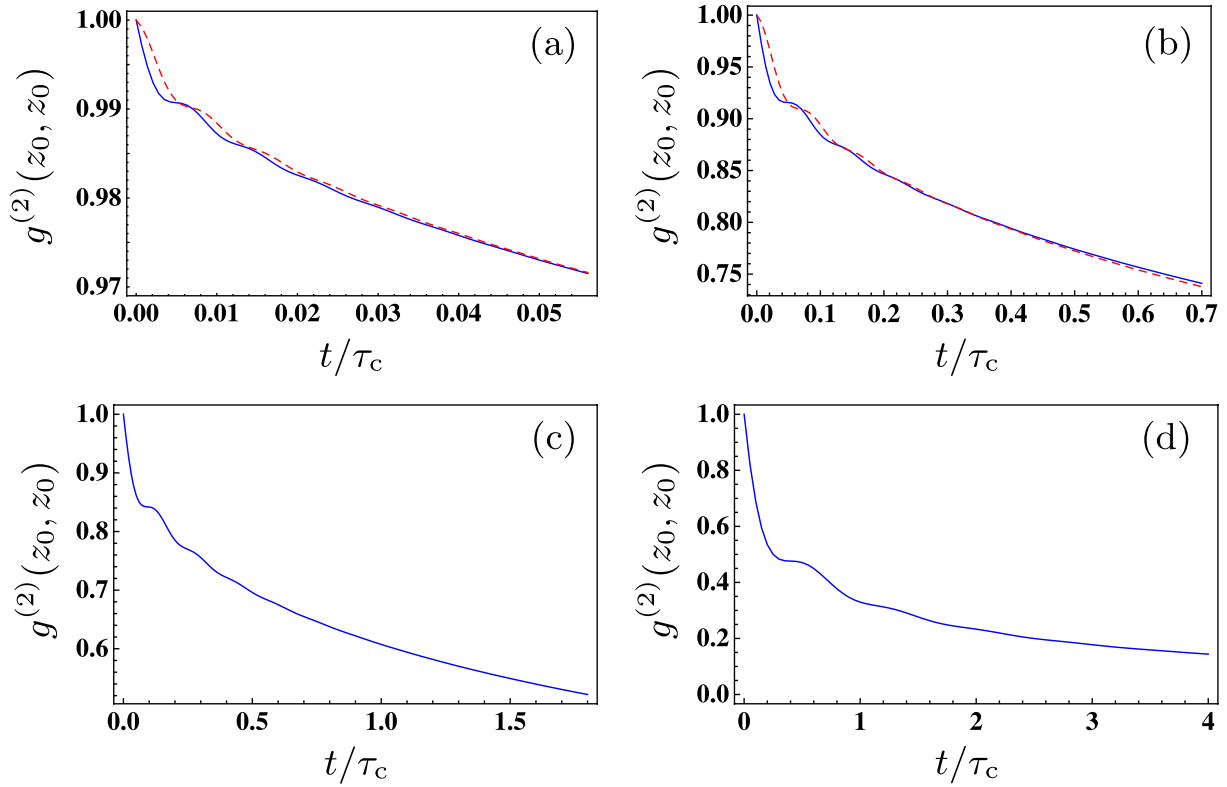


Figure 3. Temporal evolution of $g^{(2)}(z_0, z_0)$ at the centre $z_0 = L/2$ of the sample for (a) $|G| = 1$, (b) $|G| = 10$, (c) $|G| = 20$ and (d) $|G| = 100$. The timescale τ_c is defined in equation (19), and the solid lines correspond to a purely dissipative two-particle interaction, $\text{Re}(\tilde{g}) = 0$. In (a) and (b), the dashed line shows the result for an interaction that is predominantly repulsive [$|\text{Re}(\tilde{g})/\text{Im}(\tilde{g})| = 10$].

interaction, $\text{Re}(\tilde{g}) = 0$. In contrast, the dashed lines in figures 3(a) and (b) correspond to a predominantly conservative interaction $|\text{Re}(\tilde{g})/\text{Im}(\tilde{g})| = 10$.

In the case of a purely conservative interaction ($\text{Im}(\tilde{g}) = 0$), it was shown [31] that local quantities reach a stationary state on a timescale $T_{\text{loc}} = \hbar/(\tilde{g}\rho)$, where $\rho = N_{\text{ph}}/L$ is the density of particles. Note that the Lieb–Liniger gas does not thermalize globally [32]. Here we generalize this definition to the case of complex \tilde{g} and define

$$T_{\text{loc}} = \frac{\hbar}{|\tilde{g}|\rho} = \frac{m}{\hbar} \frac{1}{|G|\rho^2}. \quad (18)$$

Due to the enhanced numerical complexity of TEBD for density operators and numerical limitations, our simulations cannot cover the full time range T_{loc} . In the following, we scale time in the presentation of numerical results with

$$\tau_c = 2 \frac{\hbar}{\sqrt{U^2 + (\hbar\Gamma_2)^2}} = \frac{1}{50} T_{\text{loc}}. \quad (19)$$

The comparison between the dashed and solid lines in figures 3(a) and (b) shows that dissipative and repulsive two-particle interactions are equally effective in the repulsion of particles on a timescale proportional to the inverse interaction strength $|\tilde{g}|$. Note that for the polariton

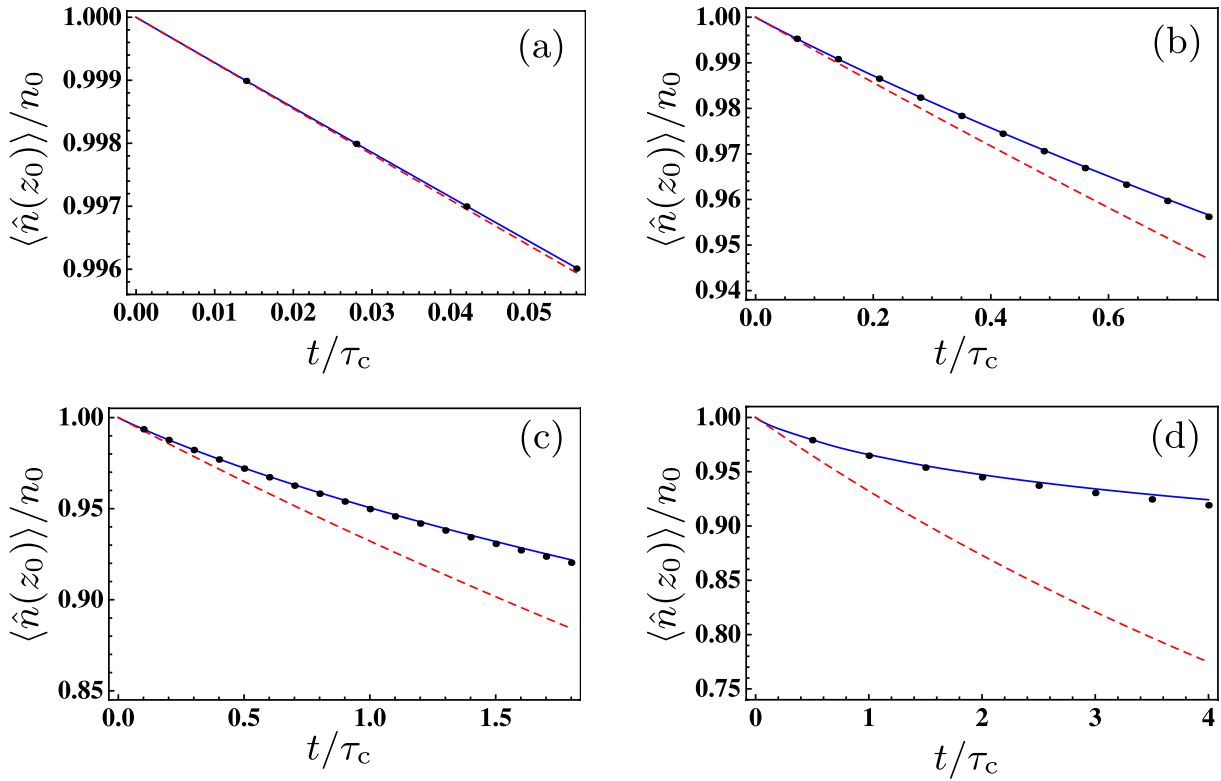


Figure 4. Temporal evolution of $\langle \hat{n}(z) \rangle$ at the centre $z_0 = L/2$ of the sample for (a) $|G| = 1$, (b) $|G| = 10$, (c) $|G| = 20$, (d) $|G| = 100$. In (a)–(d), the solid line corresponds to a numerical integration of equation (8) with $g^{(2)}(z_0, z_0)$ taken from the TEBD simulation for a purely dissipative two-particle interaction, $\text{Re}(\tilde{g}) = 0$. The dotted lines indicate the results of the TEBD simulation for $\langle \hat{n}(z) \rangle$. The dashed line shows the evolution of $\langle \hat{n}(z) \rangle$ according to equation (8) with $g^{(2)}(z_0, z_0) = 1$ for all times.

system discussed in section 2.2, $|\tilde{g}|$ is at least one magnitude larger for a purely dissipative interaction [14, 15] as compared to the conservative case. It follows that small values of $g^{(2)}(z_0, z_0)$ are reached much faster in absolute time for a dissipative two-particle interaction.

We emphasize that the minimal values for $g^{(2)}(z_0, z_0)$ in figure 3 will decrease further in time until their equilibrium values are reached. An estimate of these equilibrium values can be obtained via the work presented in [31]. Here the authors performed TEBD simulations for the unitary time evolution of bosons in 1D with two-particle repulsion. In particular, this system could be described by a pure quantum state that reduces the numerical complexity as compared to our simulations of the full density operator. Therefore, the simulations in [31] could be carried out up to times $t = T_{\text{loc}}$. Given that the initial dynamics of $g^{(2)}(z_0, z_0)$ for two-particle losses and for conservative interactions are very similar, one may suppose that the equilibrium values of $g^{(2)}(z_0, z_0)$ will also be almost the same. For this case, we estimate that $g^{(2)}(z_0, z_0)$ for our system should lie within the range $[0.1, 0.2]$ for $|G| = 10$ and $|G| = 20$ at $t = T_{\text{loc}}$.

Next we determine the temporal evolution of the particle density at the centre of the cloud via equation (8) and the numerical results for the temporal evolution of $g^{(2)}(z_0, z_0)$. The result is represented by the solid lines in figure 4 and is in good agreement with the direct evaluation

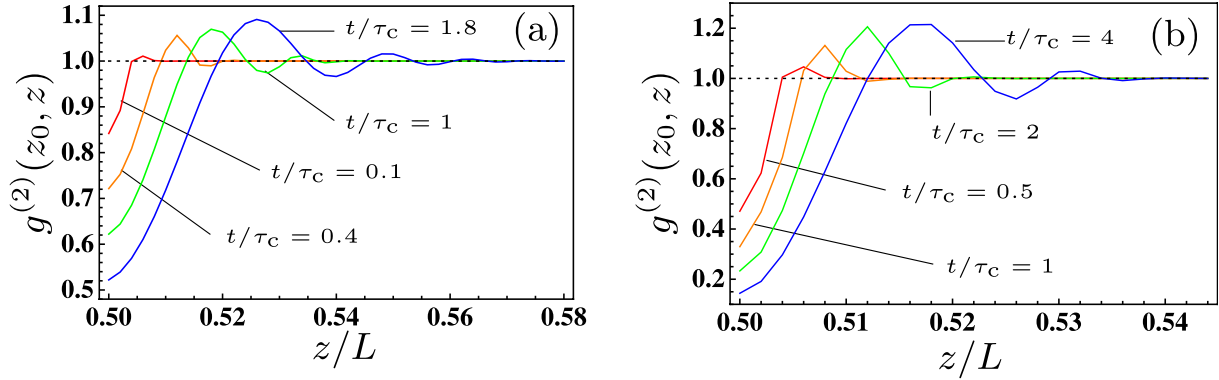


Figure 5. Spatial dependence of $g^{(2)}(z_0, z)$ for a purely dissipative two-particle interaction [$\text{Re}(\tilde{g}) = 0$]. The parameters correspond to (a) $|G| = 20$ and (b) $|G| = 100$, and $z_0 = L/2$ is the centre of the sample.

of the particle density $\langle \hat{n}(z) \rangle$ via the numerical integration of the master equation (11) (dotted lines). The small deviations are due to the diffusion term in equation (5) that results in particle losses and that was omitted from equation (8). Note that all curves in figure 4 correspond to a purely dissipative two-particle interaction, $\text{Re}(\tilde{g}) = 0$. In order to visualize the slowdown of two-particle losses due to the decrease of $g^{(2)}(z_0, z_0)$ in time, the dashed line in figure 4 shows the temporal evolution of $\langle \hat{n}(z) \rangle$ according to equation (8) with $g^{(2)}(z_0, z_0) = 1$ for all times. The slowdown of two-particle losses is most pronounced for $|G| = 100$, where a quasi-stationary regime is reached with $g^{(2)}(z_0, z_0)$ close to zero. We find that the decrease in the mean number of particles $\langle \hat{N} \rangle / \langle \hat{N} \rangle_0$ follows the same curves as the particle density at the centre of the cloud. It follows that more than 90% of the initially present particles are left at $t/\tau_c = 4$ for $|G| = 100$. Figures 4 (b) and (c) correspond to $|G| = 10$ and $|G| = 20$, respectively, and demonstrate a clear slowdown of two-particle losses. On the basis of the estimates for the equilibrium values of $g^{(2)}(z_0, z_0)$ obtained via the results presented in [31], we suppose that 50% (60%) of the initial particles are still present at $t = T_{\text{loc}}$ for $|G| = 10$ ($|G| = 20$). In contrast, $g^{(2)}(z_0, z_0)$ will not drop to values close to zero for $|G| = 1$ and hence we expect that a significant number of particles are lost at $t = T_{\text{loc}}$.

3.2. Non-local correlations

The spatial dependence of $g^{(2)}(z_0, z)$ as a function of z ($z_0 = L/2$ is the centre of the sample) is depicted in figure 5. Several snapshots in time are shown, indicating that non-local correlations exhibit oscillations that propagate outwards. The oscillations for the longest evolution times in figure 5 exhibit several minima that lie below unity. It follows that a dissipative two-particle interaction alone to some extent gives rise to spatial order of the particles. Note that non-local correlations reach a quasi-stationary regime on a timescale that is much larger than T_{loc} . In particular, we point out that the correlations shown in figure 6 are not Friedel oscillations [2] that characterize the Fermionic nature of particles in the Tonks–Girardeau regime.

In section 3.1, we concluded that repulsion and dissipation are equally effective in the creation of small values of $g^{(2)}(z, z)$. On the other hand, dissipative and conservative two-particle interactions give rise to different non-local correlations, as shown in figure 6.

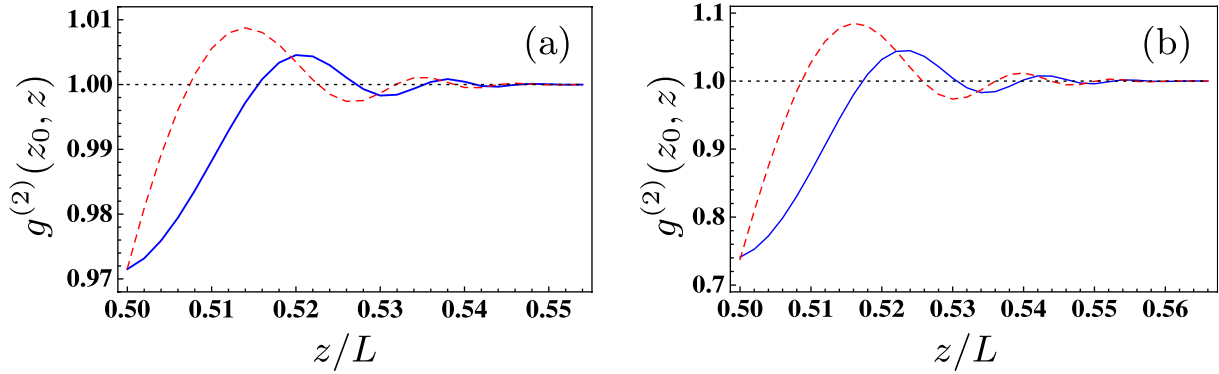


Figure 6. Spatial dependence of $g^{(2)}(z_0, z)$ for (a) $|G| = 1$, $t/\tau_c = 0.056$ and (b) $|G| = 10$, $t/\tau_c = 0.77$. $z_0 = L/2$ is the centre of the sample. The solid lines correspond to a purely dissipative two-particle interaction [$\text{Re}(\tilde{g}) = 0$], and the dashed lines show the result for an interaction that is predominantly repulsive [$|\text{Re}(\tilde{g})/\text{Im}(\tilde{g})| = 10$].

The solid and dashed lines correspond to a purely dissipative and a mostly conservative two-particle interaction, respectively. It can be seen that the non-local correlations propagate at the same velocity in space in the dissipative and conservative case, but the oscillations are more pronounced for a repulsive two-particle interaction.

In addition, two-particle losses give rise to a broader dip in $g^{(2)}(z_0, z)$ as a function of z as compared to the conservative case.

Note that the oscillation amplitudes in $g^{(2)}(z_0, z)$ are also damped by the diffusion term in equation (5).

4. Discussion and summary

In this paper, we have investigated the quantum dynamics of bosons in 1D after a sudden switch-on of two-particle losses. The master equation and the uncorrelated initial state are chosen such that our simulations directly apply to stationary-light polariton systems [13]–[15]. Apart from a (small) diffusion term, the considered master equation coincides with the dissipative Lieb–Liniger model [8]. In particular, we investigated the dissipation-induced preparation of correlations that effectively inhibit two-particle losses. We found that a metastable regime where losses are substantially suppressed can be prepared for large values of the Lieb–Liniger parameter $|G| \gg 1$.

Formally, it was shown [7, 8] that the two-particle loss term effectively results in a repulsion between particles such that they never occupy the same position in space. Therefore, dissipation via the two-particle contact interaction is inhibited. A physical explanation for this counterintuitive result can be given for a discrete lattice model [6, 7]. There it can be regarded as a manifestation of the quantum Zeno effect, where the two-particle losses play the role of a continuous measurement that always projects the system onto states with fewer than two particles in each lattice site before higher particle numbers can build up.

Furthermore, we compared the correlations induced by dissipative and repulsive interactions, respectively. We found that dissipation and repulsion are equally efficient for

the generation of local correlations $g^{(2)}(z, z) \leq 1$ on a timescale proportional to the inverse interaction strength. On the other hand, non-local correlations induced by dissipation show different features from those created by two-particle repulsion. As compared to an elastic repulsion between the particles, we find that two-particle losses give rise to a broader dip in $g^{(2)}(z_0, z)$ as a function of z (z_0 is the centre of the sample). Both repulsion and dissipation give rise to spatial oscillations in $g^{(2)}(z_0, z)$ that spread in time and indicate to some extent a spatial ordering. We find that these oscillations are more pronounced for a repulsion between the particles as compared to the dissipative case.

Acknowledgments

The authors thank D Muth and M Fleischhauer for discussions. This work was part of the Emmy Noether project HA 5593/1-1 funded by the German Research Foundation (DFG).

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