

Metacognition in multisensory perception

Ophelia Deroy¹, Charles Spence², & Uta Noppeney³

1 - Centre for the Study of the Senses, Institute of Philosophy, University of London, London, UK.

2 - Crossmodal Research Laboratory, Department of Experimental Psychology, Oxford University, Oxford, UK.

3 - Computational Neuroscience and Cognitive Robotics Centre, University of Birmingham, Birmingham, UK.

CORRESPONDING AUTHORS:

Ophelia Deroy ophelia.deroy@sas.ac.uk,

Uta Noppeney u.noppeney@bham.ac.uk

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29 **ABSTRACT**

30 Metacognition, the ability to monitor one's own decisions and representations, their accuracy and
31 uncertainty is considered a hallmark of intelligent behaviour. Little is known about metacognition
32 in our natural multisensory environment. In order to form a coherent percept the brain should inte-
33 grate signals from a common cause, but segregate those from independent causes. Multisensory
34 perception thus relies on inferring the world's causal structure, raising new challenges for metacog-
35 nition. We discuss the extent to which observers can monitor their uncertainties not only about their
36 final integrated percept but also about the individual sensory signals and the world's causal struc-
37 ture. The latter causal metacognition highlights fundamental links between perception and other
38 cognitive domains such as social and abstract reasoning.

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41 **TRENDS**

42 To form a coherent percept of our multisensory environment the brain needs to integrate signals
43 caused by a common source (e.g. event), but segregate those from different sources; natural multi-
44 sensory perception thus relies inherently on inferring the world's causal structure.

45 Human observers are known to metacognitively monitor the uncertainty of their perceptual esti-
46 mates in simple sensory tasks, but it is unclear whether they can monitor their uncertainties about
47 their integrated percept, the individual sensory signals and the causal structure of complex multi-
48 sensory environments.

49 Causal metacognition highlights fundamental links between perception and other cognitive domains
50 such as social and abstract reasoning and may be critical for our understanding of neuropsychiatric
51 diseases such as schizophrenia.

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55 **KEYWORDS:** Metacognition, Multisensory Perception, Crossmodal Integration, Bayesian Causal
56 Inference, Cue Combination, Uncertainty, Confidence

57 MAIN TEXT

58 **Metacognition: Monitoring one's own cognition**

59 'Metacognition' refers to cognitive processes about other cognitive processes, knowing about
60 knowing, or beliefs about one's own beliefs. It describes the formation of second-order representa-
61 tions that allow observers to monitor their first-order representations about objects or events in the
62 real world [1–3]. Metacognitive research investigates the extent to which observers can assess the
63 uncertainty or accuracy of their perceptual representations and judgments. For instance, observers
64 cannot only spot a friend in the crowd, but also metacognitively evaluate their uncertainty or doubt-
65 fulness about their first-order perceptual interpretation (e.g., "Is this really my friend?"). In a wider
66 sense, though, metacognition characterizes an observer's ability to introspect the perceptual infer-
67 ence processes that led to their first-order world representations [4]. Metacognition can operate in a
68 number of domains including perception [5–7], memory [8,9], collective decision-making [10] and
69 social learning [11,12].

70 Despite a recent surge of interest in metacognition, the majority of perception research to date has
71 focused on simple visual or auditory tasks that were based on one single signal stream [7,13–16].

72 Yet, in our natural environment, our senses are constantly bombarded with many different signals.
73 In order to form a coherent percept of the world, the brain is challenged to integrate signals caused
74 by common events, but segregate those caused by independent events. Natural perception thus re-
75 lies inherently on inferring the world's causal structure. In this review, we focus on the challenges a
76 natural complex environment poses not only for first-order perception, but also for second-order
77 metacognition. First, we introduce Bayesian Causal Inference as a normative model that describes
78 how an ideal observer should arbitrate between sensory integration and segregation when exposed
79 to multiple sensory signals in our natural environment [17–19]. Next, we discuss whether observers
80 can monitor their uncertainties associated with the different sorts of estimates that Bayesian Causal
81 Inference involves, such as the uncertainties about their final integrated percept, the individual sen-
82 sory estimates, and the inferred causal structure of the world [2,20,21]. Finally, we ask whether
83 human observers can move beyond the integrated percept and metacognitively introspect those per-
84 ceptual inference processes. Is multisensory perception encapsulated as an unconscious inference
85 process, or is it open to metacognitive introspection? While we focus on multisensory perception
86 and cue combination as prime examples for the integration of information from independent senso-
87 ry channels [17,22,23], the fundamental challenges and principles apply more generally to situa-

88 tions and tasks that require information integration and segregation in perception and wider cogni-
89 tion (Box 1).

90 Metacognition enables human and non-human observers [24] to act more strategically, for instance,
91 to determine whether or not to defer a response and acquire more information [20,25]. Causal meta-
92 cognition is, in particular, critical for situations with information emanating from potentially differ-
93 ent sources not only in perception, but also in social and abstract reasoning [17,26].

94

95 **Metacognition in perception**

96 In the 19th Century, Helmholtz described perception as ‘unconscious inference’ that maps from
97 noisy sensory inputs to perceptual interpretations and choices under the guidance of prior experi-
98 ence [27]. Likewise, more recent Bayesian statistical models formalize perception as a probabilistic
99 inference process whereby the brain combines prior expectations with uncertain sensory evidence to
100 infer the most likely state of the world [28]. Perception is thus inherently uncertain and error-prone.
101 Metacognitive research investigates whether observers can assess their uncertainty about the per-
102 ceptual representations that are formed on the basis of noisy sensory evidence. Are observers ap-
103 propriately confident about the accuracy of their perceptual choices and eventually use this infor-
104 mation to adjust subsequent responses [21,29]? Accumulating evidence based on decisional confi-
105 dence ratings [30], no loss gambling [31], or post-decision wagering [32,33] demonstrates that hu-
106 man and non-human observers can indeed access the uncertainty of their perceptual representations
107 and adjust their decisional confidence accordingly. In some cases, observers even compute their
108 confidence about the correctness of their perceptual judgment (e.g., motion discrimination) in a
109 Bayes-optimal fashion. In other words, their confidence truthfully reflects the probability that their
110 perceptual choices are correct given the sensory signals (e.g., motion) [29]].

111 Critically, observers’ decisional confidence depends on the uncertainty of their first-order perceptu-
112 al representations (for other influences, see [34]). For instance, when presented with weak motion
113 signals, observers will not only be close to chance when discriminating motion direction but also
114 when judging whether their motion discrimination response was correct. In other words, observers’
115 perceptual sensitivity (e.g., their ability to discriminate left from right motion, say) constrains their
116 maximally possible metacognitive sensitivity (i.e., their ability to discriminate between their correct
117 and incorrect choices) [14,35]. While d' is used as a signal-theoretic index to quantify observers’
118 perceptual sensitivity, meta- d' has recently been proposed as a signal-theoretic index to quantify
119 observer’s metacognitive sensitivity. A large meta- d' indicates that observers can reliably discrimi-
120 nate between their correct and incorrect perceptual judgments. Critically, while meta- d' depends on
121 both the quality of the sensory evidence and its metacognitive assessment, directly comparing the
122 perceptual and the metacognitive d' quantifies observer’s metacognitive efficiency [14,35]. It pro-

vides insights into an observer's ability to evaluate the uncertainty of their perceptual representations and choices. A 'metacognitively-ideal observer' (i.e., where meta-d' is equal to d') can access all information that was used for the first-order perceptual judgment for his/her second-order metacognitive evaluation.

Abundant evidence suggests that the brain is able to represent and use estimates of uncertainty for neural computations in perception, learning, and cognition more widely [21–23,36,37]. Yet, the underlying neural coding principles remain debated. For instance, uncertainty may be represented in probabilistic population codes [38,39] or else rely on sampling-based methods [40]. Likewise, it remains controversial whether metacognitive 'confidence estimates' are directly read-out from first-order neural representations [13,20] or formed in distinct 'metacognitive' neural circuitries [7,41,42]. In support of a shared system, or common mechanism, underlying perceptual decisions and confidence, neurophysiological research has demonstrated that the same neurons in a lateral parietal area encode both monkey's perceptual choice and its confidence [43,44]. Dissociations between perceptual choice and confidence may emerge when decision confidence is interrogated after the subject committed to a perceptual choice thereby relying on different sensory evidence [3,13,45]. By contrast, neuropsychological and neuroimaging studies in humans point toward dedicated metacognitive neural circuitries in the prefrontal cortex [7,42,46]. For instance, fMRI work revealed that activations in anterior prefrontal cortex reflect changes in confidence when perceptual performance is held constant [47]. Likewise, patients with anterior prefrontal lesions showed a selective deficit in metacognitive accuracy [42]. Decisional confidence estimates encoded in dedicated circuitries may serve as a common currency and enable direct comparisons across different cognitive tasks [15] or sensory modalities [5].

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146 **The multisensory challenge: Causal inference and reliability-weighted integration**

Imagine you are packing your shopping items from your trolley into the back of your car which is parked on a busy street. Suddenly you hear a loud horn. Is this sound coming from a car on the opposite side of the road, competing for a parking spot, or from a car hidden behind your back indicating that your trolley is blocking the traffic? Or is the sound perhaps coming from one of your shopping items? While the latter suggestion seems rather unlikely, the other two may be valid interpretations of the sensory inputs (see figure 1). This example illustrates the two fundamental computational challenges that the brain faces in our everyday multisensory world: First, it needs to solve the so-called causal inference problem [17–19] and determine whether or not signals come from common sources and should be integrated. Second, if two signals come from a common source, the

156 brain is challenged to integrate them into the most reliable percept by weighting them optimally in
157 proportion to their reliabilities (i.e., inverse of sensory variance [22,23,48,49]).
158 In the laboratory, the principles of multisensory integration can be studied by presenting conflicting
159 and non-conflicting signals. For instance, if auditory and visual signals are presented in synchrony
160 yet at different spatial locations, the ventriloquist illusion emerges. The perceived sound location
161 shifts towards the location of a spatially distant visual signal and vice versa depending on the rela-
162 tive auditory and visual reliabilities. Importantly, spatial biasing is reduced at large spatial dispari-
163 ties when it is unlikely that the two signals come from a common source [50,51]. This attenuation
164 of sensory integration at large spatial disparities is well accommodated by hierarchical ‘Bayesian
165 Causal Inference’ that explicitly models the potential causal structures that could have generated the
166 sensory signals i.e., whether auditory and visual signals come from common or independent sources
167 [18,52] (for related models based on heavy tailed prior distributions, please see [17,53,54]). During
168 perceptual inference, the observer is then thought to invert this generative process. Under the as-
169 sumption of a common signal source, the two unisensory estimates of a physical property are com-
170 bined and weighted according to their relative reliabilities (i.e., inverse of variance). For instance, to
171 estimate the location of a singing bird from audition and vision the observer should give a stronger
172 weight to the visual signal at day time than at night. Under the hypothesis of two different sources,
173 the auditory and visual signals are treated independently. On a particular instance, the brain needs to
174 infer the causal structure of the world (e.g., one or two sources) from the sensory inputs. Multiple
175 sorts of intersensory correspondences [55] such as spatiotemporal coincidence (i.e. auditory and
176 visual signals happening at the same time and location [56–62], semantic (e.g. the shape and
177 singing of a bird) [63–65] or higher-order correspondences (e.g., gender: female voice with female
178 face) can inform the brain as to whether signals are likely to come from a common source or
179 independent sources. Finally, an estimate of the physical property in question (e.g., auditory loca-
180 tion) is obtained by combining the estimates under the two causal structures using different deci-
181 sional functions [18,52,66]. For instance, using model averaging observers may form a final esti-
182 mate by averaging the estimates from the two causal structures weighted by their posterior probabil-
183 ities. Alternatively, they may report the estimate of the most likely causal structure as final estimate,
184 a decisional strategy referred to as model selection.

185

186 **Monitoring uncertainties about the world’s causal structure and environmental properties**

187 The additional complexity of multisensory perception or more generally tasks that rely on multiple
188 information channels raise questions and challenges that go beyond metacognition studied, for ex-
189 ample, with simple visual discrimination or detections tasks. In particular, it raises the question of

190 whether observers can monitor the different sorts of uncertainties involved in Bayesian Causal In-
191 ference:

192 First, observers may monitor their uncertainty about the causal structure that has generated the
193 sensory signals [18,19,66]. The uncertainty about the causal structure increases with the noise in the
194 sensory channels. For instance, at dawn, it is more difficult (i.e. associated with greater uncertainty)
195 to attribute a singing voice to a specific bird in the bush than in bright sunlight. Hence, the
196 uncertainty about the inferred causal structure critically depends on the sensory uncertainty given in
197 all sensory channels [52]. Moreover, causal uncertainty emerges because there is some natural
198 variability in the temporal, spatial or higher-order (e.g. semantic) relationship of the sensory signals.
199 Even when two signals are generated by a common source, they do not need to be precisely
200 temporally synchronous or spatially collocated. For speech signals, it is well established that visual
201 facial movements often precede the auditory signal to variable degrees at speech onset [67].
202 Further, differences in velocity of light and sound induce variability in arrival times of the visual
203 and auditory signals at the receptor level that depend on the distance of the physical source from the
204 observer [68,69]. Likewise, higher-order correspondences, such as gender or semantics may relate
205 probabilistically to low level physical features (e.g. a low-pitched voice is more likely to be
206 associated with a male than a female person). Experimentally, we therefore need to determine
207 whether observers' causal uncertainty reflects the uncertainty determined by the signal-to-noise
208 ratio of the sensory signals and their spatiotemporal and higher-order (e.g. semantic) statistical
209 relationships. Moreover, causal uncertainty may be influenced by participants' prior expectations
210 [70,71] that sensory signals are likely to come from a common external source, or be generated by
211 one's own voluntary actions [72,73] (see Box 3).

212 Second, it is well-established that observers use the uncertainty associated with the individual cues
213 or sensory signals to assign the appropriate weighting during cue combination or multisensory
214 integration. Yet, an unresolved question is whether these uncertainty estimates for individual cues
215 are then lost or accessible for metacognition. To approach these questions, future experiments may
216 consider asking observers to explore objects visuo-haptically (i.e., via vision and touch) and report
217 both the haptic size they perceived and their uncertainty about their perceptual estimate in the
218 context of the visual information as well as if they had fully ignored the visual information (e.g.,
219 they may be asked to imagine that they had closed their eyes and only haptically explored the
220 object). If observers maintain partial access to the unisensory estimates and their associated
221 uncertainties we would expect that the two reports differ.

222 Finally, observers may monitor their uncertainty associated with their final perceptual estimate (e.g.
223 the reported location during audiovisual localization tasks). According to Bayesian Causal
224 Inference, these final (e.g., auditory and visual) perceptual estimates are formed by combining the

estimates under the assumptions of common and independent sources according to various decision functions such as model averaging, probability matching or model selection [66]. As a result, the uncertainty of these final Bayesian Causal Inference perceptual estimates is dependent on observer's sensory and causal uncertainty. A critical question for future investigation is to determine the extent to which observers' uncertainty about their reported perceptual estimate reflects their perceived causal uncertainty or the causal uncertainty as predicted based on their sensory uncertainties.

A few studies have started to directly tackle the question of metacognitive uncertainty or confidence estimates in multisensory perception, albeit not always with these different sorts of uncertainties in mind. For instance, a recent psychophysical study [74] demonstrated that observers' correctly assessed the accuracy of their temporal order judgments in confidence ratings. These results indicate that the precision of audiovisual temporal relation estimates is accessible to metacognition. Further, a recent study by White and colleagues [75] presented observers with audiovisually non-conflicting (e.g., visual <<ba>> with auditory /ba/), conflicting phonemic cues that could be integrated into a so-called McGurk percept (e.g., McGurk: visual<<ga>> with auditory /ba/ resulting in an illusory [da] percept) and conflicting phonemic cues that could not be integrated into one unified percept (i.e., non McGurk: visual <<pa>> with auditory /ka/). Observers reported their perceived auditory phoneme, immediately before providing a second-order confidence rating. The authors demonstrated that observers were less confident about their illusory McGurk percepts than about their auditory percept for conflicting or non-conflicting stimuli. From a Bayesian Causal Inference perspective, observers' lower confidence about their McGurk responses may emerge from an increase in causal uncertainty for McGurk stimuli. While non-conflicting signals are likely to come from a common source and conflicting signals from independent sources, McGurk stimuli introduce an intermediate phonological conflict that introduces uncertainty about the underlying causal structure. This causal uncertainty may indirectly influence and increase observers' uncertainty about their final phoneme percept. However, this is only one of several possible explanations for the observed response profile (see also [76]). It highlights the need for future dual-task paradigms that ask observers concurrently to rate not only their confidence about their phonological percept, but also their causal uncertainty about whether sensory signals (e.g. auditory phoneme and facial movements in speech recognition) were generated by a common source.

255

256 **Perceptual and causal metamers**

Further insights into whether observers can move beyond the integrated percept and metacognitively monitor the perceptual inference can be obtained from so-called metamers, i.e. (near)-identical perceptual interpretations formed from different combinations of sensory signals [77]. Let's assume

260 we present an observer with two signals in synchrony, a brief flash at -2° visual angle (i.e. left) and
 261 a spatially equally reliable beep at $+2^\circ$ visual angle (i.e. right). Where will the observer perceive this
 262 event? Because of the small audiovisual spatial disparity, the observer may infer that the two sig-
 263 nals come from a common source and hence integrate them weighted by their relative reliabilities.
 264 As a result, he would perceive the audiovisual event at 0° degree visual angle, where in fact no sig-
 265 nal was presented at all. Hence, this conflicting flash-beep event would elicit the same percept as a
 266 non-conflicting flash-beep event where both auditory and visual signals are presented at 0° degree
 267 visual angle. In other words, the conflicting and the non-conflicting flash-beep events elicit percep-
 268 tual metamers. Moreover, the observer inferred that the auditory and visual signals come from a
 269 single event in both situations. Hence, the two cases elicit not only perceptual but also causal met-
 270 amers. The critical question is whether observers may nevertheless be able to discriminate between
 271 the conflicting and non-conflicting flash-beep events indicating that they can metacognitively ac-
 272 cess additional information about the underlying perceptual inference process.
 273 First, observers would be able to discriminate between the non-conflicting and conflicting signals, if
 274 they monitor their uncertainty about their perceptual interpretation and causal inference. In the
 275 small conflict case, those observers who use Bayesian Causal Inference with model selection may
 276 decide that the two signals come from a common source and integrate them weighted by their rela-
 277 tive reliabilities. Critically, even though they commit to one single event as the more likely causal
 278 structure, they should be less certain about their causal inference. In other words, monitoring their
 279 causal uncertainty would allow observers to discriminate between conflicting and non-conflicting
 280 sensory signals, even if they elicit perceptual and causal metamers. Within the framework of Bayes-
 281 ian Causal Inference and depending on decisional functions and biases [66], it is also conceivable
 282 that observers may integrate different combinations of auditory and visual signals into the same
 283 perceptual (e.g. auditory, visual) estimates and yet report different causal structures. Hence, percep-
 284 tual metamers may not necessarily imply causal metamers.
 285 Second, observers may be able to go beyond the integrated percept and maintain at least partial ac-
 286 cess to the individual sensory signals (see discussion above). Again, this partial access would allow
 287 them to discriminate between conflicting and non-conflicting flash-beep events. In a wider sense of
 288 metacognition it would demonstrate that multisensory perception is not informationally encapsulat-
 289 ed, but that observers can introspect and metacognitively monitor the unisensory representations
 290 that form the basis for their perceptual inference.
 291 Surprisingly, only a few studies to date have used perceptual metamers as an approach to character-
 292 ize observers' metacognitive access in cue combination. An intriguing early study by Hillis et al.
 293 [77] focused on the emergence of perceptual metamers in visual (slant from disparity and texture
 294 cues in vision) and visuo-haptic (object size from vision and touch, i.e., haptic cues) contexts. In an

oddity judgment task, observers were asked to identify the odd stimulus in a sequence of three stimuli: two identical standard stimuli defined by non-conflicting cues and one odd stimulus defined by conflicting cues that could be fused into a perceptual metamer of the standard stimulus [77,78]. The results revealed that observers lost access to individual cues in the visual, but not in the visuo-haptic setting: Only conflicting visual cues were mandatorily fused into perceptual metamers of the non-conflicting standard stimulus. Yet, even in the visual case participants were able to discriminate the conflicting stimulus from the non-conflicting ones for larger conflict sizes indicating that metamers emerge only for small conflict size. What happened, though, in those unisensory cases with larger conflict? As the oddity judgment task does not explicitly define the dimension according to which participants should compare the stimuli, it remains unclear whether observers identified the conflicting stimulus because they did not integrate the conflicting cues into one unified slant estimate, i.e., into a perceptual metamer of the non-conflicting stimulus, or whether instead they integrated them, but were aware that their metameric percepts emerged from different causal structures or at least associated with different causal uncertainties. Observers may still have fused conflicting signals into approximate perceptual metamers without them being causally metameric to the non-conflicting standard stimulus. In other words, observers may potentially have identified the odd-one-out because of partial access to the causal structure that has generated the sensory inputs. Indeed, observers reported a ‘weird’ percept for larger conflict sizes (personal communication, Marc Ernst) indicating that they were aware of the conflict manipulation while still integrating signals into a near-unified percept. This may perhaps be taken as initial evidence that perceptual and causal metamers may be to some extent dissociable. Future studies that explicitly assess the emergence of perceptual and causal metamers are needed to experimentally determine whether participants can form perceptual metamers while recognizing that they are based on different causal structures.

Another approach to dissociate perceptual and causal metamers is to introduce conflicts along multiple dimensions such as lower temporal and higher-order phonological dimensions. For instance, observers may be presented with conflicting and non-conflicting visual and auditory phonetic cues at multiple audiovisual asynchronies. For small audiovisual asynchronies, conflicting audiovisual signals, such as a visual <<ga>> and an auditory /ba/, may be fused into a [da] percept at the phonological level as in the classical McGurk-MacDonald illusion [79] (Figure 2). The critical question is whether the fusion of conflicting audiovisual signals into a [da] percept as a perceptual metamer of a non-conflicting audiovisual [da] emerges in cases where observers inferred that the two signals come from different sources because of their audiovisual asynchrony (i.e., no causal metamer).

Research showing that the temporal integration windows that allow the McGurk illusion to emerge mostly correspond to those where observers perceive the audiovisual signals as being synchronous has suggested that the detection of temporal conflicts precludes the emergence of perceptual meta-

mers [80]. However, other evidence suggests that conflicting visual phonetic information influences the perceived auditory phonemes even when observers are able to detect low-level temporal conflicts [81]. In the light of this controversial evidence, future studies are needed to determine whether perceptual metamers at higher representational levels emerge even when lower level temporal conflicts prevent the emergence of causal metamers.

335

336 **Concluding remarks**

337 Accumulating evidence shows that human observers can metacognitively assess the uncertainty of
338 perceptual estimates formed from vision, touch or audition, in unisensory perception. Conversely,
339 research in multisensory perception demonstrates that observers integrate signals from multiple
340 sensory modalities into percepts that take into account the uncertainty about the world's causal
341 structure. In this review, we have merged these two research fields and discuss the new challenges
342 and questions that metacognition poses for situations where the brain needs to integrate information
343 from multiple channels such as in multisensory perception and cue combination. Recent
344 developments of hierarchical Bayesian models of multisensory perception raise the possibility that
345 human observers can introspect perceptual inference processes and monitor not only the final
346 integrated percept, but also the unisensory estimates and the causal relationship - thereby
347 challenging the long-dominant view in philosophy that observers are causally naive about
348 perceptual inference (Box 2). Future studies in causal metacognition will need to determine the
349 extent to which human observers can accurately assess their uncertainty about the perceptual
350 estimates and the inferred causal structure of the environment. They open up new research avenues
351 that link metacognition in perception more tightly with higher-order cognitive capacities such as
352 abstract causal reasoning [82] or the aggregation of information across agents (Box 1 and
353 Outstanding Questions). Causal metacognition sheds new light on the emergence of the sense of
354 agency [83] (Box 3) and will be critical for our understanding of neuropsychiatric diseases such as
355 schizophrenia that affect multisensory binding, causal inference and metacognitive control [75,84–
356 87]

Box 1: Monitoring causal uncertainty beyond perception.

Causal inference is not only critical for perception but, more generally, for many other cognitive domains such as inductive, abstract, or social reasoning [82]. If two burglaries occur in the same town on the same day, the police ought to inquire as to whether they are likely to be performed by the same or different criminal gangs. Likewise, if a patient presents initially with a rash followed by high fever, cough, shortness of breath and wheezing, the medical doctor needs to infer whether all these symptoms are caused by measles infection or whether some of them may be caused by a subsequent bacterial (e.g., streptococcal) superinfection which requires antibiotic treatment. These examples highlight that causal inference is pervasive in our everyday lives. Causal metacognition enables observers to monitor their uncertainty about the underlying causal structure and decide whether to seek additional evidence in order to arbitrate between several potential causal structures. If the medical doctor is in doubt whether the patient may have incurred an additional streptococcal infection, s/he may order blood tests, chest x-ray, etc.

Causal inference is also fundamental for successful communication and interactions across social agents. For instance, if two social agents talk about a person called ‘Peter’ they usually assume that they refer to the same person as the causal source that generates their thoughts and representations associated with ‘Peter’. In fact, this shared causal perspective is fundamental for successful collective decision making [10]. Surprises and comic moments may emerge if agents discover during the course of their conversation that their inference was wrong and they had actually been referring to two different individuals that were both called ‘Peter’. In other words, they suddenly discovered that their thoughts and representations were not caused by one common source ‘Peter’, but by two different individuals.

Causal Inference as a process to arbitrate between one or multiple causes for sensory signals, medical symptoms or mental representations is part of the wider question of how observers can infer hidden structure from statistical correlations in observed data (e.g. correlations between different symptoms). How can they build veridical or at least useful models of the world? As reviewed in more detail in [17,88–90], Bayesian models can be used to accommodate human structure inference across numerous domains including inductive reasoning [82], semantics [91], social cognition [10] or aggregation of information across individuals [92].

386 **Box 2: Challenging causal naivety assumptions in philosophy**

387 The capacity to represent causation is usually granted only on the evidence that explicit causal rea-
388 soning, and inferences to hidden or distant causes are performed. As Hume's challenge goes, there
389 is a difference in predicting that one event regularly follows another, and in representing that it was
390 caused by this first event. This view, started in philosophical discussions [93], is also widespread in
391 psychology [94]. Does causal metacognition challenge this claim, suggesting that we are sensitive
392 to differences between hidden causal structures when we perceive events? How sophisticated do we
393 need to be to monitor the uncertainty of our causal models of the world?

394 Evidence of causal metacognition in younger children and non-human animals should address this
395 question, and possibly reveal whether hidden causal structures are accessed and monitored as such,
396 even in the absence of more explicit causal reasoning. But causal metacognition brings a broader
397 challenge to philosophical models of perception. It is widely assumed indeed that we are causally
398 naive when it comes to perceiving the world: Perception does not make us aware of objects as caus-
399 es of our perception [95]. When we perceive a singing bird, we do not see that a physical bird, or
400 light, is causing our perception: We perceive a bird, as a mind-independent object, not as a likely
401 cause of our percept. The claim that perception rests on a process of causal inference, at the sub-
402 personal level [96,97], though widely accepted by cognitive neuroscientists, explains from the out-
403 side what the system is set up to do, but does not suppose that causes are represented as such, even
404 less consciously accessed [98,99]. Sensitivity to differences in the causal origin of our integrated
405 percepts offers an intermediate step where the causal character of perception is made manifest.

406 How this form of causal metacognition fits within causal cognition in general, and whether it is also
407 present in more explicit forms of reasoning is an open question. While it is common to stress the
408 difference between aggregating information between agents, and combining information from dif-
409 ferent sensory modalities, it might be the case that both are optimal if the uncertainty about the un-
410 derlying causal model dictating the problem is adequately monitored.

411 **Box 3: Causal metacognition and sense of agency**

412 Causal inference enables the brain to dissociate the sensory effects caused by one's own actions
413 from those caused by other agents or events in the outside world. Previous neuroimaging and
414 neurophysiological studies have suggested that the cerebellum may form a predictive forward
415 model that maps from the action plan to the motor outputs and their sensory consequences. These
416 forward models enable the brain to distinguish between self- and other-generated sensory signals
417 leading to effects such as sensory attenuation (e.g., predicted outputs of our own tickling are not felt
418 as tickling [100]) or intentional binding (e.g. the temporal interval between a voluntary action and
419 its sensory consequences is subjectively compressed [72,73,83], see figure I). Both effects are
420 considered central to our sense of agency that is the subjective judgment or feeling that we are
421 causally responsible for changes in the environment. Critically, the temporal compression effect
422 was increased in patients with schizophrenia indicating an enhanced sense of agency [85–87]. From
423 the perspective of causal metacognition, we would expect the sense of agency to be related to the
424 degree of confidence about our beliefs that a certain sensory outcome was self- rather than other-
425 generated [84]. Further, manipulating biases in confidence by prior context or instructions may
426 influence sensory attenuation and intentional binding, even when the sensory and motor
427 components are held constant. For instance, if an agent is more confident that he/she has generated
428 certain sensory signals, he/she should experience the same signal as less tickling and the interval
429 between the action and the occurrence of the tickling sensation to be less compressed in time. A
430 critical question for future research is therefore whether the altered sense of agency in patients with
431 schizophrenia [85], may be associated with more general changes in causal metacognition.

432

433

434 **GLOSSARY**

435 Causal metamers: identical causal structures inferred from signals generated by physically different
436 causal structures.

437 Causal metacognition: monitoring the inferred causal structure underlying certain signals (e.g.
438 sensory signals)

439 Confidence rating, post-decision wagering, no loss gambling [30]: are methods to assess an
440 observer's metacognitive insights or awareness. For instance, observers may rate their confidence
441 about the correctness of their decision on a numerical scale. In post-decision wagering, they are
442 asked to bet on the correctness of their reported choices. As a result, observers should place higher
443 wagers when they are more confident about the correctness of their decision to maximize their
444 gains. In no-loss gambling, observers need to choose whether they are given a reward depending on
445 the correctness of their perceptual choice, or depending on a lottery with pre-specified probabilities.
446 Both post-decision wagering and no-loss gambling provide observers with an incentive to reveal
447 their decisional confidence and subjective probabilities truthfully. Yet, post-decision wagering may
448 be sensitive to additional biases such as risk aversiveness.

449 Bayesian Causal Inference models: normative Bayesian models that describe how an observer
450 should integrate sensory signals to compute an estimate of an environmental property. Bayesian
451 Causal Inference [17–19,52,66] explicitly models the potential causal structures (i.e. common or
452 independent sources) that could have generated the two signals.

453 Intersensory correspondences: the observer uses different sorts of correspondences such as spatial
454 colocation [50–52,58,59], temporal coincidence [56,57,60] and correlations [61,62], semantic or
455 phonological congruency [63–65] to determine which signals are likely to come from a common
456 source and should be bound during perception.

457 Perceptual metamers: are identical perceptual (e.g. spatial, phoneme) estimates formed from
458 physically different signals.

459 Metacognition: cognitive processes about other cognitive processes (e.g. formation of
460 representations about world representations [1–3,24]).

461 McGurk illusion: an audiovisual illusion [71,79,81] where observers perceive for instance the
462 phoneme [da] when presented with a video of a face articulating <<ga>> and a voice uttering /ba/.

463 The McGurk illusion is a prime example of a perceptual metamer; i.e. the conflicting signals are
464 perceived as identical to a face and voice articulating [da].

465 Sense of agency: the subjective feeling that one initiates and controls one's own actions [72,73,83].

466 Sensory reliability: is the inverse of sensory variance (or uncertainty). Reliability decreases with the
467 noise of a sensory signal.

468 Ventriloquist illusion: a multisensory perceptual illusion induced by presenting two signals from
469 different sensory modalities in synchrony, but at different spatial locations. In classical audio-visual
470 cases, the perceived location of a sound is shifted towards the actual location of the visual signal,
471 and vice versa [18,50–52].

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477 **OUTSTANDING QUESTIONS**

- 478 ▶To what extent can observers metacognitively monitor the individual signals, the inferred causal
479 structure, and their respective uncertainties in sensory or cue-integration? Do their perceptual
480 uncertainties reflect their causal uncertainties, and vice versa?

- 481 ▶How does causal metacognition in perception relate to metacognition in other cognitive domains
482 such as causal reasoning or social interactions?

- 483 ▶What are the benefits of causal metacognition in perception? Do observers adjust their future
484 perceptual interpretations based on their causal metacognitive assessments?

- 485 ▶Is the sense of agency grounded in causal metacognition?

- 486 ▶Which neural circuitries sustain causal metacognition during perceptual and other cognitive tasks
487 in the human brain?

- 488 ▶Is causal metacognition impaired in neuropsychiatric diseases such as schizophrenia?

- 489 ▶How does causal metacognition develop during infancy and childhood? Does it emerge later than
490 metacognition about perceptual decisions based on a single information stream?

- 491 ▶Non-human organisms have been shown to monitor their uncertainties about their perceptual
492 decisions. Can they also monitor their uncertainty about the causal structure of the world?

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501 **FIGURE LEGENDS**

502 **Figure 1**

503 **Metacognition in multisensory perception**

504 Left: Generative Model: The generative model of Bayesian Causal Inference for spatial localization
505 determines whether the ‘visual car’ and the ‘sound of the horn’ are generated by common (C=1) or
506 independent (C=2) sources (for details, see [18]). For common source, the ‘true’ audiovisual
507 location (S_{AV}) is drawn from one prior spatial distribution. For independent sources, the ‘true’
508 auditory (S_A) and ‘true’ visual (S_V) locations are drawn independently from this prior spatial
509 distribution. We introduce independent sensory noise to generate auditory (x_A) and visual (x_V)
510 inputs [18].

511 Middle: Bayesian Inference Model: During perceptual inference the observer is thought to compute
512 three sorts of estimates from the auditory and visual signals for spatial localization: 1. spatial
513 estimates under the assumption of common source (i.e., forced fusion estimate: $\widehat{S_{AV,C=1}}$) and
514 independent sources (i.e. full segregation estimates separately for auditory and visual locations:
515 $\widehat{S_{V,C=2}}, \widehat{S_{A,C=2}}$), 2. estimates of the causal structure and 3. the final auditory and visual Bayesian
516 Causal Inference spatial estimates based on model averaging that take into account the observer’s
517 causal uncertainty by marginalizing (i.e. integrating) over the different causal structures: $\widehat{S_V}, \widehat{S_A}$.
518 Each of those estimates is associated with uncertainties as indicated by the specified probability
519 distributions.

520 Right: Metacognition may be able to access and monitor the three sorts of estimates and their
521 uncertainty: 1. forced fusion and full segregation spatial estimates, 2. the inferred causal structure
522 and 3. the final auditory and visual Bayesian Causal Inference spatial estimates. Please note that this
523 image only serves illustrational purposes and does not indicate potential locations of neural
524 substrates of metacognition.

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526 **Figure 2**

527 **Perceptual and causal metamers in the audiovisual McGurk illusion**

528 Left: Observers are presented with non-conflicting audiovisual stimuli, i.e. a video of a face
529 articulating <<da>> and a voice uttering /da/. They will perceive the audiovisual signals as coming
530 from one source and integrate them into a [da] percept.

531 Right: Observers are presented with conflicting audiovisual stimuli, i.e., a video of a face
532 articulating <<ga>> and a voice uttering /ba/. In the McGurk illusion, they should perceive the
533 audiovisual signals as coming from one source and integrate them into a [da] percept, which would
534 be a causal and perceptual metamer to the estimates formed from the non-conflicting audiovisual
535 signals. However, perceptual and causal inference may also result in other outcomes. Observers
536 may potentially perceive a [da] and yet recognize the audiovisual conflict and hence infer that the
537 two signals come from independent sources (i.e. perceptual metamer but no causal metamer).

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540 **Figure I (Box 3)**

541 **Intentional binding, sense of agency and causal metacognition**

542 Observers have been shown to perceive the interval between an action and its sensory consequences
543 (e.g., a ‘beep’) of a certain duration that is temporally compressed, when the action was voluntary
544 and associated with a sense of agency – a phenomenon referred to as ‘intentional binding’ [72].
545 Causal metacognition may be closely related to the sense of agency by virtue of monitoring the
546 uncertainty about the causal relationship between one’s own voluntary actions and their sensory
547 consequences.

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