Superconducting super motor and generator

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Abstract—We have developed a new type of superconducting synchronous rotating machine whose self-induction is cancelled out, with the intention of achieving a very high power-to-weight ratio including the weight of the cooling system. Magnetic cores are used to direct the magnetic field from permanent magnets on the rotors onto superconducting wires on the stator, and the reaction of the Lorentz force is used to drive the rotors. Cancellation of self-induction in the cores enables the elimination of core-losses and magnetic saturation, permitting the core mass to be reduced significantly, and also reducing ac losses in the superconducting wires. In this work a prototype prepared using 100 m of second generation high temperature superconductor (2G-HTS) wire is described, and its characteristics are measured and compared with a numerical simulation. We conclude that electrical rotating machines with power-to-weight ratios comparable to jet engines could be developed with 2G-HTS wire.

Index Terms—High-temperature superconductor, motors, generators, rotating machines

I. INTRODUCTION

SINCE the discovery of Type II superconductors, especially niobium-tin, much effort has been devoted to large scale applications. Useful superconducting power devices have been developed [1], in particular for producing strong dc magnetic fields. As yet, however, ac losses in superconductors have made it difficult to create practical and useful fully superconducting rotating machines, and these losses are considered to limit their effectiveness. Perhaps the greatest advancements to date have been in the area of low rotation speed ship propulsion motors, where a power-to-weight ratio of about 0.5 kW/kg has been reported with a rotor wound from high temperature superconductor. This is an improvement by a factor of about five compared to a conventional motor, even though conventional copper air-core windings were employed on the stator, and a cryogenic cooling system, based on gaseous helium, is required [2], while several new designs and approaches are currently in progress [3, 4, 5].

It appears, however, that 2G-HTS wire [6, 7], which permits a high current density with strong magnetic fields, enables the development of rotating machines with very larger power-to-weight ratios. Consider, for example, a current of 100 A in 1,000 m of 2G-HTS wire under a magnetic field of 1 T: this will induce a Lorentz force of 100,000 N, and if this force were used in a rotating machine with a rotor diameter of 1 m rotating at a speed of 3,600 rpm, it would generate a power of about 19 MW. Assuming a copper/Hastelloy tape width of 4 mm and a thickness of 0.1 mm, the volume of the wire is only about 400 cm³ (for the superconductor itself, only 4 cm³), and the weight is less than 3.6 kg. This indicates a limiting power-to-weight ratio of 5,000 kW/kg, much higher than the 160 kW/kg achieved by the HPFTP turbopump in the Space Shuttle main engine [8].

Many practical problems remain of course: how to apply the magnetic field; how to convert the Lorentz force to torque; how to efficiently refrigerate the superconductor; the effects of self-inductance and ac losses in the superconducting wire, and so on. Here a novel design of superconducting rotating machine in which self-induction is cancelled out is proposed to address all these problems: in effect this design combines the advantages of iron and air cores while avoiding their disadvantages. Iron cores enable enhanced control of magnetic flux, allowing increased efficiency and reduced ac-losses, but they are heavy, have core losses and magnetic saturation problems. Air cores are light and do not suffer from losses or saturation, but lack the enhanced flux control. We call this machine a super motor/generator to distinguish it from conventional superconducting rotating machines. A first prototype has been constructed to demonstrate the operating principles, and magnetic field simulations have been made and compared with experimental data. These initial results suggest that super motors could be constructed with high efficiency and power-to-weight ratios comparable to jet engines used in aircraft.

II. STRUCTURE AND FEATURES OF THE SUPER MOTOR/GENERATOR

The structure of the prototype super motor/generator is schematically illustrated in Fig. 1. The two rotors and the
cancellation gives several remarkable features: the elimination of inductance enables a perfect power factor and high speed operation; prevention of magnetic saturation in the cores allows reduction of their weight; and ac losses in the superconductor due to the self-field are significantly reduced.

This cancellation is achieved by connecting the superconducting coils on the armature to each other as shown in Fig. 2 (b), so that the total induction generated in the cores by the currents in any coils is almost cancelled out through mutual-inductances. Assuming that the three inductors are equivalent, that is they have same self-inductance, $L_0$, the mutual-inductance will be $L_0\Delta L$, differing from the self-inductance only due to flux leakage, which is greatly reduced by the cores. The circuit equations can be written in matrix form as,

$$
\begin{pmatrix}
\Delta i_1 \\
\Delta i_2 \\
\Delta i_3
\end{pmatrix}
= 
\begin{pmatrix}
L_0 & L_0 - \Delta L & L_0 - \Delta L \\
L_0 - \Delta L & L_0 & L_0 - \Delta L \\
L_0 - \Delta L & L_0 - \Delta L & L_0
\end{pmatrix}
\begin{pmatrix}
\Delta i_1 \\
\Delta i_2 \\
\Delta i_3
\end{pmatrix}
+ 
\begin{pmatrix}
0 \\
\Delta L \\
0
\end{pmatrix}
\begin{pmatrix}
i_1 \\
i_2 \\
i_3
\end{pmatrix},
$$

where the second form can be obtained from the first as the currents sum to zero and so any constant can be added to the matrix. The effective inductance is then given by the leakage inductance, $\Delta L$, which is expected to be very small relative to the self-inductance for toroidal cores.

### III. THE SIMULATION

The magnetic field in the super motor has been calculated using finite element methods to estimate the torque and the power output which can be expected. In this simulation an equivalent cylindrical 2D model is used for convenience, instead of the actual 3D disk structure. Fig. 3 shows the magnetic fields for three-phase currents of amplitude 0, and 400 A, at zero degrees phase. It can be seen that the symmetry of magnetic field is broken as the current flow is increased. A torque acts on the permanent magnets as a reaction to the Lorentz force caused by the currents and the magnetic field, which can be represented as a Maxwell stress force.

Fig. 4 shows calculated torques and torque distortions as a function of current for three different core materials: silicon iron steel, ferrite, and air. Calculations for an eight-pole machine with 1km of superconducting wire are also shown in the Fig.. For air cores the torque is directly proportional to the current, but the clear curvature for iron and ferrite cores arises from magnetic saturation effects. The calculated torque distortions are also primarily caused by partial magnetic saturation. Note that the distortions for eight-pole machines are much less than those for four-pole as a result of the reduced distance between poles.

![Fig. 2. (a) Principle of torque generation in the super motor. (b) Schematic diagram of the armature coils. In the prototype each branch is wound as two separate coils of 90 turns each, on opposite sides of the stator and connected in series to give a six-pseudopole stator.](image)

![Fig. 3. Magnetic flux distribution in the axial type super motor for currents of 0 and 400 A, where 90 turns/section. The colour scale runs from 0 to 3 T.](image)

![Fig. 4. (a) Calculated torque and (b) distortion as a function of current for various machine models. The red curve (4 poles, 100 m, iron core) corresponds to the prototype described here.](image)
IV. EXPERIMENTAL RESULTS

A prototype was constructed and tested in our laboratory as shown in Fig. 5. The super motor/generator was connected to a conventional induction motor through a torque meter.

Power generation characteristics were measured with the super motor driven for a short time by a normal motor to eliminate temperature dependences (for example, the losses in the vacuum bearing depend strongly on the temperature of the ferrofluid and the superconducting armature). The open-circuit electromotive force and the voltage drop across an external 1 Ω load are shown in Fig. 6 (a) as a function of frequency. By fitting these results to the function \( a\omega R / \sqrt{R^2 + a^2\Omega^2} \), where \( \alpha \) is an amplitude, \( R = 1 \ Ω \) is the external load, \( \omega \) is angular frequency, and \( L \) is the residual inductance, the leakage inductance can be estimated at 2.2 mH. The measured result is four times larger than expected from simulations, perhaps because the superconducting wire is not wound neatly enough.

Fig. 6 (b) shows the generated output power (calculated from the voltage across the 1 Ω external load) and the consumed input power (determined using the torque meter) as a function of driving frequency. The sum of the open-circuit input power and the power output is consistent with the loaded input power, indicating that self-field ac losses in the superconducting wires are almost negligible, as expected due to the cancelation of self-induction. The good fits indicate that experimental torques, which can be calculated from the generated output power and the driving frequency, are almost proportional to current, as expected from the red curve in Fig. 4; we were unable to explore larger currents where significant curvature is expected to appear.

On open circuit most of the input power is consumed by friction in the ferrofluid vacuum bearing but ac-losses due to the rotating magnetic field are also included. These two components can be distinguished using a thermal method, as the ac-losses will be converted to heat in the stator, which is thermally isolated from the rest of the motor/generator assembly. Fig. 7 (a) shows how the temperature of the cold head changes as the driving speed was slowly changed between 300 rpm and zero, with the super generator on open circuit.

Thermal equilibrium cold head temperatures, \( \theta \), were estimated as averages of the final temperatures from the falling and rising curves, and are plotted in Fig. 7 (b). Since the whole coil, which has a transition temperature of 92 K, transits sharply to the superconducting state at cold head temperatures between 83 K and 85 K, we estimate that the temperature in the coil exceeds the cold head temperature by about 7 to 9 K. Assuming the Bean model, with the externally applied field much larger than the full penetration field so that the critical current is proportional to \( (T_c - \theta) \), the temperature below the critical temperature \( T_c \), the ac losses are given by \( Q(\theta) = a f (T_c - \theta) \) [9, 10], where \( f \) is the ac frequency in Hz. The cooling capacity of the cryocooler at constant input power is approximately linear near its limiting temperature \( \theta_0 \), and can be described by \( C(\theta) = b(\theta - \theta_0) \). Combining these two equations leads to a thermal equilibrium temperature, \( \theta_{eq}(f) = (fT_c + r\theta_0)/(f + r) \), where \( r = b/a \). This provides a good fit to the experimental data, as shown in Fig. 7 (b).

From this fit and the known value of \( b=0.31 \ W/K \) we obtain \( a=0.0713 \ W/Hz/K \), and so \( Q(77K)=1.07 \ W/Hz \). This value for the ac-losses is similar to a value of 1.24 W/Hz estimated from the experimental results of Amemiya et al. [11] assuming that the amplitude of the ac magnetic field is 0.276 T, estimated from the experimental torque.

Rotation experiments as a motor under light load were also performed with a driving circuit containing two current sources and one voltage source as shown in Fig. 8 (a), where...
the electromotive force generated on the coil from the inductance $L_c$ is cancelled by the voltage source. The instantaneous currents, electromotive force, and power when driving with the circuit in the figure (a). The speed is first increased in steps of approximately 

the cryocooler required to remove waste heat from the superconducting stator. We assume that the cryocooler requires a power equal to 15 times its cooling capacity, leading to a comprehensive efficiency of 69%.

This calculation shows the importance of minimising the remaining ac losses, which arise from the rotating magnetic field, to achieve the highest comprehensive efficiency. These are proportional to the width of superconductor perpendicular to the field. As the superconducting tape is very anisotropic, with a superconducting layer thickness of only 1 μm, these losses could in principle be reduced by a factor of thousands by winding the coil with the tape perpendicular to the stator rather than flat against it. Perfectly perpendicular winding is not practical, but it is possible to reduce the ac losses by a factor of $\sin(\alpha)$, where $\alpha$ is the average angle between the tape and the perpendicular to the stator.

In table I, the parameters for the prototype (#1) and design models (#2 to #4) of the super motor are summarized, where the wire lengths and widths, number of poles and operating temperatures are varied, and the ac-losses are estimated assuming that they are proportional to the critical current, wire length, frequency and the perpendicular component of the magnetic field. It can be seen that model #4 in Table I achieves a power-to-weight ratio comparable to jet engines. Reducing the operation temperature to 60 K would double the critical current, and thus the power-to-weight ratio, but the ac-losses also increase with critical current, and there is no efficiency advantage: indeed the comprehensive efficiency including power consumption in the cryocooler will get worse. A comprehensive power-to-weight ratio above 10 kW/kg, including the weight of the cryocoolers, would be possible if the transverse component of the magnetic field could be suppressed down to one-hundredth by optimizing both coil winding and magnetic structure.

**ACKNOWLEDGMENT**

The authors would like to thank undergraduate and graduate students of our laboratory for their contributions to the program, and Mr. Yukio Toda and Mr. Hajime Ikeda of the Toda Racing co., Ltd for supporting 3D modeling.

### Table I

<table>
<thead>
<tr>
<th>Parameters for the prototype and design models of the super motor model</th>
<th>Ucm</th>
<th>#1</th>
<th>#2</th>
<th>#3</th>
<th>#4</th>
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<tbody>
<tr>
<td>operation temp. (K)</td>
<td>27</td>
<td>77</td>
<td>77</td>
<td>77</td>
<td>60</td>
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<tr>
<td>number of poles</td>
<td>-</td>
<td>4</td>
<td>4</td>
<td>8</td>
<td>8</td>
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<tr>
<td>wire length (mm)</td>
<td>100</td>
<td>400</td>
<td>1000</td>
<td>1000</td>
<td>1000</td>
</tr>
<tr>
<td>rated speed (rpm)</td>
<td>3600</td>
<td>3600</td>
<td>3600</td>
<td>3600</td>
<td>3600</td>
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<tr>
<td>frequency (Hz)</td>
<td>120</td>
<td>120</td>
<td>240</td>
<td>240</td>
<td>240</td>
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<tr>
<td>rated phase current (A rms)</td>
<td>75</td>
<td>71</td>
<td>71</td>
<td>71</td>
<td>141</td>
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<tr>
<td>rated phase voltage (V rms)</td>
<td>82</td>
<td>260</td>
<td>894</td>
<td>740</td>
<td>551</td>
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<tr>
<td>rated torque (Nm)</td>
<td>23</td>
<td>146</td>
<td>503</td>
<td>833</td>
<td>1322</td>
</tr>
<tr>
<td>rated power output (W)</td>
<td>8,734</td>
<td>55,181</td>
<td>189,560</td>
<td>314,023</td>
<td>498,382</td>
</tr>
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<td>Power/weight (kW/kg)</td>
<td>0.29</td>
<td>1.34</td>
<td>6.32</td>
<td>10.47</td>
<td>16.81</td>
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<td>ac-losses (90%)</td>
<td>W</td>
<td>149</td>
<td>1,190</td>
<td>5,952</td>
<td>11,904</td>
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<tr>
<td>efficiency (90%)</td>
<td>%</td>
<td>98.3</td>
<td>97.8</td>
<td>96.9</td>
<td>96.2</td>
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<td>power cons. (90%)</td>
<td>W</td>
<td>2,232</td>
<td>17,856</td>
<td>89,280</td>
<td>178,560</td>
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<td>compreh. eff. (90%)</td>
<td>%</td>
<td>79.7</td>
<td>75.6</td>
<td>68.0</td>
<td>63.8</td>
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<td>ac-losses (5%)</td>
<td>W</td>
<td>13</td>
<td>104</td>
<td>519</td>
<td>1,038</td>
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<tr>
<td>efficiency (5%)</td>
<td>%</td>
<td>99.9</td>
<td>99.8</td>
<td>99.7</td>
<td>99.7</td>
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<tr>
<td>power cons. (5%)</td>
<td>W</td>
<td>195</td>
<td>1,556</td>
<td>7,781</td>
<td>15,563</td>
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<tr>
<td>compreh. eff. (5%)</td>
<td>%</td>
<td>97.8</td>
<td>97.3</td>
<td>96.1</td>
<td>95.5</td>
</tr>
</tbody>
</table>

*The comprehensive efficiencies include the power consumption of the cryocooler.

*The rated torque is estimated from simulation values divided by $\sqrt{2}$. 

Fig. 8. (a) Driving circuit for investigating motor operation. (b) The instantaneous currents, electromotive force, and power when driving with the circuit in the figure (a). The speed is first increased in steps of approximately 

V. CONCLUSIONS AND DISCUSSION

The simulations and experiments described above confirm that the prototype super motor/generator achieves the key features expected for this design. In particular the effective cancellation of inductance ensures that the ac losses are dominated by effects arising from the rotating magnetic field. The prototype achieves a power output of 2,400 W with ac losses of only 54 W at 1,500 rpm, for a nominal efficiency of 98%. This figure, however, excludes the energy consumption...
REFERENCES