

The faint source population at 15.7 GHz – I. The radio properties

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ABSTRACT

We have studied a sample of 296 faint (>0.5 mJy) radio sources selected from an area of the Tenth Cambridge (10C) survey at 15.7 GHz in the Lockman Hole. By matching this catalogue to several lower frequency surveys (e.g. including a deep GMRT survey at 610 MHz, a WSRT survey at 1.4 GHz, NVSS, FIRST and WENSS) we have investigated the radio spectral properties of the sources in this sample; all but 30 of the 10C sources are matched to one or more of these surveys. We have found a significant increase in the proportion of flat-spectrum sources at flux densities below ≈ 1 mJy – the median spectral index between 15.7 GHz and 610 MHz changes from 0.75 for flux densities greater than 1.5 mJy to 0.08 for flux densities less than 0.8 mJy. This suggests that a population of faint, flat-spectrum sources are emerging at flux densities $\lesssim 1$ mJy.

The spectral index distribution of this sample of sources selected at 15.7 GHz is compared to those of two samples selected at 1.4 GHz from FIRST and NVSS. We find that there is a significant flat-spectrum population present in the 10C sample which is missing from the samples selected at 1.4 GHz. The 10C sample is compared to a sample of sources selected from the SKADS Simulated Sky by Wilman et al. and we find that this simulation fails to reproduce the observed spectral index distribution and significantly underpredicts the number of sources in the faintest flux density bin. It is likely that the observed faint, flat-spectrum sources are a result of the cores of Fanaroff–Riley type I sources becoming dominant at high frequencies. These results highlight the importance of studying this faint, high-frequency population.

Key words: galaxies: active – galaxies: starburst – radio continuum: galaxies.

1 INTRODUCTION

The Tenth Cambridge Survey (10C; AMI Consortium: Davies et al. 2011; AMI Consortium: Franzen et al. 2011) at 15.7 GHz is the deepest high-frequency ($\gtrsim 10$ GHz) radio survey to date, complete to 1 mJy in 10 different fields covering a total of ≈ 27 deg². A further ≈ 12 deg², contained within these fields, is complete to 0.5 mJy. The 10C survey therefore enables us to study the faint source population at 15.7 GHz, a parameter space which has not been explored in any detail. Most studies of the sub-mJy population have focused on lower frequencies, due to the increased time required to survey a field to an equivalent depth at higher frequencies.

One area of particular interest has been the variation with flux density of the spectral index distribution for the samples selected at 15–20 GHz. For example, in the Ninth Cambridge Survey (9C; Waldram et al. 2003) the proportion of sources with flat or rising spectra decreased as the flux density decreased. The median spectral index between 15.2 and 1.4 GHz ($\alpha_{1.4}^{15.2}$) changed from 0.23 for the highest flux density bin ($S_{15\text{ GHz}} \geq 100$ mJy) to 0.79 for the lowest flux density bin ($5.5 \geq S_{15\text{ GHz}} > 25$ mJy). (The convention $S \propto \nu^{-\alpha}$, where S is flux density at frequency ν , is used throughout this work).

The Australia Telescope 20 GHz survey (AT20G; Massardi et al. 2011a) found a similar variation of spectral index with flux density for a sample with a flux density limit of 40 mJy. The 10C survey (AMI Consortium: Davies et al. 2011) enables us to extend these studies to lower flux densities. Although the study by AMI Consortium: Davies et al. (2011) contains a larger number of limits, it

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is clear that the fraction of flat-spectrum sources increases again as flux density decreases further.

There have been several attempts to model the high-frequency radio sky (de Zotti et al. 2005; Wilman et al. 2008; Wilman et al. 2010; Tucci et al. 2011). These simulations have extrapolated from lower frequency surveys, generally on the assumption that the sources have power-law synchrotron spectra. These models are an increasingly poor fit to the observed source counts below 10 mJy at 15 GHz. The number of sources is significantly underestimated, indicating that the properties of these sources are not well understood, largely due to the complexity and diversity of the high-frequency spectra of individual sources. To understand the nature of the faint, high-frequency population and constrain the models better, a multifrequency study is required. In this paper, we describe just such a study, examining the radio properties of a subsample of 10C sources in the Lockman Hole, a region which has been observed over a wide range of wavelengths.

The Lockman Hole is a region of the sky centred near $10^{\text{h}}45^{\text{m}}, +58^{\circ}$ (J2000 coordinates, which are used throughout this work) with exceptionally low H I column density (Lockman, Jahoda & McCammon 1986). The low infrared background (0.38 MJy sr^{-1} at $100 \mu\text{m}$; Lonsdale et al. 2003) in this area of the sky makes it ideal for infrared observations. As a result, as part of the Spitzer Wide-area Infrared Extragalactic (SWIRE; Lonsdale et al. 2003) survey sensitive infrared observations of $\approx 14 \text{ deg}^2$ of the Lockman Hole area have been made. The availability of deep infrared observations in the Lockman Hole has triggered deep observing campaigns at optical, X-ray and radio wavelengths.

The availability of data at such a wide range of frequencies makes the Lockman Hole a particularly good area for study. Here, the radio properties of sources detected in the 10C survey at 15.7 GHz in the Lockman Hole are investigated. The 10C data are combined with those from deep surveys at 610 MHz made with the Giant Meterwave Radio Telescope (GMRT; Garn et al. 2008, 2010) and at 1.4 GHz made with the Westerbork Synthesis Radio Telescope (WSRT; Guglielmino et al. 2012), along with other available data over a range of radio frequencies. The surveys used are described in more detail in Section 2 along with the process for matching them to the 10C catalogue. Section 3 describes how the parameters of the 10C sources are investigated using these surveys, including calculating the radio spectral indices and investigating the extent of the radio emission. The data are analysed and the properties of the 10C sources are discussed in Section 4. The 10C source population is compared to samples selected at 1.4 GHz in Section 5 and to the Wilman et al. (2008, 2010) simulated model of the radio sky in Section 6. Optical identifications, redshift estimates and detailed discussions of the source types will be presented in a separate paper.

Throughout this paper, the term ‘flat spectrum’ refers to an object with spectral index $\alpha \leq 0.5$ and ‘steep spectrum’ to an object with $\alpha > 0.5$.

2 SAMPLE SELECTION

2.1 Surveys used

The 10C radio survey at 15.7 GHz was made with the Arcminute Microkelvin Imager (AMI; Zwart et al. 2008) with a beam size of 30 arcsec. It covers $\approx 27 \text{ deg}^2$ complete to 1 mJy and $\approx 12 \text{ deg}^2$ complete to 0.5 mJy across 10 different fields; a full description of the 10C survey and the source catalogue can be found in AMI Consortium: Franzen et al. (2011) and AMI Consortium: Davies

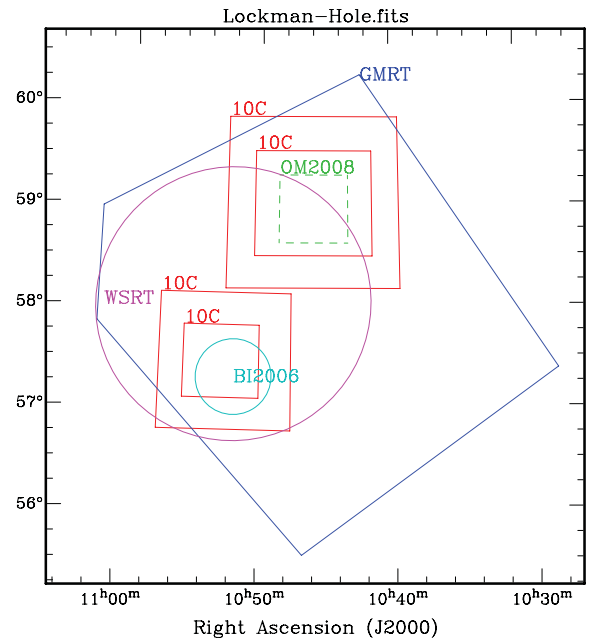


Figure 1. The deep radio surveys in the Lockman Hole region. The two larger (red) squares show the shallow region of the 10C survey fields, complete to 1 mJy. The two smaller squares contained within the larger squares are the deep 10C regions, complete to 0.5 mJy. The pentagon (dark blue) shows the GMRT survey area, the dashed square (green) shows the OM2008 survey area, the smaller circle (pale blue) shows the BI2006 survey area and the larger circle (pink) shows the WSRT survey area. The FIRST, NVSS and WENSS are not shown as they cover the whole region. See Table 1 for details of the different surveys shown.

et al. (2011). Two of the fields are in the Lockman Hole, covering an area of 4.64 deg^2 (see Fig. 1) and detecting a total of 299 sources.

To investigate the properties of these 10C sources, we have matched the 10C catalogue to other lower frequency, but usually higher resolution, radio catalogues as detailed below. This not only enables us to determine the radio spectral properties of the sources, but also allows us to investigate the extent and structure of the radio sources in more detail. The greater positional accuracy of these higher resolution catalogues is also vital for finding the counterparts of the 10C sources at optical and infrared wavelengths; the analysis of the optical and infrared properties of the 10C sources will be presented in a later paper. The other radio surveys of the Lockman Hole used in this work are listed in Table 1 and briefly described below.

A series of deep observations at 610 MHz made with the GMRT covers the whole 10C Lockman Hole area except for a small corner of the field containing five 10C sources (Fig. 1). The GMRT image has an rms noise of $\approx 60 \mu\text{Jy beam}^{-1}$ in the central area (see Garn et al. 2008, 2010, for details of the data reduction and source extraction). This deep image and the catalogue derived from it are used here.

A deep survey at 1.4 GHz carried out with the WSRT overlaps a large portion of the 10C survey (Fig. 1) in the Lockman Hole (Guglielmino et al. 2012). The rms noise in the centre of the map is $\approx 11 \mu\text{Jy}$; this map and the associated source catalogue are used in this study.

We also make use of several other catalogues and surveys covering the Lockman Hole region. The Faint Images of the Radio Sky at Twenty cm (FIRST; White et al. 1997), NRAO VLA Sky Survey (NVSS; Condon et al. 1998) and Westerbork Northern Sky Survey

Table 1. Radio catalogues in the Lockman Hole.

Catalogue	Reference(s)	Epoch of observation	Frequency (GHz)	Beam size (arcsec)	rms noise (mJy)	Area covered (deg ²)
10C – shallow	AMI Consortium: Franzen et al. (2011)	2008 August–2010 June	15.7	30	0.1	4.64 (deep areas included)
10C – deep	AMI Consortium: Davies et al. (2011)	2008 August–2010 June	15.7	30	0.05	1.73
GMRT	AMI Consortium: Franzen et al. (2011)	2008 August–2010 June	15.7	30	0.05	1.73
	AMI Consortium: Davies et al. (2011)	2008 August–2010 June	15.7	30	0.05	1.73
	Garn et al. (2008)	2004 July–2006 October	0.610	6 × 5	0.06	13
	Garn et al. (2010)	2004 July–2006 October	0.610	6 × 5	0.06	13
WSRT	Guglielmino et al. (2012)	2006 December–2007 June	1.4	11 × 9	0.011	6.6
OM2008	Owen & Morrison (2008)	2001 December–2004 January	1.4	1.6	0.0027	0.011
OMK2009	Owen et al. (2009)	2006 February–2007 January	0.324	6	0.07	3.14
BI2006	Biggs & Ivison (2006)	2001 January–2002 March	1.4	1.3	0.0046	0.089
FIRST	White et al. (1997)	1997–2002	1.4	5	0.15	Whole area
NVSS	Condon et al. (1998)	1997	1.4	45	0.45	Whole area
WENSS	Rengelink et al. (1997)	1991–1996	0.325	54	3.6	Whole area

(WENSS; Rengelink et al. 1997) cover the whole area. There are also several deep observations made with the VLA within the Lockman Hole area: Owen et al. (2009) at 324 MHz (OMK2009) and Biggs & Ivison (2006) and Owen & Morrison (2008) at 1.4 GHz (BI2006 and OM2008). The locations of these surveys are shown in Fig. 1 and are summarized in Table 1.

16 10C sources in the Lockman Hole are labelled in the 10C catalogue as part of a ‘group’ (see AMI Consortium: Davies et al. 2011 for details) – in this case consisting of eight pairs. Contour maps of these eight pairs were examined by eye, along with images of their counterparts in the FIRST and/or GMRT. For three of these pairs, there is evidence of structure connecting the two components, so it was decided to combine the two components into one source (an example of one such source is shown in Fig. 2). The position listed

in the catalogue for these three pairs is the point mid-way between the two components. For the remaining five pairs the components were left as separate sources. This leaves a total of 296 sources in the 10C sample.

These 296 sources, selected at 15.7 GHz, are the subject of this paper. A subsample of 89 sources, with flux densities greater than 0.5 mJy, selected from the region complete to 0.5 mJy is defined as ‘Sample A’. A second subsample of 118 sources, ‘Sample B’, which has some overlap with Sample A, forms a sample complete to 1 mJy. 62 10C sources, 43 of which form a sample complete to 0.5 mJy at 15.7 GHz, are in the deep areas observed with the VLA at 1.4 GHz by Biggs & Ivison (2006) and Owen & Morrison (2008) (BI2006 and OM2008, respectively). All 62 sources are detected at 1.4 GHz so spectral information is available for all of them. They therefore form a particularly useful subsample, defined as Sample C. Table 2 contains a summary of the different subsamples used in this paper.

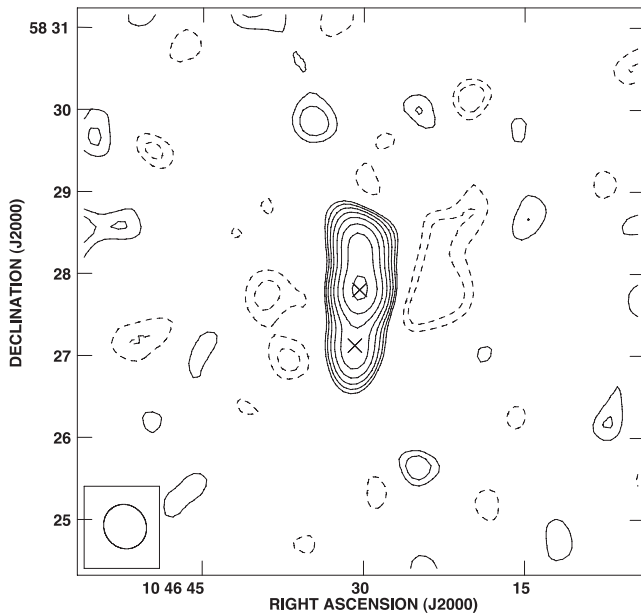


Figure 2. 15.7-GHz image of an example extended source listed as two components in the 10C catalogue. The contours are plotted at $(\pm 2\sqrt{n}) \times 0.136$ mJy. The crosses mark the positions of the two sources in the 10C catalogue. There are three such pairs of sources in the 10C Lockman Hole fields; in each case, the flux densities of the separate components are combined.

2.2 Matching the radio catalogues

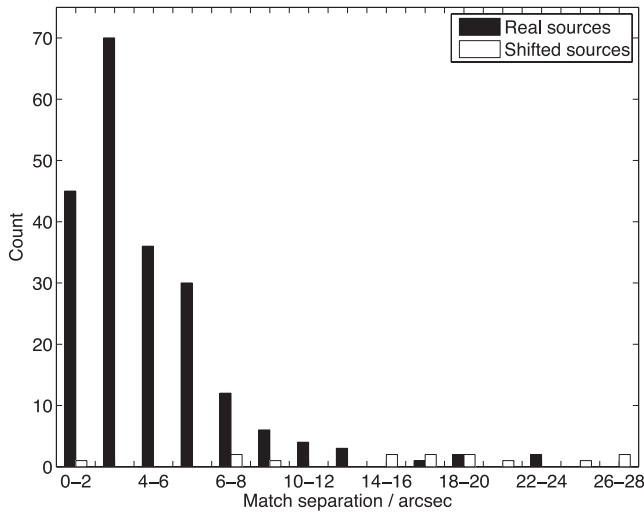
2.2.1 Choosing a match radius

The TOPCAT software package¹ was used to match the catalogues. The match radius was chosen so as to maximize the number of real associations and avoid false matches. The error in the 10C positions is ≈ 6 arcsec, which is larger than the errors in the other catalogues used here (e.g. the error in the GMRT positions is $\lesssim 1$ arcsec), so the errors in the 10C positions tend to dominate. Here we describe the process by which we chose a suitable match radius and assessed the probability of genuine and random matches for the 10C and GMRT catalogues. To create a random distribution of sources, the 10C sources were shifted by 5 arcmin in declination. Both this shifted catalogue and the true 10C catalogue were then matched to the GMRT catalogue and the angular separation between a shifted or true 10C source and its nearest GMRT source was recorded. Once a shifted or true 10C source was matched to a source in the GMRT catalogue, no further matches were sought for that source. The matches were then binned according to their separation for both the true and shifted sources. The resulting distribution is shown in Fig. 3. It can be seen that beyond 15 arcsec the numbers of random matches become comparable for both the

¹ See <http://www.starlink.ac.uk/topcat/>

Table 2. The different subsamples in the Lockman Hole used in this paper.

Sample	Description	Number of sources
All sources	All sources detected at 15.7 GHz (including sources below 0.5 mJy)	296
Sample A	Complete to 0.5 mJy at 15.7 GHz	89
Sample B	Complete to 1.0 mJy at 15.7 GHz	118
Sample C	All sources in the deep regions surveyed at 1.4 GHz with the VLA by Owen & Morrison (2008) and Biggs & Ivison (2006). This sample contains sources below the completeness limit at 15.7 GHz.	62

**Figure 3.** The number of matches with a given separation between the 10C and GMRT catalogues for the true and shifted distributions of 10C sources. Beyond 15 arcsec the number of true and shifted matches becomes comparable so 15 arcsec is chosen as the match radius.

true and shifted catalogues; thus, 15 arcsec was chosen as the match radius. The number of matches with the shifted distribution within a separation of 15 arcsec is 4 (out of 296 sources), meaning the probability of a random match within 15 arcsec is ≈ 1.5 per cent of the total number of sources being matched. 15 arcsec corresponds to 2.5σ , where σ is the typical error in the 10C source positions, suggesting that the matching is limited by the error in the 10C source positions.

This process was repeated for the other catalogues and it was decided that 15 arcsec was a suitable match radius to use when matching each of the catalogues to the 10C catalogue. The number of random matches within 15 arcsec for each catalogue is shown in Table 3.

2.2.2 Results of the matching

A summary of the matching between the 10C sources and the other radio catalogues is shown in Table 3. In total, 266 out of the 296 10C sources are detected at at least one other wavelength. Table 4 summarizes the number of sources with matches in more than one other catalogue.

For the 30 10C sources with no other detections, upper limits on the flux density at 610 MHz from the GMRT and at 1.4 GHz from the WSRT and FIRST can be used, as described in Section 3.1. All of the 10C sources with no other detections have a low flux density (see Fig. 4), with the majority below 1 mJy and all below 2 mJy.

Table 3. A summary of the matching between the 10C catalogue and other radio catalogues in the Lockman Hole. Column (2) shows the number of matches to 10C sources within 15 arcsec and column (3) shows the number of 10C sources in the survey area. Column (4) shows the number of random matches within 15 arcsec, i.e. the number of matches to the shifted 10C sources.

Catalogue	Number of matches	Number of 10C sources	Number of random matches
(1)	(2)	(3)	(4)
GMRT	205	291	8
WSRT	160	182	10
FIRST	196	296	0
NVSS	166	296	0
WENSS	86	296	6
OM2008	27	27	2
OMK2009	116	156	2
BI2006	35	35	3

Table 4. A summary of the number of 10C sources with multifrequency matches.

Number of matches	Number of sources
10C only	30
One match only	46
Two matches	36
Three matches	27
Four matches	55
Five matches	78
Six matches	23
Seven matches	1

3 DERIVING THE SOURCE PARAMETERS

3.1 Flux density values

3.1.1 GMRT

The large difference in resolution between the 10C (beam size 30 arcsec) and GMRT (beam size 6 arcsec) observations means that care must be taken when comparing flux densities. As illustrated in Fig. 5, many 10C sources are extended or resolved into multiple components at 610 MHz. The components of such sources will be listed as separate entries in the GMRT catalogue. In addition, for some of the sources in the GMRT catalogue there may be extended low brightness structure too faint to be seen in the high-resolution images. In order to reduce these problems, contour plots of all the GMRT sources which matched to a source in the 10C catalogue (using a 15 arcsec match radius as described in Section 2.2.1) were examined by eye. For the 50 sources which appeared multiple or

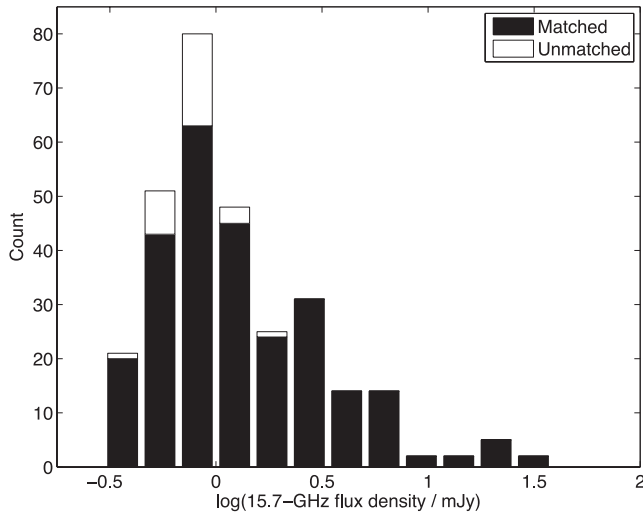


Figure 4. The distribution of 10C sources with and without associations in the other radio catalogues as a function of flux density. This diagram contains all 296 sources detected, some of which are below the completeness levels of the 10C survey. All of the 10C sources with no matches have a flux density below 2 mJy.

extended, the GMRT images were convolved in AIPS² to a 30-arcsec Gaussian to create an image of comparable resolution to the 10C data (see Fig. 5). The total 610-MHz flux density of each source (which had already been matched to a 10C source from the higher resolution image) was then estimated from the smoothed GMRT image. The integrated 610-MHz flux densities were estimated by fitting a Gaussian using the AIPS task JMFIT. In the few cases where JMFIT did not converge (due to the presence of another bright source in the subimage) the integrated flux density was found by hand using the AIPS task TVSTAT.

For the 84 10C sources for which a counterpart was not present in the full resolution GMRT catalogue, the GMRT images were used to place an upper limit on the source flux density at 610 MHz. A subimage of 2.5 arcmin was extracted and smoothed (as described above) to check for any large-scale structure which might have been resolved out in the original image. In eight cases, a source could be seen in the smoothed GMRT images with a peak within 15 arcsec of the 10C source position; for these sources, a value for the integrated flux density was obtained manually using TVSTAT. For the remaining sources, the upper limit on the flux density was taken to be three times the noise in this smoothed image. It was not possible to get any information about the flux density at 610 MHz for the five 10C sources outside the GMRT area so these sources are excluded from all discussions relating to 610-MHz data.

3.1.2 NVSS

NVSS has a resolution comparable to the 10C survey so the flux densities can be directly compared without any problems caused by resolution differences. Because of this, it is useful to be able to calculate spectral indices using NVSS and 10C values only, so upper limits were found for all sources not matched in the NVSS catalogue despite the fact that some of these sources have a counterpart in one of the deeper 1.4-GHz surveys used. NVSS images of all 10C sources without a match in the NVSS catalogue were examined to

see if there was a source present which was below the catalogue limit and for the few sources where this was the case, the flux density of the NVSS source was found manually using the AIPS task TVSTAT. For the remaining unmatched sources, an upper limit of three times the local noise in the NVSS image was placed on the flux density.

3.1.3 WSRT and FIRST

As the WSRT synthesized beam (12 arcsec) is smaller than the 10C synthesized beam (30 arcsec), several sources were resolved into multiple components in the WSRT catalogue but appeared as a single component in the 10C catalogue. In order to reduce the effects of resolution when comparing the flux densities, subimages of the WSRT image at the position of each 10C source were examined by eye; for those sources where there were multiple WSRT components associated with one 10C source, the flux densities of the WSRT components were added together. (In fact, in all cases except one, the WSRT sources in question were listed as a multicomponent source in the WSRT catalogue and the total flux density from the catalogue was used). This process was also carried out for FIRST sources.

For those 10C sources in the WSRT survey area without a match to the WSRT catalogue, the WSRT image was examined to see if there was a source present which was below the catalogue limit. This was not the case for any of the unmatched 10C sources in the WSRT area. The upper limit of flux density was taken to be three times the local noise in the WSRT image. For the 28 sources which were unmatched at 1.4 GHz and outside the WSRT area, an upper limit of 1 mJy was placed on the flux density because this is the FIRST completeness limit and these sources are all within the FIRST survey area but not detected.

3.1.4 OM2008 and BI2006

The two deep 1.4-GHz surveys made with the VLA (OM2008 and BI2006) have very small synthesized beams (≈ 1.5 arcsec) compared to the 10C survey. As images are not available for these surveys, the flux density values from the catalogues were used. OM2008 does account for the fact that some of the sources may be extended when calculating flux densities. They convolve the full resolution images to an effective beam size of 3, 6 and 12 arcsec and compare the flux densities derived from the four images. BI2006 does not attempt to account for extended sources when calculating the flux densities; however, there is only one 10C source which has a counterpart in BI2006 and not in any other 1.4-GHz catalogue so this will not significantly affect these results.

3.2 The effects of variability

The different surveys used in this paper were not carried out simultaneously so it is important to consider the possible effects of variability on the observed spectral index distributions. The epoch of observation for each survey is shown in Table 1. The time interval between the 15-GHz and the 610-MHz observations is in the region of 4–6 yr and between the 15- and 1.4-GHz observations 5–10 yr.

Whilst there are currently no data on the variability of sources at 15 GHz at the low flux density end of our sample, there have been some systematic studies at higher flux densities. Bolton et al. (2006) studied the 15-GHz variability of 51 9C sources with flux densities > 25 mJy over a 3-yr period. They found that while there was

² Astronomical Image Processing System, see <http://www.aips.nrao.edu/>.

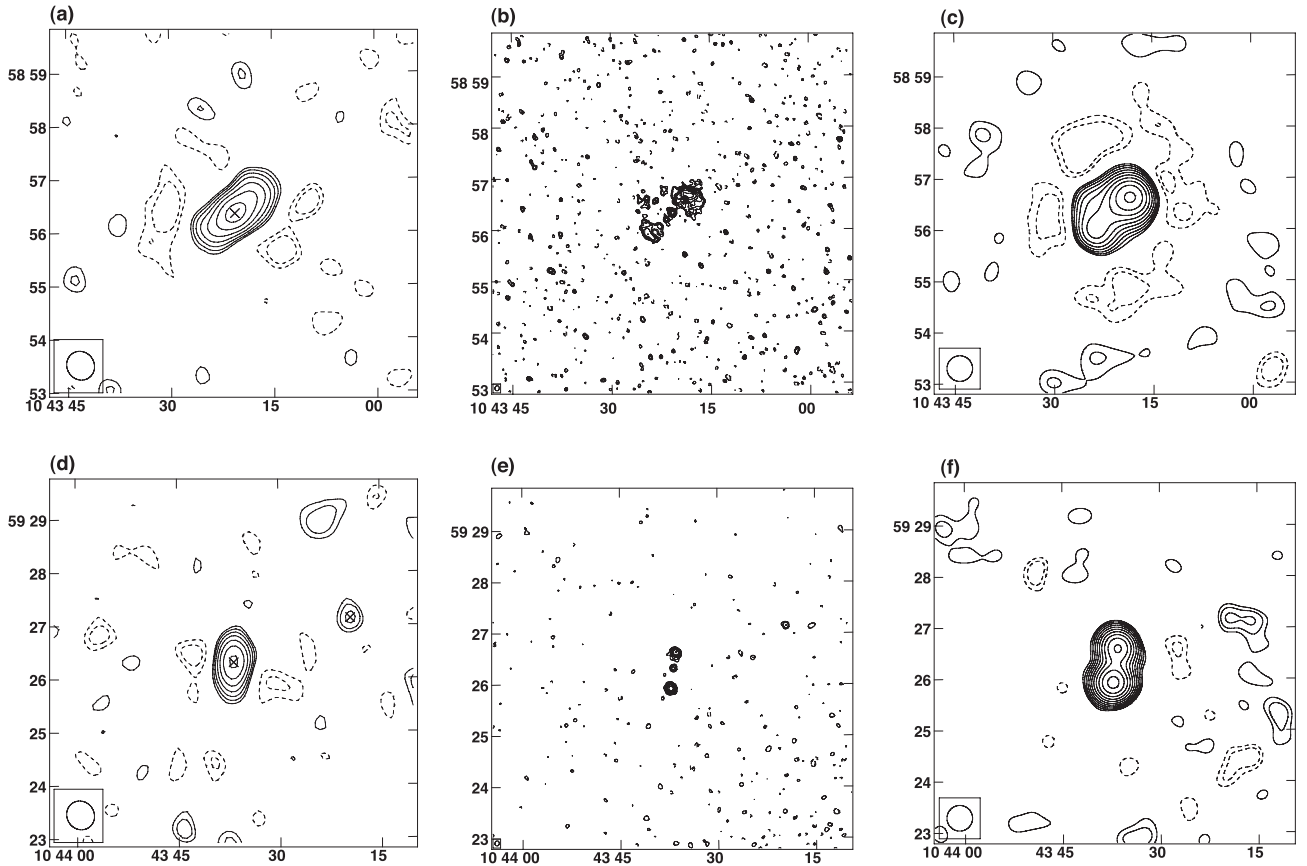


Figure 5. The difference in resolution between the AMI Large Array (used for the 10C survey) and GMRT. Panels (a) and (d) each shows a source imaged with AMI, panels (b) and (e) show the same sources imaged with GMRT. In both cases, several sources in the GMRT catalogue correspond to one source in the 10C catalogue, so care must be taken when comparing the catalogues. In panels (c) and (f) the GMRT images have been smoothed to create an image with a resolution comparable to the 10C images. This allows for a more direct comparison between the two surveys. The contours are drawn at $(\pm 2\sqrt{2^n}, n = 0, 1, \dots, 7) \times x$ mJy, where $x = 0.074$ for panel (a), 0.1 for panel (b), 0.3 for panel (c), 0.086 for panel (d), 0.16 for panel (e) and 0.3 for panel (f).

no evidence for variability (above the ~ 6 per cent flux calibration uncertainties) in steep-spectrum sources, half of the flat-spectrum objects were variable. In total, 29 per cent of the sources studied were found to vary. Sadler et al. (2006) observed 173 20-GHz sources with flux densities > 100 mJy over a 2-yr period and found that 42 per cent varied by more than 10 per cent. However, they found no correlation between variability and radio spectral index. More recently, Bonavera et al. (2011) investigated the variability of 159 sources with 20-GHz flux densities > 200 mJy and found the variability to be slightly larger than that found by Sadler et al., with an rms amplitude of 38 per cent at 20 GHz on a time-scale of a few years. Bonavera et al. note that there is some indication that the variability decreases as flux density decreases. Massardi et al. (2011b) studied the variability of a brighter sample ($S_{20\text{ GHz}} > 500$ mJy) at 20 GHz and found similar levels of variability to Sadler et al. At higher flux densities still Franzen et al. (2009) have looked at variability at 16 GHz in a complete sample of 97 sources with flux densities > 1 Jy over time-scales of about 1.5 yr. They found that 15 per cent of the sources vary by more than 20 per cent; however, in contrast to the results of Sadler et al. but in agreement with those of Bolton et al., the spectra of the variable sources are flatter than those of the non-variable ones.

The variability properties of the population studied here are not known. However, on the assumption that the faint sources in the 10C sample exhibit the same sort of flux density variations as shown

in the higher flux density samples discussed above, a significant fraction of them are likely to have varied over the period between the observations. Thus, the spectral indices of individual objects may be unreliable. However, given that the sources are probably equally likely to increase or decrease in flux density, this should not have a major effect on the overall spectral index distribution.

3.3 Spectral indices

To investigate the spectral properties of the source sample in a quantitative way, the spectral index was calculated between 15.7 GHz and 1.4 GHz ($\alpha_{1.4}^{15.7}$), and 15.7 GHz and 610 MHz ($\alpha_{0.61}^{15.7}$) for each source. For $\alpha_{1.4}^{15.7}$ all 296 sources are studied and for $\alpha_{0.61}^{15.7}$ the five sources outside the GMRT area are excluded as there is no 610-MHz flux density information available. For the sources with no match in the GMRT, a limiting spectral index was calculated from the upper limit placed on the flux density from the GMRT image, as described in Section 3.1.1.

The distributions of $\alpha_{1.4}^{15.7}$ were investigated in two ways, using slightly different procedures, to check the effects of resolution on the data. The first, $\alpha_{1.4}^{15.7} M$, makes use of all of the 1.4-GHz data available; for the sources where there is more than one 1.4-GHz flux density, flux densities are chosen according to resolution in the following order of preference: NVSS, WSRT, OM2008, FIRST, BI2006; FIRST and BI2006 are the last as they are the most likely

to resolve out some of the flux of the 10C sources because of their small beam sizes (5 and 1.5 arcsec, respectively). OM2008 also has a small beam (1.6 arcsec) but the sources have been convolved with Gaussians of varying radius to try and overcome the resolution problem. NVSS and WSRT have larger beam sizes (30 and 12 arcsec, respectively) which are more comparable to the 10C beam. For the sources with no match in any of the 1.4-GHz catalogues which are in the WSRT survey area, the upper limit from the WSRT image (as described in Section 3.1.3) is used to calculate a limiting spectral index. For the remaining sources, an upper limit of 1 mJy from the FIRST survey is used.

The second value, $\alpha_{1.4}^{15.7} N$, only uses values from the NVSS catalogue as this has a resolution comparable to the 10C survey. For the 10C sources which do not appear in the NVSS, the limit is derived from the NVSS image (see Section 3.1.2). These values of the spectral index contain a larger number of upper limits but provide a useful comparison when considering the effects of resolution.

Possible effects of variability on the spectral indices are discussed in Section 3.2.

3.4 Extent of the radio emission

To determine in a quantitative manner whether a source is extended or not, a compactness ratio R is often used. This is usually taken as the ratio of the integrated or total flux density of a source S_{int} and its peak flux density on a map S_{peak} , that is, $R = S_{\text{int}}/S_{\text{peak}}$. For the 10C sample considered here we do not use the 10C observations to find R because the large beam size of ≈ 30 arcsec means that the majority of the sources are unresolved. Instead, we use the matched data from the lower frequency catalogues, which have smaller beam sizes and can therefore provide more information about the angular size of a source. Four values of R are calculated, using data from the GMRT, FIRST and OMK2009 (324-MHz VLA observations) catalogues, which all have beam sizes ≈ 6 arcsec, and the WSRT catalogue which has a beam size of 12 arcsec. The deep 1.4-GHz VLA observations (OM2008 and BI2006) are not used in this analysis because their beam sizes are considerably smaller (≈ 1 arcsec) so that the data are not comparable with those from the other catalogues used here.

To take account of the effects of noise, several other studies (e.g. Prandoni et al. 2006; Bondi et al. 2007) plot R against the signal-to-noise ratio and fit a lower envelope to the data; reflecting this about $R = 1$ gives a curve which provides the cut-off between the extended and compact sources. We have not used this method for the sample of sources in this paper due both to the relatively small number of sources in the sample and to the range of different surveys used. Instead, each source was examined by eye and the criteria described below were decided upon to identify the extended sources.

At lower signal-to-noise ratios, the errors in the R values become larger, due to the larger errors in the integrated and peak flux density values. This is evident in Fig. 6 for the GMRT data, where the number of sources with values of $R < 1$, which must be due to errors in the flux density values, increases at lower signal-to-noise ratios. Therefore, different criteria are used to identify the extended sources at high and low signal-to-noise ratio. Sources were classified as extended if they had a signal-to-noise ratio greater than 20 in the GMRT data and values of $R > 1.35$ in at least two of the data sets used, or a value of $R > 2$ in at least one of the data sets. Sources with a signal-to-noise ratio less than 20 in the GMRT data were classified as extended if the value of R was greater than 2 in any of the data sets. A comparison of two of the R values used is shown

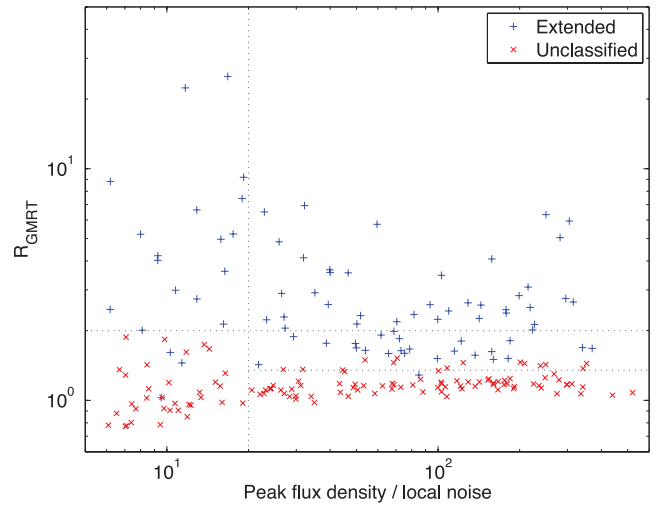


Figure 6. Compactness ratio calculated using GMRT data, R_{GMRT} , against the signal-to-noise ratio from the GMRT catalogue. The vertical line shows the divide at peak flux density/noise = 20 and the horizontal lines at $R = 1.35$ and 2.00 indicate the cut-offs in R used when classifying the extended sources (see text for details).

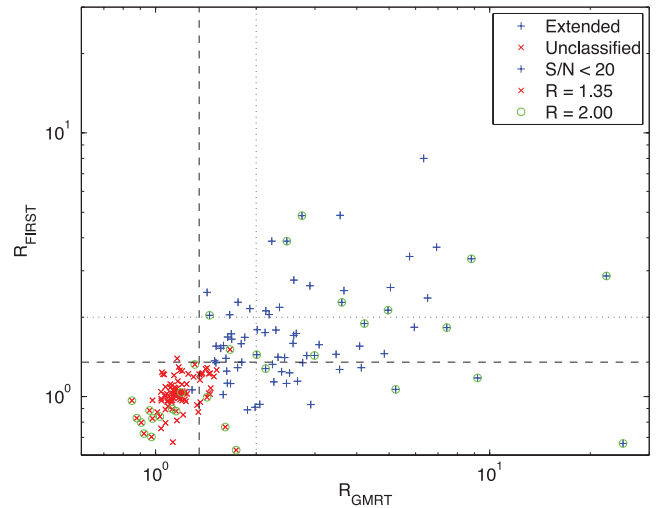


Figure 7. Value of the compactness ratio, R , calculated using FIRST and GMRT data. The horizontal and vertical lines indicate the values used when identifying the extended sources (see text for details). Sources classified as extended and those not classified are shown separately. Sources with a signal-to-noise ratio < 20 in the GMRT data are indicated with a green circle.

in Fig. 7. For most sources the two values are similar and some of the largest variations are for those sources with low signal-to-noise values, which is expected because the errors in the integrated flux densities are larger for the fainter sources.

We are confident that all the sources which fulfil these criteria are extended; however, as we have erred on the side of caution, there will be some sources which have not been classified as extended but do in fact have extended emission on the scale investigated here. In particular, sources which only have a value of R from the WSRT catalogue are not classified as extended as the WSRT beam is larger than that of the other catalogues used here. For this reason, those sources which are not classified as extended are placed in the ‘unclassified’ bin. The 36 sources which do not have a counterpart in any of the four catalogues used here are classified

as ‘no information’. The criteria used to select the extended sources here are roughly equivalent to selecting sources with angular sizes larger than ≈ 6 arcsec.

A catalogue containing the flux density, spectral index and R values will be available online at <http://cdsweb.u-strasbg.fr>.

4 SAMPLE ANALYSIS

4.1 Radio spectral properties

Some example radio spectra are shown in Fig. 8, demonstrating the different spectral types observed. Spectral indices are calculated for all sources, as described in Section 3.3. The spectral index $\alpha_{1.4}^{15.7} M$ against 15.7-GHz flux density for all sources is shown in Fig. 9. It is clear from this plot that there is a greater proportion of flat-spectrum sources at lower flux densities. This trend is further investigated by calculating the median spectral indices $\alpha_{0.61}^{15.7}$ and $\alpha_{1.4}^{15.7} M$ in three different flux density bins containing equal numbers of sources and the results are shown in Tables 5 and 6. Upper limits are included by using the *ASURV* Revised v1.2 package which implements the survival analysis methods presented in Feigelson & Nelson (1985). The distributions of both $\alpha_{0.61}^{15.7}$ and $\alpha_{1.4}^{15.7} M$ as a function of 15.7-GHz flux density show a sharp change at flux densities between 1 and 2 mJy. The spectral index distributions for these three flux density bins for both $\alpha_{0.61}^{15.7}$ and $\alpha_{1.4}^{15.7} M$ are shown in Fig. 10 and are very similar. There is a distinct peak at $\alpha \sim 0.7$ in the highest flux density bin (S_{high}). As flux density decreases the peak broadens as the contribution from flat-spectrum sources becomes much more significant. In the lowest flux density bin (S_{low}), the sources display a wide range of spectral index values, with a broad peak at $\alpha \sim 0.3$. The sources shown in white are upper limits and could only move to the left-hand side in these plots, making the S_{low} distribution even more different from the S_{high} distribution.

This is illustrated in Fig. 11 which shows the median $\alpha_{0.61}^{15.7}$, $\alpha_{1.4}^{15.7} M$ and $\alpha_{1.4}^{15.7} N$ and the percentage of sources with $\alpha > 0.5$ in narrower 15.7-GHz flux density bins – there is a far higher proportion of flat-spectrum sources at lower flux densities. The values for $\alpha_{1.4}^{15.7} N$ (using NVSS flux densities only) are very similar to those for $\alpha_{1.4}^{15.7} M$, except in the lowest flux density bin which is dominated by upper limits in the NVSS-only case. This implies that resolution differences between 10C and the other surveys is not having a major effect on the derived spectral indices. The same plots for the complete samples A and B are shown in Fig. 12. There are fewer sources in this sample so the uncertainties are larger but the general trend towards decreasing spectral indices below ≈ 2 mJy remains the same.

A plot of $\alpha_{1.4}^{15.7} M$ against $\alpha_{0.61}^{15.7}$ and for all sources is shown in Fig. 13. There is a good correlation between the two values of spectral index. The majority of the points in the bottom left-hand corner which deviate from the correlation are upper limits and therefore could move closer to the one-to-one correlation line shown. Of the points which are not upper limits, slightly more lie above the one-to-one correlation line than below it, indicating a slight spectral steepening at higher frequencies.

Possible effects of variability are discussed in Section 3.2. The variability properties of the population studied here are not known, but it seems likely that, if anything, variability would increase the proportion of steep-spectrum sources rather than producing the decrease observed. It is possible, for example, that variability in some of the genuinely flat spectrum sources over the epochs covered by the surveys used here could make them appear to have steep spectra. On the other hand, the genuinely steep spectrum sources

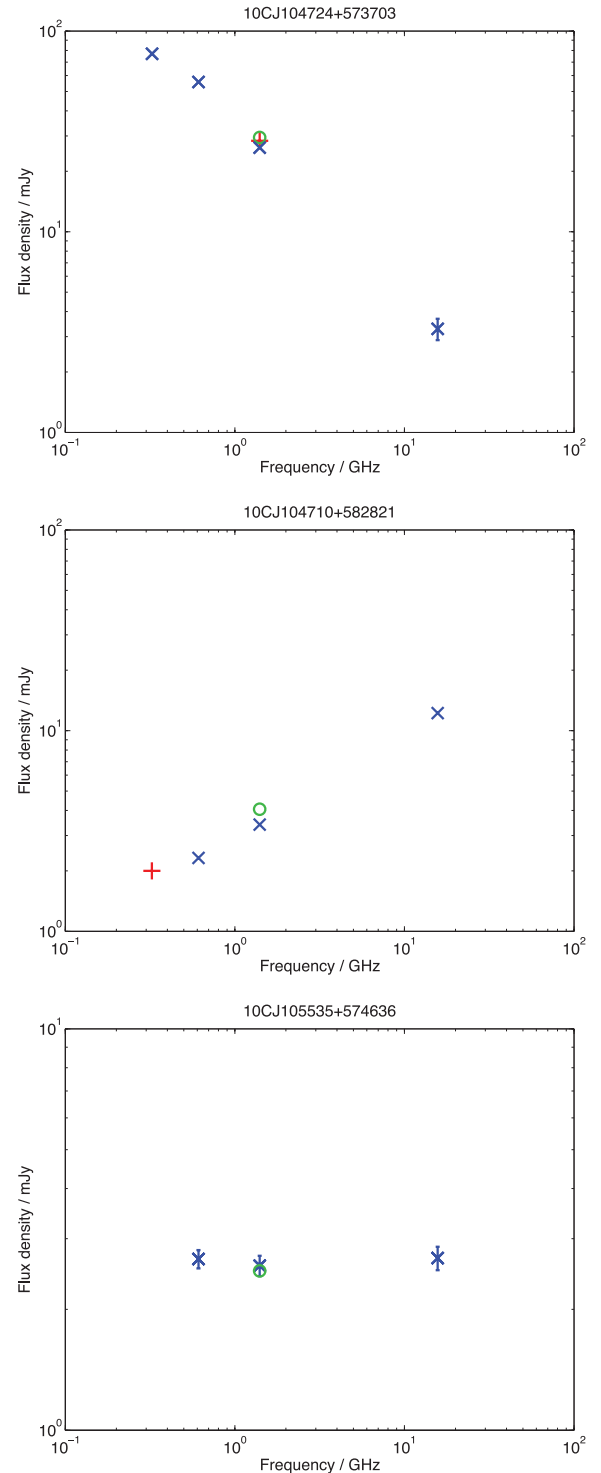


Figure 8. Example spectra. 10C J104724+573703 is an example of a steep-spectrum object, 10C J104710+582821 is a rising spectrum object and 10C J105535+574636 is an example of a flat-spectrum object. The blue cross at 324 MHz (if present) is from the WENSS, the red plus at 324 MHz is from OMK2009 and the value at 610 MHz is from the GMRT. The blue cross at 1.4 GHz is from the FIRST, the green circle is from the WSRT and the red plus is from the NVSS. The value at 15.7 GHz is from 10C. Error bars are not shown when they are smaller than the symbol plotted.

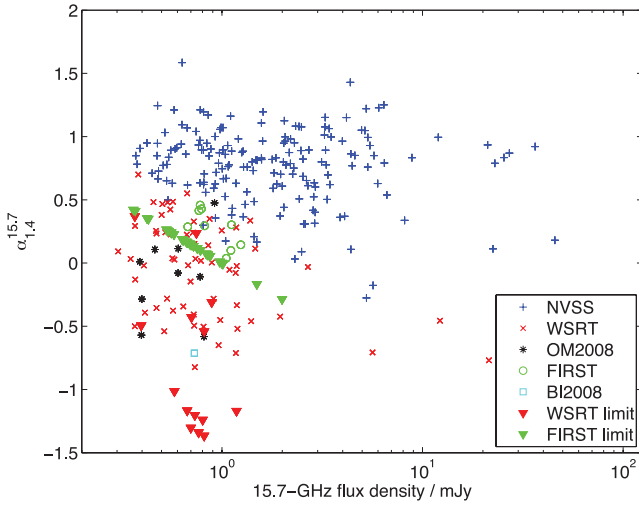


Figure 9. The spectral index $\alpha_{1.4}^{15.7}$ against 15.7-GHz flux density, showing which catalogue the 1.4-GHz flux density values come from.

in our faint sample are unlikely to be variable (unless their properties differ markedly from the steep-spectrum sources at higher flux densities) so their spectral indices will not be affected at all.

4.2 Comparison with other spectral index studies

The variation in spectral index with flux density at higher (~ 10 mJy–1 Jy) flux densities has been investigated by WalDRAM et al. (2010) and Massardi et al. (2011a). WalDRAM et al. and Massardi et al. used samples selected at 15 and 20 GHz, respectively, and, by matching them to catalogues at 1.4 GHz, found that the median spectral index becomes rapidly larger with decreasing flux density; for example, WalDRAM et al. found that the median $\alpha_{1.4}^{15}$ changed from around 0 at 1 Jy to 0.8 at 10 mJy. Our study of 10C sources shows that as the flux density decreases further the median spectral index drops again, with the median $\alpha_{1.4}^{15}$ decreasing from around 0.8 for flux densities > 1.5 mJy to around 0.1 at 0.5 mJy. As discussed in Section 4.1, the change occurs fairly abruptly at ≈ 1 mJy, indicating that the nature of the 15-GHz source population is changing at this flux density. The relationship between spectral index and flux density is summarized in Fig. 14 which shows the WalDRAM et al. results from 9C along with the results from this study.

We have shown here that the spectral index distribution changes dramatically below ~ 1 mJy for a sample of sources selected at

15.7 GHz. A similar trend has been found by other studies at slightly lower frequencies. For example, Prandoni et al. (2006) studied a complete sample of 131 sources detected at 5 and 1.4 GHz with a comparable flux density range to the sample studied here. They found that the median spectral index between 5 and 1.4 GHz changed from 0.56 ± 0.06 for sources with $S_{5\text{GHz}} > 4$ mJy to 0.24 ± 0.06 for sources with $S_{5\text{GHz}} < 4$ mJy.

4.3 Extent of the radio emission

The sources were split into three groups (extended, unclassified and no information) as described in Section 3.4. A summary of the properties of these three groups of sources in terms of spectral index and flux density is given in Table 7 and the flux density distribution for the three groups is shown in Fig. 15. A larger proportion of the brighter sources are extended, with extended sources making up 38 per cent of the total number of sources with $S > 1$ mJy, compared to 19 per cent of sources with $S < 1$ mJy. This could be a result of the more stringent criteria for classifying sources with low signal-to-noise ratio as extended as well as the fact that extended low surface brightness emission is more likely to be missed at low signal-to-noise ratio levels. As expected, the majority of the sources with no information are faint, with $S < 1$ mJy.

The spectral index distributions for the extended sources and those not classified are, as anticipated, significantly different, as shown in Fig. 16 and Table 7. The majority (70/85) of the extended sources are steep spectrum, with the spectral index distribution peaking at $\alpha \approx 0.8$. The distribution of the unclassified sources is much broader and is less peaked, with the distribution stretching between $\alpha \approx -0.2$ and $\alpha \approx +1$. The majority of the sources with no information display a flat spectrum, as these are the sources which are too faint to be detected at the lower frequencies of 610 MHz/1.4 GHz. For these sources, the value of α plotted is an upper limit, which explains the large peak at $\alpha \approx 0$. Fig. 17 shows R_{GMRT} against $\alpha_{0.61}^{15.7}$ for all sources matched to the GMRT catalogue. It is evident from this plot that, as expected, a greater number of the extended sources have a steep spectrum.

The distribution for extended sources displays a flat-spectrum tail, 15 sources having $\alpha_{0.61}^{15.7} < 0.5$. It is likely that these extended, flat-spectrum sources are extended sources with a flat-spectrum core which dominates at high frequency. We might therefore expect that the lower frequency images of most of these sources would display a dominant core surrounded by some, possibly fainter, extended emission, whereas the steep-spectrum extended sources would have relatively more pronounced lobes. Examination of the

Table 5. The $\alpha_{0.61}^{15.7}$ results for three 15.7-GHz flux density bins.

Bin name	15.7-GHz flux density range (mJy)	Number of sources	Number of upper limits	Median α	Mean α	Per cent ($\alpha > 0.5$)
S_{low}	$0.300 < S \leq 0.755$	99	45	0.08	0.25 ± 0.04	25 ± 4
S_{med}	$0.755 < S \leq 1.492$	97	29	0.36	0.31 ± 0.05	40 ± 5
S_{high}	$1.492 < S \leq 45.700$	95	4	0.75	0.57 ± 0.05	67 ± 5

Table 6. The $\alpha_{1.4}^{15.7}$ results for three 15.7-GHz flux density bins.

Bin name	15.7-GHz flux density range (mJy)	Number of sources	Number of upper limits	Median α	Mean α	Per cent $\alpha > 0.5$
S_{low}	$0.300 < S \leq 0.755$	99	27	0.10	0.11 ± 0.07	29 ± 4
S_{med}	$0.755 < S \leq 1.492$	99	13	0.43	0.30 ± 0.07	46 ± 5
S_{high}	$1.492 < S \leq 45.700$	98	2	0.79	0.66 ± 0.05	76 ± 4

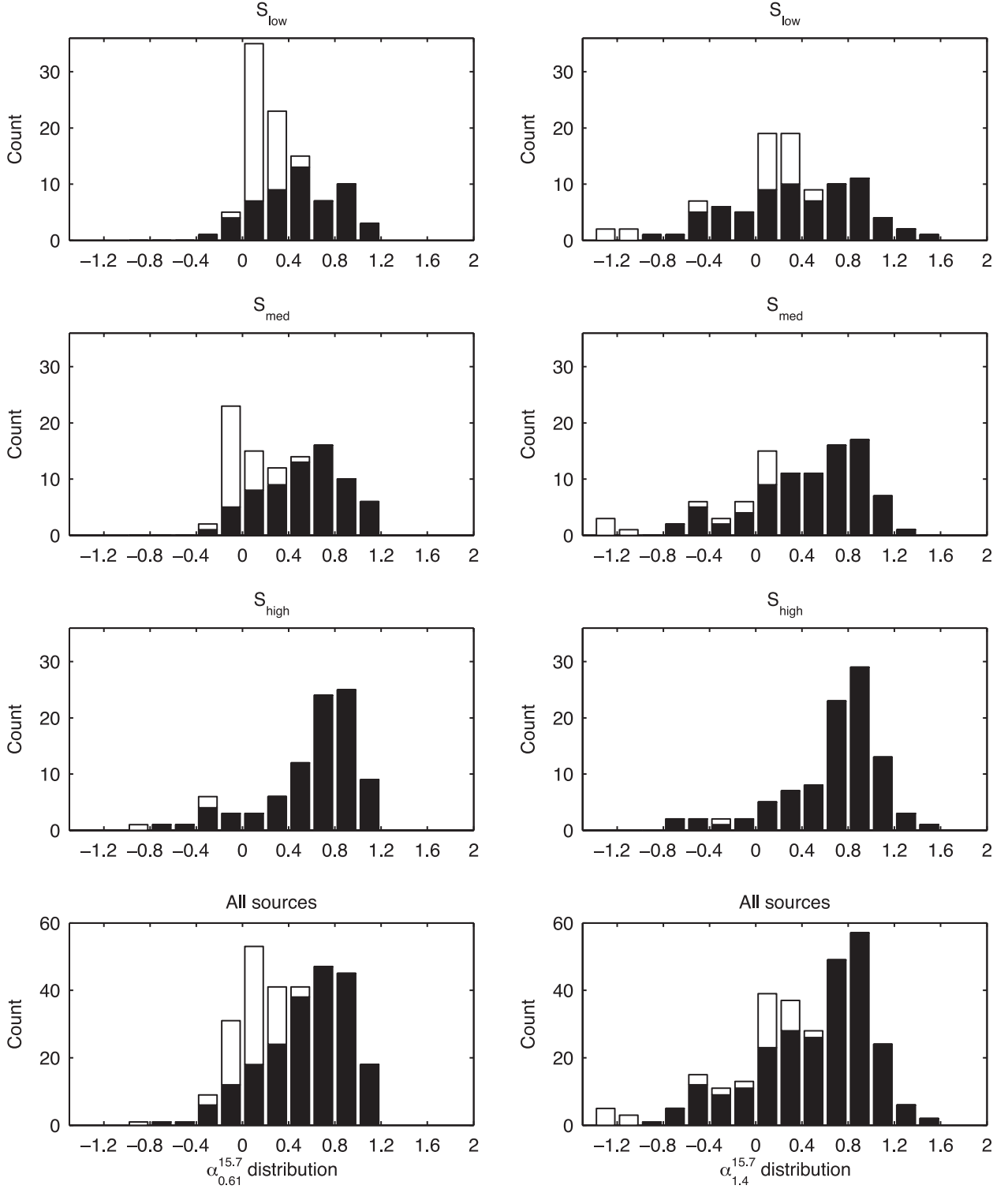


Figure 10. The spectral index distribution for three different flux density bins are shown in the top three panels. S_{low} : $0.300 < S_{15.7\text{ GHz}} \leq 0.755$ mJy, S_{med} : $0.755 < S_{15.7\text{ GHz}} < 1.492$ mJy, S_{high} : $1.492 < S_{15.7\text{ GHz}} \leq 47$ mJy. The spectral index distribution for the whole 10C sample is shown in the bottom panel. $\alpha_{0.61}^{15.7}$ is calculated using the GMRT values and limits, accounting for the resolution difference as described in Section 3.1, and using the integrated flux density from the 10C catalogue. $\alpha_{1.4}^{15.7}$ was calculated using the best 1.4 GHz flux density available (order of preference = NVSS, WSRT, OM2008, FIRST, B12006). In both cases upper limits on α are included for sources where no low-frequency flux density data are available; these are shown in white, while values are plotted in black.

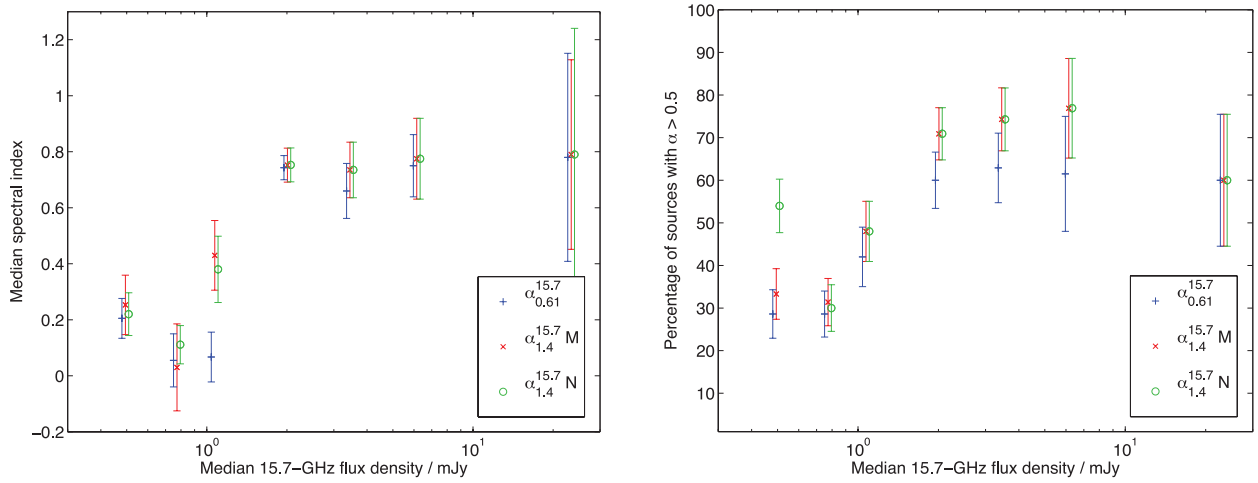


Figure 11. The median spectral index and percentage of sources with $\alpha > 0.5$ as a function of 15.7-GHz flux density for all 10C sources. The values of $\alpha_{1.4}^{15.7} M$ are calculated using the best 1.4-GHz flux density values available (order of preference = NVSS, WSRT, OM2008, FIRST, B12006), while the values of $\alpha_{1.4}^{15.7} N$ are calculated using 1.4-GHz flux density values from NVSS only. The points are plotted at the median flux density in each bin but are offset for clarity. Limiting spectral indices are included in the median using survival analysis (see text). The error bars in the median spectral index plot show the interquartile range divided by \sqrt{N} to give an indication of the errors in the medians. Note the large change in spectral index between 1 and 2 mJy.

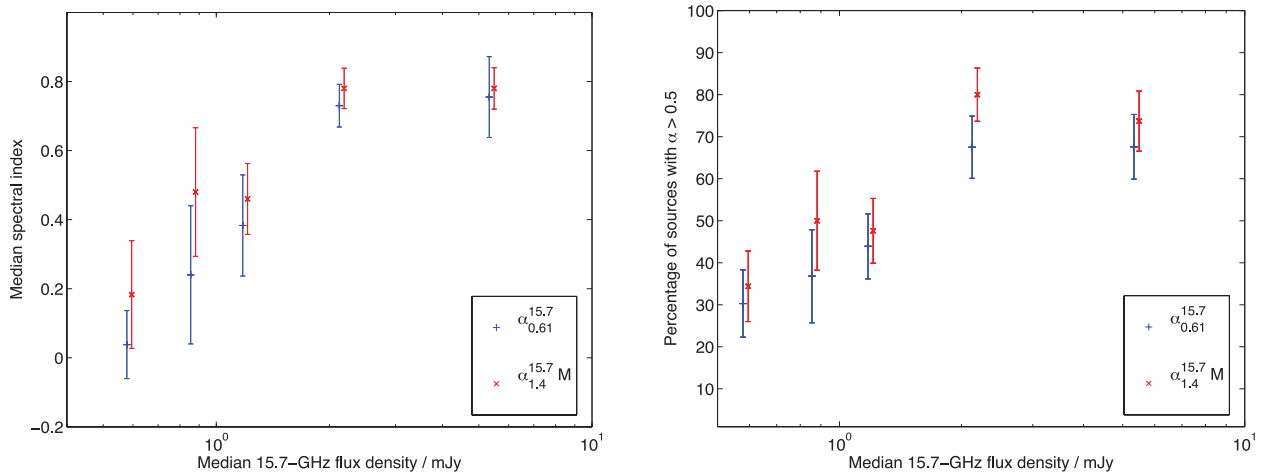


Figure 12. The median spectral index and percentage of sources with $\alpha > 0.5$ as a function of 15.7-GHz flux density for sources in the complete samples A and B. The values of $\alpha_{1.4}^{15.7} M$ are calculated using the best 1.4-GHz flux density values available (order of preference = NVSS, WSRT, OM2008, FIRST, B12006). The points are plotted at the median flux density in each bin but are offset for clarity. The sources in the lowest two flux density bins are from Sample A, which is complete above 0.5 mJy, and the remaining three flux density bins contain sources from sample B, complete above 1 mJy. Limiting spectral indices are included in the median using survival analysis (see text). The error bars in the median spectral index plot show the interquartile range divided by \sqrt{N} to give an indication of the errors in the medians.

images shows this to be the case for most sources; typical examples of steep- and flat-spectrum extended sources are shown in Fig. 18.

4.4 Correlations between size and spectral index

In Section 4.3 it is shown that the majority of the flat-spectrum sources are not classified as extended and therefore probably compact. However, a small but significant number (15 out of 163) of the flat-spectrum sources are clearly extended, indicating a variety of source types. There are also a significant number of sources (34) for which we have no information about their structure.

Recent work by Massardi et al. (2011a) using the AT20G survey found that for α_1^5 there was a clear divide between the ex-

tended, steep-spectrum sources and the compact, flat-spectrum sources. However, when looking at the higher frequency spectral index, α_8^{20} , they found that the extended sources displayed a much broader range in spectral index. This is consistent with the flat-spectrum tail in the spectral index distribution for extended sources observed here and supports the idea that a flat-spectrum core is becoming increasingly dominant at higher frequencies. A study by Prandoni et al. (2006) investigated the properties of a sample of 111 sources using data at 1.4 and 5 GHz and found that nearly all the extended or multiple sources were steep spectrum. The lack of flat-spectrum, extended sources in the Prandoni et al. study is probably due to the lower frequencies used, as at these frequencies the flat-spectrum core has not yet become dominant.

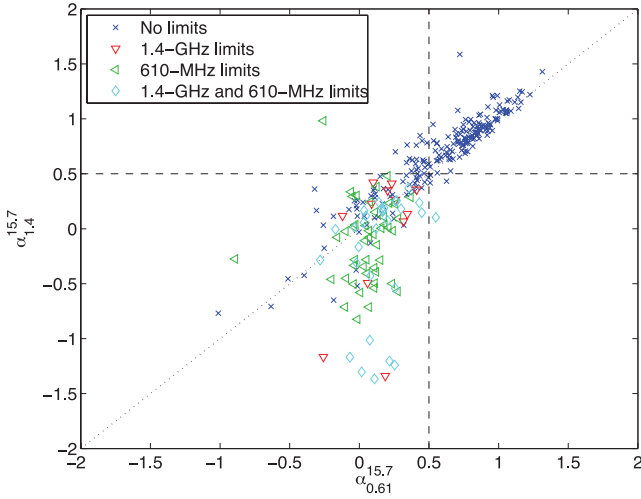


Figure 13. Values of $\alpha_{0.61}^{15.7}$ and $\alpha_{1.4}^{15.7} M$, showing which values are upper limits. The arrows indicate the direction in which the points which are upper limits could move. The dashed lines at $\alpha = 0.5$ illustrate the division between steep- and flat-spectrum sources; sources with $\alpha > 0.5$ are classified as steep spectrum, while sources with $\alpha < 0.5$ are classified as flat spectrum. The dotted line illustrates $\alpha_{0.61}^{15.7} = \alpha_{1.4}^{15.7} M$.

4.5 Effect on the source counts

The 15.7-GHz source count derived from the full 10C survey is presented in AMI Consortium: Davies et al. (2011). The function fitted to the source count is a broken power law, as shown below:

$$n(S) \equiv \frac{dN}{dS} \approx \begin{cases} 24 \left(\frac{S}{\text{Jy}} \right)^{-2.27} \text{Jy}^{-1} \text{sr}^{-1} & \text{for } 2.8 \leq S \leq 25 \text{ mJy}, \\ 376 \left(\frac{S}{\text{Jy}} \right)^{-1.80} \text{Jy}^{-1} \text{sr}^{-1} & \text{for } 0.5 \leq S < 2.8 \text{ mJy}. \end{cases} \quad (1)$$

It is significant that the break in this power law occurs at 2.8 mJy, that is, at approximately the same flux density as the change in the spectral index distribution observed here.

To examine this further, the source counts for the complete sample of sources (made up of samples A and B) studied in this paper are presented in Table 8. The counts for steep- and flat-spectrum sources are shown separately; the flux density bins are double the bins used in presenting the full 10C counts in AMI Consortium: Davies et al. (2011). No attempt is made to fit the source count due to the small number of sources in each bin. However, it is clear that the source counts are significantly different for the two populations, with, as expected, a greater proportion of flat-spectrum sources in the fainter flux density bins ($S_{15\text{GHz}} \lesssim 1 \text{ mJy}$), while the steep-spectrum sources dominate at the higher flux densities. Taken with the flattening of the overall counts for flux densities $< 2.8 \text{ mJy}$, this indicates that the source counts for the steep-spectrum sources must be flattening significantly at flux densities below about 1 mJy.

There is evidence from other studies that the Fanaroff–Riley type II (FR II; Fanaroff & Riley 1974) population is dropping out at around the flux density where we observe the flattening of the steep-spectrum source count. For example, Gendre & Wall (2008) used a sample of Combined NVSS–FIRST Galaxies (CoFIG) to construct a 1.4-GHz source count for FR I and FR II sources. They found that the FR II population is dropping out as flux density decreases below approximately 20 mJy at 1.4 GHz, leaving a source population dominated by FR I sources at lower flux densities. This change in the population at $S_{1.4\text{GHz}} \approx 20 \text{ mJy}$ corresponds to S

$\approx 3 \text{ mJy}$ at 15 GHz for a steep-spectrum source ($\alpha = 0.75$). The simulated source counts produced by Wilman et al. (2008) (which are discussed in more detail in Section 6) also show that the FR II population drops out at a few mJy at 18 GHz. It therefore seems likely that the changes in the spectral index distributions at around 1 mJy in our 15-GHz sample are due in part to the disappearance of the FR II sources. However, as discussed in Section 6, the dominance of a flat-spectrum population at flux densities below 1 mJy is in clear disagreement with the models of Wilman et al. (2008), de Zotti et al. (2005) and Tucci et al. (2011).

5 COMPARISON WITH SAMPLES SELECTED AT 1.4 GHz

The source population at 1.4 GHz has been much more widely studied than the higher frequency population and models of the faint population at higher frequencies are often extrapolated from these lower frequency data. It is therefore useful to see how the spectral index distribution of the 10C source population compares to that for sources selected at 1.4 GHz.

Two samples of sources at 1.4 GHz were used: the first sample was selected from the FIRST catalogue (Sample P) and the second from the NVSS catalogue (Sample Q). The FIRST catalogue is deeper so Sample P provides more information about the faint source population; the NVSS survey, on the other hand, has a beam size comparable to the 10C survey so provides more reliable spectral indices.

Some consideration needs to be given to the limiting flux densities of the FIRST and NVSS catalogues and the 10C catalogue which they are being matched. A source with a 1.4-GHz flux density of 3.4 mJy (the completeness limit of the NVSS) should be detected in 10C unless it has a spectral index greater than 0.8. It is therefore expected that counterparts will be found at 15.7 GHz for the majority of the NVSS sources. The FIRST, however, has a completeness limit of 1 mJy; a source with a 1.4-GHz flux density of 1 mJy could be detected at 15.7 GHz if it had $\alpha_{1.4}^{15.7} < 0.3$. We therefore expect a larger proportion of lower limits on the spectral indices for FIRST sources.

5.1 Sample selected from the FIRST

All FIRST sources in the 10C deep fields (the areas containing Sample A) were selected (see Fig. 1) giving a sample of 127 sources selected at 1.4 GHz. These sources were matched to the full 10C catalogue using a match radius of 15 arcsec, as described in Section 2.2. The difference in resolution between the two catalogues meant that there were several sources which were resolved into multiple components in the FIRST but unresolved in 10C. For those cases where several FIRST sources matched to one 10C source, the flux densities of the individual FIRST sources were combined, giving a sample of 105 FIRST sources, 70 of which have a match to 10C.

10C maps of the unmatched FIRST sources were examined by eye. In 10 cases, a source was visible in the 10C image – however, its flux was clearly below the 10C completeness limit; the flux density of such a source was found using TVSTAT in AIPS. For the remaining unmatched sources, an upper limit of three times the local noise was placed on the flux density. This allows a lower limit to be placed on the spectral index.

The flux density distribution of the 105 sources in Sample P is shown in Fig. 19.

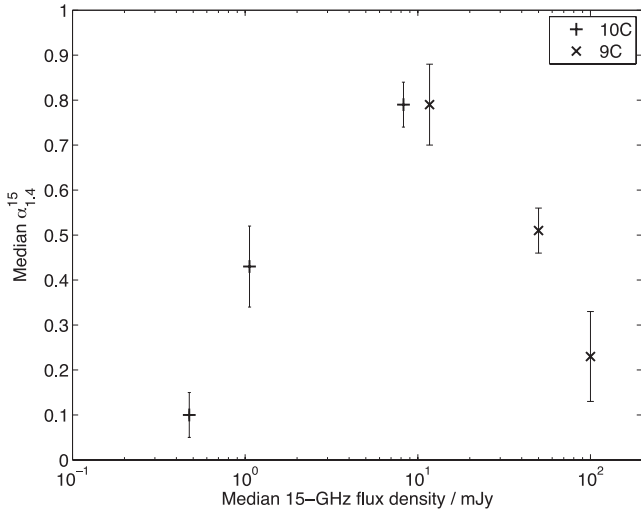


Figure 14. The median spectral index as a function of flux density from the study of 9C sources by Waldram et al. (2010) and the 10C sources studied in this paper. The points are plotted at the bin mid-point, except for the highest flux density bin ($S > 100$ mJy) where the point is plotted at the bin lower limit.

Table 7. A summary of the properties of sources classified as extended, those not classified and those with no information. The value of the spectral index used here is $\alpha_{0.61}^{15.7}$ so the five sources which are outside the GMRT survey area are not included. The numbers in brackets refer to the percentage of sources in each classification.

Bin	Total	Number of sources with. . .			
		$S_{15.7} > 1$ mJy	$S_{15.7} < 1$ mJy	$\alpha > 0.5$	$\alpha < 0.5$
Extended	85	55 (65)	30 (35)	70 (82)	15 (18)
Unclassified	170	80 (47)	90 (53)	56 (33)	114 (67)
No information	36	5 (14)	31 (86)	2 (6)	34 (94)

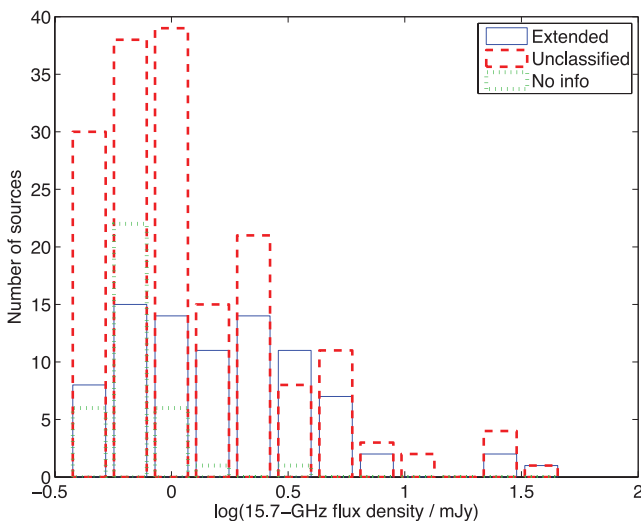


Figure 15. The 15.7-GHz flux density distribution for the extended sources, those which are unclassified and those with no information. The three histograms are overlaid.

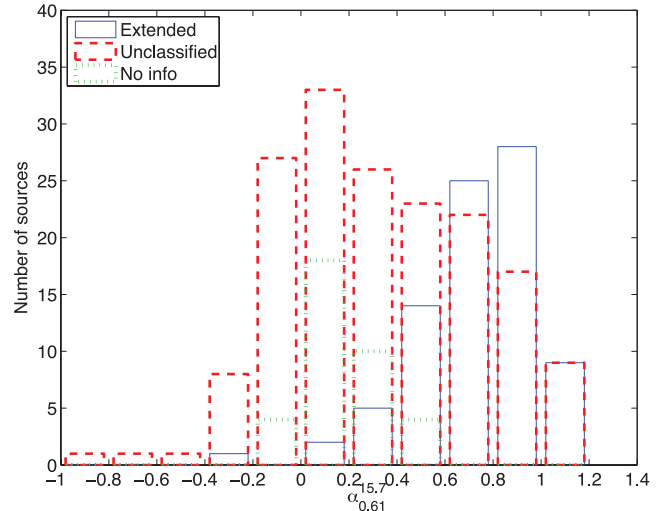


Figure 16. The spectral index distribution for sources classified as extended and unclassified, and those with no information. The three histograms are overlaid. Upper limits in α are plotted for the sources with no information which explains the apparent peak at $\alpha \approx 0$.

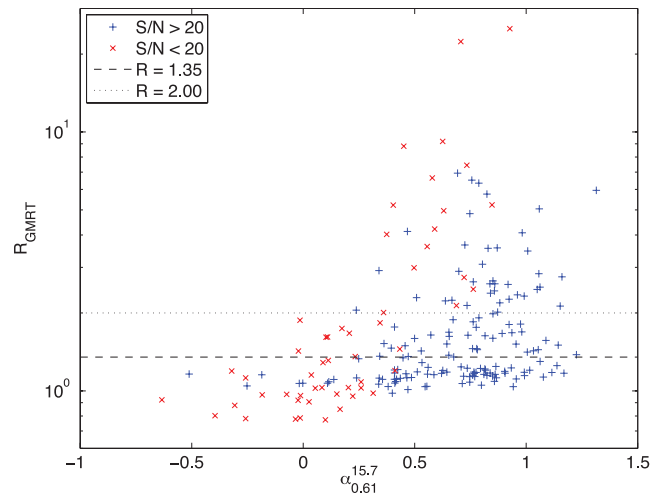


Figure 17. R_{GMRT} as a function of $\alpha_{0.61}^{15.7}$ for all sources in the GMRT area. Sources with peak flux/noise < 20 in the GMRT catalogue are shown separately and the horizontal lines at $R = 1.35$ and 2.00 indicate the cut-offs in R used when classifying the extended sources (see text for details).

5.2 Sample selected from the NVSS

In order to have enough NVSS sources to be able to draw statistically significant conclusions, sources were selected from the deep areas of four 10C fields. Two of these are the fields in the Lockman Hole studied in this paper, the other two fields are centred on $17^{\text{h}}33^{\text{m}}, +41^{\circ}48^{\text{m}}$ and $00^{\text{h}}24^{\text{m}}, +31^{\circ}52^{\text{m}}$. There are 292 sources in these four fields, giving a sample of comparable size to the sample of 10C sources studied in this paper. The NVSS sources were matched to the 10C catalogue, with limits placed on the unmatched sources as described in Section 5.1. This sample (Sample Q) contains 292 NVSS sources, 223 of which have a match to the 10C catalogue. The flux density distribution of Sample Q is shown in Fig. 20.

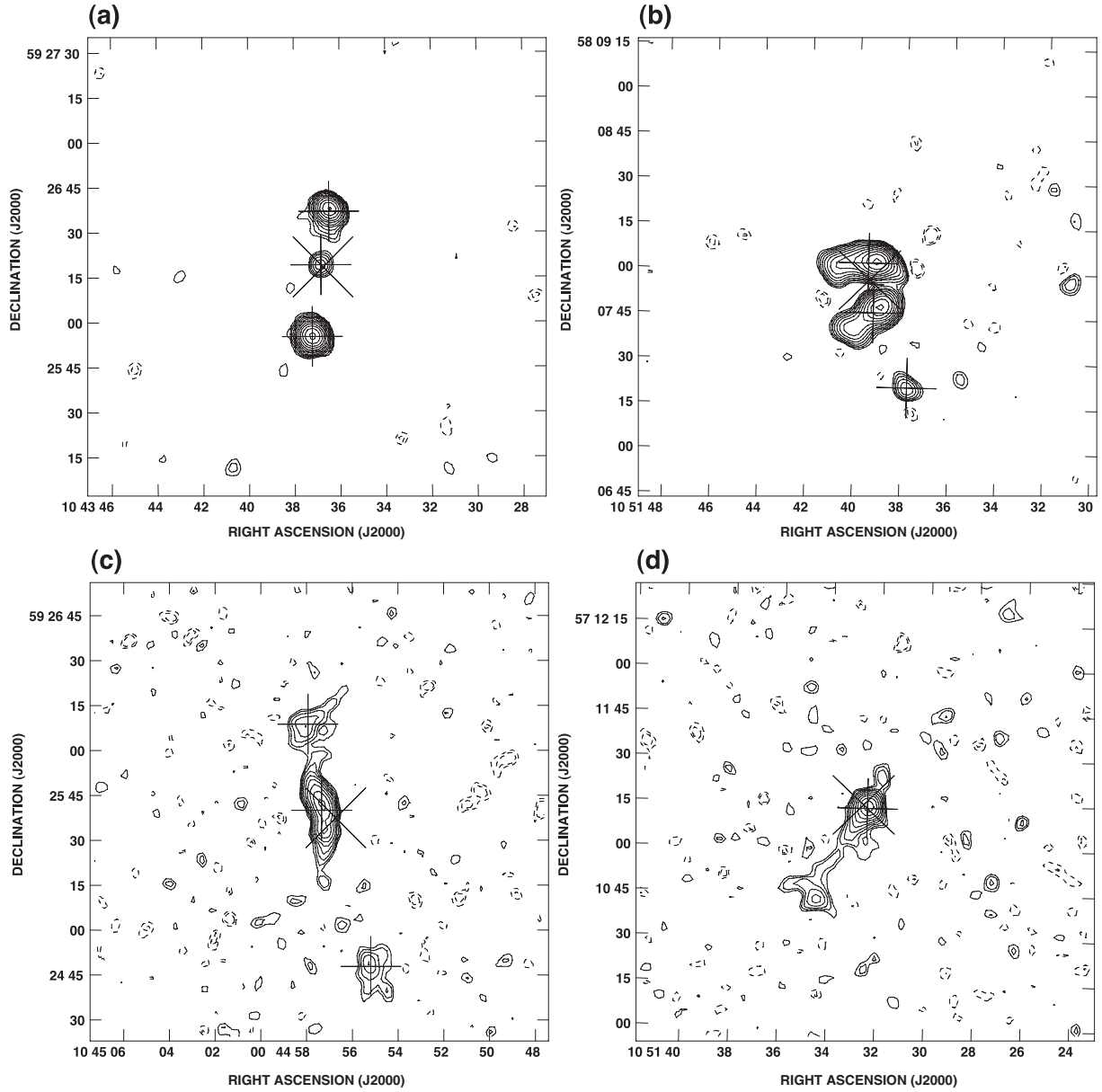


Figure 18. GMRT images of some example extended sources. The contours are drawn at $(\pm 2\sqrt{2^n}, n = 0, 1, \dots, 7) \times x$ mJy, where $x = 0.16$ for panel (a), 0.15 for panel (b), 0.086 for panel (c) and 0.076 for panel (d). The \times symbol marks the position of the 10C source and the $+$ symbols mark the positions of the components listed in the GMRT catalogue for each source. Panels (a) and (b) show steep-spectrum sources with $\alpha_{0.61}^{15.7} = 0.93$ and 1.08, respectively. Panels (c) and (d) demonstrate flatter spectra with $\alpha_{0.61}^{15.7} = 0.49$ and 0.34, respectively.

5.3 Spectral index distribution of samples selected at 1.4 GHz

The spectral index $\alpha_{1.4}^{15.7}$ was calculated for all sources in Samples P and Q with a match in 10C. For the unmatched sources, a lower limit was placed on the spectral index using the upper limit from the 10C map. Fig. 21 shows a comparison of the spectral index distributions of the sources selected at 15.7 GHz and those selected at 1.4 GHz. As expected the distributions are noticeably different; the sources selected at 1.4 GHz show one peak at $\alpha_{1.4}^{15.7} \approx 0.7$, while the sample selected at 15.7 GHz displays an additional peak at $\alpha_{1.4}^{15.7} \approx 0.3$. The additional population of flat-spectrum sources, as expected, are poorly represented by selecting at 1.4 GHz. This is the challenge that extrapolating from lower frequencies to predict the high-frequency radio population presents. It relies on accurate modelling of the source population and of how the spectral behaviour of sources

varies with frequency; it is particularly unreliable when there are no observations at nearby frequencies at the required flux density. The 10C sample is compared to one such model in Section 6.

6 COMPARISON WITH THE SKADS SIMULATED SKY

Wilman et al. (2008, 2010) produced a semi-empirical simulation of the extragalactic radio continuum sky which contains ≈ 320 million sources. This simulation covers a sky area of 20×20 deg² out to a cosmological redshift of $z = 20$ and down to flux density limits of 10 nJy at 151 MHz, 610 MHz, 1.4 GHz, 4.86 GHz and 18 GHz. The sources in the simulation are split into six distinct source types: radio-quiet active galactic nuclei (AGNs), radio-loud

Table 8. Source counts for the complete 10C sample from the Lockman Hole fields (made up of samples A and B). Steep- and flat-spectrum sources (with $\alpha_{0.61}^{15.7} > 0.5$ and $\alpha_{0.61}^{15.7} < 0.5$, respectively) are shown separately. Each flux density bin corresponds to two of the flux density bins used in presenting the full 10C source counts in AMI Consortium: Davies et al. (2011) (except for the highest flux density bin).

Bin start (mJy)	Bin end (mJy)	Number of sources with $\alpha > 0.5$	Number of sources with $\alpha < 0.5$	Area (deg ²)
9.000	25.000	4	4	4.64
2.900	9.000	22	11	4.64
1.500	2.900	27	10	4.64
1.000	1.500	18	24	4.64
0.775	1.000	5	11	1.73
0.600	0.775	5	11	1.73
0.500	0.600	6	12	1.73

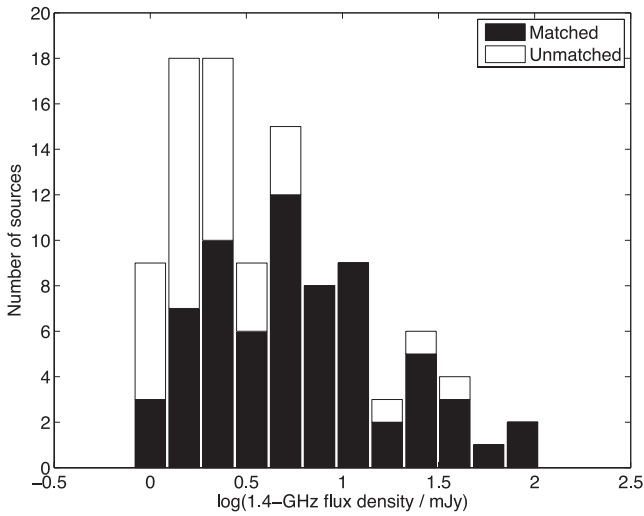


Figure 19. The flux density distribution of the sources in Sample P, selected from the FIRST catalogue. Sources with and without a match to the 10C catalogue are shown separately.

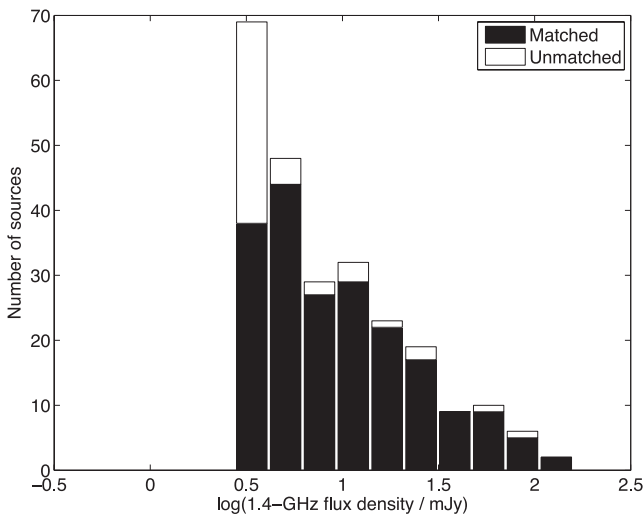


Figure 20. The flux density distribution of the sources in Sample Q, selected from the NVSS catalogue. Sources with and without a match to the 10C catalogue are shown separately.

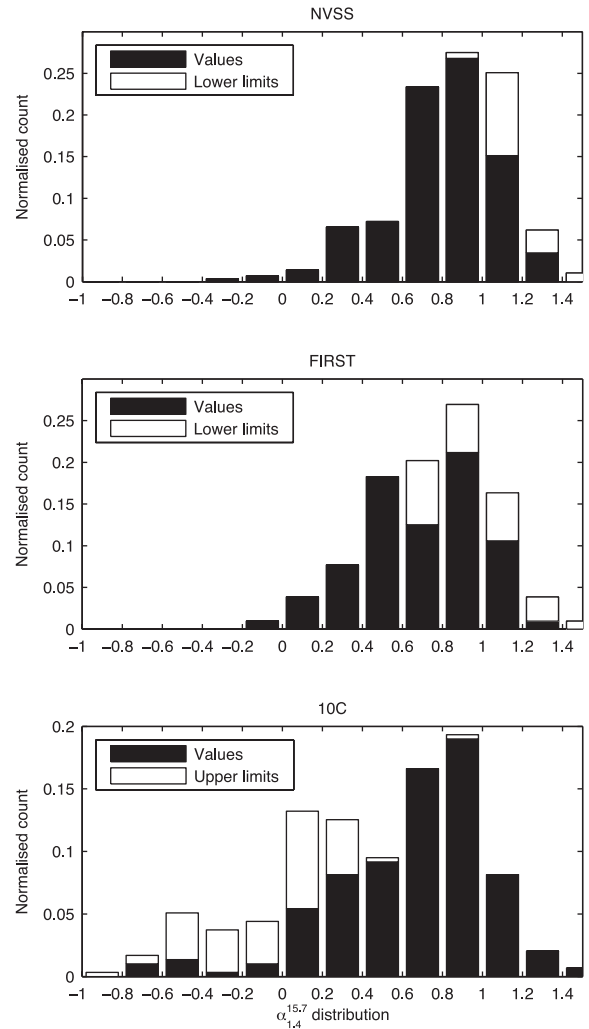


Figure 21. The spectral index distributions for sources selected at 1.4 GHz from the NVSS (Sample Q, shown in the top panel) and FIRST (Sample P, middle panel) and 10C sources selected at 15.7 GHz (bottom panel). Limiting spectral indices for the unmatched sources are shown in white – note that these are lower limits in the FIRST and NVSS cases, therefore could only move to the right-hand side, and upper limits in the 10C case.

AGNs of FR I and FR II, GHz-peaked spectrum (GPS) sources, quiescent star-forming and starbursting galaxies. These simulated sources are drawn from the observed or extrapolated luminosity functions. In order to produce a subsample of simulated sources comparable to the sources observed in this work, sources with a flux density greater than 0.5 mJy at 18 GHz were selected from the simulation. This produced a simulated subsample of 16 235 sources (Sample S³). The spectral index between 610 MHz and 18 GHz was calculated from the flux densities in the catalogue.

The S³ sample is dominated by FR I sources, which make up 71 per cent of the source population (Table 9) in agreement with the discussion in Section 4.5. The second largest source population is made up of FR II sources, while radio-quiet AGNs, GPS sources and star-forming galaxies each make only small contributions to the simulated source population. The S³ sample covers a region of area 400 deg², while the deep 10C regions from which Sample A is drawn cover 1.73 deg². In order to investigate the possible impact of clustering on these results, five regions of the S³ sample with areas of 1.73 deg² were selected at random. The fraction of

Table 9. The proportion of different source types in the subsample of simulated sources selected to be directly comparable to the sources observed in this study. This subsample contains 16 235 sources with a flux density at 18 GHz greater than 0.5 mJy. The range of percentages calculated from five regions of equivalent size to the 10C deep survey area is also given.

Source type	Percentage	Range
FR I	71	57–85
FR II	13	6–30
Radio-quiet AGN	3	0–6
GPS	3	0–8
Starburst	4	0–11
Quiescent star forming	3	1–11

different source types in each of these five regions was calculated and the range of values this gave is shown in Table 9. Although the exact percentages of source types vary across the five regions, the general proportions remain the same, indicating that clustering will not have a major effect on the 10C results.

The spectral index distributions of the different groups of sources in the simulation are shown in Fig. 22. All FR I, FR II and GPS sources have been modelled assuming their extended emis-

sion has a constant spectral index of 0.75, hence the prominent peaks at $\alpha = 0.75$. An orientation-dependent relativistic beaming model is used to find the contribution of the flat-spectrum core to the overall emission from each source; this gives the flat-spectrum tail in each spectral index distribution. The radio-quiet AGNs have been assumed to have a constant spectral index of 0.7. The spectra of the starburst and star-forming galaxies have been modelled using thermal and non-thermal components and in the case of starbursts a thermal dust component has been included.

Fig. 23 shows a comparison of the spectral index and flux density distributions of the observed 10C sources (Sample A, complete to 0.5 mJy) and S^3 sample. It is clear that the simulation fails to reproduce the spectral index distribution of the 10C sources. The discrepancy for $\alpha > 0.7$ is due to the input assumption of the model that all sources have $\alpha = 0.75$; however, the model fails to reproduce the distribution for $\alpha < 0.7$ with a conspicuous absence of sources with $\alpha < 0.3$. There are two main possibilities here: either the distribution of sources has not been modelled correctly and FR I sources do not dominate at this frequency and flux density level, but instead a new population with flat spectra are becoming important, or the emission from FR I sources has not been modelled correctly and that their flat-spectrum cores are more dominant than predicted by the model in this frequency range. It is also possible that starburst galaxies may be causing this flattening in spectral index, although

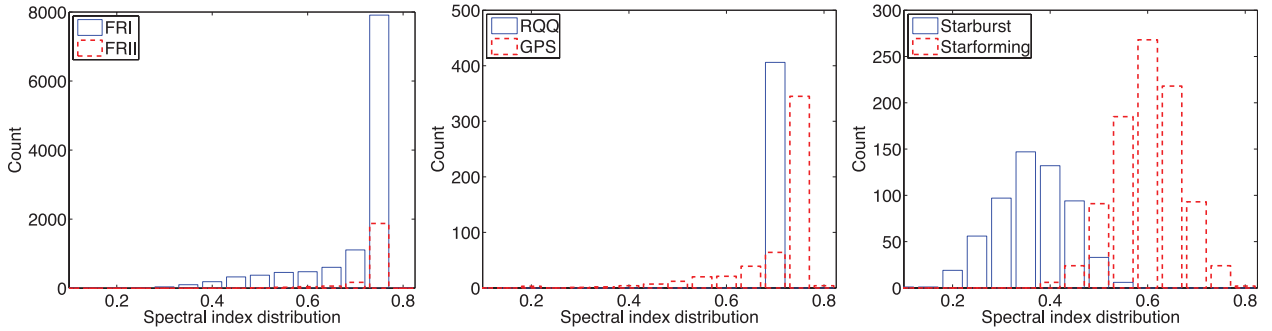


Figure 22. The spectral index distribution of the different source populations in the S^3 sample with $S_{18\text{GHz}} > 0.5$ mJy. The left-hand panel shows FR I and FR II sources, the middle panel shows radio-quiet AGNs and GHz-peaked sources, and the right-hand panel shows starburst and quiescent star-forming sources.

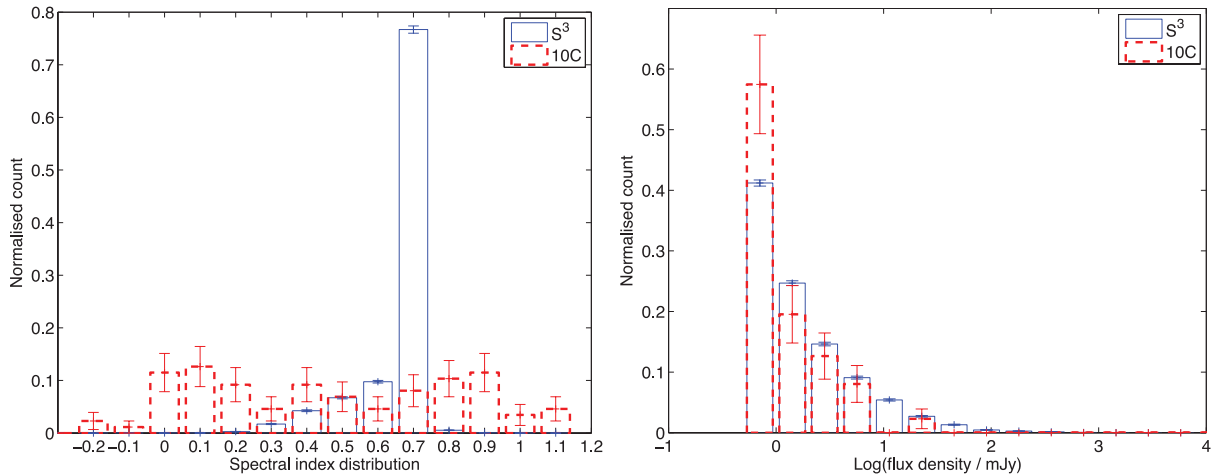


Figure 23. Comparison of the 10C and the simulated samples. The spectral index distribution (left-hand panel) and flux density distribution (right-hand panel) for sources in the S^3 sample with $S_{18\text{GHz}} > 0.5$ mJy and for 10C sources with $S_{15.7\text{GHz}} > 0.5$ mJy is shown. Note that for the S^3 sample the values plotted are $\alpha_{0.61}^{18}$ and 18-GHz flux density, while for the 10C sources $\alpha_{0.61}^{15.7}$ and 15.7-GHz flux density are plotted. We do not expect this to make any difference to the results. Error bars show the Poisson errors.

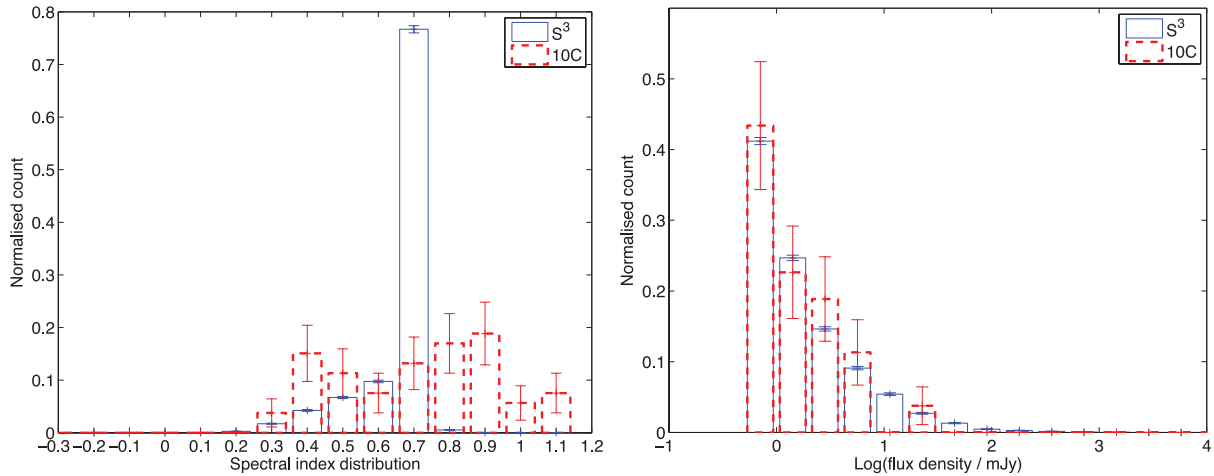


Figure 24. Comparison of the spectral index distribution and flux density distribution for sources in the S^3 sample with $S_{18\text{ GHz}} > 0.5$ mJy and for 10C sources with $S_{15.7\text{ GHz}} > 0.5$ mJy and a spectral index ($\alpha_{0.61}^{15.7}$) greater than 0.3 only. Note that for the S^3 sample the values plotted are $\alpha_{0.61}^{18}$ and 18-GHz flux density, while for the 10C sources $\alpha_{0.61}^{15.7}$ and 15.7-GHz flux density are plotted. We do not expect this to make any difference to the results. Error bars show the Poisson errors.

this is unlikely as it would require the contribution of starbursts to be greater than modelled by at least a factor of 10.

The actual and simulated flux density distributions are similar, but the 10C distribution contains a larger proportion of sources with flux densities less than 1 mJy. To test the possibility that there is a population of faint flat-spectrum sources observed here which are missing from the simulation, the spectral index and flux density distributions were replotted, this time excluding all sources in the 10C sample with $\alpha < 0.3$ (Fig. 24) as essentially no sources with $\alpha < 0.3$ are predicted by the model. The distributions are now more similar.

This analysis indicates that the extrapolations of the luminosity functions coupled with the models for the effects of beaming on the spectra of the radio-loud AGNs used in this simulation have failed to reproduce the observed properties of the high-frequency population. It is worth noting that the recent models of the source population at 15 GHz by de Zotti et al. (2005) and Tucci et al. (2011) also fail to reproduce the observed source count at flux densities $\lesssim 10$ mJy, significantly underpredicting the observed number of sources. The updated version of the model of the 15-GHz source count by de Zotti et al. (2005), extracted from their website,³ shows that steep-spectrum sources outnumber flat-spectrum sources until the flux density drops below approximately 2 μ Jy, in clear disagreement with the counts in Table 8. The de Zotti et al. model predicts that at $S_{15\text{ GHz}} = 1$ mJy steep-spectrum sources outnumber flat-spectrum sources by nearly a factor of 3. The results in Table 8 show that for $S_{15\text{ GHz}} < 1$ mJy there are twice as many flat-spectrum sources as steep-spectrum sources. The recent high-frequency predictions of the source counts by Tucci et al. (2011) significantly underpredict the number of sources observed at 15 GHz below approximately 5 mJy. This underprediction of the total number of sources could be explained by there being a greater number of flat-spectrum sources at faint flux densities than are included in the model. These results highlight the difficulties inherent in predicting the behaviour of the high-frequency radio source population by extrapolating from lower frequencies.

7 CONCLUSIONS

The radio spectral properties of 296 sources detected as part of the 10C survey at 15.7 GHz in the Lockman Hole are investigated in detail using a number of radio surveys, in particular a deep GMRT image at 610 MHz and a WSRT image at 1.4 GHz. Matches at other radio frequencies were found for 266 out of 296 sources, allowing their radio spectra to be investigated. For the 30 sources which were only detected at 15.7 GHz, upper limits are placed on their spectral indices.

There is a clear change in spectral index with flux density – the median $\alpha_{0.61}^{15.7} = 0.75$ for flux densities greater than 1.5 mJy, while the median $\alpha_{0.61}^{15.7} = 0.08$ for flux densities less than 0.8 mJy. This demonstrates that there is a population of flat-spectrum sources emerging below 1 mJy. This result is consistent with results from other studies of the spectral indices of sources at lower frequencies.

The 10C source population was compared to two samples selected at 1.4 GHz from the FIRST and NVSS at a comparable flux density. The spectral index distribution of these two samples is significantly different from that of the 10C sample selected at 15.7 GHz, the flat-spectrum population present at 15 GHz being poorly represented in the 1.4-GHz samples. This demonstrates the well-known problem with extrapolating from lower frequencies to predict the properties of the high-frequency population.

The 10C sample was compared to a comparable sample selected from the SKADS Simulated Sky constructed by Wilman et al. (2008). The spectral index distributions of the two samples differ significantly; there are essentially no sources in the simulated sample with $\alpha \ll 0.3$ while 40 per cent of the 10C sample have $\alpha_{0.61}^{15.7} < 0.3$. There is also a larger proportion of sources with flux densities below 1 mJy in the 10C sample than in the simulated sample – 57 per cent of the 10C sources have a flux density below 1 mJy compared to 40 per cent of simulated sources. This indicates that the simulation does not accurately reproduce the observed population at 15.7 GHz. We conclude that either there is a population of faint, flat-spectrum sources which are missing from the simulation or the high-frequency radio emission of a known population is not modelled correctly in the simulation. If the relative contributions of the different populations are modelled correctly, it is likely that the observed flat-spectrum population is due to cores of FR I sources being much more dominant than the model suggests.

³ http://web.oapd.inaf.it/rstools/srcnt/srcnt_tables.html

Our unique, faint 15-GHz samples are of great value when investigating the faint, high-frequency source population. We will use optical and infrared data in the Lockman Hole to investigate the nature of this population of sources in a later paper. We are also extending this study to fainter flux densities at 15 GHz.

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