

Competitive Nucleation Mechanism for CsPbBr₃ Perovskite Nanoplatelets Growth

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Abstract

We analyse nucleation-controlled nanocrystal growth in a solution containing surface-binding molecular ligands, which can also nucleate compact layers on the crystal surfaces. We show that if the critical nucleus size for ligands is larger and the nucleation barrier is lower than those for crystal atoms, the ligands nucleate faster than the atoms on relatively wide crystal facets but much slower, if at all, on narrow facets. Such competitive nucleation of ligands and atoms results in ligands covering predominantly wider facets, thus excluding them from the growth process, and acts as a selection mechanism for the growth of crystals with narrower facets, the so-called nanoplatelets. We illustrate this mechanism by simulating the growth process of an ensemble of crystals using a kinetic Monte-Carlo technique. Our predictions are confirmed experimentally for CsPbBr₃ high-quality nanoplatelets grown from the solution using a three-precursors facile synthetic approach. We find that the anisotropic crystal growth resulting in nanoplatelets is controlled by two main factors: the growth temperature and the strength of surface bonding for the passivating molecular ligands. A subtle variation in the latter parameter makes the choice of surface ligands a critical component in controlling the growth process. The present study provides a theoretical framework and a set of computational tools for the design and control of nanocrystal shapes through growth, which is essential in many nano-electronic and nano-photonics applications.

28 **Introduction**

29 Lead halide perovskites (LHPs) display remarkable optoelectronic properties encompassing a
30 panchromatic absorption profile, intense narrow-band luminescence, excellent ambipolar
31 charge transport, and low non-radiative losses, all of which makes them desirable materials for
32 light-emitting diodes (LEDs).¹⁻⁵ Based on these unique properties and a variety of simple
33 fabrication methods, which allow for selection space in both components of the LHPs and the
34 device architecture, research into LHPs has been pushed to the forefront of optoelectronics
35 community in recent years.^{6, 7} Despite significant success in fabricating LHP thin films for
36 green^{8, 9}, red¹⁰⁻¹², and near infrared^{13, 14} emission LEDs, obtaining suitable structures for stable
37 blue LHP-based emitter remains an issue.¹⁵ The poor performance of LHP in the blue spectral
38 range requires further understanding of their growth process and of how they can be tailored in
39 low dimensional shapes with wide bang-gaps.

40 One of the approaches to synthesising LHPs highly emissive in the effective blue region
41 (i.e. near 2.65 eV) is to create anisotropic quasi-two-dimensional CsPbBr₃ particles in the shape
42 of nanoplatelets (NPLs), which produce narrow PL due to strong quantum confinement.¹⁵⁻²³
43 An efficient way of producing such nanocrystals is by using surfactants, or surface-binding
44 molecular ligands.²⁴⁻²⁹ For instance, synthesis of the anisotropic CsPbBr₃ NPLs has been
45 established using the standard hot-injection method developed by Protesescu *et al.*³⁰ Initially
46 this method has been used for producing green-emitting cubic CsPbBr₃ nanocrystals by
47 appropriate choice of the concentration and type of molecular ligands in solution.^{18, 19, 31-35} In
48 the past few years the approach has been successfully implemented for solution-growth of
49 CsPbBr₃ NPLs^{18, 19, 22, 33, 36-41}, a promising material for optoelectronic applications.^{2, 42-44}
50 Despite the clear potential of the approach its original implementation is not free of some
51 drawbacks, e.g. the reported NPLs tendency to blend and, after a while usually lose their blue

52 emission .^{18, 19, 31-35} The approach also has the limitation of using lead halide (PbX₂) as the only
53 source of anion and cation in a swift metathesis reaction, which causes difficulty in tuning the
54 composition of the nanocrystals.⁴¹ Specifically, the presence of an excess of PbX in the reaction
55 products along with the nanoparticles causes phase transformation of the CsPbBr₃ into
56 undesired Cs₄PbBr₆.^{41, 45}

57 Quasi-two-dimensional semiconductor quantum dots in the shape of NPLs, such as CdSe,
58 have been the most studied^{46,47}, and their growth has been explained in terms of intrinsic growth
59 instability leading to NPLs formation.⁴⁸ Such a mechanism is apparently not applicable to
60 perovskite crystals, which in most cases grow as cuboids and only in special conditions they
61 form NPLs. Despite experimental success in determining conditions for perovskite NPLs
62 growth^{18, 19, 33, 34, 49}, little is understood about the mechanisms that lead to highly anisotropic
63 crystal shapes and how these shapes can be designed and controlled precisely at the atomic-scale
64 thickness. For example, Pan *et al.*²⁴ and other groups^{18, 19, 22, 32, 36-41} report that the precise type
65 of surface capping ligands and the reaction temperature are essential for the growth of 2D
66 CsPbBr₃ perovskite NPLs. However, the physical mechanism that reveals the effect of these
67 parameters on nanocrystal growth remains elusive.

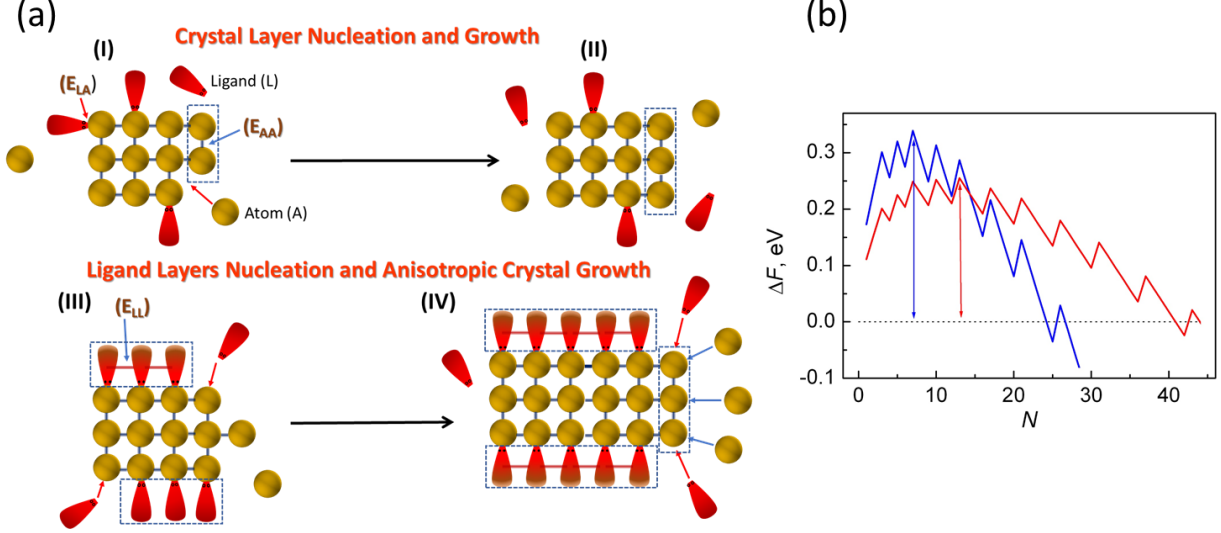
68 Here, we present a model of nanocrystal growth that explains NPLs formation in terms
69 of competitive nucleation of crystal monolayer versus ligand monolayer. Our model predicts
70 the effects of the temperature T and ligand-ligand interaction energy ε_{LL} on the shape of
71 growing nanocrystals. In particular, we predict that increasing ε_{LL} or decreasing T from some
72 optimum values results in the predominant growth of thinner NPLs while changing these
73 parameters otherwise stimulates the growth of cuboid-shaped crystals. Our experimental
74 studies fully recover these trends and illustrate that an appropriate choice of the surface binding
75 ligands and growth temperature result in the desired NPLs for an effective blue emission.

76 To validate the proposed model experimentally, we implement a new synthetic approach
77 that allows stoichiometric control of the concentration of all elements in the reaction in contrast
78 to the previously reported approach (i.e. Protesescu *et al.*³⁰ method) where PbX_2 is the only
79 source of both anions and cations. Our synthesis is based on the three-precursor approach first
80 reported by Wei *et al.*⁵⁰ and adopted by others^{51, 52}, which initially used to synthesise CsPbX_3
81 and FAPbX_3 cubic nanocrystals (for more details see experimental section). We modified this
82 approach as described below to achieve controlled growth of CsPbBr_3 NPLs. As our simulations
83 illustrate it, the regime of nano-platelets growth is achieved in a relatively narrow range of the ligand-
84 ligand interaction energies. For fine-tuning these interaction energies, we used a mixture of
85 ligands in solution (see details in Section 1 of Supporting Information). By fine-tuning the
86 ligand composition, it is possible to achieve the effective ligand-ligand interaction energy required
87 for efficient NPLs growth. As a result, we managed to generate NPLs, which produce *effective*
88 blue emission in the region $\sim 460\text{--}467$ nm.

89 **Results and Discussion**

90 The underlying mechanism of NPLs growth is based on the following theoretical model.
91 Consider a solution containing precursors (atoms) for crystal growth, small nucleated seed
92 crystals, and molecular ligands binding atoms on the crystals' surfaces. We assume that the
93 crystals grow layer by layer with each new atomic layer growing from some nucleus or critical
94 cluster of atoms on the crystal surface. It implies that the slowest event in the growth process
95 is the formation of the critical atomic cluster known as the critical nucleus. The rate of this
96 nucleation process is determined by the critical nucleus' size (number of atoms in the critical
97 cluster) N_{CA} and the nucleation barrier Δ_{CA} . This nucleation barrier characterises the free
98 energy penalty for transferring atoms from solution to the cluster on the crystal surface.
99 Molecular ligands present in the solution can also form a cluster on the crystal surface, which,
100 if this cluster grows over the critical size, can create a compact layer over the entire crystal

101 facet and block any subsequent growth on it. The process of ligand cluster nucleation is also
 102 characterised by the corresponding critical nucleus size N_{CL} and the nucleation barrier Δ_{CL} .



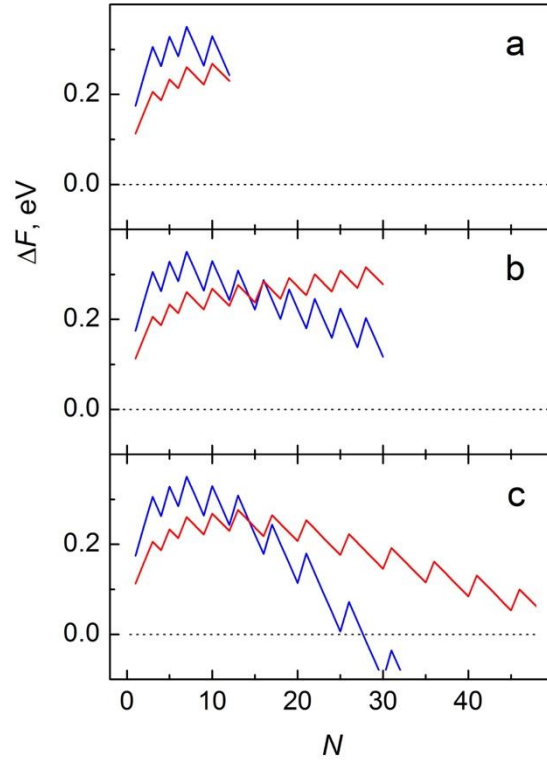
103
 104 Figure 1. a) Nucleation (panel (I)) and growth (panel (II)) of a new layer of atoms (spheres
 105 outlined with dashed lines) on the crystal side. Molecular ligands (cones) cannot nucleate the
 106 critical cluster on the short crystal side of 3 atoms (panel (I)), but can do it on the longer side
 107 of 4 atoms – see panel (III), which shows two nucleated layers of ligands (cones outlined with
 108 dashed lines). Molecular ligands block crystal growth in the vertical direction, leaving the
 109 crystal with the ligand layers grow horizontally (panel (IV)). b) Free energy ΔF of the surface
 110 cluster (nucleus) calculated on a square lattice of the size 7×7 unit cells as a function of the
 111 constituent number N of atoms (blue) or ligands (red) for $k_B T = 34 \text{ meV}$ (122°C), $\varepsilon_{AA} = 109 \text{ meV}$
 112 $\varepsilon_{LL} = 66 \text{ meV}$, $\varepsilon_{LA} = 171 \text{ meV}$ and $n_A = n_L = 2.5 \cdot 10^{-4}$. The arrows in b) show nucleation barriers
 113 Δ_{CA} and Δ_{CL} and indicate corresponding sizes of critical nuclei N_{CL} and N_{CL} for crystal atoms
 114 and molecular ligands, respectively.

115 Both the nucleation barrier and critical nucleus size can be determined by plotting the
 116 nucleus' excess free energy $\Delta F_{A(L)}(N)$ versus the number N of constituent atoms/ligands:

$$117 \quad \Delta F_A(N) = E_A(\varepsilon_{AA}, N) - Nk_B T \ln(n_A), \quad \Delta F_L(N) = E_L(\varepsilon_{LL}, \varepsilon_{LA}, N) - Nk_B T \ln(n_L), \quad (1)$$

118 where $E_A(\varepsilon_{AA}, N)$ and $E_L(\varepsilon_{LL}, \varepsilon_{LA}, N)$ are the total interaction energies of atomic and ligand
 119 cluster on the crystal surface, respectively, ε_{AA} , ε_{LL} and ε_{LA} are the pair-wise atom-atom,
 120 ligand-ligand, and ligand-atom interaction energies measured relative to atom and ligand

121 energies in solution, n_A and n_L are the volume fractions of corresponding bare (unbound)
 122 species in solution and $k_B T$ is the temperature in energy units. The interaction energies
 123 $E_A(\varepsilon_{AA}, N)$ and $E_L(\varepsilon_{LL}, \varepsilon_{LA}, N)$ are the sums of the pair-wise interaction energies assuming
 124 that the atoms/ligands in the nuclei occupy the cells in a square lattice and interact only with a
 125 maximum of four nearest neighbours in the plane and one neighbour beneath it. The minimum
 126 energy configuration of a nucleus on a square lattice is either a square for a wide enough facet
 127 or a rectangle otherwise (see Figure S1 in Supporting Information for details). Figure 1a
 128 illustrates the mechanism of nucleation and growth of NPLs, while Figure 1b shows the typical
 129 shape of the functions $\Delta F_A(N)$ and $\Delta F_L(N)$. The latter curves have serrated shape due to
 130 fluctuations in the number of nearest neighbours for each subsequent atom/ligand added during
 131 the nucleus formation. Figure 1b presents the most interesting case when the ligands form the
 132 critical nucleus much quicker than the atoms due to the lower nucleation barrier $\Delta_{CL} < \Delta_{CA}$
 133 (indicated by the red arrow) despite the fact that the critical size of the ligand nucleus is bigger
 134 than that for atoms, namely $N_{CL} > N_{CA}$ (shown by the arrows' position). The ratio of the
 135 classical nucleation rates for the atoms (W_A) and ligands (W_L) is estimated for the parameters
 136 presented in the caption to Figure 1 as $W_A / W_L \approx 0.1$. Due to the smaller critical nucleus size,
 137 the atoms can nucleate new layers on rather small facets where the ligand's critical nucleus
 138 cannot be formed at all, as illustrated in Figure 2a. The tiny crystals can, therefore, grow until
 139 some of their facets become large enough to accommodate the ligands critical nucleus, as
 140 illustrated in Figure 2c. Once this happens, the corresponding facet is quickly covered with
 141 ligands which then block any further growth on it. However, the narrower facets which are less
 142 likely to be covered with ligands continue supporting the growth process (see Figure 2b). The
 143 most likely outcome, in this case, is the growth of narrow-facets crystals, or NPLs.



144

145 Figure 2. Free energy ΔF of nucleated surface clusters versus the number N of constituent
 146 atoms (blue) and ligands (red) on rectangular crystal faces made of a) $3 \times 4 a_0^2$ (a_0 is the unit
 147 cell length), b) $3 \times 10 a_0^2$, and c) $5 \times 10 a_0^2$ (for other parameters see the caption for Figure 1).
 148 Energy curve for atoms in a) has its maximum at $N=7$ indicating that if it is passed then the
 149 further growth is favourable. In contrast, ΔF for ligands keeps rising meaning that any nucleus
 150 will eventually dissolve. A similar picture is shown in b) for a longer face of the same width.
 151 In a wider face c) both atomic and ligand nuclei can grow further decreasing their energy.

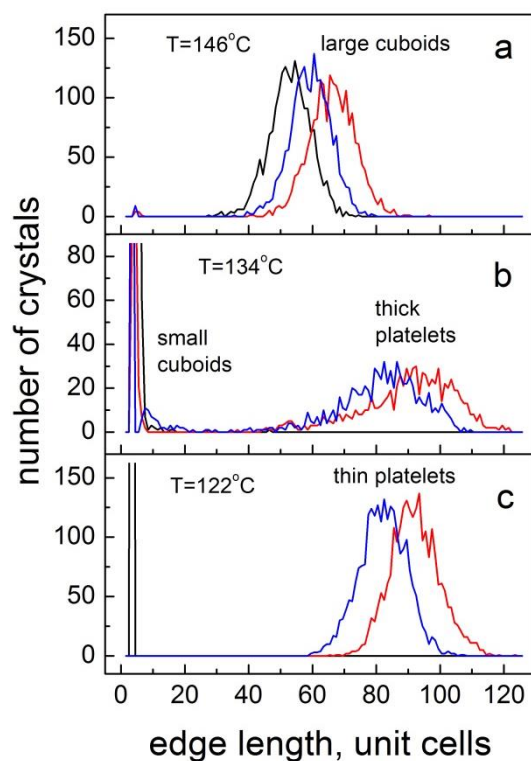
152 Kinetic Monte Carlo Simulations

153 The predictions of our model have been verified numerically using kinetic Monte Carlo (KMC)
 154 method to simulate the growth process of an ensemble of 3000 crystals of tetragonal shape.
 155 Each crystal facet is assigned two reaction rates, one for the formation of a new atomic layer,
 156 and the other one for the creation of a compact layer of ligands. These reaction rates are taken
 157 proportional to the classical nucleation rates of the corresponding critical nuclei

$$158 \quad P_A = K_A \cdot \exp\left(-\frac{\Delta_{CA}}{k_B T}\right), \quad P_L = K_L \cdot \exp\left(-\frac{\Delta_{CL}}{k_B T}\right). \quad (2)$$

159 Here the Zel'dovich factors, $K_A = 1 - \exp\left(-\frac{\Delta_{AA}}{k_B T}\right)$ and $K_L = 1 - \exp\left(-\frac{\Delta_{LL}}{k_B T}\right)$, are proportional
160 to the probabilities for the corresponding critical cluster to grow and spread over the
161 corresponding crystal facet. The energy factor $\Delta_{AA(LL)}$ represents the difference in the free
162 energy given by Eq. (1) of the complete atomic (ligand) layer ($N = N_{facet}$) and that of the
163 corresponding critical cluster ($N = N_{crit}$). At each time step, a single reaction is randomly
164 chosen according to its relative rate, and the corresponding facet is covered with an extra layer
165 of atoms, or with a layer of ligands. In the former case, the four adjacent facets increase their
166 size, and their reaction rates are updated accordingly. In the case of ligand's layer, the chosen
167 facet becomes inactive, and the corresponding reaction rates are set to zero. Initial volume
168 fractions $n_A = n_L = 2.5 \cdot 10^{-4}$ are decreased at every step according to the numbers of deposited
169 atoms/ligands (see Figure S2 in Supporting Information) illustrating the role of n_A .

170 To characterise the average crystal shape qualitatively in the ensemble of crystals we
171 introduce distributions of the short, medium, and long edges for constituent crystals with the
172 following interpretation: If all three distributions are grouped close to each other, the crystals'
173 shapes are close to cubic. If the short edges distribution is placed around low values while the
174 other two are centred around large values, the crystals have plate-like shape. If two of the
175 distributions are centred at low values, and the third one is at large values, the crystals are rod-
176 like.



177

178 Figure 3. Distributions of short (black), medium (blue) and long (red) crystal edges in an
 179 ensemble of 3000 crystals at different temperatures for the initial concentrations of atoms and
 180 ligands in solution $n_A = n_L = 2.5 \cdot 10^{-4}$. All other energy parameters are the same as in the
 181 caption to Figure 1. a) crystals are large and have close to cubic shape (large cuboids), b) a
 182 mixture of small cuboids (the edges are 6–10 a_0) and relatively thick (6–8 a_0) platelets with a
 183 rather broad distribution of lateral sizes, c) thin ($\sim 4 a_0$) platelets with a narrow distribution of
 184 lateral sizes (see also Figure S3 in the Supporting Information).

185

186 Initially, all 3000 crystals are identical cubes of $3 \times 3 \times 3 a_0^3$ (a_0 is unit cell length) volume;

187 hence, all crystal facets have identical pairs of atom-related and ligand-related reaction rates.

188 After about a million simulation steps, the shape of crystals changes, as shown in Figure 3, in

189 terms of the edge distributions. According to Figure 3a, at the higher temperatures (146° C),

190 the crystals' shape is close to cubic, as the ligands do not nucleate critical clusters at this

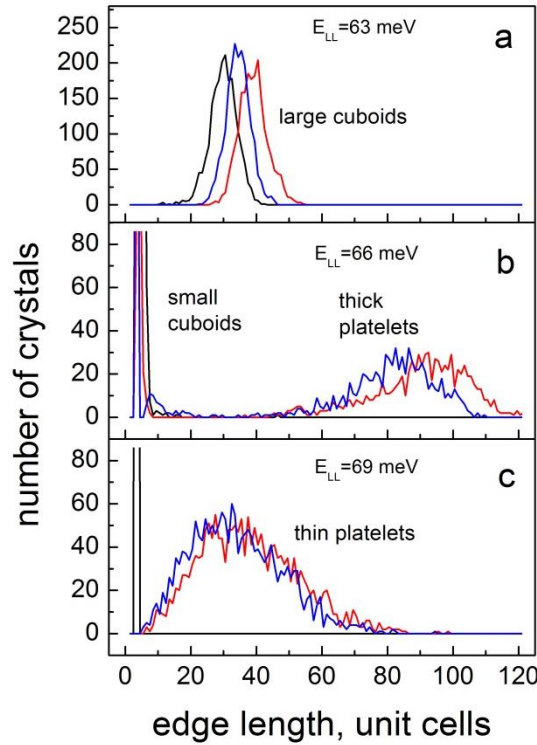
191 temperature; therefore, they cannot affect spontaneous growth of cubic crystals. With a

192 decrease in temperature (see Figures 3b and 3c), the positive entropic contribution to the

193 nucleation barrier and critical nucleus size both decrease and ligands become able to nucleate

194 and produce blocking layers on synthesis facets thus changing the shapes of the crystals.

195 According to Figure 3b, at $T=134^\circ\text{C}$ there is a mixture of crystals; some have the shape close
 196 to cubic (cuboids) with edge sizes $6\text{--}10 a_0$ while the others are platelet-like with the thickness
 197 around $8\text{--}10 a_0$ and the length of $60\text{--}110 a_0$. A further decrease in temperature down to $T=122^\circ$
 198 C (Figure 3c) results in the growth of just thin ($\sim 4 a_0$) platelets.



199

200 Figure 4. Distributions of short (black), medium (blue) and long (red) crystal edges in an
 201 ensemble of 3000 crystals for $\varepsilon_{AA} = 109\text{meV}$, $\varepsilon_{LA} = 171\text{meV}$, $n_A = n_L = 2.5 \cdot 10^{-4}$, $T = 134^\circ\text{C}$
 202 and different values of ε_{LL} . a) $\varepsilon_{LL} = 63\text{meV}$, crystals grow as cuboids (see text for
 203 explanation), b) $\varepsilon_{LL} = 66\text{meV}$, this is the same as the curves in Figure 3b, a mixture of small
 204 ($6\text{--}10 a_0$) cuboids and thick ($6\text{--}10 a_0$) platelets, c) $\varepsilon_{LL} = 69\text{meV}$, crystals grow as thin ($\sim 4 a_0$
 205) platelets with very broad lateral size distribution.

206 In simulations, we can also easily vary the ligand-ligand interaction energy ε_{LL} , to study
 207 how the ligand choice affects the crystal shape. Experimentally, this energy can be tuned by
 208 varying the length of chain-like molecular ligands: the longer the chain, the higher ε_{LL} . Note,
 209 that the value of ε_{LA} can be still kept the same if the atomic group binding the surface remains

210 unchanged. As shown in Figure 4, the effect of increasing ε_{LL} is similar to that of decreasing
211 the temperature. In particular, for $\varepsilon_{LL} = 63\text{meV}$ (Figure 4a), the edge length distributions are
212 very similar to those shown in Figure 3a (the difference in peak positions is due to different
213 growth time). The distributions shown in Figure 4b for $\varepsilon_{LL} = 66\text{meV}$ are the same as in Figure
214 3b and are presented for comparison. The distributions for $\varepsilon_{LL} = 69\text{meV}$ in Figure 4c like those
215 in Figure 3c show thin ($\sim 4a_0$) platelets, but the platelets' lateral sizes vary significantly more
216 than those in Figure 3c. This could be due to a very low probability of new atomic layer
217 formation for small crystals (see Supporting Information for details). Any further increase in
218 ε_{LL} results in a significant decrease in ligands layer nucleation barrier, therefore, all the seed
219 crystals' facets become covered with ligands straight away, thus inhibiting any further growth
220 (see Figures S5 and S6 in Supporting Information).

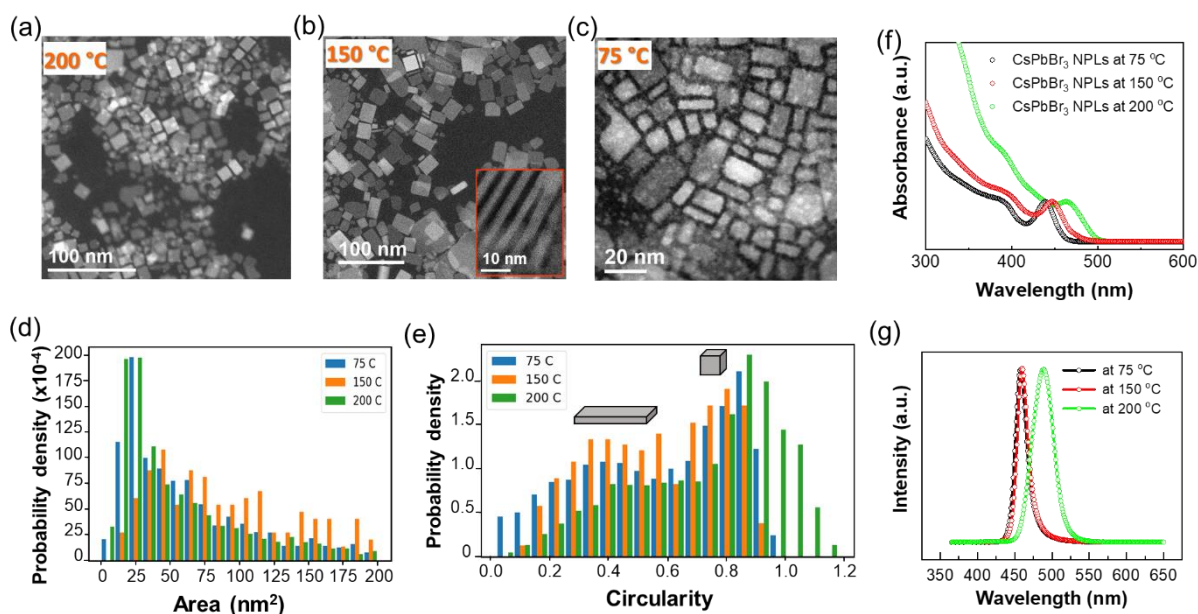
221 The rationale behind the nucleation-controlled crystal growth mechanism can be
222 understood as follows. The conditions for wide crystal facets to be covered with ligands leaving
223 the narrow facets uncovered are i) a relatively broad distribution of facet widths (crystal edge
224 sizes), and ii) a low enough crystal growth rate. Both these conditions can be met if the growth
225 process is nucleation controlled. Indeed, such growth is characterised by a relatively low
226 probability of layer formation; hence it allows for significant fluctuations in the facet sizes (see
227 Supporting Information). Simultaneously it also means a moderate growth rate giving ligands
228 enough time to form compact layers on broader facets. If the two broader parallel facets are
229 covered with ligands, then the crystal grows as an NPL. If the broader facets are perpendicular
230 to each other, then we would expect the growth of nanorods. The latter regime has also been
231 found in our KMC simulations (see Figure S7 in the Supporting Information). By increasing
232 the temperature or decreasing the ligand-ligand interaction energy ε_{LL} , the probability for a

233 ligand to nucleate and form a compact layer can be significantly reduced, even down to zero.
234 This decrease results in the growth of bulk crystals rather than platelets (Figures 3a and 4a).

235 Based on the obtained KMC simulation results, we can identify two main trends taking
236 place upon variation of such system parameters as i) temperature (Figure 3) and ii) ligand-
237 ligand interaction energy (Figure 4). We found that with decreasing temperature, the growing
238 crystals' shape changes from cuboids to platelets. A similar effect takes place when we
239 gradually increase ligand-ligand interaction energy. Both effects were observed experimentally
240 on an example of CsPbBr₃ crystals using the three-precursors synthetic approach.

241 **Experimental verification**

242 To characterise the shape of synthesised nanoparticles (see details below and in
243 Supporting Information), the nanoparticles' crystal structure has been characterised using
244 scanning transmission electron micrograph (STEM) analysis. Photoactive perovskites are
245 generally beam-sensitive,^{53, 54} and under electron beam exposure the lead (Pb) atoms can
246 segregate out of the CsPbBr₃ crystal structure.⁵⁵ However, since we are interested in crystal
247 shape rather than high-resolution imaging, the Pb segregation had little effect on the particle
248 size distribution. We also optimised the STEM imaging parameters to avoid the structure
249 damage by the electron beam while keeping the required image resolution (see Supporting
250 Information for details). We examine the optical properties of the synthesised nanoparticles
251 using UV–vis spectroscopy and steady-state PL measurements.



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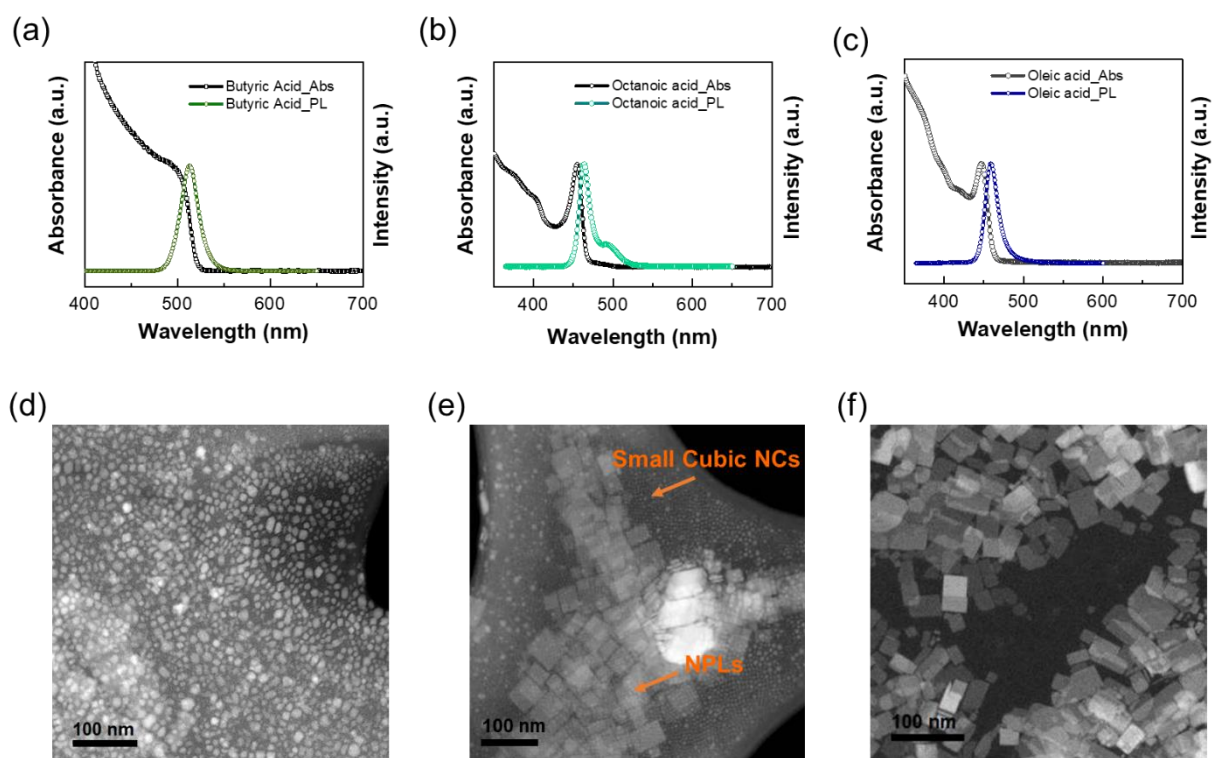
253 **Figure 5. Influence of reaction temperature on the optical and structural properties of**
 254 **caesium lead tribromide perovskite (CsPbBr₃) nanocrystals grown in the presence of oleic**
 255 **acid.** (a) (a–c) Low-magnification scanning transmission electron (STEM) images for CsPbBr₃
 256 NCs synthesised from three-precursor approach: (a) at 200 °C giving cuboid crystals, (b) at
 257 150 °C giving quasi-NPLs (reaction time ~10 seconds); inset: high-resolution electron
 258 microscopy (HRTEM) where NPLs prepared at 150 °C stack face-to-face or edge-on with the
 259 lateral size of (10–15nm), and the thickness of ≥3 nm), and (c) at 75 °C show platelets with
 260 lateral size (5–10nm). (d) Normalised histogram of the particle size distribution for the three
 261 conditions (T=200, 150, and 75 °C). (e) Normalised histogram of the particle circularity (see
 262 text for definition) for the three conditions (T=200, 150, and 75 °C) (f) Normalised absorption
 263 spectra of as-prepared pristine CsPbBr₃ NPLs (unwashed) in toluene where the NCs are
 264 exhibiting a quantum confinement effect. (g) Their normalised steady-state photoluminescence
 265 (PL) spectra.

266 *Testing the Temperature Effect.* The impact of reaction temperature on the shape of CsPbBr₃
 267 nanocrystals has been studied in the range of 75–200 °C while keeping the ratio of oleic acid
 268 (1.5 mL)/oleylamine (1 mL) constant. Panels (a) through (c) in Figure 5 show representative
 269 STEM-HAADF images of the three samples prepared at 200, 150, and 75 °C, respectively. As
 270 these images depict the particles in projection, we need to perform further analysis to better
 271 characterise their three-dimensional shape. We used ParticleSpy python package⁵⁶ (which
 272 wraps Scikit-image⁵⁷ and Hyperspy⁵⁸ for image analysis and segmentation) and measured the
 273 total of 2635, 272, and 1524 particles from 200, 150 and 75 °C samples, respectively. We
 274 measured two parameters- presented as histograms in panels (d) and (e): (i) area of the detected

275 particles and (ii) their circularity, defined as $f_{circularity} = \frac{4\pi A}{P^2}$, where A is the particle's area, and
276 P is the particle's perimeter. We find from the area histogram (panel d) that the peak frequency
277 in area of the particles for 75 and 200 °C case is close to 25 nm², whereas for 150 °C case it
278 seems to be slightly lower than 50 nm². The circularity parameter, assuming the particles are
279 distributed close to randomly onto the carbon grid support, allows us to make a distinction
280 between the square cuboid and the rectangular cuboid. The inset of panel (b) shows that we
281 routinely encounter particles that have landed on their narrow sides, but there well may be a
282 tendency for them to land on the support with their broad face. Thus, making a distinction between
283 the square cuboid and NPLs (rectangular cuboid) can be drawn indirectly from the circularity plot. The
284 circularity of a perfect circle is 1.0, the circularity of an ideal square is 0.78 while the circularity of a
285 rectangle with a side length of (a x 3a) is 0.59 and of a rectangle with a side length of (a x 5a) is 0.44.
286 Accordingly, in the case of rectangular cuboids, when their narrow face being projected, it would
287 contribute to the peaks around 0.4-0.5 range in the circularity plot. In contrast, the perfectly square
288 cuboid would show a singular peak at 0.78. We expect to see two peaks in the circularity histogram
289 even in the case of pure NPLs; where a fraction of NPLs showing their widest face would look like
290 square cuboids, while those showing one of the narrow faces would be looking like rectangular cuboids.
291 Based on the above and the circularity histogram in panel (e), we can observe that the 150 C sample
292 shows the strongest frequency of the circularity factors of 0.4 with respect to the 0.78 corresponding to
293 perfect square cuboid shape, followed by the 200 C and 75 C cases.

294 We characterise the optical properties of the as-synthesised batches. We find that decreasing
295 the temperature from 200 °C down to 150 °C and below results in a significant shift of the PL
296 peak position from 490 nm down to 458–460 nm as illustrated in Figure 5f–g The absorption
297 spectrum exhibits a sharp excitonic peak, which also shifts from 465 nm at T=200 °C, down to
298 448 nm at 150 °C and to 437 nm at 75 °C. The blue shift of the PL spectrum and the of the
299 excitonic absorption peak are attributed to the strong quantum confinement (in NPLs).^{18, 33, 34}

300 We note that Bekenstein *et al.*,¹⁸ examined the influence of the reaction temperature on
 301 the morphology of the CsPbBr₃ nanocrystals, and they found a similar temperature dependence
 302 on the shape's tunability from cuboids to platelets. However, in their case, the value of
 303 maximum temperature that can be reached for NPLs' formation is below 130 °C, i.e.
 304 significantly lower than our 150 °C. We believe that the cut-off temperature for producing
 305 NPLs is mainly influenced by the content of the reaction mixtures and their concentration.



306
 307 Figure 6. Effect of ligand-ligand interaction on the optical and structural properties of CsPbBr₃
 308 nanocrystals grown at 140 °C. (a–c) Normalised absorption and steady-state
 309 photoluminescence (PL) spectra of as-prepared pristine CsPbBr₃ nanocrystals (unwashed) in
 310 toluene in the presence of (a) butyric acid, (b) octanoic acid, and (c) oleic acid. (d–f) The
 311 corresponding low-magnification scanning transmission electron (STEM) HAADF images for
 312 CsPbBr₃ NCs synthesised from a three-precursors approach using acetate salts giving cubic
 313 structure in case of butyric acid; (d), mixed cubic/NPLs in case of octanoic acid (e), and (f)
 314 NPLs in case of oleic acid where the reaction time is 20 seconds.

315 *Effect of Ligand-ligand interaction energy.* To check the influence of ligand-ligand interaction
 316 energy ϵ_{LL} , we carried out the CsPbBr₃ crystal growth in the presence of different ligands:
 317 butyric acid, octanoic acid, and oleic acid. Recently Manna and co-workers⁴¹ reported the effect
 318 of acid/amine ratio on the dimensionality of the CsPbBr₃ nanocrystals from cubic to platelets.

319 They found that the addition of oleylamine in the presence of excess acids which is needed for
320 protonation and formation of oleylammonium, which is essential for the formation of the 2D
321 structures like platelets or rods.^{41, 59} In another study, they examined amine-free synthesis of
322 CsPbBr₃ nanocrystal, whereby they obtained pure cubic crystals and no any 2D shapes.⁶⁰
323 Therefore, we sought to investigate the influence of the fatty acid chain length on the
324 concentration and solubility of oleylammonium moiety and consequently the growth where we
325 add oleylamine with a fixed concentration in all experiments as the amine source. To
326 characterise the relative strength of ligand-ligand interaction for these acids, we considered
327 their boiling points and used Trouton's rule^{61, 62} to relate the former to ligand-ligand interaction
328 energy. According to Trouton's rule, the latter is proportional to average thermal energy at the
329 boiling temperature, namely $\varepsilon_{LL} \approx \frac{3}{2} k_B T_{boil}$, which for the above set of ligands are
330 $T_{boil} = 160^\circ C$, $\varepsilon_{LL} \approx 37 meV$ – butyric acid, $T_{boil} = 240^\circ C$, $\varepsilon_{LL} \approx 44 meV$ – octanoic acid, and
331 $T_{boil} = 360^\circ C$, $\varepsilon_{LL} \approx 54 meV$ – oleic acid.

332 The obtained values of ε_{LL} most likely give the lowest estimate for the interaction energies
333 between ligands on the crystal surfaces because the ligands on a flat surface are at least partly
334 oriented hence may interact stronger than in the solution. Our experimental results clearly show
335 the shift of the PL peak position towards the blue spectral region from ~512 nm for butyric
336 acid to a very narrow PL (with FWHM = 17 nm) at ~460 nm for oleic acid (see Figures 6a–6c)
337 indicating a decrease in at least one dimension of the crystals, i.e. the thickness of NPLs. We
338 also notice that the PL spectrum for octanoic acid has two peaks, as shown in Figure 6b
339 indicating inhomogeneity of the crystal ensemble from this batch. Figures 6d–6f present the
340 corresponding STEM images of the crystal ensembles for the three synthetic conditions. Panel
341 6e also illustrates the inhomogeneity of the ensemble of crystals. In the case of butyric acid
342 (Figure 6d), the product is nanocubes and virtually no NPLs are present. We observe NPLs

343 only in case of using oleic acid as the acid source in the reaction – see Figure 6f. However, we
344 obtain two distinct shapes, small cubic and NPLs, in the same reaction pot by replacing oleic
345 acid by lower carbon chains of octanoic acid. This explains the multiple peaks in the PL of that
346 sample. This observation is consistent with the trend predicted by our KMC simulations, as
347 illustrated in Figure 4. We investigated the surface of the NPLs prepared at 150 C using oleic
348 acid using attenuated total reflection Fourier transform infrared powder spectroscopy (ATR-
349 FTIR) and proton nuclear magnetic resonance (¹HNMR), see Figures S11–12. Both FTIR and
350 ¹HNMR show the presence of fatty chain ligands (oleic acid, oleylamine and mainly
351 oleylammonium moiety) terminating the surface of the NPLs.

352 Similarly, Cho *et al.*,³² observed multiple peaks upon using ligands with the shorter
353 carbon chains in the synthesis of NPLs. We explain the tunability of the particles' morphology
354 as a function of the surface ligand chain length as the following. Increased ligand's chain length
355 results in a stronger ligand-ligand interaction and higher boiling point. Such ligands form the
356 compact layer on the crystal surfaces easier hence can help to generate NPLs at a higher
357 temperature than ligands with shorter chain length in agreement with our KMC simulation
358 results.

359 **Conclusions**

360 The presented simulation and experimental results are consistent with the proposed model of
361 NPLs formation based on competitive nucleation of atoms and ligands on crystal facets. Both
362 modelling and experimental studies found that decreasing the crystal growth temperature or
363 using stronger interacting ligands (the ones with higher boiling temperature) generally helps to
364 obtain crystals in the form of platelets. Development of a more sophisticated theoretical-
365 modelling framework of ligand-controlled crystal growth would be beneficial to improve
366 control over crystal shape and to predict conditions for the formation of rod-like and platelet-

367 like crystals with a given aspect ratio. Such studies are extremely important for the growing
368 demands of nano-electronics and nano-photonics for sophisticated crystal shapes. Our work
369 also represents a significant advance in the particular problem of synthesis of well-controlled
370 anisotropic CsPbBr₃ shapes where the three-precursor approach allows stoichiometry control
371 on the concentration of all elements in the reaction rather than the common use of lead halide
372 (PbX₂) as the only source of anions and cations.

373 **EXPERIMENTAL SECTION:**

374 All procedures were carried on a Schlenk line under oxygen-free conditions and nitrogen gas
375 flow.

376 **Materials.** All chemicals were used as received without further purification. Lead acetate
377 trihydrate (Pb(CH₃COO)₂·3H₂O, 99.99%), caesium carbonate (Cs₂CO₃, reagent Plus, 99%), 1-
378 octadecene (ODE, technical grade, 90%), oleylamine (OLAM, 70%), butyric acid (≥99%),
379 octanoic acid (≥98%), oleic acid (OA, 90%), and HBr acid (48% in water) were purchased
380 from Sigma-Aldrich and used without further purification. All solvents such as toluene, diethyl
381 ether and methyl acetate were anhydrous, and the absolute ethanol were purchased from Sigma-
382 Aldrich.

383 **Preparation of Oleylammonium Bromide Precursor.**

384 The reaction was performed in an ambient condition in fume hood following the procedure
385 reported by Protesescu *et al.*,⁵¹ with modification as following. In a 500 mL flask, oleylamine
386 (OLA, 25 mL), HBr (48% in water, 30 mL), and ethanol (100 mL, absolute >99.8%) were
387 mixed and vigorously stirred for 4 hours at room temperature. Then the content of the flask
388 was evaporated at 40 °C via rotary evaporation to remove all solvents. The obtained product
389 was dissolved back in the minimum amount of absolute ethanol for the re-precipitation process
390 to purify the product from any contamination. The solution was titrated drop by drop of diethyl
391 ether until very few crystals start to precipitate. The flask was moved to the fridge at (−10 °C)

392 for overnight to complete the re-precipitation of pure white crystals. The white precipitate was
393 then filtrated using Buchner filtration and placed for drying in a vacuum dryer oven at 40 °C
394 for overnight.

395 **Preparation of Caesium Oleate Precursor.**

396 Synthesis of Caesium (Cs)-oleate was done according to literature.³⁰

397 **Synthesis of Caesium Lead Tribromide Perovskite Nanoplatelet.**

398 In a typical synthesis of pristine CsPbBr₃ NPLs, a 2mmol of lead acetate trihydrate (76 mg)
399 was dissolved in 1.5 mL oleic acid and 1 mL oleylamine in 5 mL of octadecene (ODE) at 120
400 °C, using the standard air-free technique. A previously prepared and stored under an inert
401 atmosphere, 0.6 mL (0.125 M) of caesium oleate (preheated at 100 °C) was then injected to the
402 solubilised lead precursor and the reaction flask left to continue stirring under vacuum at 120
403 °C for 1–2 hours. Then, the temperature was increased to 150 °C under the flow of N₂. In a
404 separate vial under N₂, six mmol of oleylammonium bromide (0.21 g) was dissolved in 2 mL
405 of anhydrous toluene and then was swiftly injected into the reaction flask at 145–150 °C. This
406 resulted in changing the colour of the reaction mixture from colourless to transparent light
407 green (chartreuse) colour indicating the formation of the CsPbBr₃ NPLs. The growth of the
408 NCs was halted after 10–20 seconds by removing the heat source, and the system was cooled
409 with ice-water bath while simultaneously injecting cold anhydrous toluene into the reaction
410 mixture. The crude solution was collected into a centrifuge tube and was centrifuged for 10
411 min at 8000 rpm. The supernatant was collected for further use, and any precipitate was
412 discarded.

413 **Washing Process.**

414 For further use or characterisations, these NCs went through a washing process. Typically, we
415 purify the reaction crude solution by precipitating the NPLs with methyl acetate (anti-solvent)

416 and subsequently re-dissolve in toluene to remove excess unreacted precursors. The toluene
417 colloidal solution is added to methyl acetate in a ratio of 1 to 3. Then this mixture is centrifuged
418 at 8000 rpm for 5 minutes to precipitate the NPs on the sidewall of the centrifuge tube. We
419 then discard the supernatant and re-dissolve the precipitate in toluene. This washing process is
420 repeated twice before further using of the NCs in device fabrication.

421 **Characterisation**

422 **Microstructure Characterisation**

423 Aberration-corrected scanning transmission electron microscopy (STEM) was used for atomic
424 resolution characterisation of the as-synthesised NPLs. Samples were deposited on standard
425 lacey carbon grids suspended in toluene (after two cycles of washing by methyl acetate) and
426 left in the air to dry. STEM imaging was performed on an image and probe-corrected JEOL
427 ARM300CF, operated at 300 kV accelerating voltage. We used a probe current of 2.2 pA for
428 imaging (using a 20 μm probe-forming aperture), providing a probe convergence semi-angle
429 of 16.4 mrad. The annular dark-field signal was acquired at 20 cm camera length, summing the
430 scattered electrons over the range of 36.7 and 200 mrad in semi-angle. This choice of imaging
431 condition, with low beam current (amounting to around 50 $\text{e}^-/\text{\AA}^2$ dose per probe position at 2.4
432 μs dwell time at 3M magnification) was necessary to minimise the effect of electron induced
433 beam damage.

434 *UV-vis Absorption* spectra were recorded using a commercial Varian Cary 60 in a 1 cm cuvette.

435 *Steady-state PL* measurement was carried out with an automated spectrofluorometer
436 (Fluorolog, Horiba Jobin-Yvon), with a 450 W Xenon lamp excitation source and a
437 photomultiplier tube detector. The excitation wavelength was 350 nm.

438 **ASSOCIATED CONTENT**

439 **Supporting Information**

440 The Supporting Information is available free of charge on the

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451 Notes

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