

Haze and Cloud structure of Saturn's North Pole and Hexagon Wave from Cassini/ISS imaging

J.F. Sanz-Requena^a, S. Pérez-Hoyos^b, A. Sánchez-Lavega^b, A. Antuñano^b, Patrick G.J. Irwin^c

a) Departamento de Ciencias Experimentales. Universidad Europea Miguel de Cervantes, Valladolid, Spain.

b) Departamento de Física Aplicada I, Escuela Técnica Superior de Ingeniería, Universidad del País Vasco, Bilbao, Spain

c) Atmospheric, Oceanic and Planetary Physics, University of Oxford, Clarendon Laboratory, Parks Road, Oxford OX1 3PU, UK

Abstract

In this paper we present a study of the vertical haze and cloud structure in the upper two bars of Saturn's Northern Polar atmosphere using the Imaging Science Subsystem (ISS) instrument onboard the Cassini spacecraft. We focus on the characterization of latitudes from 53° to 90° N. The observations were taken during June 2013 with five different filters (VIO, BL1, MT2, CB2 and MT3) covering spectral range from the 420 nm to 890 nm (in a deep methane absorption band). Absolute reflectivity measurements of seven selected regions at all wavelengths and several illumination and observation geometries are compared with the values produced by a radiative transfer model. The changes in reflectivity at these latitudes are mostly attributed to changes in the tropospheric haze. This includes the haze base height (from 600±200 mbar at the lowest latitudes to 1000±300 mbar in the pole), its particle number density (from 20±2 particles/cm³ to 2±0.5 particles/cm³ at the haze base) and its scale height (from 18±0.1 km to 50±0.1 km). We also report variability in the retrieved particle size distribution and refractive indices. We find that the Hexagonal Wave dichotomizes the studied stratospheric and tropospheric hazes between the outer, equatorward regions and the inner, Polar Regions. This suggests that the wave or the jet isolates the particle distribution at least at tropospheric levels.

Keywords:

Atmospheres, structure; Saturn; Saturn, atmosphere; Radiative transfer

Highlights

- We study the North Polar Region of Saturn based on Cassini ISS images.
- The changes in reflectivity are attributed to changes in the tropospheric haze.
- The Hexagonal Wave dichotomizes the latitudes: the outer, and the inner regions.
- Retrieved atmospheric model are in agreement with dynamical models of the polar region.

1. Introduction

The North Pole of Saturn is a region where we find unique atmospheric features as we move from the Equator to higher latitudes. Examples of these are the Hexagon Wave, a fast eastward jet, a large number of “puffy” clouds mixed with local cyclonic and anticyclonic vortices, and the polar vortex, which includes a fast eastward jet (Godfrey, 1988; Fletcher et al., 2008; Sánchez-Lavega et al., 2014; Antuñano et al., 2015, 2018).

Saturn’s Hexagon Wave is a singular feature centered close to 75° N planetocentric latitude (all latitudes in this work will be given as planetocentric). The feature was discovered in 1980–1981 in images taken during Voyager 1 and 2 flybys (Godfrey, 1988). In 1991 the Hexagon Wave was observed again after a long polar Saturnian winter by the Hubble Space Telescope (Caldwell et al., 1993) and, afterwards, even with ground-based telescopes (Sánchez-Lavega et al., 1993). This showed that it is a long-lived atmospheric feature. This was confirmed one Saturnian year after its discovery with the arrival of the Cassini mission in 2004. Since 2012, the Hexagon Wave has also been clearly and routinely discernible in images captured by ground-based telescopes and amateur astronomers (Sanchez-Lavega et al., 2014). In short, the Hexagonal Wave has been studied since 1980 until 2017 and due to its stable rotation period, it has been proposed that it could track the rotation rate of the planet (Sanchez-Lavega et al., 2014).

Since the arrival of Cassini at Saturn in 2004, the Hexagon Wave was observed in 2006–2007 in the thermal infrared using the Visible and Infrared Mapping

Spectrometer (VIMS) (Brown et al., 2004) at 5 μm , while the North Pole was still in winter with little or no solar illumination. Since 2008, the Hexagon Wave has been observed in reflected sunlight throughout the remaining years with the Cassini Image Science Subsystem (ISS) cameras (Antuñano et al. 2015; Sayanagi et al., 2017). It is well known that Saturn shows an intense zonal circulation at the cloud top level formed by a system of jet streams that alternate their east-west direction depending on latitude (see e.g. García-Melendo et al., 2011 for a review). Saturn's North Pole Hexagon Wave encloses a fast ($\sim 100 \text{ ms}^{-1}$) eastward jet at latitude 75.8° N (Godfrey, 1988).

The Hexagon Wave has been proposed to be a vertically-trapped Rossby wave (Allison et al., 1990; Sánchez-Lavega et al., 2014) located in a range of latitudes from 75.3° to 76.3° N . It has a planetary scale, with a length of approximately 30,000 kilometers centered at the North Pole of the planet and with wave number six. It could possibly result from an instability of the strong jet in its interior (Barbosa-Aguiar et al., 2010; Morales-Juberías et al., 2011). Nothing like a polygonal wave has been found in any other planet of the Solar System, except some features in the eye of Earth hurricanes (Kossin and Schubert, 2001). Jupiter for example, displays a complex structure of polar waves, but with no polygonal shapes (Sánchez-Lavega et al., 1997; Barrado-Izagirre et al., 2008).

Another interesting atmospheric features at high latitudes are the intense cyclonic polar vortices. These vortices were detected in Saturn's poles in the Cassini era, extending in latitudes from 88.5° to 90° north and south (Sánchez-Lavega et al., 2006; Dyudina et al., 2008, Fletcher et al., 2008; Baines et al., 2009; Dyudina et al., 2009; Sayanagi et al., 2013). Both vortices are enclosed by a very fast ($\sim 140\text{-}160 \text{ ms}^{-1}$) eastward jet at latitude 88.5° (Antuñano et al, 2015, Sayanagi et al., 2017).

The dynamics at Saturn polar latitudes is particularly appealing for a number of reasons (Sayanagi et al., 2016). For example, the presence of intense polar vortices is particularly intriguing, as Juno mission has not revealed anything similar in Jupiter's atmosphere. Given the tilt of the rotation axis, Saturn's poles suffer long periods of darkness during the polar winter and, although seasonal changes have been reported at the stratosphere in both the temperature field and hydrocarbon distribution (Fletcher et al., 2015), the dynamical features described above were able to survive from one season to the next without noticeable changes. This suggests deeply rooted structure that have been suggested to be linked with the internal rotation period (Sánchez-Lavega et al., 2014).

In order to understand such lively atmospheric dynamics it is essential to know the vertical distribution of haze and clouds, which are used as its tracers. This also requires the knowledge of the physical and optical properties of the cloud and haze particles in the stratosphere and upper troposphere of Saturn. Our current understanding of Saturn's clouds and hazes is constrained by several decades of remote sensing data. Thus, we can divide Saturn into three large separate latitudinal regions (Pérez-Hoyos et al., 2005) and an overall vertical structure formed by a thin stratospheric haze and a denser tropospheric haze, both above a thick cloud layer (Pérez-Hoyos et al., 2005; Roman et al. 2013). An excellent review of the state of the art regarding Saturnian hazes and clouds can be found in West et al. (2009). Particles in the uppermost stratospheric haze are commonly assumed or obtained to be small (tenths of microns), but most likely they are not spherical in view of results regarding Jupiter's atmosphere (West et al., 1991). The deepest detectable particle layer in visible wavelengths is putatively formed by ammonia ice and has uncertain properties that require longer and more penetrating wavelengths than those used in this work (Fletcher et al., 2008).

Most of the information contained in the visible light scattered by the atmosphere comes from the upper tropospheric cloud, whose variable cloud-top pressure strongly dominates the brightness of the planet at near infrared methane bands (Roman et al., 2013). While very often assumed to be spherical (Karkoschka et al., 2005), it is known that their phase function does not match this shape and some efforts have been performed in order to retrieve a more accurate description (Tomasko and Doose, 1984; Pérez-Hoyos et al., 2016). This general picture of the vertical structure of particles is able to explain also the structure of particle features of the atmosphere (Roman et al., 2013), such as vortices (del Río-Gaztelurrutia et al., 2010) or the periodic giant storms (Sanz-Requena et al., 2011).

However, no previous work has been able to study the northern polar region of Saturn in the context of a radiative transfer model of the reflected sunlight. The orbits by the Cassini orbited allowed an unprecedented spatial resolution over the pole and provided access to a region of the planet that had been unexplored so far. For example, Cassini ISS polarization images of the region (West et al., 2015) revealed changes in the aerosol properties inside and outside the Hexagon but a quantitative analysis is still missing. Retrievals of the properties of the upper tropospheric cloud and stratospheric hazes in the polar region has important implications for studies of the dynamical coupling between the stratosphere and troposphere (Del Genio et al., 2009), and the

composition and chemistry in the stratosphere (Fouchet et al., 2009). Particularly important is to understand how singular dynamical features observed at tropospheric level, like the already mentioned hexagon and its jet and the polar vortex, penetrate and leave their imprint at the stratospheric level. Comparison with dynamical conditions in the stratosphere, via thermal winds and static stability conditions from temperature data can shed light on vertical wave propagation in the polar stratosphere, for example (Sánchez-Lavega et al., 2017). The long-term unchanging behavior observed in the tropospheric jets and upper cloud morphology (Antuñano et al., 2017), but with changes in the temperature and ortho-para hydrogen distribution could influence the cloud structure (Fletcher et al., 2016). The aerosol vertical distribution has a profound influence on the heating and cooling rates in the stratosphere where the insolation seasonal cycle can be studied in detail (Sylvestre et al., 2015; Fletcher et al. 2016).

The goal of this paper is to evaluate the structure of the clouds and hazes and the distribution of aerosols and particles in the upper troposphere and lower stratosphere of Saturn's North Pole and its surrounding area, using Cassini Image Science Subsystem (ISS) data sets in different filters. Baines et al. (2009) modeled the properties of clouds below this level (altitude range 2-5 bar) using Cassini-VIMS spectra in the 5 μm wavelength range. In order to avoid complications arising from the temporal evolution of the atmosphere, we are restricted to a snapshot around 2013 when the observations used here were made. In this paper we analyze the variation of the absolute reflectivity with observation/illumination geometries at filters from 420 nm (VIO) to the deep methane band at 890 nm (MT3). We intend to build the simplest atmospheric model that concurrently satisfies the observed reflectance and contrast at multiple wavelengths and viewing angles. By exploiting the wavelength and geometric dependencies in the radiative transfer equations, we will be able to constrain different atmospheric parameters, mostly of the tropospheric haze around the tropopause level

The paper is organized as follows: Section 2 is devoted to a short description of the observations used in this work. Section 3 covers the radiative transfer model, including the description of the vertical cloud structure model and the a priori assumptions. Results are presented and discussed in Section 4. We also present in this section the sensitivity to the model parameters. The results are discussed in Section 5 in terms of the local dynamics. A summary of the main conclusions of this work is presented in Section 6.

2. Observations

2.1. Description of the observations

In this study we have used 40 images taken with the Imaging Science Subsystem (ISS) onboard the Cassini spacecraft. A full description of the ISS instrument can be found in Porco et al. (2004). We show in Figure 1 a representative set of the Saturn images used in this work, shown as polar projections. Images were taken from June 3 to June 26, 2013 with five different filters, all pertaining to ISS 2083. In Table 1 we show the image identification number, date of observation, filter name, date and time of image acquisition, the sub-spacecraft planetocentric latitude B , the sub-solar planetocentric latitude B' and the phase angle α , defined as the observer-planet-Sun angle (Sánchez-Lavega, 2011). The observing period was close to Saturn's Northern Hemisphere summer solstice (West et al., 2009). All the images were navigated using PLIA software (Hueso et al., 2010) and photometrically calibrated to absolute reflectivity using Cassini Imaging Science Subsystem CALibration software (CISSCAL v3.6) described by Porco et al. (2004) and West et al. (2010).

The selection includes two broad-band filters at short wavelengths, violet (VIO, 420 nm) and blue (BL1, 451nm), as well as three near-infrared narrow-band filters matching methane bands MT2 (727nm), MT3, (890 nm) and an intermediate continuum filter (CB2, 752 nm). Transmission curves can be found in Porco et al. (2004). A representative image of Saturn in each of the five filters is shown in Figure 1. VIO and BL1 filters (Fig 1a and Fig. 1b) are sensitive to the colors of the clouds and hazes, which provide compositional information and scattering properties at various heights, and to Rayleigh scattering by the H_2 and He atmosphere. In images taken with the filters BL1 and VIO the interior of the Hexagon Wave is brighter than the exterior and a gradual darkening is observed as we approach the pole.

The methane-band filters (MT2, intermediate absorption, and MT3, deep absorption, Figures 1c and 1e) are sensitive to the upper tropospheric haze layer (Pérez-Hoyos et al., 2016). These filters sense particles at altitudes between 60 mbar and 250 mbar (West et al., 2009; García-Melendo et al., 2009, 2011). The continuum band filter (CB2, 752 nm, Fig.1d) is sensitive to an intermediate region of the tropospheric haze (altitudes between 350 mbar and 700 mbar, García-Melendo et al., 2009, 2011), down to the top of the tropospheric cloud deck, assumed here to be located at 1.4 bar and

putatively formed of ammonia ice (Sanchez-Lavega, 2011). At the wavelengths of the CB2 filter, sunlight penetrates the hazes and Saturn's North polar region reveals a variety of dynamical features, such as an ample field of 'puffy clouds' with sizes between 10 and 500 km, and cyclones and anticyclones of different sizes and lifetimes distributed in the region (Antuñano et al., 2018). These features are usually not observable at the wavelengths of the VIO, MT2 and MT3 filters.

2.2. Data clustering and selection

To divide the range of latitudes studied here (from 53° to 90° N) into a manageable number of sets, we used a K-means supervised clustering algorithm (MacQueen, 1967) as in Pérez-Hoyos et al. (2012). We initially populated seven clusters manually for each phase angle. This was done to avoid differences in viewing and illumination geometry that are sometimes greater than the reflectivity changes from one cluster to another at a given geometry. Then, the algorithm classifies the rest of the data assigning each instance to the nearest group. Each cluster center is updated to be the average of its constituent members. The algorithm converges when no more changes are possible in the allocation of clusters.

We show in Fig. 1f, the whole range of latitudes divided into 7 families. Regions 1, 2 and 3 correspond to latitudes equatorward of the Hexagonal Wave. Region 1 covers a bright zone from 53° to 57° N, region 2 a dark belt from 57° to 65° N and region 3 a zone again from 65° to 73° N. Region 4 corresponds to latitudes 73° to 77° N that encloses the Hexagonal Wave (Sánchez-Lavega, et al., 2014). Regions 5, 6, and 7 are associated with latitudes closer to the North Pole, comprising 77° to 90° N. Region 5 is a polar region which shows no cloud structure in the continuum CB2 filter, while region 6 is composed by samples with clouds bright at CB2. Finally, region 7 is the polar vortex itself, which looks dark at all filters and dates. These regions correspond to areas of different mean zonal flow vorticity (cyclonic–anticyclonic) according to the wind velocity profile shown in Figure 2 (García-Melendo et al., 2011; Antuñano et al., 2015, 2018). In Figure 3, we show an example of the actual data in Region 3 for a couple of filters, together with their average and standard deviation. This reduced data set will be used to retrieve the model parameters.

3. Methodology

3.1 Radiative Transfer code

In this work we have used the radiative transfer code and retrieval suite NEMESIS (Non-Linear Optimal Estimator for Multivariat ESpectral AnalySIS) developed by the Oxford team (Irwin et al., 2008). The version of NEMESIS used here is based a doubling-adding scheme that assumes a plane-parallel atmosphere. We include Rayleigh scattering due to the mixture of H_2 and He, which is very important in VIO and BL1 filters, as well as the absorption due to CH_4 , which is essential at certain filters like MT2 and MT3 (Sayanagi et al., 2016).

The goal of our modeling is to reproduce the observed dependence of absolute reflectivity with geometry (location on the disk and solar phase angle) for all wavelengths at the same time. We assume that the vertical structure does not change during the observations, hence the importance of focusing in a relatively narrow time span (Pérez-Hoyos et al., 2005). In order to reproduce all observations simultaneously, NEMESIS uses the optimal estimator scheme to find the most likely model that best accounts for the observations.

3.2 Vertical cloud structure model

In previous work (Pérez-Hoyos et al., 2005; Sanz- Requena et al. 2012; Pérez-Hoyos et al., 2016), Saturn’s atmosphere was initially considered to be divided into three distinct layers of particles: an upper stratospheric haze (at 10s of mbar), a tropospheric haze in the upper troposphere (at a few 100s of mbar) and a bottom cloud at the ammonia condensation level. This approach has been found to be complex enough to account for spectral and geometrical variations of absolute reflectivity at visible wavelengths (Karkoschka and Tomasko, 1993, 2005). The vertical structure assumed in the present work is shown in Figure 4 and a complete list of the parameters, free and fixed, can be found in Table 2. It must be noted that NEMESIS assumes an a priori model from which we iterate until convergence to a satisfactory fit. This process is determined by the parameters assumed to be free but also by their a priori error bars. The election of free and fixed parameters was mostly based on a previous analysis and results by Pérez-Hoyos et al., 2016. In short, we fixed the parameters that have little or none impact on the observed radiances at the filters of interest. Most of the influential parameters are found to be related with the tropospheric haze and hence this is the layer described in

more detail by the model. Most of the a priori assumptions do not alter the retrieved free parameters, but a few comments will be discussed later on for some specific cases.

The uppermost particle layer corresponds to the stratospheric haze. We assume that this layer is located between pressures $P_1 = 1$ mbar and $P_2 = 100$ mbar (Pérez-Hoyos et al., 2016) and its particle density is constant with height (Pérez-Hoyos et al., 2005). The only free parameter of this layer, the stratospheric haze, is its total optical thickness (τ_{str}). As a starting point we have taken the value of $\tau_{str} = 0.03 \pm 0.02$ (at $0.8 \mu\text{m}$) given by Pérez-Hoyos et al. (2016) for the EZ, (Equatorial Zone) at $0.89 \mu\text{m}$. As in previous work (Pérez-Hoyos et al., 2005, Sanz-Requena et al., 2012), the phase function is described by the Mie formalism, which requires a refractive index with real part (m_r) and imaginary parts (m_i). We assume for the real part a value of $m_r = 1.43$ and for the imaginary part $m_i = 10^{-3}$, both constant with wavelength and similar to the observed indices of ammonia ice at these wavelengths (Martonchik et al., 1984). In this case we employed the log-normal particle size distribution of Hansen and Travis (1974) (Pérez-Hoyos et al., 2016) with an effective radius (r_{eff}) of $0.15 \mu\text{m}$ and an effective variance (σ_{eff}) of 0.1 (as in Sanz-Requena et al., 2012, and Ortiz et al., 1996), although these parameters are found to have little impact in the retrievals compared with others.

The intermediate layer corresponds to the tropospheric haze. In our model, the profile for the tropospheric haze is represented by a variable base height, a peak particle number density and scale height in terms of the atmospheric scale height. In this case, for the base altitude pressure (P_{bot}) we have taken 700 mbar as the a priori value following the result of 625 ± 96 mbar found by Roman et al., 2013. This second layer is allowed (and in fact found to) overlap with the upper haze. For the particle number density (N) we have taken as reference the one found by Pérez-Hoyos et al. (2016) at a latitude 60° N of 10 ± 5 particles/ cm^3 . As an initial value for the height scale of the particles we have used the gas scale height (H_g) in Saturn's atmosphere (35 ± 10 km at 100 mbar, Sánchez-Lavega, 2011).

For the tropospheric haze, we used Mie theory for the particle phase function calculations. In this work, we have a relatively narrow range of phase angles used but it is centered around some features specific of spherical particles. In order to remove these features, while retaining the ability to compute the particle cross section as a function of wavelength, we used in all calculations a fit to the expected Mie phase function using a

Henyeey-Greenstein phase function. A comparison with previous values for the Mie phase function and the Henyeey-Greenstein fit will be provided in the corresponding section. Therefore, we also require as initial parameters the effective radius and variance of the size distribution. The values of initial $r_{eff} = 1.5 \pm 0.5$ and $\sigma_{eff} = 0.1 \pm 0.1$ were taken from Ortiz et al. (1996).

The refractive indices as a function of wavelength are also left as free parameters. In this model, the code of the real part of the refractive index spectrum is calculated with the Kramers-Kronig's relation (Lucarini et al, 2005) from an a priori value of $m_r = 1.43$ expected for ammonia at a reference wavelength of $0.89 \mu\text{m}$. (Martonchik et al., 1984), while the imaginary part is left as a free parameter. We use as initial value at all wavelengths $m_i = 10^{-3}$ (Pérez-Hoyos et al., 2005).

Let's focus on the standard gamma distribution used in this work for the tropospheric particles, as in Roman et al. (2013). This can be expressed as following (Sánchez-Lavega, 2011):

$$n(r) = C r^{(1-3\sigma_{eff})/\sigma_{eff}} e^{-r/r_{eff}\sigma_{eff}}$$

Where r is the radius of the particle, r_{eff} is the effective radius and σ_{eff} is the effective variance and C a normalization constant. The effective radius is the average radius weighted by its geometrical cross-section:

$$r_{eff} = \frac{\int_{r_1}^{r_2} r \pi r^2 n(r) dr}{\int_{r_1}^{r_2} \pi r^2 n(r) dr}$$

However, we can also define the mean radius (r_{mean}) as the arithmetic mean of the radii between r_1 and r_2 , in terms of number of particles:

$$r_{mean} = \frac{\int_{r_1}^{r_2} r n(r) dr}{\int_{r_1}^{r_2} n(r) dr}$$

Thus the mean and effective radii can be substantially different, as it is possible to find many small particles that reduce the mean radius, but do not contribute significantly to the effective scattering. This digression will be of interest later on.

Finally, the lower particle layer corresponds to the cloud that is expected to be located at some 1.4 bar, putatively formed by ammonia ice (Pérez-Hoyos et al., 2016). The cloud

is assumed to be located between $P_5 = 1.0$ bar and $P_6 = 1.4$ bar with the particle optical thickness (τ_{cloud}) as the only free parameter. As in the stratospheric haze, the particle specific density (particles/gram) is assumed to be constant with altitude. In this layer, the phase function is described again by a Mie phase function with wavelength-independent refractive index $m_r = 1.43$ and $m_i = 10^{-3}$. The particle size distribution is a log-normal distribution with an effective radius of $10\ \mu\text{m}$ and an effective variance of $0.1\ \mu\text{m}$ (West et al., 2009). As our a priori assumption we have taken the value of $\tau_{cloud} = 10 \pm 10$ from Pérez-Hoyos et al. (2016), who found $\tau_{cloud} > 10$.

We show in Table 2 the set of 11 free parameters that define our inversion problem. To avoid over-fitting the imaginary refractive index, we started fitting the seven selected regions only at MT2, CB2 and MT3 filters, but fixing $m_i = 10^{-3}$ for little tropospheric absorption at those wavelengths. Once an acceptable fit was found, we added shorter wavelength filters VIO and BL1, adding the refractive indices as free parameters. In this way we were able to find a maximum likelihood model that was acceptable in all the cases ($\chi^2/n < 1$). We performed several initial runs to test if an increase of the number of free parameters at any of the layers (i.e. a more complex model) resulted in a better fit, with negative results.

4. Modeling Results

4.1. General results

We show in Fig. 5a, 5b and 5c the measured center-to-limb profiles compared to the best fit models for all regions and filters, and the different images (phase angles) used in this work. Table 3 summarizes the χ^2/n values for each region and filter, showing that fits are acceptable, but not always perfect. The mean χ^2/n values are always smaller than 1 and most of the individual χ^2/n values are less than 1. However, the worst fit is found at MT2 filter in region 4, particularly at $\alpha = 48^\circ$. Although in all regions the average χ^2/n is less than 1, the worst global fit is found in region 4.

There are some causes that could partly explain the discrepancies between observations and models. First, the model could not be complex enough to account for the vertical distribution of tropospheric aerosols, hence affecting MT2 fitting, sensitive to pressures below the tropopause. Second, the assumption of sphericity is not likely to be correct for the tropospheric particles. Both aspects were already discussed in Pérez-Hoyos et al.

(2016). A more complex model is not supported by the current data, and a better spectral resolution is required to increase its complexity. Regarding phase function, phase angle coverage is not enough to find influence due to variations in the scattering properties and it is mostly based on the dependence of optical thickness with wavelength, something that cannot be predicted independently with a synthetic phase function as the one used in Pérez-Hoyos et al. (2016). All in all, fits are within acceptable margins and therefore are taken as reliable estimations of the atmospheric parameters. Uncertainties and sensitivities will be discussed later on.

In order to rule out and quantify a possible systematic deviation of the limb-darkening in the different regions and filters and in order to improve our model we fitted both observations and best-fitting models to a Minnaert law (Pérez-Hoyos et al., 2005). (Fig. 6a and 6b). In this figure, we assume that all observations, at different phase angles, will follow the Minnaert law with the same Minnaert parameters, which seems to be the case. We do not find any systematic deviation in the limb darkening when compared with the original data, as the same filter or region can give differences as low as 2% or as high as 10%, with average differences of 8%. It must be noted that an alternate strategy could be used to take advantage of the better precision in the relative ($\sim 1\%$) than in the absolute photometry ($\sim 10\%$), by giving more weight to the limb-darkening than to the absolute nadir-corrected reflectivity value. While we did not perform a systematic study, our explorations of such strategy did not show any substantial improvement of the fits.

4.2. Best-fitting results

Table 4 shows the best-fitting values of the parameters showing that there is a clear latitudinal dependence for most of them.

The optical thickness of the stratospheric haze at $0.8\ \mu\text{m}$ ranges from $\tau_{str} = 0.01 \pm 0.01$ (region 1) to 0.03 ± 0.005 (region 7). This is a change of a factor of 3 in the stratospheric particle density from the lower to the upper latitudes. Values at $0.4\ \mu\text{m}$ are also given, and found to be somewhat higher: $\tau_{str} = 0.07 \pm 0.02$ (region 1) to 0.2 ± 0.03 (region 7), as it is expected for the sub-micron sized particles used here. These results are similar to those found in other studies, e.g. Perez-Hoyos et al. (2016).

Regarding the parameters that describe the vertical distribution of the tropospheric haze, we give both the altitude (with respect to the 1 bar level) and the pressure level of the base of the haze. While the former is the actual free parameter in our model, the latter is easier to compare with previous results. There is a clear change from region 1 to region 7, as demonstrated by Figure 7. In the Hexagon Wave (region 4), the altitude of the base of the tropospheric haze reaches its lowest value before entering into the Polar Region (900 ± 200 mbar.). Within the Hexagon and approaching the North Pole the value is 800 ± 200 mbar until reaching 1000 ± 300 mbar in the polar vortex. This is consistent with the dynamical interpretation that the North polar vortex is a region of subsidence with fewer particles and deeper clouds (Sánchez-Lavega et al., 2006). While some changes can be within the uncertainties of the parameters, there is an obvious difference between the values of the pressure of the base within the Polar Region (regions 4 to 7) and those found outside (regions 1 to 3).

The behavior of the concentration of tropospheric particles is similar to that of tropospheric haze base pressure, as shown in Figure 8. It decreases from region 1 to 3 (20 ± 2 to 15 ± 1 particles/cm³) reaching a minimum value again in the region of the Hexagonal Wave (region 4, 4 ± 0.5 particles/cm³). It slightly increases within the polar region (regions 5 and 6, 5 ± 0.5 particles/cm³), reaching a minimum value in the polar vortex of 2 ± 0.5 particles/cm³. All these values, except the one at the most northerly latitude, are in good agreement with those found in other works such as Pérez-Hoyos et al. (2016).

In contrast to the concentration, the scale height of the tropospheric haze increases as we approach the North Pole from 18 ± 0.1 km in region 1 to 50 ± 0.1 km in region 7. The scale height reaches the largest value beyond the Hexagon, where the values for region 6 (cloudy region at continuum wavelengths) are 32 ± 2 km and 40 ± 2 km for region 5 (region without cloud structure). These results range from half to one Saturnian gas scale height at the tropopause level, which is significantly higher than the values reported by Pérez-Hoyos et al. (2016) of around ~ 0.2 gas scale heights, or 7 km.

The parameters in the preceding paragraphs can be integrated vertically (taking into account the particle cross-section) to provide the optical thickness τ_{trop} of the tropospheric haze. While this is not the actual parameter of our model, it is always useful for comparison with previous works. Outside the Polar Region we found (at

0.8 μm) a maximum $\tau_{trop} = 6 \pm 3$ (decreasing slightly until reaching the region of the Hexagon Wave with $\tau_{trop} = 1 \pm 0.5$). In the interior regions $\tau_{trop} = 2 \pm 1$ for region 5, reaching the minimum value in the region 6 and within the polar vortex with $\tau_{trop} = 1 \pm 0.5$. These are low values and difficult to compare with the results of previous models since a high inclination orbit is required to observe more northerly latitudes, and they do not consider this type of observations, at least within the plane parallel approximation used here.

The particle size distribution also displays a dramatic dichotomy on both sides of the Hexagon Wave. For regions 1, 2 and 3, the values for $r_{eff} = 7 \pm 0.1 \mu\text{m}$ and $\sigma_{eff} = 0.6 \pm 0.1 \mu\text{m}$. This is quite a peculiar size distribution, as shown in Figure 9. It implies that the number of small particles is substantially higher than the larger ones. Since these have larger cross sections, they are the most effective ones scattering radiation, but the mean radius in terms of number of particles (using as a lower limit a reasonable value at molecular scales) is much smaller $r_{mean} = 0.2 \pm 0.01 \mu\text{m}$. However, when we reach region 4 we found again a distribution of particles centered around a mean value with values of r_{eff} and σ_{eff} respectively $2 \pm 0.2 \mu\text{m}$ and $0.2 \pm 0.02 \mu\text{m}$. In this case, the mean radius by number of particles is $1 \pm 0.01 \mu\text{m}$. In region 5 the values of r_{eff} and σ_{eff} are 6 ± 0.2 and $0.03 \pm 0.02 \mu\text{m}$, while in the region 6 they are respectively $4 \pm 0.4 \mu\text{m}$ and $0.1 \pm 0.02 \mu\text{m}$. Thus, the value of the mean radius is $5.0 \pm 0.5 \mu\text{m}$ and $3 \pm 0.3 \mu\text{m}$ for region 5 and region 6. For the polar vortex the value of r_{eff} and σ_{eff} are respectively $4 \pm 0.1 \mu\text{m}$ and $0.02 \pm 0.01 \mu\text{m}$, while the mean radius is $4 \pm 0.4 \mu\text{m}$. Even though particle size cannot be estimated with full confidence without a better coverage of scattering angles (and other parameters might influence the result), there is an evident change in the particle microphysics on either side of the Hexagon Wave. The differences in size distribution leads to a different behavior of the tropospheric optical thickness with wavelength, being nearly flat in the polar region and increasing strongly towards shorter wavelengths in regions 1 to 3.

Figure 10 shows the imaginary refractive indexes for the tropospheric haze. For all regions, the value of m_i decreases with wavelength as we previously determined (Sánchez-Lavega et al., 2006). We find again a difference between the values corresponding to the outer and the inner regions. In regions 1, 2 and 3 the values range from $(1 \pm 0.1) \times 10^{-4}$ (at $0.4 \mu\text{m}$) to $(0.3 \pm 0.1) \times 10^{-7}$ (at $1 \mu\text{m}$), whereas in regions 5, 6 and 7 the values range from $(0.2 \pm 0.04) \times 10^{-4}$ ($0.4 \mu\text{m}$) to $(0.1 \pm 0.07) \times 10^{-8}$ ($1 \mu\text{m}$). Region 4 again marks the difference, where the values are $(0.1 \pm 0.03) \times 10^{-2}$ for $0.4 \mu\text{m}$ and

(0.5 ± 0.2) $\times 10^{-6}$ for 1 μm . The imaginary refractive index strongly influences the particle cross section, and these results may be degenerated with those for the particle size distribution, as they may also force an increase or decrease of particle cross-section.

We must highlight that the imaginary refractive indices a priori value was constant for all wavelengths. Motivated by the results found in the best-fit values of imaginary refractive indexes in regions 1, 2, and 3, as well as the parameters of the particle size distribution, we have performed simulations in which the a priori values of imaginary refractive indexes were different for all wavelength (10^{-2} (0.4 μm), 10^{-3} (0.6 μm), 10^{-4} (0.8 μm) and 10^{-4} (1 μm)); sub-optimal solutions were found that do not differ qualitatively from the results discussed in the preceding paragraphs. Finally, we do not have much sensitivity to the bottom cloud at the ammonia condensation levels, as the results were found to be above 10 for all cases, but too close to priors to be informative.

4.3. Sensitivity to the Model Parameters.

The process of finding the best fit starts from an a priori assumption of the free parameters, accompanied by their corresponding a priori error. Therefore, we assume some initial uncertainty for the parameters we are trying to retrieve. When our model conforms to the observations, we get both the a posteriori maximum likelihood value of each parameter and its corresponding error. A very useful measure of the information gained after the retrieval of one parameter is the improvement factor (Irwin et al., 2015), which compares the a priori and a posteriori relative errors. A low value of the improvement factor implies no information gain over the free parameter with respect to the a priori uncertainty, while a high value implies a substantial reduction of our initial uncertainty.

In this way, we find that for the stratospheric haze and bottom cloud opacities that the improvement factors are very low (3% and 2% respectively). Given this low sensitivity, we tested to fix these parameters for a few cases and found essentially the same results for the rest of parameters. For the tropospheric haze, we find a significant improvement factor for the base altitude, peak concentration and scale height of 93%, 95% and 78%, respectively. For the rest of the free parameters the improvement factors are smaller, such as for the effective radius, the effective deviation and the imaginary refractive indexes around 15% for all of them. Therefore, the role of these parameters can be accepted to be secondary and the retrieval less informative.

To stress the importance of the most informative free parameters, we have compared the best fit obtained with two other models, 1- σ above and below the nominal result. Figure 11 shows this comparison applied to region 1. We observe that the most affected filters are MT2 and MT3. Another view of the same problem is to evaluate the change of the reflectivity for small (1%) variations of each free parameter, also shown in Fig. 11. This is intended to show the geometrical variation of the sensitivity, which can be seen to be different in some cases at the central meridian or at the limb or terminator of the planet. Some parameters affect more strongly limb-darkening than others, that have a flatter behavior with wavelength. In Figure 11d, we see that the value of $\Delta I/F$ is very small for the VIO, BL1 and CB2 filters. The variation of $\Delta I/F$ is important in the filters MT2 and MT3, in which we observe that the most influential parameter is the scale height. For most cases, an increase in the parameter results in an increase of limb-darkening at a given phase angle, except a change in the scale height, which strongly reduces limb-darkening at the methane absorption filters.

We have extensively tested the impact that the bottom cloud may have in other free parameters of the tropospheric haze above it, particularly in its bottom pressure. We have considered models with extreme values of cloud's optical thickness and we have not observed variations of the lower pressure of the tropospheric haze in the any region. We find that the bottom pressure of the tropospheric haze is relatively robust and independent from the bottom cloud parameters which are neutral to the fitting procedure.

5. Discussion.

We have found that the retrieved optical thickness of both the stratospheric haze and tropospheric haze depend strongly on the latitude in the different reflectivity regions of the subpolar and Northern polar region of Saturn. As a general rule we note that the pressure of the base of the tropospheric haze increases towards polar latitudes (from 600 ± 200 mbar to 1000 ± 300 mbar in the vortex. However, the model is consistent with a bottom cloud of fixed altitude in the whole region but with some variability in its optical depth. Lack of sensitivity, however, precludes investigating alternate scenarios for the bottom cloud.

As already explained, NEMESIS uses a Henyey-Greenstein approximation to the Mie-calculated phase function, which neatly averages out features from purely spherical particles such as the ‘rainbow’ and back-scattering ‘glory’. In particular, we used the Mie theory to generate the phase function at 41 scattering angles and then fitted the parameters f , g_1 and g_2 of the combined Henyey-Greenstein function to this Mie-calculated phase function using the Levenberg-Marquardt technique. While there are more sophisticated methods to retain some optical features as the glory (Kattawar, 1975), we find this approximation good enough for our purposes. In any case, the actual values of the Henyey-Greenstein parameters used are given below for comparison with previous works.

In Figure 12 we can see the comparison of both phase functions for region 3 and region 5 with those obtained by Tomasko and Doose (1984) and that of Pérez Hoyos et al. (2016). The phase function of Tomasko and Doose corresponds to latitudes of the southern hemisphere where the two asymmetry parameters g_1 and g_2 are respectively 0.6 and -0.3 while parameter f accounts for the relative weighting between them is 0.77. For the phase function of Pérez Hoyos et al. (2016) we have used the values of $g_1 = 0.81$, $g_2 = -0.31$ and $f = 0.85$ corresponding to latitudes of the northern polar region. The values of Henyey-Greenstein approximation to the Mie-calculated phase function in this work are $g_1 = 0.84$, $g_2 = -0.41$ and $f = 0.89$ for the region 3 and $g_1 = 0.78$, $g_2 = -0.54$ and $f = 0.98$ for the region 5. These values are substantial different from those obtained by Tomasko and Doose (1984) but similar to those by Pérez-Hoyos et al. (2016). However, while the former values refer to the southern equatorial zone of the planet, the latter ones are taken for a more geographically similar region.

The Hexagonal Wave separates the polar region into two broad areas according to the particle properties, one enclosing the pole and the other outside the pole (Figs. 6, 7 and 8). This result is in agreement with the ones found by West et al. (2015) using Cassini ISS polarization images where structural differences are observed inside and outside the hexagon. Poleward of the Hexagonal Wave above latitude $\sim 75^\circ$ N (regions 5, 6 and 7) we found a large anticyclonic region (region 5) with an embedded field of discrete “puffy” clouds typically with a size of 100 and 400 kilometers (region 6) (Antuñano et al., 2018). The radiative transfer model indicates that this “puffy” cloud field is distinguished from the surrounding region by a larger optical depth at the upper cloud level. Few differences are noted in the tropospheric haze between the two regions. This

supports the idea that denser clouds form the “puffy” region, each element being convective in origin, similar to the convective clusters of the mesoscale cellular convection (MCC) found on Earth and ascending by the internal heat flow (Antuñano et al., 2018). The whole polar region (regions 5, 6 and 7) has an optically denser stratospheric haze (in particular in the UV). The origin of this haze could be related to the bombardment of the upper atmosphere by particles trapped by the magnetic field (West et al., 2009).

The cyclonic north polar vortex (region 7) extends from the pole to latitude 88.5° , where peak velocities reach $140\text{--}160\text{ ms}^{-1}$ (Antuñano et al., 2015, Sayanagi et al., 2017). The MT2 and MT3 filters show the cyclone to have low brightness relative to the surroundings, but turns bright in violet wavelengths, consistent with low particle density in the tropospheric haze and deeper clouds (Sánchez-Lavega et al., 2006; Baines et al., 2009). This is in agreement with our results since we found a minimum optical thickness and low concentration of particles ($2 \pm 0.5\text{ particles/cm}^3$) in the cyclone tropospheric haze. This is consistent with the polar cyclone being a “hole” within the upper cloud system, where descending motions occur (Sánchez-Lavega et al., 2006; Dyudina et al., 2009).

Saturn’s Hexagon Wave encloses a fast eastward jet centered at 75.8° N that reaches a mean peak velocity of $104 \pm 15\text{ ms}^{-1}$ (Antuñano et al., 2015). Our analysis shows that in the Hexagon Wave region and in the latitudes it encloses the effective radius of the tropospheric particles and the number density is smaller than outside. This is accompanied by a descent of the haze base. Dynamical conditions are probably involved in this dichotomy, but they have not been yet identified.

Equatorward of the Hexagon Wave latitude the base of the tropospheric haze reaches higher altitudes and the particle effective radius, optical depth and particle density increases. Dynamically this region contains a broad westward jet and a double-peaked eastward jet, with alternating cyclonic and anticyclonic vorticity domains (Figure 2). The banding we observe in these regions (Figure 1) does not match exactly the east-west jet system. The belt/zone aspect is due to changes in the particle properties of the hazes, with no requirement for additional haze layers, according to our model.

6. Conclusions

In this work we have performed a photometric analysis and radiative transfer modeling of the subpolar and North polar regions of Saturn using a set of Cassini ISS images spanning a spectral range from ~ 400 nm to 890 nm, including two methane absorption bands at 727 and 890 nm. We retrieve the vertical distribution and properties of the upper cloud and hazes from latitudes $\sim 50^\circ$ to 90° N. The following highlights are the most important conclusions of our work.

- In this range of latitudes we distinguish seven regions. These seven regions account for the overall spectral and geometrical variation of reflectivity of the North Polar Region of Saturn.
- The Hexagon Wave and embedded jet stream represents a boundary in the aerosol properties between the outer and inner regions (West et al., 2015), which are substantially different in various aspects of the tropospheric haze (in particular the particle number density (15 ± 1 part/cm³ for region 3 to 4 ± 0.5 part/cm³ for region 5), the scale height (22 ± 0.1 km for region 3 to 40 ± 2 km for region 5), the base height (13 ± 2 km for region 3 to 10 ± 4 km for region 5), and size distribution ($r_{eff} = 7 \pm 0.1 \mu\text{m}$ and $\sigma_{eff} = 0.7 \pm 0.1 \mu\text{m}$ for region 3 to $r_{eff} = 6 \pm 0.2 \mu\text{m}$ and $\sigma_{eff} = 0.03 \pm 0.02 \mu\text{m}$ for region 5).
- Both the optical thickness of stratospheric haze and the optical thickness of tropospheric haze gradually change with latitude. While the optical thickness of the stratospheric haze increases with latitude (0.01 ± 0.01 for region 1 to 0.03 ± 0.005 for region 7 at $0.8 \mu\text{m}$) the opposite is true for the tropospheric haze (6 ± 3 for region 1 to 1 ± 0.5 for region 7 at $0.8 \mu\text{m}$). The variation of the total optical thickness of the tropospheric haze with latitude is correlated with the base pressure of this haze, which increases with latitude, showing a lower haze (600 ± 200 mbar at the lowest latitudes to 1000 ± 300 mbar in the pole). The scale height also changes, resulting in quite a different vertical distribution of particles on either sides of the Hexagon Wave (18 ± 0.1 km for region 1 to 50 ± 0.1 km for region 7).
- The optical thickness of the tropospheric haze shows a greater variation in the regions outside the Hexagon Wave (6 ± 3 for region 1 at $0.8 \mu\text{m}$) than in the interior regions (1 ± 0.5 for region 7 at $0.8 \mu\text{m}$).
- Aerosol properties (particle size distribution and refractive indices) seem to change on either side of the Hexagon Wave, too. It is unclear whether or not this

reveals real particle properties changes or results from the dependence of optical thickness with wavelength.

- The low values of the optical thickness and particle concentrations found in the region enclosed by the Hexagon Wave, together with the retrieved behavior of the tropospheric haze base height, suggests that in this regions subsidence takes place.
- The polar vortex can be considered to be a depressed region of the atmosphere with possibly associated subsidence as quantified by Sánchez-Lavega et al. (2006).
- The radiative transfer model agrees with the consideration that puffy clouds have a convective origin similar to the convective clusters of the mesoscale cellular convection (MCC) found on Earth, and ascending by the internal heat flow (Antuñano et al., 2018).

While this work represents one snapshot for the situation of Saturn's Northern Polar atmosphere, it must be highlighted that the final orbits of the Cassini spacecraft are providing invaluable data with unprecedented spatial resolution for this part of the planet. Data acquired during Cassini's Grand Finale will surely complement the analysis shown here and will help to increase our understanding of Saturn's atmosphere.

Acknowledgments

We gratefully acknowledge the work of the Cassini ISS team that made the data available. This work was supported by the Spanish project AYA2015-65041-P (MINECO/FEDER, UE), Grupos Gobierno Vasco IT-765-13 and by Universidad del País Vasco UPV/EHU through program UFI11/55. We wish to thank Dr. R. West and Dr. U. Dyudina for their comments and suggestions during the review of the manuscript.

641

Image ID	Date	Filter	B(°)	B'(°)	α (°)
W1748990013	06/03/2013	BL1	18.73	14.75	5.49
W1748990135	06/03/2013	MT3	18.73	14.73	5.52
W1748990103	06/03/2013	MT2	18.73	14.73	5.51
W1748990051	06/03/2013	VIO	18.73	14.75	5.50
W1748990152	06/036/2013	CB2	18.73	14.72	5.53
W1750945864	06/13/2013	BL1	18.97	47.29	36.25
W1750945881	06/13/2013	VIO	18.97	47.28	36.24
W1750945932	06/13/2013	MT2	18.97	47.27	36.21
W1750945956	06/13/2013	MT3	18.97	47.26	36.20
W1750945973	06/13/2013	CB2	18.97	47.25	36.19
W1750953248	06/13/2013	BL1	18.97	44.83	32.62
W1750953265	06/13/2013	VIO	18.97	44.82	32.61
W1750953316	06/13/2013	MT2	18.97	44.81	32.59
W1750953340	06/13/2013	MT3	18.97	44.80	32.58
W1750953357	06/13/2013	CB2	18.97	44.79	32.57
W1750959544	06/13/2013	BL1	18.97	42.73	29.66
W1750959561	06/13/2013	VIO	18.97	42.73	29.65
W1750959612	06/13/2013	MT2	18.97	42.71	29.63
W1750959636	06/13/2013	MT3	18.97	42.70	29.62
W1750959653	06/13/2013	CB2	18.97	42.70	29.61
W1750937288	06/14/2013	BL1	18.97	50.10	40.67
W1750937305	06/14/2013	VIO	18.97	50.09	40.66
W1750937356	06/14/2013	MT2	18.97	50.08	40.64
W1750937380	06/14/2013	MT3	18.97	50.07	40.62
W1750937397	06/14/2013	CB2	18.97	50.06	40.61
W1750934464	06/24/2013	BL1	18.97	51.00	42.18
W1750934481	06/24/2013	VIO	18.97	51.00	42.17
W1750934532	06/24/2013	MT2	18.97	50.98	42.15
W1750934556	06/24/2013	MT3	18.97	50.97	42.13
W1750934573	06/24/2013	CB2	18.97	50.97	42.12
W1750902567	06/26/2013	BL1	18.96	58.79	61.28
W1750902617	06/26/2013	VIO	18.96	58.78	61.24
W1750902674	06/26/2013	MT3	18.96	58.78	61.21
W1750902698	06/26/2013	MT2	18.96	58.77	61.19
W1750902731	06/26/2013	CB2	18.96	58.77	61.17
W1750923064	06/26/2013	BL1	18.97	54.43	48.57
W1750923081	06/26/2013	VIO	18.97	54.43	48.56
W1750923132	06/26/2013	MT2	18.97	54.41	48.53
W1750923156	06/26/2013	MT3	18.97	54.41	48.52
W1750923173	06/26/2013	CB2	18.97	54.40	48.50

642

643 **Table 1:** Summary of the observations, see the text for an explanation of the symbols used.

644

Layer	Parameter	Type	A priori
StratosphericHaze	P_1	Fixed	1mbar
	P_2	Fixed	100 mbar
	τ_{str}	Free	0.03 ± 0.02
	m_r	Fixed	1.43
	m_i	Fixed	10^{-3}
	r_{eff}	Fixed	$0.15 \mu\text{m}$
	r_{eff}	Fixed	$0.1 \mu\text{m}$
Tropospheric Haze	P_{bot}	Free	$625 \pm 96 \text{ mbar}$
	N	Free	$10 \pm 5 \text{ part/cm}^3$
	H	Free	$35 \pm 10 \text{ km}$
	r_{eff}	Free	$1.5 \pm 0.5 \mu\text{m}$
	σ_{eff}	Free	$0.1 \pm 0.1 \mu\text{m}$
	m_r	Fixed	1.43
	$m_i(0.4 \mu\text{m})$	Free	$10^{-3} \pm 10^{-3}$
	$m_i(0.6 \mu\text{m})$	Free	$10^{-3} \pm 10^{-3}$
	$m_i(0.8 \mu\text{m})$	Free	$10^{-3} \pm 10^{-3}$
	$m_i(0.8 \mu\text{m})$	Free	$10^{-3} \pm 10^{-3}$
Bottom Cloud	P_5	Fixed	1.0 bar
	P_6	Fixed	1.4 bar
	τ_{cloud}	Free	10 ± 10
	m_r	Fixed	1.43
	m_i	Fixed	10^{-3}
	r_{eff}	Fixed	$10 \mu\text{m}$
	σ_{eff}	Fixed	$0.1 \mu\text{m}$

Table 2: Model atmosphere parameters.

649

Filter	Region 1	Region 2	Region 3	Region4	Region 5	Region6	Region 7	Average filter
VIO	0.553	0.564	0.848	0.625	0.886	0.523	0.233	0.604
BL1	0.462	0.490	0.479	1.460	1.059	1.236	0.073	0.741
MT2	0.876	1.128	1.100	2.225	0.692	0.822	0.860	1.100
CB2	0.341	0.442	0.512	0.656	0.164	0.646	0.217	0.425
MT3	1.603	0.902	0.884	0.603	0.383	0.927	0.427	0.818
Region Average	0.772	0.705	0.765	0.994	0.637	0.831	0.362	

650

651 **Table 3:** χ^2/n values for each region and filter.

652

	Region 1	Region2	Region 3	Region 4	Region 5	Region 6	Region 7
Stratospheric Haze							
$\tau_{str}(0.8 \mu\text{m})$	0.01 ± 0.01	0.03 ± 0.01	0.01 ± 0.05	0.01 ± 0.001	0.03 ± 0.006	0.03 ± 0.005	0.03 ± 0.005
$\tau_{str}(0.4 \mu\text{m})$	0.07 ± 0.02	0.2 ± 0.04	0.08 ± 0.02	0.06 ± 0.01	0.2 ± 0.04	0.2 ± 0.03	0.2 ± 0.03
TroposphericHaze							
$z(\text{km})$	30 ± 6	20 ± 4	13 ± 2	5 ± 1	10 ± 4	10 ± 4	0.2 ± 0.1
$P_{bot}(\text{mbar})$	600 ± 200	700 ± 100	800 ± 100	900 ± 200	800 ± 200	800 ± 200	1000 ± 300
$N(\text{part}/\text{cm}^3)$	20 ± 2	19 ± 2	15 ± 1	4 ± 0.5	4 ± 0.5	5 ± 0.5	2 ± 0.5
$H(\text{km})$	18 ± 0.1	20 ± 0.1	22 ± 0.1	30 ± 0.1	40 ± 2	32 ± 2	50 ± 0.1
$\tau_{trop}(0.8 \mu\text{m})$	6 ± 3	5 ± 2	4 ± 2	1 ± 0.5	2 ± 1	1 ± 0.5	1 ± 0.5
$r_{eff}(\mu\text{m})$	7 ± 0.1	7 ± 0.1	7 ± 0.1	2 ± 0.2	6 ± 0.2	4 ± 0.4	4 ± 0.10
$\sigma_{eff}(\mu\text{m})$	0.6 ± 0.10	0.6 ± 0.01	0.7 ± 0.1	0.2 ± 0.02	0.03 ± 0.02	0.1 ± 0.02	0.02 ± 0.01
$r(\mu\text{m})$	0.2 ± 0.01	0.1 ± 0.01	0.1 ± 0.01	1 ± 0.01	5 ± 0.5	3 ± 0.3	4 ± 0.4
$m_i(0.4 \mu\text{m})$	$1 \pm 0.1\text{E-}04$	$0.7 \pm 0.1\text{E-}04$	$0.1 \pm 0.01\text{E-}03$	$0.1 \pm 0.03\text{E-}02$	$0.2 \pm 0.04\text{E-}04$	$0.2 \pm 0.1\text{E-}04$	$0.2 \pm 0.001\text{E-}03$
$m_i(0.6 \mu\text{m})$	$0.7 \pm 0.2\text{E-}04$	$0.6 \pm 0.2\text{E-}04$	$0.7 \pm 0.2\text{E-}04$	$0.3 \pm 0.05\text{E-}03$	$0.4 \pm 0.2\text{E-}06$	$0.6 \pm 0.5\text{E-}05$	$0.4 \pm 0.01\text{E-}07$
$m_i(0.8 \mu\text{m})$	$0.3 \pm 0.2\text{E-}04$	$0.4 \pm 0.1\text{E-}04$	$0.5 \pm 0.2\text{E-}04$	$1 \pm 0.001\text{E-}04$	$0.8 \pm 0.1\text{E-}07$	$0.6 \pm 0.2\text{E-}06$	$0.8 \pm 0.02\text{E-}08$
$m_i(1.0 \mu\text{m})$	$0.3 \pm 0.1\text{E-}07$	$0.4 \pm 0.1\text{E-}07$	$0.5 \pm 0.1\text{E-}07$	$0.5 \pm 0.2\text{E-}06$	$0.1 \pm 0.07\text{E-}08$	$0.5 \pm 0.5\text{E-}08$	$0.1 \pm 0.03\text{E-}08$
Cloud							
$\tau_{cloud}(0.8 \mu\text{m})$	15 ± 3	24 ± 5	25 ± 5	11 ± 2	10 ± 2	16 ± 9	10 ± 2

Table 4: Best-fit parameter values and their uncertainties.

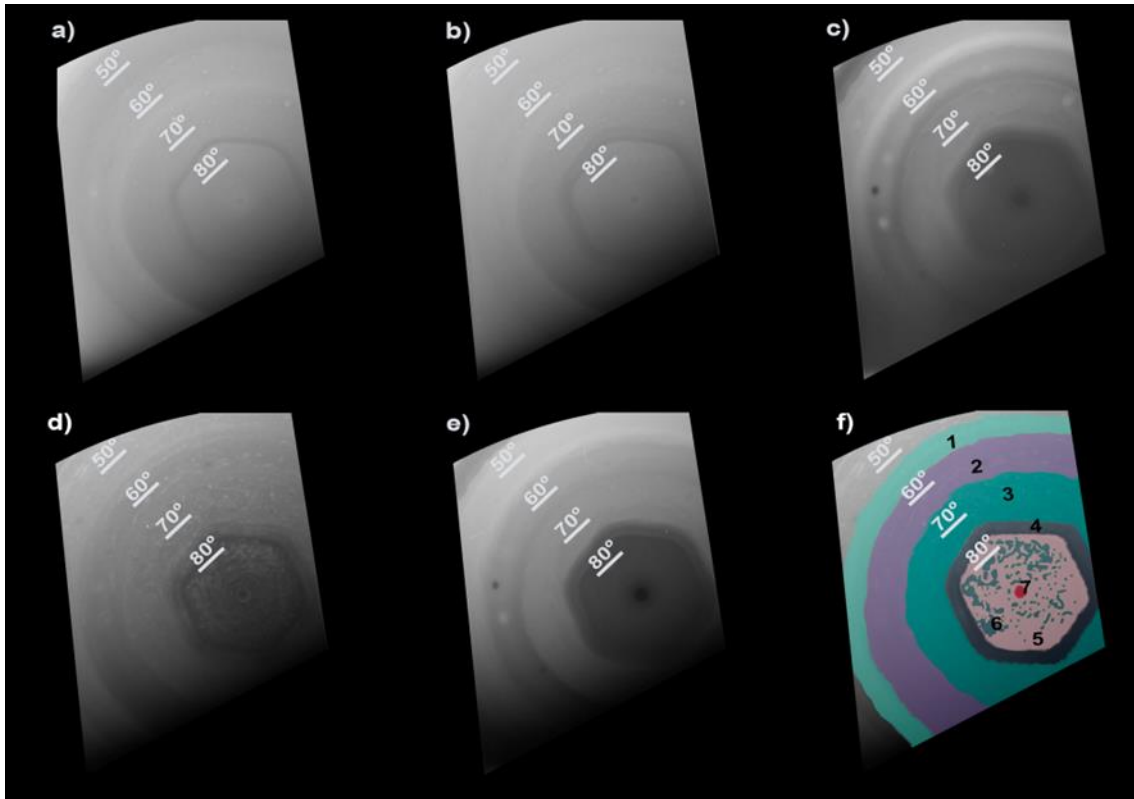


Figure 1: Polar projections of the images taken on June 26, 2013 for the five filters used in this work: (a) VIO; (b) BL1; (c) MT3; (d) MT2; and (e) CB2. Panel (f) shows the spatial distribution of the seven data clusters analyzed here.

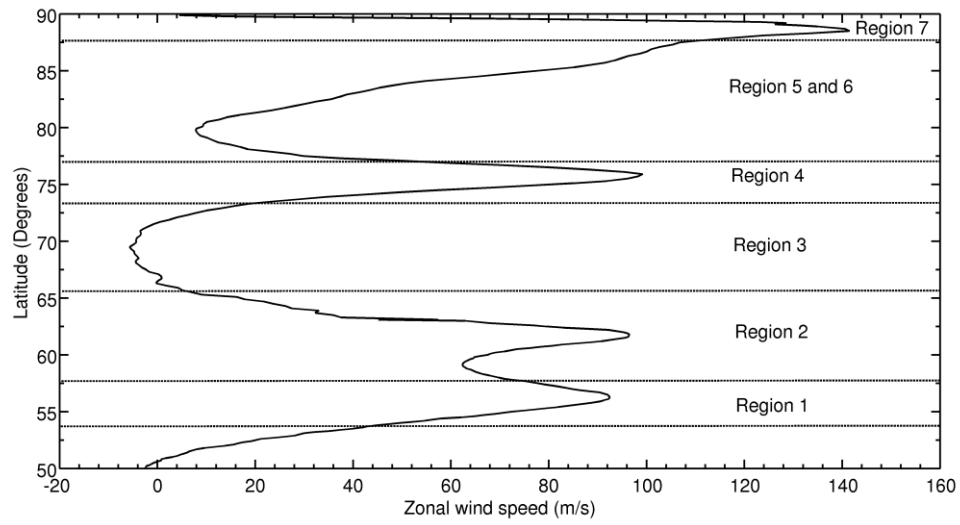
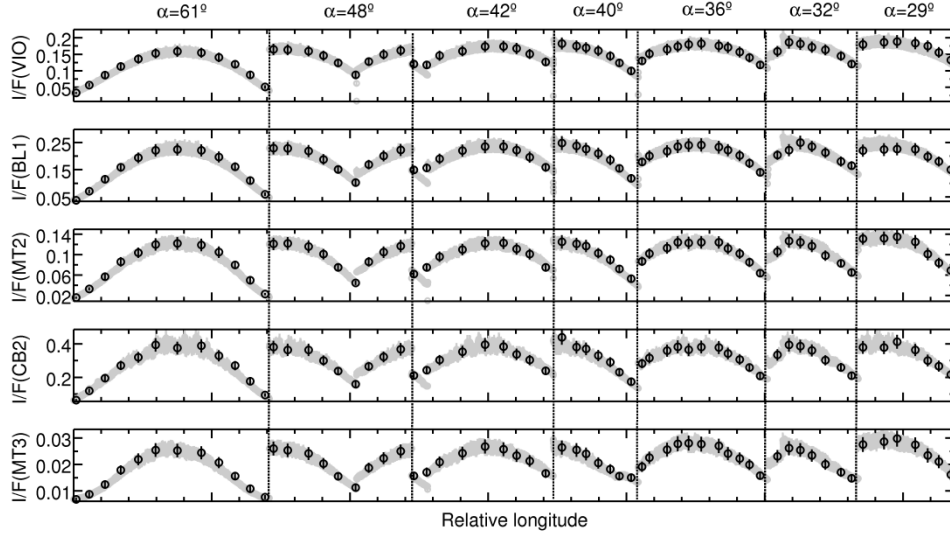


Figure 2: Zonal wind profiles for the seven regions identified in this work. The values were obtained with Cassini ISS images with the CB2 filter in the years 2004, 2009 (Garcia-Melendo et al., 2011) and 2013 (Antuñano et al., 2015).



668

669 **Figure 3:** Reflectivity values for region 3 (65° to 73° N) for all filters are shown (grey line)
 670 together with their average and standard deviation (black circles). The points shown here are
 671 those used as inputs for the model. Vertical lines divide regions observed in every imaged, at
 672 different phase angles (α). In this and some of the following figures, we use longitude measured
 673 in degrees (every tick is 10°) from an arbitrary reference longitude. The changes in the
 674 reflectivity with the longitude for each phase angle are due to the changes in the incidence and
 675 emission angles.

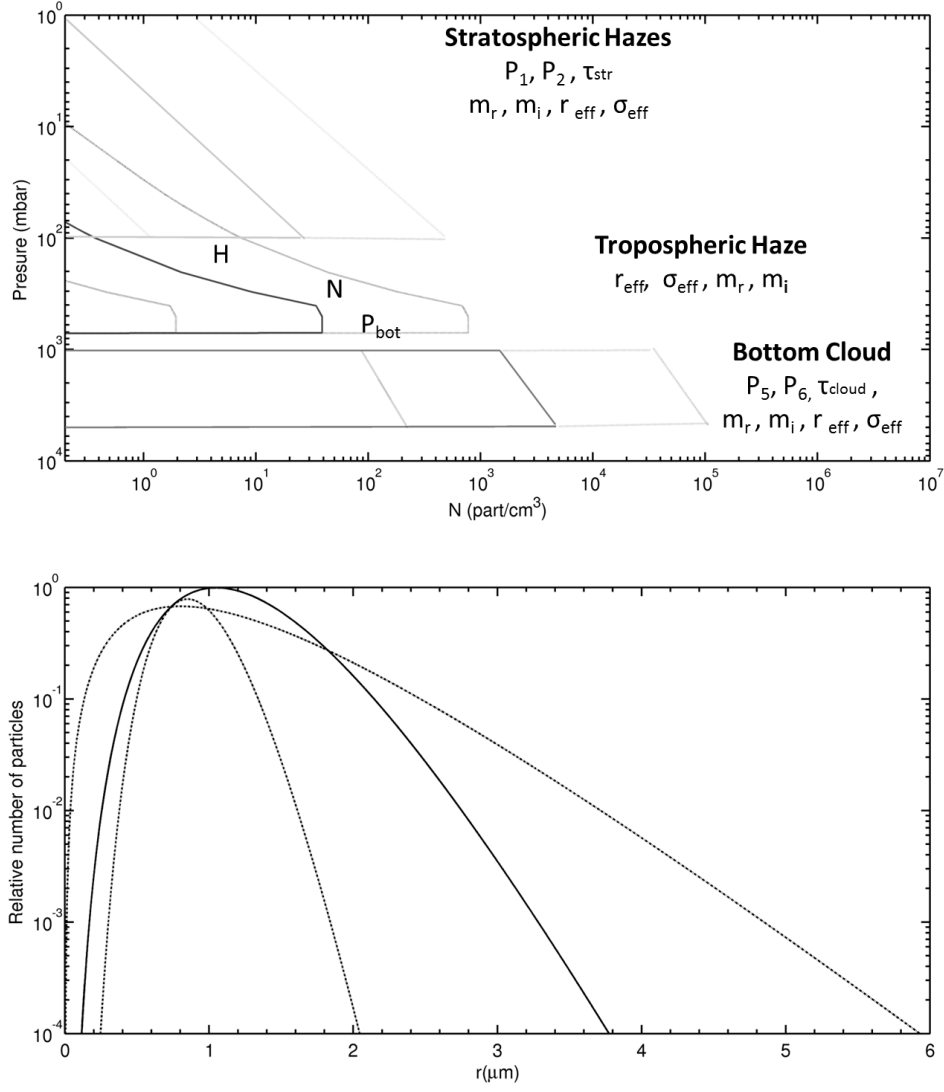
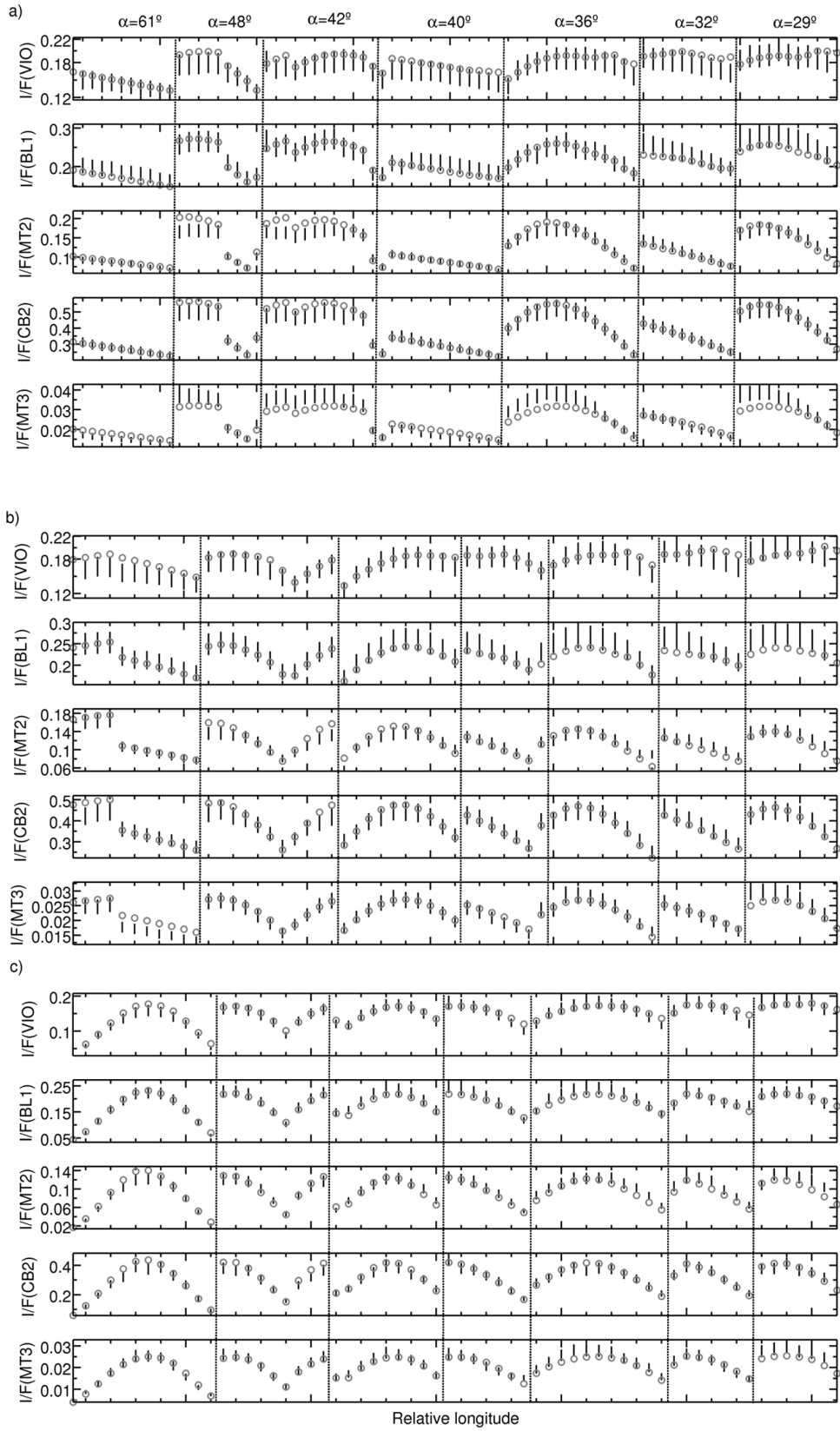


Figure 4: Top panel shows the a priori assumptions (solid lines) and their corresponding uncertainties (gray lines) for the vertical distribution of particles. Parameters of the model for each layer are also indicated (see the text for a full explanation). Bottom panel shows the a priori size distribution of tropospheric particles (solid line), and uncertainties (dashed lines).



681

682

683

684 **Figure 5a:** Comparison of best fits models with observed values of reflectivity. Gray circles are
 685 used for the modeled values and the black lines correspond to the observed reflectivity and its
 686 corresponding error bar. For an explanation of x axis, see Figure 3 caption. Panel a) shows
 687 Region 1, panel b) shows Region 2, and panel c) shows Region 3.

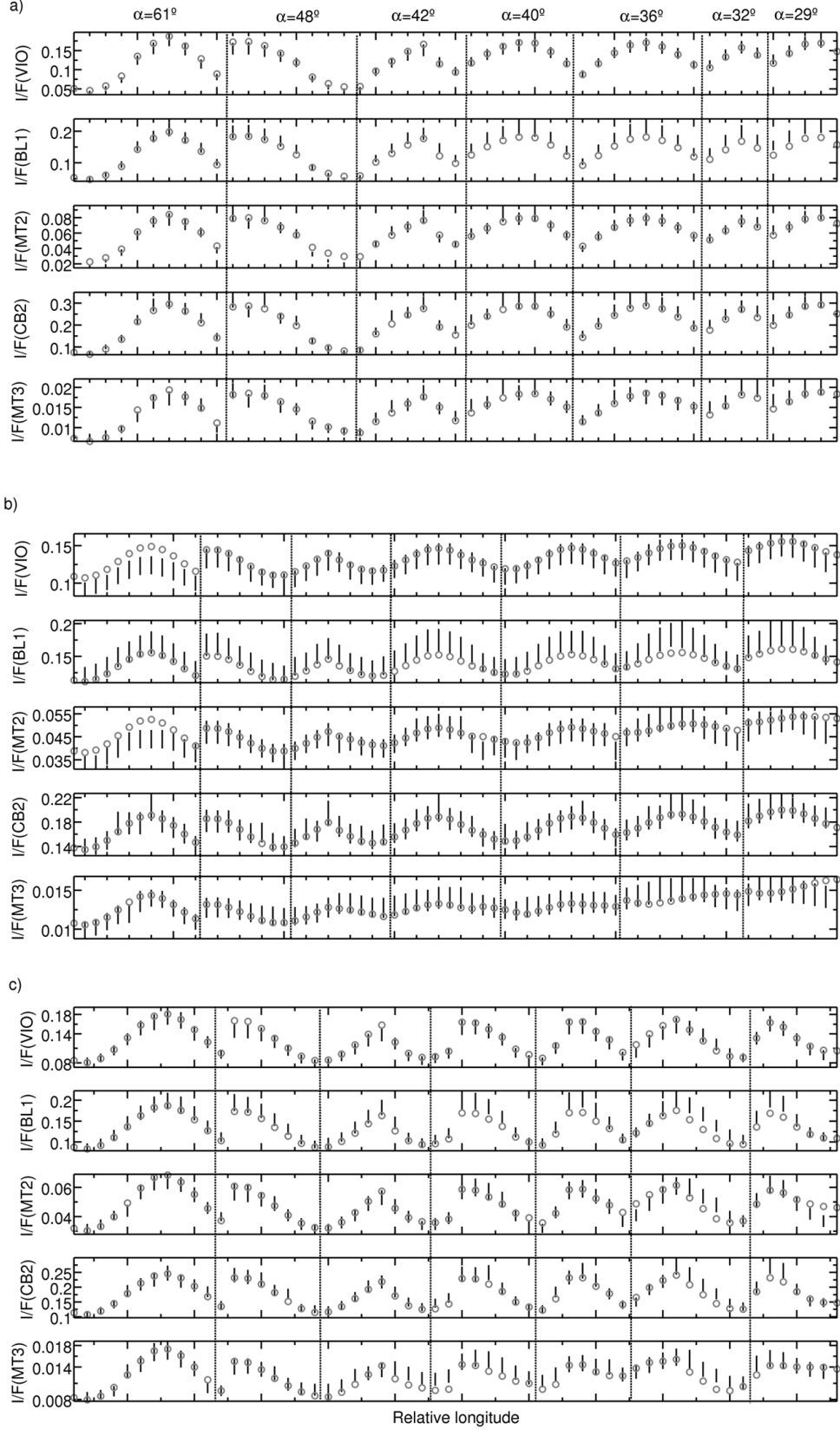


Figure 5b: Comparison of best fits models with observed values of reflectivity. Gray circles are used for the modeled values and the black lines correspond to the observed reflectivity and its corresponding error bar. Vertical dashed lines divide each region into the different phase angles (α). Panel a) shows Region 4, panel b) shows Region 5, and panel c) shows Region 6.

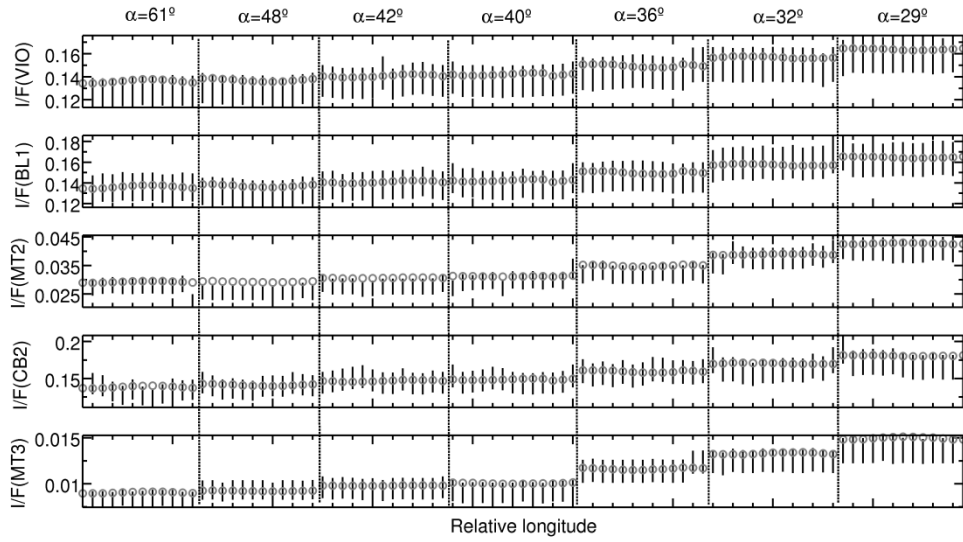


Figure 5c: Comparison of best fits models with observed values of reflectivity for region 7. Gray circles are used for the modeled values and the black lines correspond to the observed reflectivity and its corresponding error bar. For an explanation of x axis, see Figure 3 caption.

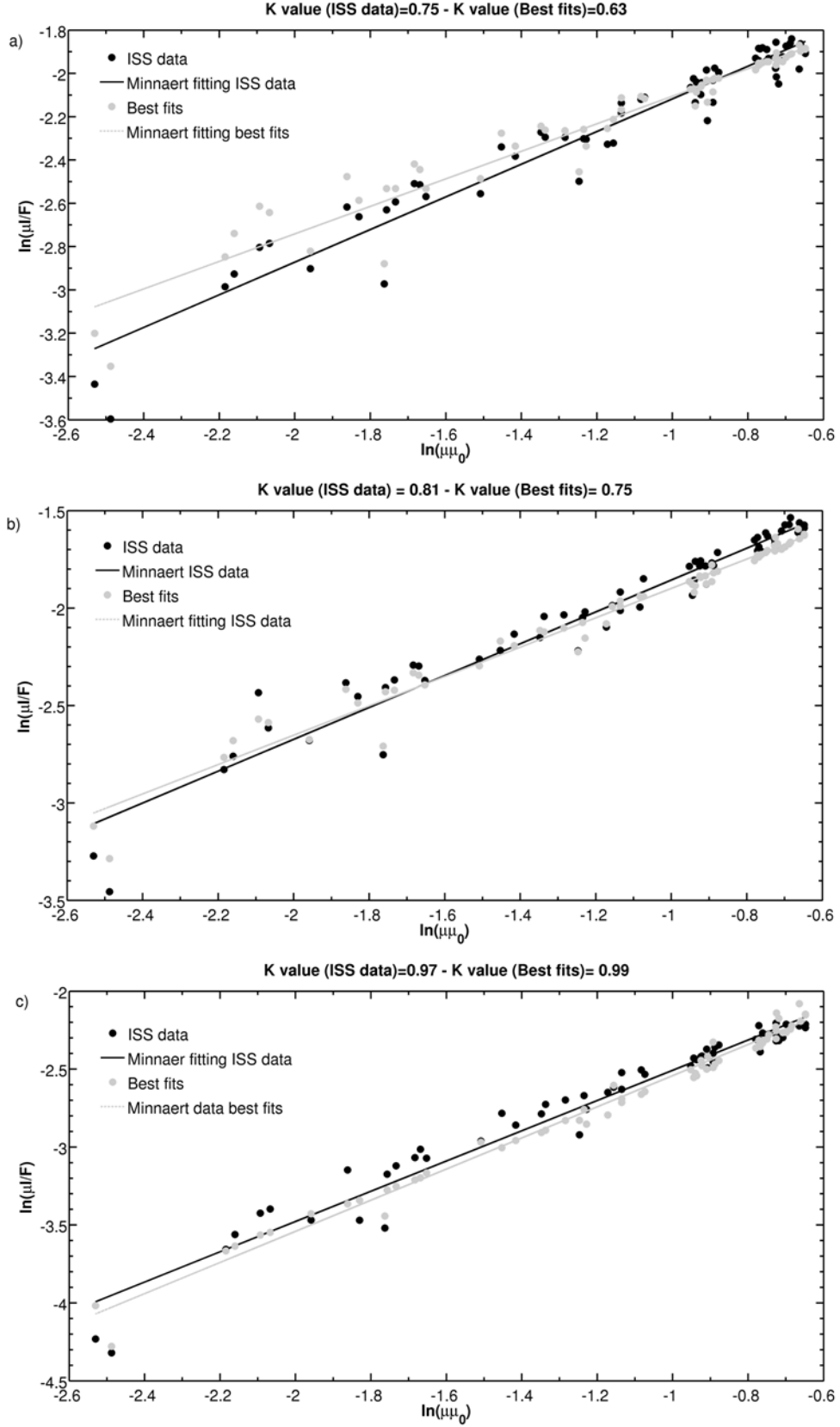
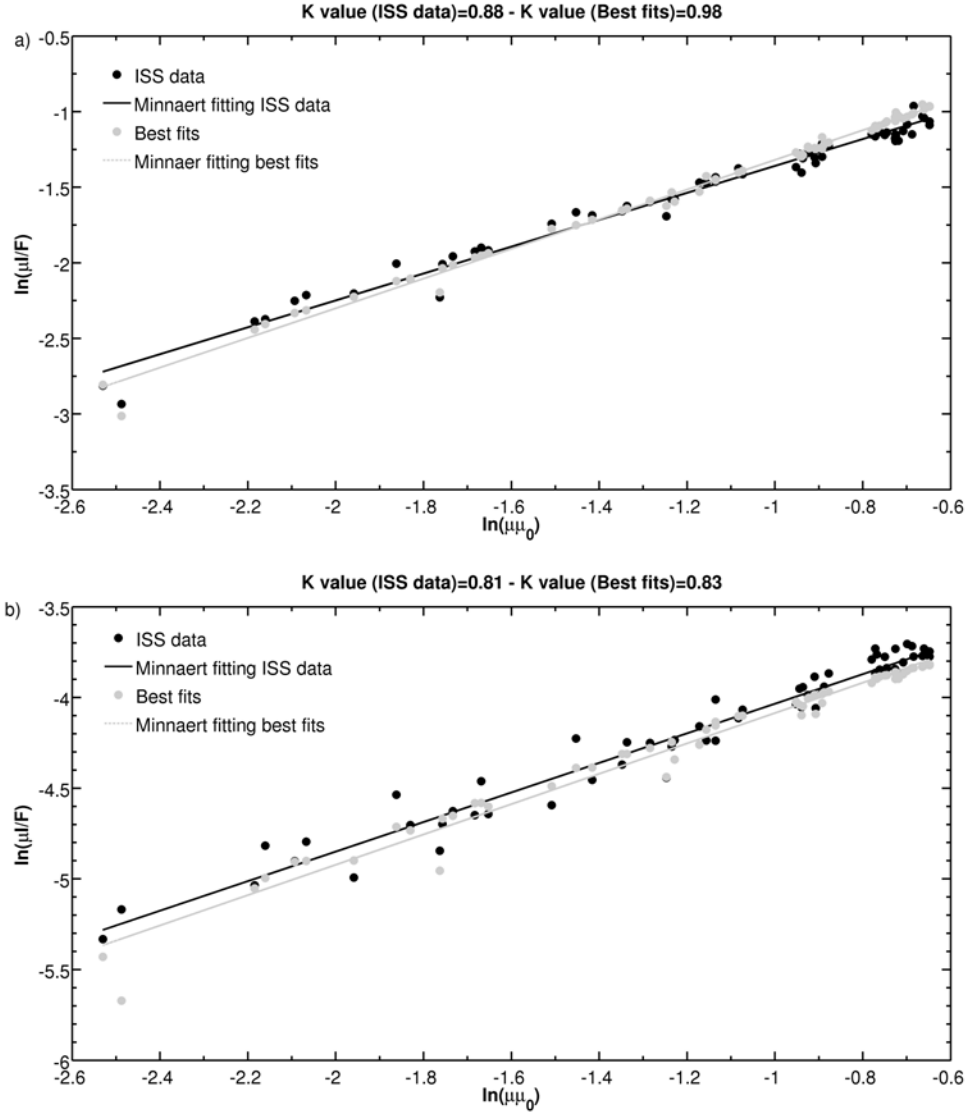


Figure 6a: Comparison of Minnaert limb-darkening model law of fitting ISS data with Minnaert limb-darkening model law of data best fits for region 3. Gray circles and lines are used for the modeled values and the black circles and lines correspond to the observed reflectivity.

704 Panel a) shows VIO filter, panel b) shows BL1 filter, and panel c) shows MT2 filter. K is the
 705 Minnaert limb-darkening coefficient.



706

707

708 **Figure 6b:** Comparison of Minnaert limb-darkening model law of fitting ISS data with
 709 Minnaert limb-darkening model law of data best fits for region 3. Gray circles and lines are used
 710 for the modeled values and the black circles and lines correspond to the observed reflectivity.
 711 Panel a) shows CB2 filter, panel b) shows MT3 filter. K is the Minnaert limb-darkening
 712 coefficient.

713

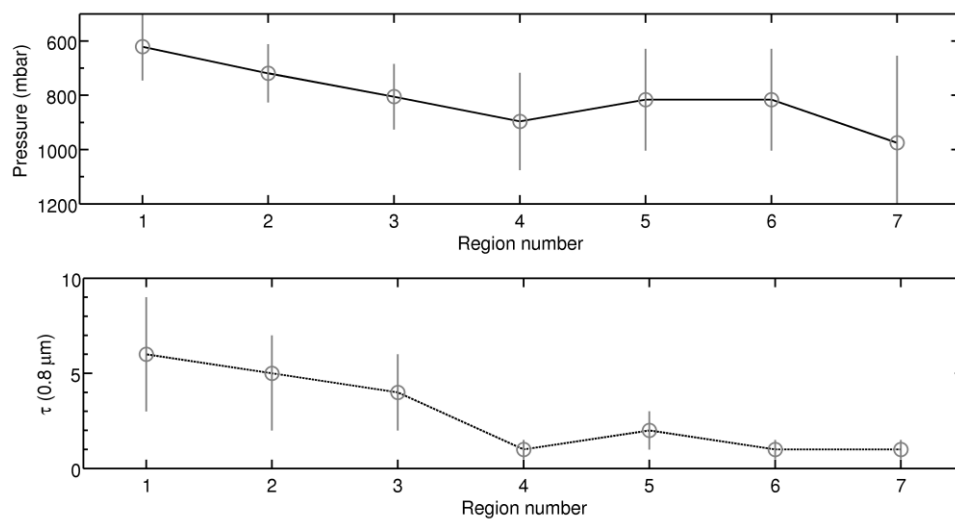


Figure 7: Altitude level for the base (in pressure) and optical thickness of the tropospheric haze at 0.8 μm as a function of the modeled regions, which roughly correspond to increasing latitude.

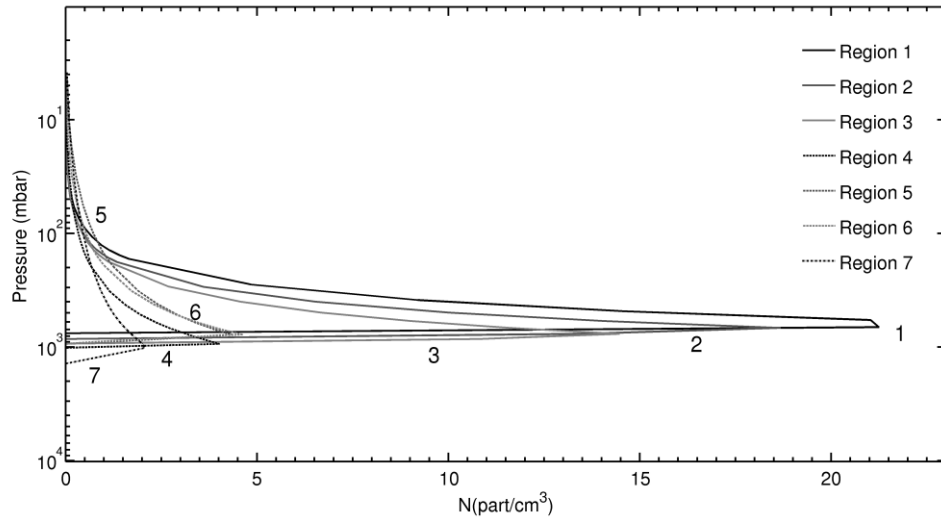


Figure 8: Retrieved particle number concentration as a function of pressure (or altitude) of the tropospheric haze for all regions. Solid lines are used for regions equatorward of the Hexagon Wave and dashed lines for the others.

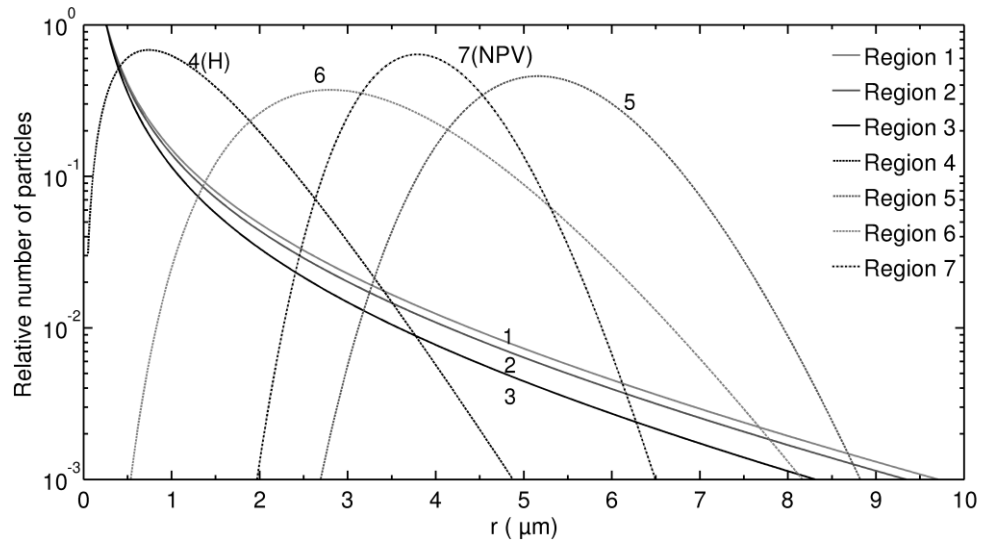


Figure 9: Size distributions of the tropospheric particles for all regions. Solid lines are used for regions equatorward of the Hexagon Wave and dashed lines for the others. H stands for Hexagon Wave and NPV for North Pole Vortex.

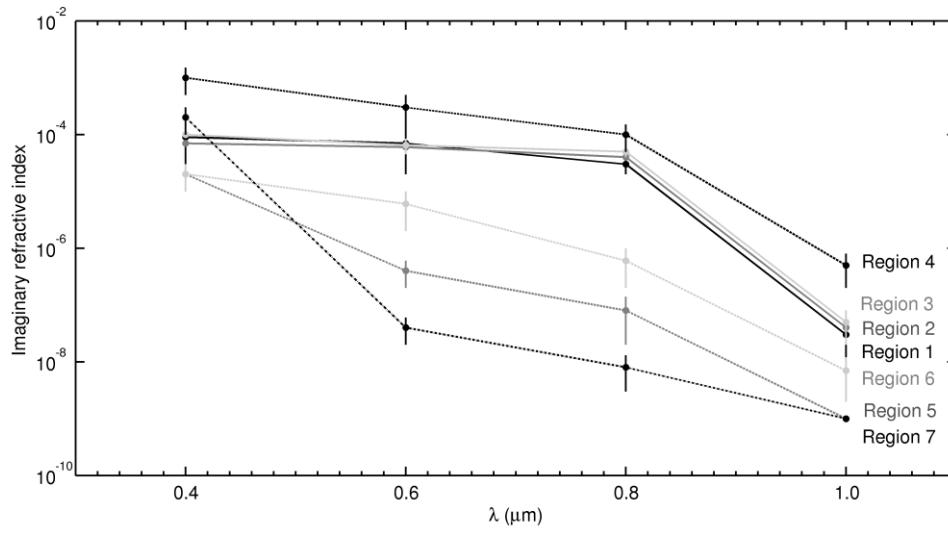


Figure 10: Retrieved imaginary refractive index of the tropospheric particles as a function of wavelength for all regions. Solid lines are used for regions equatorward of the Hexagon Wave and dashed lines for the others.

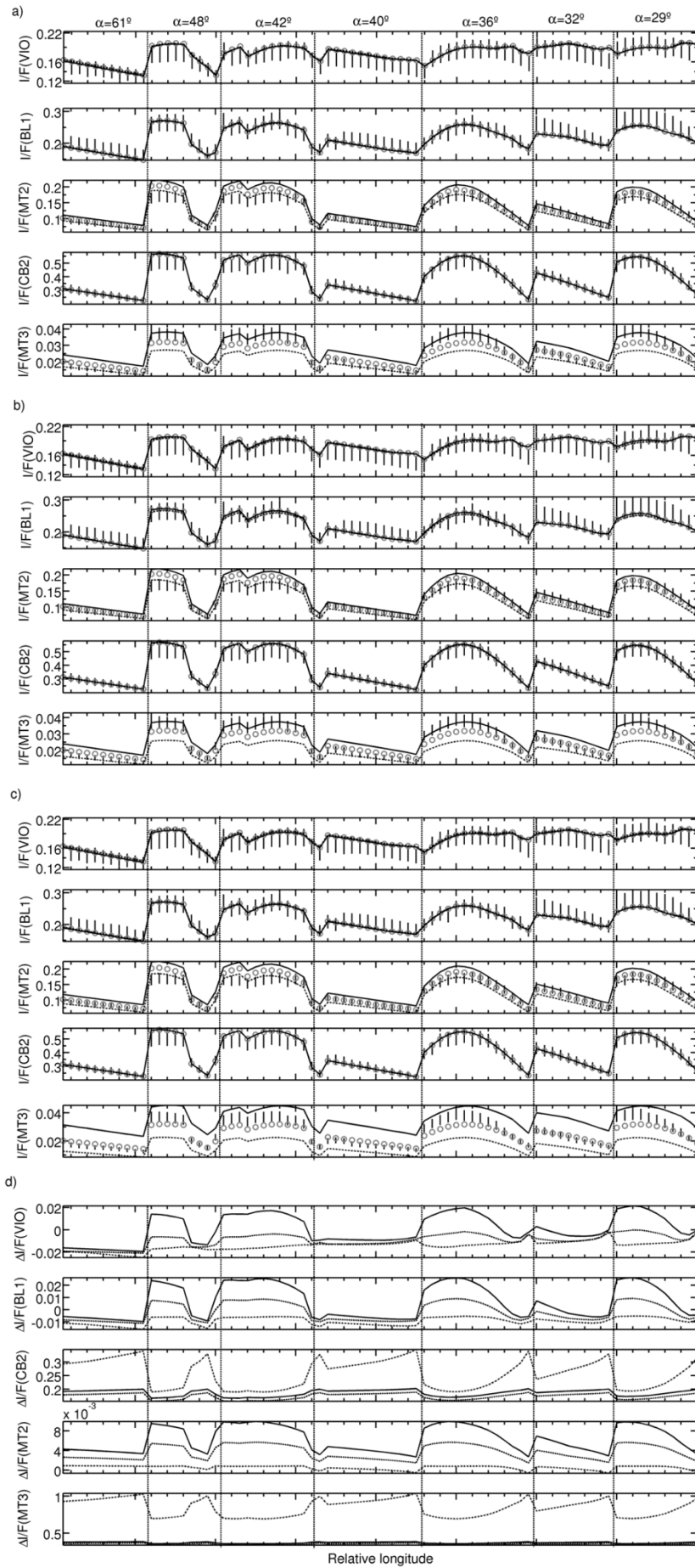
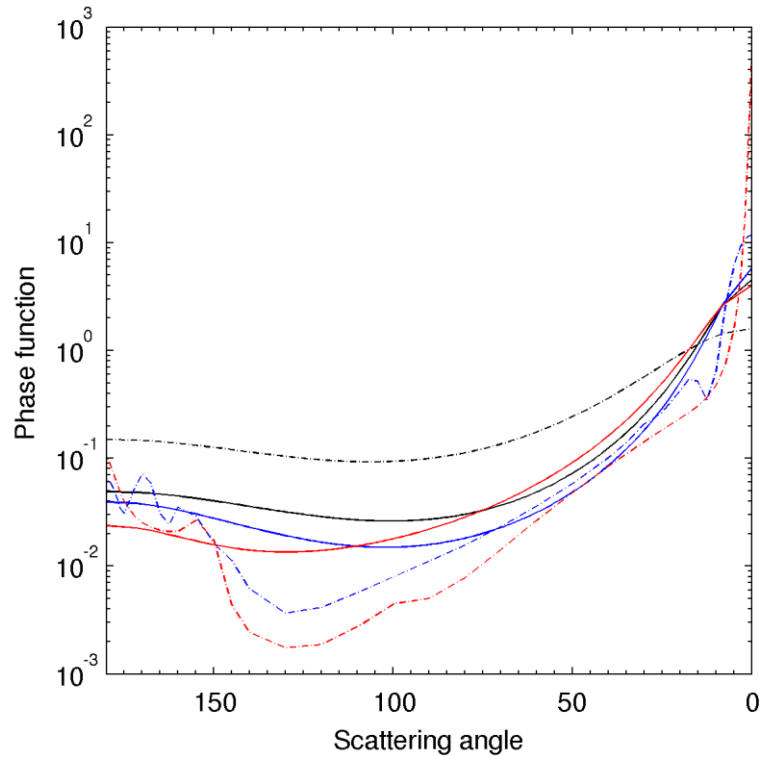


Figure 11: Sensitivity analysis based in a change for a given parameter of the tropospheric haze 1- σ above (solid line) and below (dashed line) of the nominal value for the following parameters: a) altitude of the haze base; b) particle peak concentration; c) scale height. In a), b) and c) the gray circles correspond to the best model, the vertical solid lines are for the measured values and their corresponding uncertainties. Panel shows the reflectivity change $\Delta I/F$ for small changes (1%) of the tropospheric parameters for each of the filters. Here, the solid line corresponds to the variation of the height of the base of the tropospheric haze, the dashed line corresponds to the variation of the particle peak concentration and the dot-dashed line the variation of the scale height. Vertical lines separate the different phase angles (α). For an explanation of x axis, see Figure 3 caption.

745



746

747 **Figure 12.** Henyey-Greenstein approximation to the Mie-calculated phase function and
 748 comparison with the phase function of Tomasko and Doose and the phase function of Pérez-
 749 Hoyos. The dashed black line corresponds to the phase function of Tomasko and doose (1984)).
 750 The black line to the phase function of Pérez-Hoyos et al. 2016. The blue line is the 2HG of the
 751 región 3 while the dashed blue line is the Mie phase function of that region. The red line
 752 corresponds to the 2HG of region 5 and the dashed red line to the Mie phase function of this
 753 region.

754

755 **References**

756 Allison, M., D. A. Godfrey, and R. F. Beebe, 1990. A wave dynamical interpretation of
757 Saturn's Polar Hexagon, *Science*, 247, 1061–1063.

758 Antuñano, A., Río-Gaztelurrutia, T., Sánchez-Lavega, A., 2015. Dynamics of Saturn's
759 polar regions. *Journal of Geophysical Research (Planets)* **120**(Feb.), 155–176.

760 Antuñano, A. Río-Gaztelurrutia, T., Sánchez-Lavega, A and Rodriguez_Aseguinolaza
761 J., 2018. Cloud, morphology and dynamics in Saturn's Northern Polar Region. *Icarus*
762 299, 117 – 132.

763 Baines, K.H., Momary, T.W., Fletcher, L.N., et al., 2009. Saturn's north polar cyclone
764 and hexagon at depth revealed by Cassini/VIMS. *Planetary and Space Science* 57 (Dec.),
765 1671–1681.

766 Barbosa-Aguiar, A. C., P. L. Read, Robin D. Wordsworth, T. Salter, and Y. H.
767 Yamazaki, 2010, A laboratory model of Saturn's North Polar Hexagon, *Icarus*, 206,
768 755–763.

769
770 Barrado-Izagirre, N., Sánchez-Lavega, A., Pérez-Hoyos, S., et al., 2008. Jupiter's polar
771 clouds and waves from Cassini and HST images: 1993 - 2006. *Icarus* 194 (Mar.), 173–
772 185.

773
774 Baines, K. H., Momary, T. W., Fletcher, L. N. et al., 2009. Saturn's north polar cyclone
775 and hexagon at depth revealed by Cassini/VIMS. *Planetary and Space Science*, 57,
776 1671-1681.

777
778 Brown, R.H., Baines, K.H., Bellucci, G., et al., 2004. The Cassini Visual and Infrared
779 Mapping Spectrometer (VIMS) Investigation. *Space Science Reviews* 115 (Dec.), 111–
780 168.

781
782 Caldwell, J., T. Benoit, X.-M. Hua, C. D. Barnett, and J. A. Westphal, 1993. An
783 observed drift of Saturn's Polar Spot by HST, *Science*, 260, 326–329.

784 del Río-Gaztelurrutia, T., Legarreta, J., Hueso, R., et al., 2010. A long-lived cyclone in
785 Saturn's atmosphere: Observations and models. *Icarus* 209, 665–681.

786 Del Genio, A.D., R. K. Achterberg, K. H. Baines, F. M. Flasar, P.L. Read, A. Sánchez-
787 Lavega, A. P. Showman, 2009 . Saturn Atmospheric Structure and Dynamics. Chapter 6
788 in *Saturn after Cassini-Huygens*. M. Dougherty, L. Esposito and T. Krimigis (editors),
789 Springer-Verlag, pp. 113-159.

790 Dyudina, U.A. , Ingersoll, A.P. , Ewald, S.P. , Vasavada, A.R. , West, R.A. , Del Genio,
791 A.D. , Barbara, J.M. , Porco, C.C. , Achterberg, R.K. , Flasar, F.M. , Simon-Miller, A.A
792 ., Fletcher, L.N., 2008. Dynamics of Saturn's south polar vortex. *Science* 319, 1801.

- 793 Dyudina, U.A., et al., 2009. Saturn's south polar vortex compared to other large vortices
794 in the solar system, *Icarus*, 202, 240–248.
- 795 Fletcher, L.N., et al., 2008. Temperature and composition of Saturn's polar hot spots
796 and Hexagon. *Science* 319, 79–81.
- 797 Fletcher, Leigh N., Irwin, P. G. J., Achterberg, R. K.; et al., 2016. Seasonal variability of
798 Saturn's tropospheric temperatures, winds and para-H₂ from Cassini far-IR
799 spectroscopy. *Icarus*, 264, 137–159
- 800 Fouchet T., J. I. Moses, B.J. Conrath., 2009. Saturn: Composition and Chemistry.
801 Chapter 5 in *Saturn after Cassini-Huygens*. M. Dougherty, L. Esposito and T. Krimigis
802 (editors), Springer-Verlag, pp. 83–112.
- 803 García-Melendo, E., A. Sánchez-Lavega, J. F. Rojas, S. Pérez-Hoyos, and R. Hueso,
804 2009. Vertical shears in Saturn's eastward jets at cloud level. *Icarus* 201, 818–820.
- 805 García-Melendo, E., A. Sánchez-Lavega, S. Pérez-Hoyos, and R. Hueso, 2011. Saturn's
806 zonal wind profile in 2004 - 2009 from Cassini ISS images and its long-term variability.
807 *Icarus* 215, 62–74.
- 808 Godfrey, D.A., 1988. A hexagonal feature around Saturn's North Pole. *Icarus* 76, 335–
809 356.
- 810 Hansen, J.E., Travis, L.D., 1974. Light scattering in planetary atmospheres. *SpaceSci.*
811 *Rev.* 16, 527–610.
- 812 Hueso, R., J. Legarreta, J. F. Rojas, J. Peralta, S. Pérez-Hoyo, T. del Río-Gaztelurrutia,
813 and A. Sánchez-Lavega, 2010. The Planetary Laboratory for Image Analysis (PLIA).
814 *Adv. Space Res.* 6, 1120–1138.
- 815 Irwin, P.G.J., Teanby, N.A., de Kok, R., et al., 2008. The NEMESIS planetary
816 atmosphere radiative transfer and retrieval tool. *J. Quant. Spectrosc. Radiat. Transf.* 109,
817 1136–1150.
- 818 Irwin, P.G.J., Fletcher, L.N., Read, P.L., et al., 2015. Spectral analysis of Uranus' 2014
819 bright storm with VLT/SINFONI. *Icarus* 264, 72–89
- 820 Karkoschka, E., and M.G. Tomasko, 1993. Saturn's upper atmospheric hazes observed
821 by the Hubble Space Telescope. *Icarus* 126, 428–441.
- 822 Karkoschka, E., Tomasko, M.G., 2005. Saturn's vertical and latitudinal cloud structure
823 1991–2004 from HST imaging in 30 filters. *Icarus* 179, 195–221.
- 824 Kossin, J.P., and Schubert, W.H., 2001. Mesovortices, Polygonal Flow Patterns, and
825 Rapid Pressure Falls in Hurricane-Like Vortices. *Journal of Atmospheric Sciences*
826 58(Aug.), 2196–2209.

- 828 Kattawar, G.W., 1975. A three parameters analytic phase function for multiple
829 scattering calculations . J. Quant. Spect. & Rad. Transfer 15, 839-849.
- 830 Lucarini, V., Saarinen, J.J., Peiponen, K.E., Vartiainen, E.M., 2005. Kramers–
831 Kronig Relations in Optical Materials Research. Springer-Verlag Berlin Heidelberg.
832 Germany.
- 833 MacQueen, J. B., 1967. Some methods for classification and analysis of multivariate
834 observations. Proceedings of the Fifth Symposium on Math, Statistics, and Probability
835 (pp. 281-297). Berkeley, CA: University of California Press.
- 836 Martonchik, J.V., Orton, G.S., Appleby, J.F., 1984. Optical properties of NH₃ ice from
837 the far infrared to the near ultraviolet. Appl. Optics 23, 541–547.
- 838 Morales-Juberías, R., K.M. Sayanagi, T.E. Dowling, and A.P. Ingersoll, 2011.
839 Emergence of polar-jet polygons from jet instabilities in a Saturn model. Icarus 211,
840 1284–1293.
- 841 Ortiz, J.L, Moreno, M., And A. Molina., 1996. Saturn 1991–1993: Clouds and Hazes.
842 Icarus 119, 53–66.
- 843 Pérez-Hoyos, S., Sánchez-Lavega, A., French, R.G., Rojas, J.F., 2005. Saturn’s cloud
844 structure and temporal evolution from ten years of Hubble space telescope images
845 (1994–2003). Icarus 176, 155–174.
- 846 Pérez-Hoyos, S., J.F. Sanz-Requena, A. Sánchez-Lavega, M.H. Wong, H.B. Hammel,
847 G.S. Orton, I. de Pater, A.A. Simon-Miller, J.T. Clarke, and K. Noll, 2012. Vertical
848 cloud structure of the 2009 Jupiter impact base from HST/WFC3 observations. Icarus
849 221, 106–1078.
- 850 Pérez-Hoyos S., José Francisco Sanz-Requena, Agustín Sánchez-Lavega, Patrick G.J.
851 Irwin, Andrew Smith, 2016. Saturn’s tropospheric particles phase function and spatial
852 distribution from Cassini ISS 2010–11 observations. Icarus 277, 1-18.
- 853 Porco, C.C., West, R.A., Squyres, S., et al., 2004. Cassini Imaging Science: Instrument
854 Characteristics and Anticipated Scientific Investigations at Saturn. Space Science
855 Reviews 115 (Dec.), 363–497.
- 856 Roman, M.T., Banfield, D., Gierasch, P.J., 2013. Saturn’s cloud structure from Cassini
857 ISS, Icarus 225. 93-110.
- 858 Sanz-Requena, J.F., Pérez-Hoyos, S., Sánchez-Lavega, A., et al., 2012. Cloud structure
859 of Saturn’s 2010 storm from ground-based visual imaging. Icarus 219, 142–149.
- 860 Sánchez-Lavega, A., J. Lecacheux, F. Colas, and P. Laques, 1993. Ground-based
861 observations of Saturn’s North Polar Spot and Hexagon. Science, 260, 329–332.
- 862 Sánchez Lavega, A., J. F. Rojas, J. R. Acarreta, J. Lecacheux, F. Colas, and P. V. Sada,
863 1997. New observations and studies of Saturn’s long-lived North Polar Spot, Icarus,
864 128, 322–334.

- 865 Sánchez-Lavega, A., R. Hueso, S. Pérez-Hoyos, and J. F. Rojas, 2006. A strong vortex
866 in Saturn's south pole. *Icarus* 184, 524–531.
- 867 Sánchez-Lavega, A., T. del Río-Gaztelurrutia, R. Hueso, J. M. Gomez-Forrellad, J. F.
868 Sanz-Requena, J. Legarreta, E. García-Melendo, F. Colas, J. Lecacheux, L. N. Fletcher,
869 D. Barrado-Navascués, D. Parker & the International Outer Planet Watch Team, T.
870 Akutsu, T. Barry, J. Beltran, S. Buda, B. Combs, F. Carvalho, P. Casquinha, M.
871 Delcroix, S. Ghomizadeh, C. Go, J. Hotershall, T. Ikemura, G. Jolly, A. Kazemoto, T.
872 Kumamori, M. Lecompte, P. Maxson, F. J. Melillo, D. P. Milika, E. Morales, D. Peach,
873 J. Phillips, J. J. Poupeau, J. Sussenbach, G. Walker, S. Walker, T. Tranter, A. Wesley,
874 T. Wilson & K. Yunoki for The International Outer Planet Watch (IOPW) Team, 2011 .
875 Deep winds beneath Saturn's upper clouds from a seasonal long-lived planetary-scale
876 storm. *Nature* 475, 71-74 (2011);doi:10.1038/nature10203.
- 877 Sánchez-Lavega, A., 2011. *An Introduction to Planetary Atmospheres*. CRC Press, Boca
878 Raton, FL, USA.
- 879 Sánchez-Lavega, A., Río-Gaztelurrutia, T., Hueso, R., et al., 2014. The long-term
880 steady motion of Saturn's Hexagon and the stability of its enclosed jet stream under
881 seasonal changes. *Geophysical Research Letters*, 41 (Mar.), 1425–1431.
- 882 Sánchez-Lavega A., D. Garcia, T. del Rio-Gaztelurrutia, A. Garcia-Muñoz, S. Perez-
883 Hoyos, R. Hueso, 2017. Cassini limb images of hazes in Saturn's northern hemisphere,
884 49th DPS meeting, abstract 205.6.
- 885 Sayanagi, K. M., S. P. Ewald, U. A. Dyudina, and A. P. Ingersoll, 2013. American
886 Astronomical Society, DPS meeting #45, #509.06.10.
- 887 Sayanagi, K.M., Kevin H. Baines, Ulyana A. Dyudina, Leigh N. Fletcher, Agustin
888 Sánchez-Lavega, Robert A. West, 2016. Saturn's polar atmosphere. Chapter for Saturn
889 in the 21st Century.
- 890 Sayanagi, K.M., Blalock, J.J, Dyudina, U.A., Ewald, S.P., Ingersoll, A.P., 2017. Cassini
891 ISS observation of Saturn's north polar vortices comparison to the south polar vortex.
892 *Icarus* 285, 68-82.
- 893 Sylvestre, M., Guerlet, S., Fouchet, T. Spiga, A., Flasar, F.M., Hesman, B., Bjoraker,
894 G.L. 2015 Seasonal changes in Saturn's stratosphere inferred from Cassini/CIRS limb
895 observations. *Icarus*, 258, 224-238.
- 896 Tomasko, M.G., Doose, L.R., 1984. Polarimetry and photometry of Saturn from Pioneer
897 11: Observations and constraints on the distribution and properties of cloud and aerosol
898 particles. *Icarus* 58, 1–34.
- 899 West, R.A., Smith, P.H., 1991. Evidence for aggregate particles in the atmospheres of
900 Titan and Jupiter. *Icarus* 90, 330–333.
- 901 West, R.A., Baines, K.H., Karkoschka, E., Sánchez-Lavega, A., 2009. Clouds and
902 aerosols in Saturn's atmosphere. In: Dougherty, M.K., Esposito, L.W., Krimigis,
903 S.M. (Eds.), *Saturn from Cassini-Huygens*. Springer, Netherlands, pp.161–179.

904 West, R. et al., 2010. In-flight calibration of the Cassin imaging sciencesub-system
905 camera.Planet. Space Sci.58, 1475-1488.

906 West, R.A., P.A. Yanamandra-Fisher and V. Korokhin, 2015. Polarization of the gas
907 giant planets, Saturn's rings, and Titan: Observations and Interpretation", in Polarimetry
908 of stars and planetary systems, L. Kolokolva, J. Hough and A.-Chantal Levasseur-
909 Regourd Eds., Cambridge Univ. Press.

910