

# Supporting Information:

## A dynamic simulation model to support reduction in illegal trade within legal wildlife markets

### **Appendix S1. Open-ended Key Informant Interviews**

Key-informant open-ended semi-structured interviews started with an explanation of the project scope and objectives and followed with a list of reference questions (see below). Interviews were performed during March-April 2019. Due to COVID-19, all interviews were done over the phone or email. Before each interview, we informed participants that participation was voluntary and that participants could refuse to answer any particular question. We used snowballing sampling, starting with leaders of the main fishers' associations in the region and known contacts of the researchers. In total, we interviewed 23 informants, including fishers, government officials, intermediaries, vendors, NGOs staff, and enforcement agents. Depending on the key-informant's role, some questions were omitted, and others were explored in more depth. Interviews over the phone lasted between 30 and 90 minutes. The study complied with Oxford University's ethical requirements (approval number R68516/RE001). These methods represent a subsample of those reported in Oyanedel et al. 2021.

Key-informant interview list of reference questions

*a. Factors affecting actor's decision to trade legal or unreported products*

- What are the main factors that affect the decision to trade legal or unreported/illegal common hake?

24 - Do intermediaries always carry legal hake? How much?

25 - What determines the legal/illegal purchase ratio?

26 - Does this ratio vary?

27 - What affects its variability?

28

29 *b. Operation of the legal/unreported market*

30 - Can legal and unreported products be distinguished at the market?

31 - How does fish enter the market without a permit?

32 - Is there a price premium for legal products? How much is it?

33

34 *c. Overarching market dynamic*

35 - What are the most important factors that determine prices?

36 - Does fishing activity respond to prices? Or, alternatively, are prices driven by the  
37 quantities of fish landed

38

39 *d. Prior ranges*

40 - What is the price of a legal and an illegal unit, at the port and at the market?

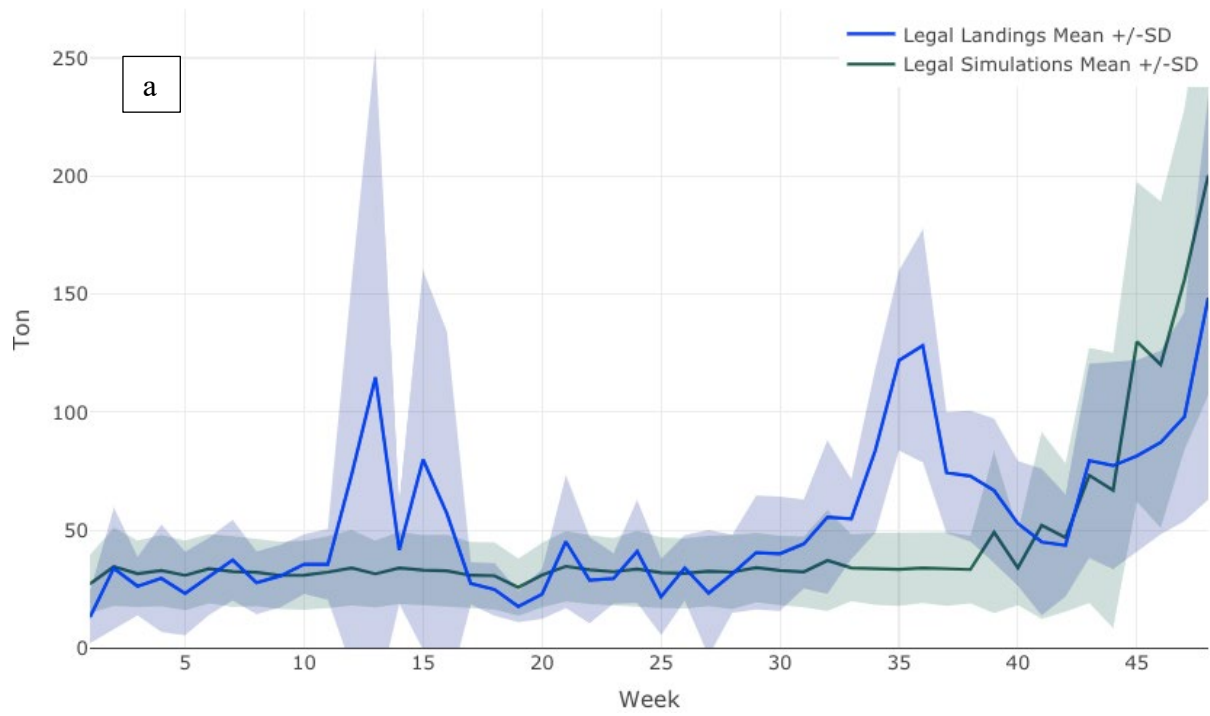
41

## 42 **Appendix S2. Model runs without and with enforcement data**

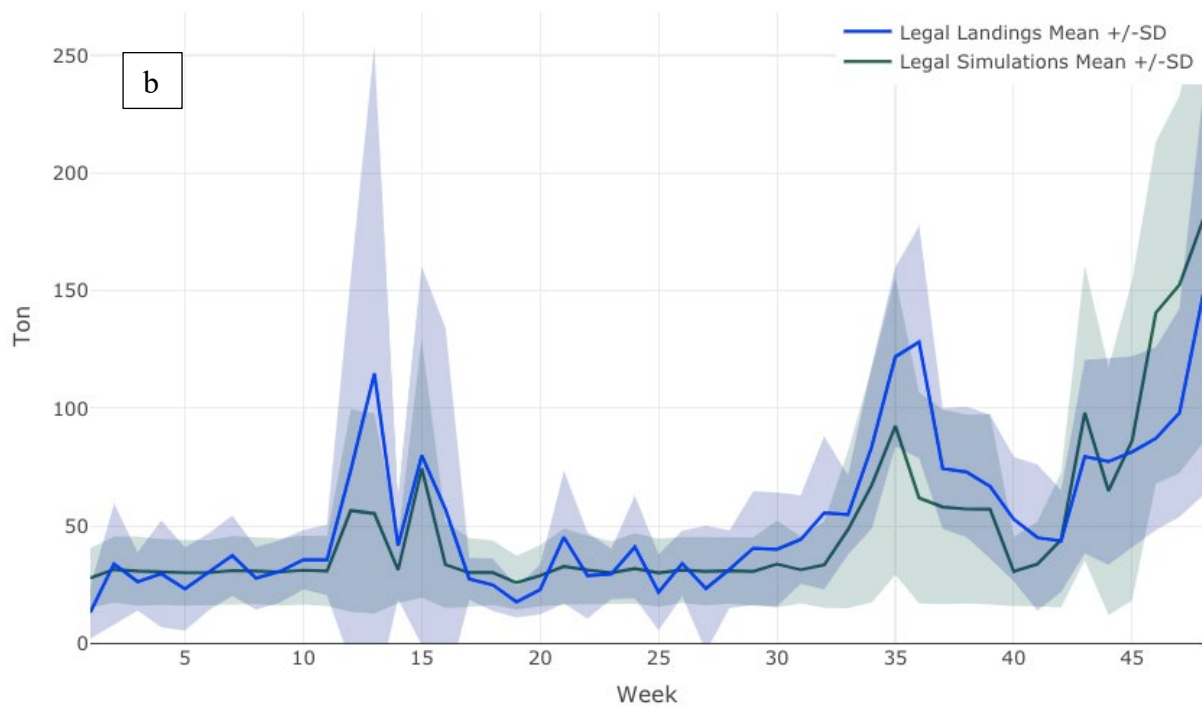
43

44 To test the appropriateness of including weekly enforcement effort data into the  
45 model, we first run the model with a randomly generated weekly vector of enforcement  
46 effort (with minimum and maximum similar to data). We then run the model again, included  
47 the weekly enforcement effort data (average of 2014-2019). We found that including the

48 enforcement data helped better predict the legal landings data dynamics (Figure SM 1). This  
49 was especially so for the peaks in legal landings around week 11-16 and 33-37.



50



51

52 **Figure SI 1.** Model run without (a) and with (b) weekly enforcement effort data

53

54

55 **Appendix S3. Prior range construction and data sources**56 **Table S1.** Parameters used in the simulation model case study application and their source.

Parameter	Description	Type	Value	Source
Theta: Efficiency of enforcement ( $\theta_e$ )	Fraction of illegal units that each enforcement action detects. We fixed this parameter for each simulation, so the same value is used across weeks	Prior – Uniform distribution	Range: 2e-7 - 2e-8 units/enforcement action	Number of activities from enforcement records and overall illegal units traded estimates from Oyanedel et al. 2021. See below for detail
Beta: Price premium ( $\beta_1$ )	Price paid to traders for legal units at the end-market. Unit is Chilean pesos. We fixed this parameter for each simulation	Prior – Uniform distribution	Range: CLP 0-3,000 (4,3 USD)	Range obtained from key informant interviews
Minimum legal fraction per week ( $x_{l,m}$ )	Percentage set minimum of legal units that traders take each week. We fixed this parameter for each simulation	Prior – Uniform distribution	Range: 10-20% of a truckload	Range obtained from key informant interviews
Price elasticity ( $\epsilon_p$ )	Elasticity of the price of units at the end-market, depending on units available. We fixed this parameter for each simulation and used the same value for legal and illegal units	Prior – Uniform distribution	Range: proportion from 0 to 1	Broad range used because we obtained no information from key informant interviews
Cost elasticity ( $\epsilon_c$ )	Elasticity of the cost of units at the port, depending on units available. We fixed this parameter for each simulation and used the same value for legal and illegal units	Prior – Uniform distribution	Range: proportion from 0 to 1	Broad range used because we obtained no information from key informant interviews
Permit fee ( $V_l$ )	Value charged to traders for legal units at the ports. Unit is Chilean pesos. We fixed this parameter for each simulation	Data	CLP\$ 3,000 (4,3 USD) except towards end of the year	Value obtained from key informant interviews
Permit fee elasticity ( $\epsilon_v$ )	The rate at which permit fee value decreases towards the end of the year. We fixed this parameter for each simulation	Prior – Uniform distribution with range	Proportion from 0.15 to 0.25	We obtained the range for this parameter through iterations of the model and fit of data, see below for formula
Total units traded ( $\delta$ )	Sum of legal and illegal units. This parameter changes each week, when we draw random values from the prior	Prior – Uniform distribution	Range: 2000 – 13333 units/week	Upper limit obtained from illegal estimates from Oyanedel et al. 2021. The lower limit is no illegal landings
Legal units traded ( $x_{l,d}$ )	Data on legal units traded each week	Data – Weekly mean value and SD for 2014-2019 period	See Table S2	From government landings data

Enforcement actions ( $\theta_a$ )	Data on the number of enforcement actions (officers doing enforcement in the region) each week	Data – Weekly mean value and SD for 2014-2019 period	See Table S2	From government enforcement data
Price reference ( $P_R$ )	We used a reference price to calculate price considering elasticity. We used a reference quantity, which we set at the mean of the total landing's prior. We fixed this parameter across weeks and simulations	Data	CLP\$ 30,000 (43 USD)	Value obtained from key informant interviews
Cost reference ( $C_R$ )	We used a reference cost to calculate price considering elasticity. We also used a reference quantity, which we set at the mean of the total landing's distribution. We fixed this value across weeks and simulations	Data	CLP\$ 15,000 (21,5 USD)	Value obtained from key informant interviews
Fixed fine if detected ( $f_i$ )	Monetary fixed fine if detected trading illegal units, which we fixed across weeks and simulations	Data	CLP 9,200,00 (13,090 USD)	From government legislation
Fine per illegal unit constant ( $c_i$ )	Monetary fine if detected trading illegal units, per unit, fixed across weeks and simulations	Data	4P <sub>i</sub>	From government legislation
Overall and stage-specific quota (Q)	Total quota for legal trading in a year, which we fixed across simulations. The government gives this quota in 3 periods within the year	Data – Mean value for 2014-2019	98,000 units. See below for periods	From government registers

57

58

59 *a. Efficiency of enforcement ( $\theta_e$ )*

60 For the efficiency of enforcement ( $\theta_e$ ) parameter, the lower range of the prior  
61 was calculated as:

$$62 \quad \theta_e = x_c / (\theta_E n_T i_r)$$

63 Where:  $x_c$ = total amount of units confiscated by the enforcement authority  
64 during the 2014-2019 period (10,230);  $\theta_E$ = sum of the effort in terms of number of  
65 enforcement visits during the 2014-2019 period (1,538);  $n_T$ = total units traded  
66 (3,788,373) considering legal catch, and using  $i_r$  from Oyanedel et al. 2021 that

67 illegal rate maximum is 88%. For the upper range of the prior, we multiplied this  
 68 lower range value by ten, to account for a broad dispersion of how much the real  
 69 value of  $\theta_e$  could be.

70

71 *b. Permit fee ( $V_l$ ) equation*

72 Based on the permit fee elasticity ( $\epsilon_v$ ), we calculated  $V_l$  in the model as follow:

73 
$$V_l = \max(0, V_r(1 - \epsilon_v(\max(0, R - R_0) / R_0)))$$

74 Where:  $V_r$ = permit fee reference value (CLP 3,000);  $R = ql_t / (T-t+1)$ ;  $R_0 =$   
 75  $Q / (T+1)$ ;  $ql_t$  = quota left in time t;  $Q$  = overall quota;  $T$ = time horizon.

76

77 *c. Overall and staged quota ( $Q$ )*

78 The overall quota for the 2014-2019 period mean was 98,000 units, given in stages,  
 79 according to government data as:

- 80 ○ January= 8,613
- 81 ○ February to June=49,000
- 82 ○ July to December=98,000

83

84 *d. Data sets used*

85 **Table S2.** Data sets used: landings mean (+/- SD) per week and enforcement (mean) count  
 86 of visits per week in the region.

Week	Landings			Enforcement
	Mean	Mean + SD	Mean - SD	Mean
1	493	902.49	83.51	1.33
2	1258	2203.79	312.21	4.00
3	977	1434.60	519.40	6.00
4	1101	1942.55	259.45	4.50

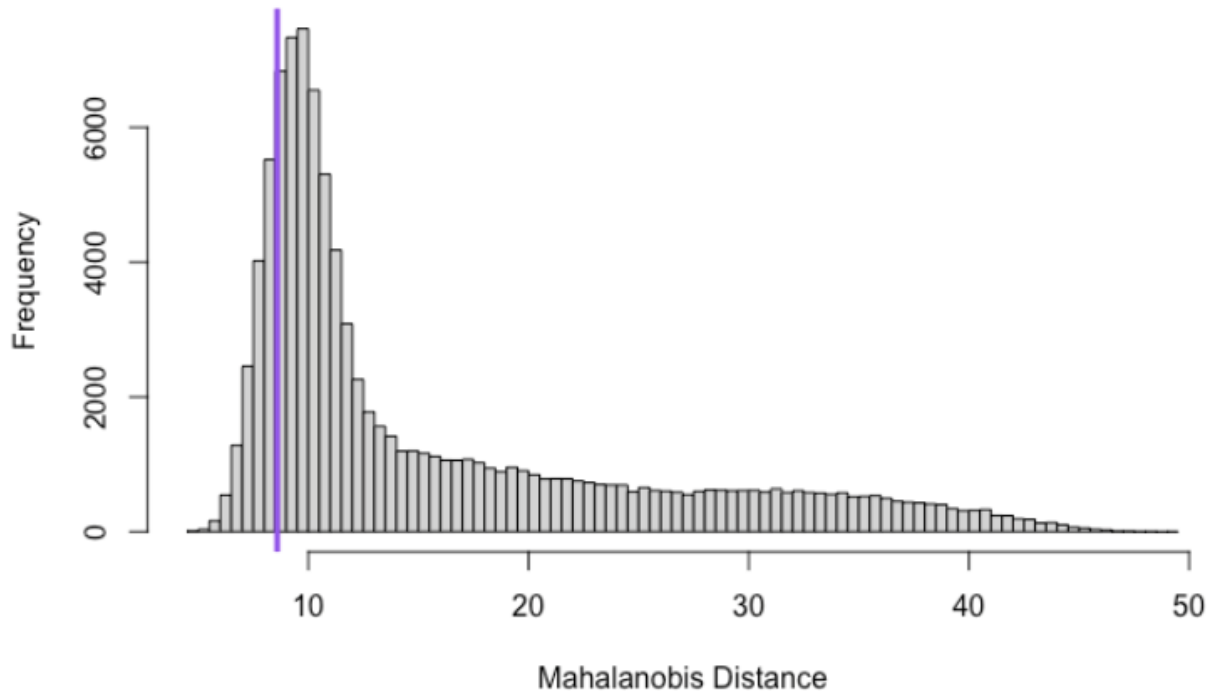
5	862	1518.96	205.04	2.33
6	1134	1739.31	528.69	4.17
7	1388	2019.79	756.21	5.00
8	1031	1521.88	540.12	5.50
9	1137	1627.28	646.72	4.83
10	1323	1791.84	854.16	4.83
11	1320	1874.06	765.94	5.67
12	2731	5767.54	-305.54	9.67
13	4254	9402.74	-894.74	9.33
14	1544	2389.20	698.80	4.17
15	2964	5935.31	-7.31	11.83
16	2117	4973.98	-739.98	6.17
17	1022	1353.31	690.69	6.33
18	927	1340.03	513.97	3.17
19	657	900.70	413.30	3.17
20	851	1241.07	460.93	4.33
21	1675	2715.87	634.13	6.00
22	1072	1749.47	394.53	5.67
23	1098	1496.17	699.83	4.33
24	1522	2329.96	714.04	5.67
25	812	1409.37	214.63	2.67
26	1264	1780.41	747.59	4.33
27	870	1859.05	-119.05	2.17
28	1173	1785.84	560.16	3.33
29	1504	2398.33	609.67	3.83
30	1486	2384.21	587.79	5.33
31	1639	2336.42	941.58	3.67
32	2060	3264.83	855.17	4.83
33	2030	2656.30	1403.70	7.17
34	3099	4386.78	1811.22	8.50
35	4517	5926.72	3107.28	10.83
36	2091	4705.74	-523.74	7.50
37	4314	6070.10	2557.90	7.50
38	2647	3659.65	1634.35	7.33
39	2590	3331.04	1848.96	7.17
40	2316	3352.96	1279.04	3.00
41	1760	2829.25	690.75	4.00
42	1549	2439.28	658.72	4.83
43	2336	4086.18	585.82	7.33
44	3071	4191.20	1950.80	4.33
45	2896	4470.63	1321.37	3.50

46	2868	4262.47	1473.53	5.83
47	3532	5136.05	1927.95	5.50
48	5350	8660.61	2039.39	3.50

87

88

89 **Appendix S4. Mahalanobis distance distribution**



90

91 **Figure SI 2.** Mahalanobis distance distribution of model results. Purple line indicates  
 92 threshold, so simulations to the left are accepted (~15%).

93

94

95

96

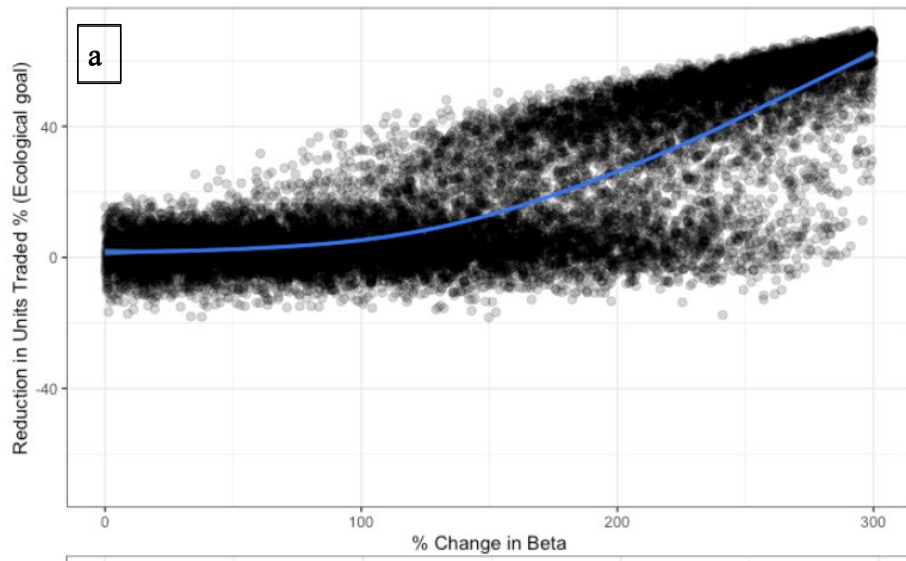
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98

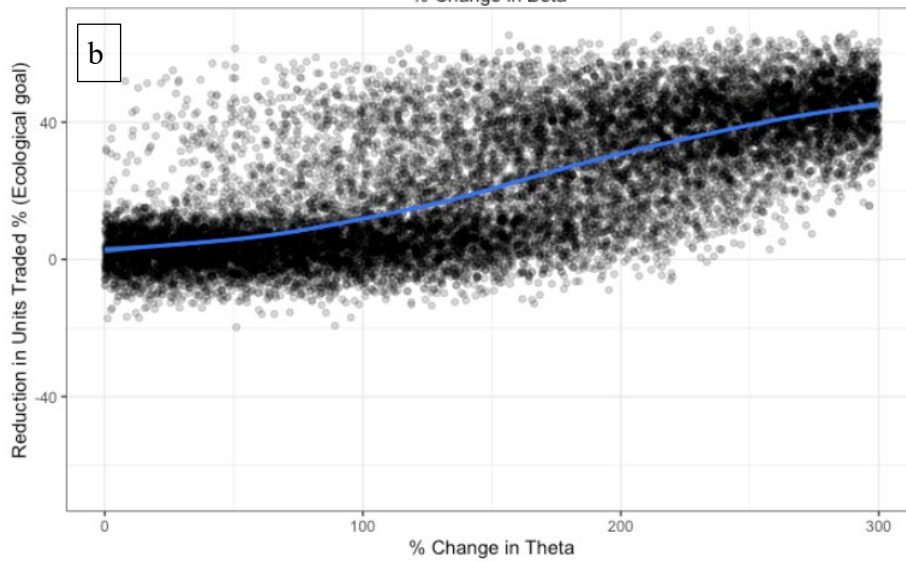
99

100

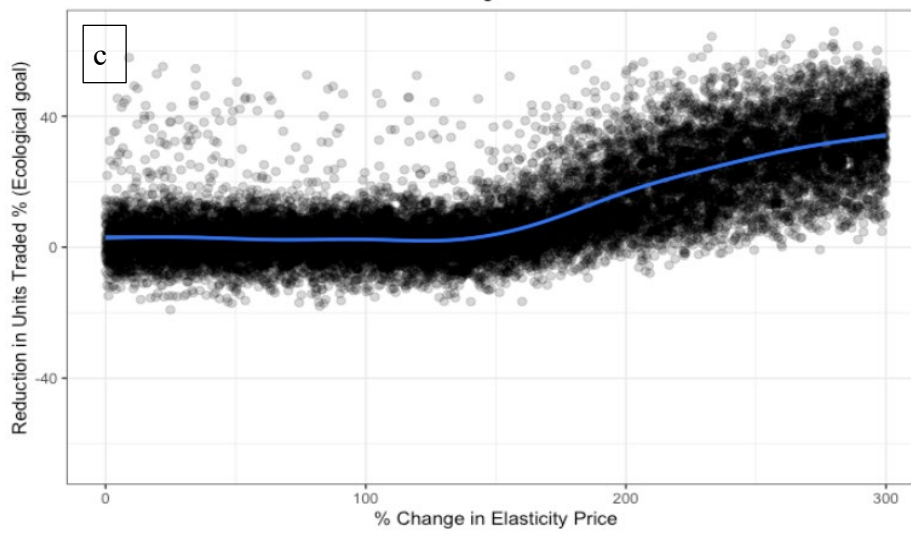
101 **Appendix S5. Sensitivity Analysis**



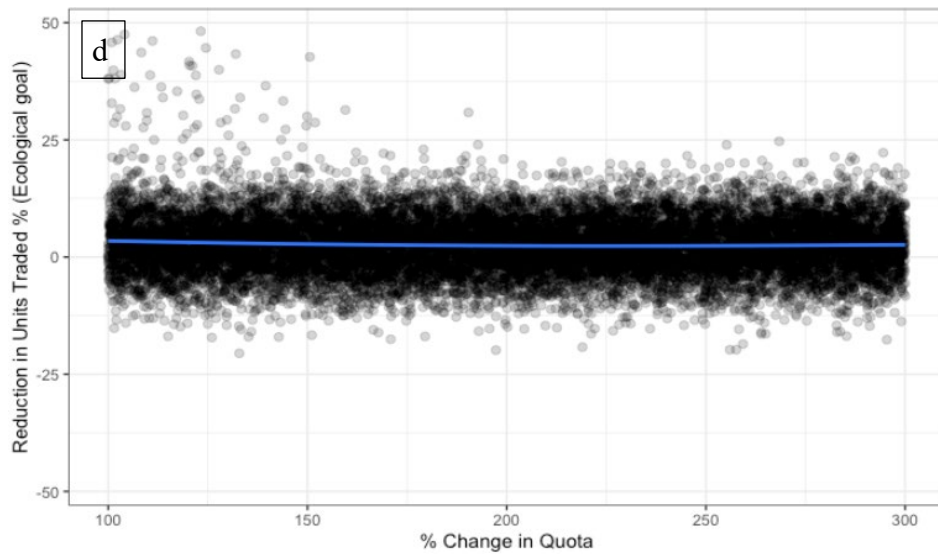
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105  
106  
107  
108  
109  
110  
111  
112

**Figure S3.** Evaluation of ecological sustainability of the fishery improvements (as measured by decreases in units traded) when changing the value of parameters that are proxies for possible policy levers: a) theta (efficiency of enforcement); b) beta (price premium); c) price elasticity, and d) quota. Black dots represent simulation results, and the blue line is the smoothed conditional mean.

113

## R Code

114

### A dynamic simulation model to support reduction in illegal

115

### trade within legal wildlife markets

116

#### Load required packages

117

```
```{r, cache=FALSE}
```

118

```
library(ggplot2)
```

119

```
library(plotly)
```

120

```
```
```

121

122

#### Load data

123

```
```{r, cache=FALSE}
```

124

```
legal_units_data <- #Here Load a vector of data for legal units traded  
(mean). For instance, use per week value. If no data available can use the  
following to try the model read.csv('https://raw.githubusercontent.com/XXX  
/illegal_fishing/master/data/unitsYear.csv')
```

125

126

127

128

```
enforcement_data <- #Same than units, could use this dataset for demonst  
ration: read.csv ('https://raw.githubusercontent.com/XXX/illegal_fishing/m  
aster/data/enfcomnocom.csv')
```

129

130

131

```
```
```

132

133

#### Setting variable

134

```
```{r, cache=FALSE}
```

135

```
####Setting variables for the model. All monetary values are in Chilean pes  
os
```

136

137

```
iterations= 10000    ### Number of times the model is ran
```

138

```
weeks= 48           ### Weeks in a normal year, for demonstration purpos  
es we use 48 which excludes September when there is no fishing in our case  
study
```

139

140

141

```
legal_units_data = legal_units_data[1:weeks,]
```

142

```
cost = 500          ### Approximate per unit traded
```

143

```
fine = 9.2e+05     ### Fine expected if detected trading illegal produc  
ts
```

144

145

```
permit_fee = 3000  ### Use if there is a cost difference between legal  
and illegal products at the harvest level
```

146

147

```
c_ref= 15000       ### Reference cost per unit
```

148

```
p_ref= 30000       ### Reference price per unit
```

149

```
mean_land=mean(legal_units_data$mean)*weeks
```

150

151

```
##### Creates a vector of quota available in each week. Can be the same val
```

```

152 ue across weeks, or can be given in stages (see Supplementary Material)
153 quota_overall= 98000 ### Yearly overall quota for the species
154 quota_available      = (1:weeks)
155 quota_available[1:weeks] = quota_overall
156
157 #### Create a data frame of enforcement activities mean per week
158 enforcement=as.data.frame((enforcement_data[,3]))
159 ````

```

160

## 161 Create priors for Approximate Bayesian Approach

```

162 ````{r, cache=FALSE}
163 ###First, create ranges
164 ####Prior range for beta (price premium)
165 beta_min=0 ### price premium lower limit
166 beta_max=3000 ###price premium higher limit
167
168 ####Prior range for overall units trade
169 ####First define overall range of units traded and how much are illegal uni
170 ts traded ratio
171 MaxIllegalrate=0.85 #85% Illegal, higher limit (this can be changed if
172 there is an estimate of % of illegal units traded in the market)
173 MinIllegalrate=0.0 #0% Illegal, lower limit
174
175 ###Then calculate Prior range
176 T_min=(quota_overall/weeks) * (1/(1-MinIllegalrate)) ## Min overall units
177 traded
178 T_max=(quota_overall/weeks) * (1/(1-MaxIllegalrate)) ## Max overall units
179 traded
180 qr=(T_min+T_max)/2 ## Reference quantit
181 y for elasticities
182
183 ####Prior range for Theta (probability of detection per unit for each enfo
184 rcement action)
185 theta_max= 2e-7 ### See supporting information
186 theta_min= 2e-8
187
188 ###Prior range for cost elasticity
189 E_minC=0
190 E_maxC=1
191
192 ###Prior range for price elasticity
193 E_minP=0
194 E_maxP=1
195
196 ###Prior range for end of year permit_fee elasticity
197 permit_feeend_min=0.15 ### See supporting information, but this might no
198 t be necessary outside of the case study. If there is no need for this par
199 ameter, then use 0
200 permit_feeend_max=0.25
201

```

```

202 ###prior range for minimum Legal per week
203 minlegal_min=0.1 ### See supporting information
204 minlegal_max=0.2
205
206 ####This creates the priors based on the ranges above
207 beta_P = runif(n=iterations, min = beta_min, max = beta_max)
208 theta_P = runif(n=iterations, min=theta_min, max=theta_max)
209 T_I = runif(n=iterations, min=T_min, max=T_max)
210 permit_fee_elasticity_P = runif(n=iterations, min=permit_feeend_min, max
211 =permit_feeend_max)
212 Price_elasticity_P = runif(n=iterations, min=E_minP, max=E_maxP)
213 Cost_elasticity_P = runif(n=iterations, min=E_minC, max=E_maxC)
214 min_legal_P = runif(n=iterations, min=minlegal_min, max=minlegal_m
215 ax)
216 ```

```

217

## 218 Run Simulation model

```

219 ```{r, cache=FALSE}
220 ###Tracks time it takes to run
221 start_time <- Sys.time()
222 start_time
223
224 ##Create matrix for results
224 results = matrix(0,iterations,14) ### Keeps track of simulati
225 on results
226 legal_units = matrix(0,weeks,iterations) ### Keeps track of legal un
227 its in each simulation
228 illegal_units = matrix(0,weeks,iterations) ### Keeps track of illegal
229 units in each simulation
230 permit_fee_value = matrix(0,weeks,iterations) ### Keeps track of permit_f
231 ee value in each simulation
232 Quota_left = matrix(0,weeks,iterations) ### Keeps track of quota Le
233 ft in each simulation
234 ratio = matrix(0,weeks,iterations) ### Keeps track of quota Le
235 ft in each simulation
236
237 ### Start Loop of iterations
238 for (simulation in 1:iterations) ### Start iterations
239 {
240 ###Sample each parameter from the prior
241
242 beta = sample(beta_P,1)
243 theta = sample(theta_P,1)
244 price_elasticity = -(sample(Price_elasticity_P,1))
245 cost_elasticity = -(sample(Cost_elasticity_P,1))
246 permit_fee_elasticity = (sample(permit_fee_elasticity_P,1))
247 min_legal = (sample(min_legal_P,1))
248
249 ##Start Loop of weekly simulations
250 weekly_simulation = matrix(0,weeks,11)

```

```

251
252   for (t in 1:weeks)
253   {
254     prob_detection = theta*enforcement[t,1] # uses the enforcement data per
255     week, otherwise enforcement could be a vector of 1s of length weeks
256     x_T           = sample(T_I,1)           # Sample units for that week
257
258     ###Calculates quota left for end of year and value of permit_fee in t
259     quota         = quota_available[t]
260     quota_left    = (quota-sum(weekly_simulation[,1]))
261     rate_r        = quota_overall/(weeks+1)
262     rate          = quota_left/(weeks-t+1)
263     permit_fee_t = max(0, permit_fee * (1 - permit_fee_elasticity * (max(0, r
264     ate - rate_r) / rate_r)))
265
266     #Calculates prices and costs
267     C_L= (c_ref * (1-((cost_elasticity*((qr-x_T)/qr)))) + permit_fee_t
268     #Elasticity of cost for legal boxes, wrt units + permit_fee
269     C_I= (c_ref * (1-((cost_elasticity*((qr-x_T)/qr))))
270     #Elasticity of cost for illegal boxes, wrt units
271     P_L= (p_ref * (1-((price_elasticity*((qr-x_T)/qr)))) + beta
272     #Elasticity of price legal boxes, wrt units + beta
273     P_I= (p_ref * (1-((price_elasticity*((qr-x_T)/qr))))
274     #Elasticity of price illegal boxes, wrt units
275
276     ###Calculates x_l (legal units), x_i (illegal units) with constraint tha
277     t x_l cannot be higher than x_T, or lower than 0 and there is no trading i
278     f there is no quota left
279     x_l         = x_T-((((P_I-C_I-P_L+C_L-(fine* prob_detection))/(8* prob_
280     detection*(P_L)))) ##Legal units (here we use 8 insted of 2 as indicated
281     in the manuscript, because fines in Chile the variable fine is 4P_L (Suppl
282     ementary Material)
283     min_bound   = if(quota_left>0) {min_legal * x_T} else 0
284     max_bound   = min(x_T, quota_left)
285     x_l         = if(x_l <= max_bound) {x_l} else {max_bound}
286     x_l         = if(x_l <= min_bound) {min_bound} else {x_l}
287     x_i         = if(quota_left>0) {x_T-x_l} else 0
288
289
290     weekly_simulation[t,1] = x_l
291     weekly_simulation[t,2] = x_i
292     weekly_simulation[t,3] = C_L
293     weekly_simulation[t,4] = C_I
294     weekly_simulation[t,5] = P_L
295     weekly_simulation[t,6] = P_I
296     weekly_simulation[t,8] = permit_fee_t
297     weekly_simulation[t,9] = quota_left
298     weekly_simulation[48,9] = quota_left - x_l
299     weekly_simulation[t,10] = (x_i/(x_i+x_l))
300     weekly_simulation[t,11] = (x_l*C_L) + (x_i*C_I)
301
302   }
303

```

```

304
305 ### Fill matrices for posterior analysis
306 legal_units[,simulation] = weekly_simulation[,1]
307 illegal_units[,simulation] = weekly_simulation[,2]
308 permit_fee_value[,simulation] = weekly_simulation[,8]
309 Quota_left[,simulation] = weekly_simulation[,9]
310 ratio[,simulation] = weekly_simulation[,10]
311
312 ## Fill results of each simulation, by summing across weeks and capture
313 prior values
314 results[simulation,1] = sum(weekly_simulation[,1])
315 results[simulation,2] = sum(weekly_simulation[,2])
316 results[simulation,3] = sum(weekly_simulation[,1])+sum(weekly_simulation
317 [,2])
318 results[simulation,4] = beta
319 results[simulation,5] = theta
320 results[simulation,6] = price_elasticity
321 results[simulation,7] = cost_elasticity
322 results[simulation,8] = permit_fee_elasticity
323 results[simulation,9] = sum(weekly_simulation[,2])/(sum(weekly_simulatio
324 n[,1])+sum(weekly_simulation[,2])) ## Ratio
325 results[simulation,10]= simulation
326 results[simulation,12]= min_legal
327
328 }
329
330
331 end_time <- Sys.time()
332 end_time - start_time
333
334
335

```

334

### 335 Mahalanobis distance rejection criteria calculation

```

336 ```{r, cache=FALSE}
337 #Create matrices and units values needed to calculate Mahalanobis distance
338 SimResults = data.frame(results)
339 mahalanobis_dist = matrix(0,iterations,2)
340 true_mean = apply(legal_units_data, 1, mean, na.rm=TRUE)
341 true_std = apply(legal_units_data, 1, sd, na.rm=TRUE)
342 true_cov = diag(true_std ** 2)
343
344
345 #Calculate the Mahalanobis distance for each simulation result
346 for (m in 1:iterations)
347 {
348 mahalanobis_dist[m,1]= sqrt(mahalanobis(legal_units[,m], true_mean, true_c
349 ov))
350 mahalanobis_dist[m,2]=m
351 }
352
353 ##Reject those simulations above the threshold

```

```

354 p=0.95          ## Rejection criteria
355 threshold      = sqrt(qchisq(p=p, df=weeks))
356 mahalanobis_dist_filter= subset(mahalanobis_dist,mahalanobis_dist[,1]<thre
357 hold)
358
359 ## Plot distances and threshold (Line)
360 hist          (mahalanobis_dist[,1], breaks=100, xlab="Mahalanobis Distance",
361 ylab="Frequency of Simulations")
362 abline        (v=threshold, col="purple", lwd=3)
363
364 ## Select those simulations that were accepted
365 Accepted_Legs  = legal_units[,c(mahalanobis_dist_filter[,2])]      #
366 ##Select those legal vectors that passed the filter
367 Accepted_Ills  = illegal_units[,c(mahalanobis_dist_filter[,2])]    #
368 ##Select those illegal vectors that passed the filter
369
370 filter        = mahalanobis_dist_filter[,2]
371 SimResults     = subset(SimResults,SimResults$X10 %in% filter)      ##Select
372 parameter values of those simulations that passed the filter
373
374 #Create posteriors variables for graphs
375 Legalboxes    = SimResults$X1
376 Illegalboxes  = SimResults$X2
377 unitsboxes    = SimResults$X3
378 Beta          = SimResults$X4
379 Theta         = SimResults$X5
380 ElasticityPrice= SimResults$X6
381 ElasticityCost = SimResults$X7
382 permit_feeEndofyear = SimResults$X8
383 Minlegal      = SimResults$X12
384 Ratio         = SimResults$X9
385
386
387
388
389
390
391
392
393
394
395
396
397
398
399
400
401

```

### 387 Parameter Posterior Graphs

```

388 ```{r, cache=FALSE}
389
390
391 ####Theta
392 options(scipen=999)
393 old.par <- par(mfrow=c(2, 3))
394 DDetIn  = density(Theta, n=iterations, adjust=3,from=theta_min, to=theta_
395 max) #
396 yDetecIN = DDetIn$y
397 xDetecIN = DDetIn$x
398 plot(xDetecIN,yDetecIN, type="l",xlab="Theta (efficiency of enforcement)"
399 ,ylab="Probability density", col="black", bty="n")
400
401

```

```

402 ###Beta
403 DDetIn = density(Beta, n=iterations, adjust=3, from=beta_min, to=beta_max)
404 #
405 yDetecIN = DDetIn$y
406 xDetecIN = DDetIn$x
407 plot(xDetecIN,yDetecIN, type="l",xlab="Beta (price premium)",ylab="Probability density", col="black", bty="n")
408
409
410
411 ###Min Legal
412 DDetIn = density(Minlegal, n=iterations, adjust=3, from=minlegal_min, to=minlegal_max)
413 #
414 yDetecIN = DDetIn$y
415 xDetecIN = DDetIn$x
416 plot(xDetecIN,yDetecIN, type="l",xlab="Minimum legal fraction per week",ylab="Probability density", col="black", bty="n")
417
418
419
420
421 ###Price Elasticity
422 DDetIn = density(-ElasticityPrice, n=iterations, adjust=3, from=0, to=1)
423 #from=E_minP, to=E_maxP)
424 yDetecIN = DDetIn$y
425 xDetecIN = DDetIn$x
426 plot(xDetecIN,yDetecIN, type="l",xlab="Price elasticity",ylab="Probability density", col="black", bty="n")
427
428
429
430
431 ###Cost Elasticity
432 DDetIn = density(-ElasticityCost, n=iterations, adjust=3, from=0, to=1)
433 #from=E_minC, to=E_maxC
434 yDetecIN = DDetIn$y
435 xDetecIN = DDetIn$x
436 plot(xDetecIN,yDetecIN, type="l",xlab="Cost elasticity",ylab="Probability density", col="black", bty="n")
437
438
439
440 ###permit_fee Elasticity
441 DDetIn = density(permit_feeEndofyear, n=iterations, adjust=3, from=permit_feeend_min, to=permit_feeend_max)
442 #
443 yDetecIN = DDetIn$y
444 xDetecIN = DDetIn$x
445 plot(xDetecIN,yDetecIN, type="l",xlab="Permit fee elasticity",ylab="Probability density", col="black", bty="n")
446
447
448
449 ###Total units
450 old.par <- par(mfrow=c(2, 2))
451 DDetIn = density(unitsboxes, n=iterations, adjust=3)
452 #
453 yDetecIN = DDetIn$y
454 xDetecIN = DDetIn$x
455 plot(xDetecIN,yDetecIN, type="l",xlab="Total units traded",ylab="Probability density", col="black", bty="n")

```

```

455
456 ##Ratio
457 DDetIn = density(Ratio, n=iterations, adjust=3)
458 yDetecIN = DDetIn$y
459 xDetecIN = DDetIn$x
460 p7 = plot(xDetecIN,yDetecIN, type="l",xlab="Ratio of illegal to tota
461 l units",ylab="Probability density", col="black", bty="n")
462
463 ##Illegalboxes
464 DDetIn=density(Illegalboxes, n=iterations, adjust=4)
465 SimY=DDetIn$y
466 SimX=DDetIn$x
467 plot(SimX,SimY, type="l",xlab="Illegal units",ylab="Probability density",
468 col="black", bty="n")
469
470
471 ## Legal Boxes
472 DDetIn = density(Legalboxes, n=iterations, adjust=4)
473 yDetecIN = DDetIn$y
474 xDetecIN = DDetIn$x
475 p8 = plot(xDetecIN,yDetecIN, type="l",xlab="Legal units",ylab="Proba
476 bility density", col="black", bty="n")
477
478
479 Graph units over time and comparison to data
480
481
482
483 ##Calculate weekly means
484 unitsMean = transform(Accepted_Legs, MEAN=apply(Accepted_Legs,1, mean,
485 na.rm = TRUE))
486 IllegalMean = transform(Accepted_Ills, MEAN=apply(Accepted_Ills,1, mean,
487 na.rm = TRUE))
488 unitsSD = transform(Accepted_Legs, SD =apply(Accepted_Legs,1, sd, na
489 .rm = TRUE))
490 IllegalSD = transform(Accepted_Ills, SD =apply(Accepted_Ills,1, sd, na
491 .rm = TRUE))
492
493 ###Create data frame with units data, mean and SD
494 units_plot = matrix(0,weeks,9)
495 units_plot[,1] = legal_units_data$mean
496 units_plot[,2] = legal_units_data$mean_p_std
497 units_plot[,3] = legal_units_data$mean_m_std
498
499 ###Calculate means and SD for simulations Legal
500 units_plot[,4] = unitsMean$MEAN
501 units_plot[,5] = unitsMean$MEAN+unitsSD$SD
502 units_plot[,6] = unitsMean$MEAN-unitsSD$SD
503
504 ###Calculate means and SD for simulations illegal

```

478

#### 479 **Graph units over time and comparison to data**

```

480 `` `{r, cache=FALSE}
481 ##This code creates figure 4
482
483 ##Calculate weekly means
484 unitsMean = transform(Accepted_Legs, MEAN=apply(Accepted_Legs,1, mean,
485 na.rm = TRUE))
486 IllegalMean = transform(Accepted_Ills, MEAN=apply(Accepted_Ills,1, mean,
487 na.rm = TRUE))
488 unitsSD = transform(Accepted_Legs, SD =apply(Accepted_Legs,1, sd, na
489 .rm = TRUE))
490 IllegalSD = transform(Accepted_Ills, SD =apply(Accepted_Ills,1, sd, na
491 .rm = TRUE))
492
493 ###Create data frame with units data, mean and SD
494 units_plot = matrix(0,weeks,9)
495 units_plot[,1] = legal_units_data$mean
496 units_plot[,2] = legal_units_data$mean_p_std
497 units_plot[,3] = legal_units_data$mean_m_std
498
499 ###Calculate means and SD for simulations Legal
500 units_plot[,4] = unitsMean$MEAN
501 units_plot[,5] = unitsMean$MEAN+unitsSD$SD
502 units_plot[,6] = unitsMean$MEAN-unitsSD$SD
503
504 ###Calculate means and SD for simulations illegal

```

```

505 units_plot[,7] = IllegalMean$MEAN
506 units_plot[,8] = IllegalMean$MEAN+IllegalSD$SD
507 units_plot[,9] = IllegalMean$MEAN-IllegalSD$SD
508 units_plot = as.data.frame(units_plot)
509 boxtoton = 27/1000
510
511 ###Creates Graph
512 ##Legal units simulations
513 units_Figure <- plot_ly(units_plot, x = ~seq(1:weeks), y = ~units_plot$V4*
514 boxtoton, type = 'scatter', mode = 'lines',
515 line = list(color='rgb(0,100,80)'),
516 name = 'Legal Simulations Mean +/-SD')
517 units_Figure <- units_Figure %>% add_trace(y = ~units_plot$V5*boxtoton, ty
518 pe = 'scatter', mode = 'lines',
519 line = list(color = 'transparent'), name = 'High
520 units',showlegend = FALSE)
521
522 units_Figure <- units_Figure %>% add_trace(y = ~units_plot$V6*boxtoton, ty
523 pe = 'scatter', mode = 'lines',
524 fill = 'tonexty', fillcolor='rgba(0,100,80,0.2)',
525 line = list(color = 'transparent'),
526 showlegend = FALSE, name = 'Low units')
527
528 ##Data
529 units_Figure <- units_Figure%>% add_trace(units_plot, x = ~seq(1:weeks), y
530 = ~units_plot$V2*boxtoton, type = 'scatter', mode = 'lines',
531 line = list(color = 'transparent'),
532 showlegend = FALSE, name = 'High units')
533 units_Figure <- units_Figure %>% add_trace(y = ~units_plot$V3*boxtoton, ty
534 pe = 'scatter', mode = 'lines',
535 fill = 'tonexty', fillcolor='rgba(0,17,157,0.2)',
536 line = list(color = 'transparent'),
537 showlegend = FALSE, name = 'Low units')
538 units_Figure <- units_Figure %>% add_trace(y = ~units_plot$V1*boxtoton, ty
539 pe = 'scatter', mode = 'lines',
540 line = list(color='blue'),
541 name = 'Legal units Mean +/-SD')
542
543
544 ##Illegal units simulations
545 units_Figure <- units_Figure%>% add_trace(units_plot, x = ~seq(1:weeks), y
546 = ~units_plot$V8*boxtoton, type = 'scatter', mode = 'lines',line = list(co
547 lor = 'transparent'),showlegend = FALSE, name = 'High units')
548 units_Figure <- units_Figure %>% add_trace(y = ~units_plot$V9*boxtoton, ty
549 pe = 'scatter', mode = 'lines',fill = 'tonexty', fillcolor='rgba(220,20,60
550 ,0.2)', line = list(color = 'transparent'),showlegend = FALSE, name = 'Low
551 units')
552 units_Figure <- units_Figure %>% add_trace(y = ~units_plot$V7*boxtoton, ty
553 pe = 'scatter', mode = 'lines',line = list(color='red'),name = 'Illegal Si
554 mulation Mean +/-SD')
555
556
557 units_Figure <- units_Figure %>% layout(yaxis = list(range = c(0,270)))
558 units_Figure <- units_Figure %>% layout(showlegend = TRUE)

```

```
559 units_Figure <- units_Figure %>% layout(xaxis = list(title = "Week of the
560 year"))
561 units_Figure <- units_Figure %>% layout(legend = list(x = 0.67, y = 1))
562 units_Figure <- units_Figure %>% layout(yaxis = list(title = "Quantity tra
563 ded (tons)"))
564 units_Figure
565 ```
566
567
```