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Abstract

We develop a novel approach to investigate the presence of financial contagion during the European sovereign debt crisis. The novelty lies in modelling bond yield market comovements allowing the individual long-run variances to be time-dependent and the correlations to change smoothly between two extreme states according to time and observable financial variables. The new model has the flexibility to discern between long-run and short-run contagion effects on the basis of the variable used as indicator for the time-variation in correlations. The main results provide evidence of long-run contagion effects across peripheral countries following the more acute phase of the sovereign crisis.

JEL classification codes: C32; C58; G01; G15.

Keywords: Financial contagion; European sovereign debt crisis; Multivariate GARCH model; Dynamic correlations; Multiplicative decomposition of volatility.

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1 Introduction

Financial globalisation and the ensuing increased levels of financial interdependence across countries have contributed greatly in the manner country-specific shocks affect other markets. This means that a financial crisis occurring in one market can adversely affect other markets and, in extreme cases, result in the disruption of the stability of the entire financial system. The recent global financial crisis of 2007-2009 and the European sovereign debt crisis are prime examples of these phenomena.

The extent of such financial crises is partly linked to the degree of financial market integration, how quickly shocks spread from one market to another, and by what means shocks change the transmission mechanism itself. Motivated by these issues, a large body of research on market interdependence and contagion has spurred in recent years to gain new insights into understanding the dynamics of propagation of shocks. Empirical evidence on the effects of the sovereign transmission of shocks can be found, among others, in [Giordano et al. \(2013\)](#), [Ludwig \(2014\)](#), [De Santis and Stein \(2015\)](#), [Bacchiocchi \(2017\)](#), and [Caporin et al. \(2018\)](#). Yet the literature focussing on the transmission of shocks during the sovereign debt crisis using bond yields remains scarce as most studies shifted their attention to the sovereign credit risk spreads based on credit default swaps data.

This paper seeks to address empirically the central question of whether the transmission of shocks occurs differently in periods of calm and financial distress. In particular, we shall examine whether recent episodes of market turbulence lead to financial contagion in government bond yields across eurozone countries. To achieve this goal, we develop a novel approach which builds upon recent developments in the nonstationary volatility literature (e.g., [van Bellegem and von Sachs \(2004\)](#), [Engle and Rangel \(2008\)](#), [Amado and Teräsvirta \(2013\)](#)) by extending the analysis to the multidimensional case for investigating financial linkages. This is done by allowing the long-run variances to be time-dependent and the correlations to change between two states according to an observable variable. Another key contribution of the paper is to introduce in the literature the concepts of long-run and short-run contagion. An appealing feature of our econometric approach

is the distinction between long-run and short-run contagion effects on the basis of the variable used as indicator of the changes in correlations. One may relate these concepts with the work of [Kaminsky et al. \(2003\)](#). These authors argue that some financial events can trigger immediate effects or the "fast and furious" phenomenon (term coined by the same authors), where similar events, on other occasions, originate a gradual and enduring international reaction to adverse news.

Despite the vast literature on financial contagion, there is not yet consensus on the definition of contagion and it remains unclear the underlying transmission mechanism of shocks across markets. For an overview of the existing definitions and methods for measuring contagion, we refer to surveys of [Pericoli and Sbracia \(2003\)](#), [Dungey et al. \(2005\)](#), and [Forbes \(2013\)](#). The focus of this work lies on the correlation-based analysis approach popularised by [Forbes and Rigobon \(2002\)](#) and contagion shall be defined as a significant increase in cross-market linkages after a shock to one country.

We identify two main limitations in the existing literature of utilising the correlation-based approach. The first is related to the distinction between an abnormal increase in market interactions at times of crisis, and normal market interactions in tranquil times. In periods of market turbulence, cross-country correlations tend to be upwardly biased due to presence of heteroskedasticity, which can misguidedly lead to the presence contagion. Thus, an increase in cross-market comovements during a period of financial turmoil cannot be perceived *per se* as evidence of contagion, but merely a continued high level of market interdependence. Contagion, in turn, is identified as a structural change in the level of market interdependence in periods of distress. This problem has been addressed in [Forbes and Rigobon \(2002\)](#), [Bae et al. \(2003\)](#), [Corsetti et al. \(2005\)](#), and [Dungey and Renault \(2018\)](#). The second limitation is associated to the timing of crisis and the country originating the crisis. This is often not a data-driven process, but it is usually defined beforehand by the modeller. Examples of this are the attempts of identifying Greece as the source of contagion on the sovereign crisis as in [Missio and Watzka \(2011\)](#), [Mink and de Haan \(2013\)](#), and [Buchholz and Tonzer \(2015\)](#), and October, 2009 as the beginning of the crisis when Greece revealed its distressed debt position.

We contribute to the literature by developing a novel approach based on the smooth transition conditional correlation GARCH model with multiplicative decomposition to investigate the presence of contagion during the sovereign debt crisis. We shall name the proposed model the multivariate Multiplicative Time-Varying Smooth Transition Conditional Correlation (MTV-STCC-) GARCH. A special case of this model is the specification with deterministically time-varying correlations introduced by [Silvennoinen and Teräsvirta \(2017\)](#). The new model introduces flexibility by allowing the individual unconditional variances to be time-dependent and the correlations to change smoothly between two extreme states according to time and observable financial variables.

Our modelling strategy addresses several pitfalls identified in the contagion literature. First, it has the advantage of adjusting the correlations to long-term and short-term volatility, and therefore avoiding the bias in cross-market correlations. For an example of how volatility affects the correlation coefficients, see [Forbes and Rigobon \(2002\)](#). As showed by [Mikosch and Stărică \(2004\)](#), the standard GARCH model is not suitable for fitting data with a long observation period because of deterministic changes in the long-run volatility. One way of dealing with this nonstationarity is to explicitly allow for a time-varying unconditional variance and model it accordingly as in [Amado and Teräsvirta \(2013, 2017\)](#). Second, we are able to control for time-variation in correlations using time and financial indicators. We can thus capture long-term and short-term movements in correlations depending on which variable is being used as driver of the regime-changes in correlations. Third, the timing of changes in volatility is estimated endogenously instead of being pre-defined exogenously. The identification of the crisis phases will be purely determined from the data and we shall rely on the estimates of the location parameters to distinguish those phases. For a similar procedure on different modelling frameworks, we refer to [Kasch and Caporin \(2013\)](#), [Blatt et al. \(2015\)](#), and [Dungey et al. \(2015\)](#).

The new model is applied to daily data on 10-year government bond yields for nine member states of the Eurozone from 2007 until 2017. First we choose time as the transition variable controlling the time-varying correlations. Because conditional correlations may respond to country-specific (or idiosyncratic) and common (or systemic) shocks to sovereign

yields, we also consider financial variables as transition variables. An appealing feature of the new model is the discrimination between long-run and short-run contagion effects on the basis of the variable used as indicator of the changes in correlations. Later, in this article, we will relate these concepts with pure and "wake-up-call" contagion effects. The main results provide no evidence of asymmetric response of bond yield comovements to negative shocks, as opposed to the size of innovations from the periphery which is expected to affect the dynamics of correlations. Overall, the model provides to be a useful tool for studying market contagion by explicitly focussing on the effects of mechanisms of shocks propagation in periods of tranquility and turbulence.

This paper is organized as follows. Section 2 sets up the modelling framework used to examine the presence of contagion. Section 3 provides a description of the data and some preliminary analysis. Section 4 is devoted to model specification concerning testing the constancy of correlations. Section 5 contains the empirical results of the new MTV-STCC-GARCH model applied to the daily data on 10-year government bonds for nine Eurozone countries and the results of the correlation-based tests for contagion are discussed. Finally, Section 6 concludes the paper.

2 Modelling framework

2.1 The model setup

In this section, we shall briefly describe the econometric tool used to study the presence of contagion in the European sovereign bond markets. More formally, consider an N -dimensional vector of bond yields with the representation:

$$\mathbf{y}_t = \mathbb{E}[\mathbf{y}_t | \mathcal{F}_{t-1}] + \boldsymbol{\varepsilon}_t, \quad t = 1, \dots, T, \quad (1)$$

where $\mathcal{F}_{t-1}$ is the sigma-field containing the historical information available at time $t - 1$. To filter out any linear dependence in the data, we model the conditional mean for each

series as an autoregressive process of order r :

$$y_{it} = \psi_{i0} + \sum_{j=1}^r \psi_{ij} y_{i,t-j} + \varepsilon_{it}, \quad i = 1, \dots, N, \quad (2)$$

where the innovation sequence ε_{it} has a conditional mean $E(\varepsilon_{it}|\mathcal{F}_{t-1}) = 0$ and a potentially time-varying conditional variance $\text{Var}(\varepsilon_{it}|\mathcal{F}_{t-1}) = \sigma_{it}^2$, for $i = 1, \dots, N$. Each univariate error process is decomposed as follows:

$$\varepsilon_{it} = z_{it}\sigma_{it},$$

where z_{it} forms a sequence of independent random variables with mean zero and variance one, and the variance σ_{it}^2 is further multiplicatively decomposed as:

$$\sigma_{it}^2 = h_{it}g_{it}, \quad (3)$$

where h_{it} is a stationary component describing the short-run dynamics of volatility and g_{it} is a positive-valued deterministic component capturing long-run movements in volatility. We explicitly introduce nonstationarity in the variance to account for long-run movements and model volatility by the multiplicative time-varying (MTV-) GARCH model of [Amado and Teräsvirta \(2013, 2017\)](#). Specifically, the h_{it} component is modelled as the standard GARCH(p, q) representation:

$$h_{it} = \alpha_{i0} + \sum_{j=1}^q \alpha_{ij} \phi_{i,t-j}^2 + \sum_{j=1}^p \beta_{ij} h_{i,t-j} \quad (4)$$

where $\alpha_{i0} > 0$, $\alpha_{ij} \geq 0$, $j = 1, \dots, q-1$, $\alpha_{iq} > 0$, $\beta_{ij} \geq 0$, $j = 1, \dots, p$, and $\phi_{it} = \varepsilon_{it}/g_{it}^{1/2}$. For the process to be covariance-stationary it is required that $\sum_{j=1}^q \alpha_{ij} + \sum_{j=1}^p \beta_{ij} < 1$, $i = 1, \dots, N$. The slowly time-varying trend g_{it} functions as a proxy for all factors that affect the unconditional variance and it is defined as:

$$g_{it} = \delta_{i0} + \sum_{l=1}^{m_i} \delta_{il} G_{il}(t/T; \gamma_{il}, \mathbf{c}_{il}), \quad \gamma_{il} > 0 \quad (5)$$

where $\delta_{il}, l = 0, \dots, m_i$, are parameters such that $m_i = 1, \dots, M$, with M being a finite integer. For identification reasons, the intercept δ_{i0} is assumed known and fixed to the value obtained in the first iteration when estimating (5) and setting $h_{it} = 1$; see Amado and Teräsvirta (2013) for further details. The function $G_{il}(s_t; \gamma_{il}, \mathbf{c}_{il})$ is the generalised logistic transition function:

$$G_{il}(s_t; \gamma_{il}, \mathbf{c}_{il}) = (1 + \exp\{-\gamma_{il} \prod_{k=1}^{K_{il}} (s_t - c_{ilk})\})^{-1} \quad (6)$$

where $\gamma_{il} > 0$ and $\mathbf{c}_{il} = (c_{il1}, \dots, c_{ilK_{il}})'$ such that $c_{il1} \leq \dots \leq c_{ilK_{il}}$. In (5) we choose the transition variable s_t as time t/T defined on the interval $[0, 1]$. The parameters c_{ilk} and γ_{il} determine, respectively, the location of the change and the smoothness of the transition between one regime to another. As $\gamma_{il} \rightarrow \infty$, g_{it} approaches a step function with a switch at c_{ilk} . For small values of γ_{il} , the transition between regimes is smooth. When γ_{il} is large, it is numerically convenient to use the transformation $\gamma_{il} = \exp(\eta_{il})$ and estimating η_{il} instead of γ_{il} ; see Goodwin et al. (2011) and Hurn et al. (2016) for further details.

The transition function (6) allows the unconditional variance to change deterministically as a function of time. By construction, function (6) is continuous for $\gamma_{il} < \infty$, $l = 1, \dots, m_i$, and bounded between zero and unity. In practice, the parametric structure of the g_{it} component is determined from the data, which involves determining the number of m_i transitions and choosing the integer K_{il} using statistical inference; see Amado and Teräsvirta (2017) for more details. Visual inspection may be also useful for choosing K_{il} .

2.2 Dynamics of correlation structure

It follows that the N -dimensional vector of innovations $\boldsymbol{\varepsilon}_t$ is defined as

$$\boldsymbol{\varepsilon}_t = \mathbf{H}_t^{1/2} \mathbf{z}_t = \mathbf{S}_t \mathbf{G}_t \mathbf{z}_t, \quad (7)$$

where $\mathbf{H}_t$ is an $N \times N$ positive definite matrix, and the error vector $\mathbf{z}_t$ form a sequence of independent and identically distributed variables with $\mathbb{E}(\mathbf{z}_t | \mathcal{F}_{t-1}) = \mathbf{0}$ and positive definite covariance matrix $\mathbb{E}(\mathbf{z}_t \mathbf{z}_t' | \mathcal{F}_{t-1}) = \mathbf{P}_t$. This implies that $\mathbf{P}_t^{-1/2} \mathbf{z}_t \sim iid(\mathbf{0}, \mathbf{I}_N)$. The

stochastic diagonal matrix $\mathbf{S}_t = \text{diag}(h_{1t}^{1/2}, \dots, h_{Nt}^{1/2})$ contains the conditional standard deviations of ϕ_{it} , $i = 1, \dots, N$, as defined in (4) and $\mathbf{G}_t = \text{diag}(g_{1t}^{1/2}, \dots, g_{Nt}^{1/2})$ is a deterministic diagonal matrix containing positive-valued time-dependent elements $g_{it}^{1/2}$. Under these assumptions, the time-varying conditional covariance matrix of $\boldsymbol{\varepsilon}_t$ has the representation introduced by Amado and Teräsvirta (2014):

$$\mathbb{E}[\boldsymbol{\varepsilon}_t \boldsymbol{\varepsilon}_t' | \mathcal{F}_{t-1}] = \mathbf{H}_t = \mathbf{S}_t \mathbf{G}_t \mathbf{P}_t \mathbf{G}_t \mathbf{S}_t, \quad (8)$$

where $\mathbf{P}_t = [\rho_{ij,t}]_{i,j=1,\dots,N}$ is a positive definite conditional correlation matrix for $\boldsymbol{\varepsilon}_t$ to be defined in the next section whose elements can be time-varying for $i \neq j$. It follows that when $\mathbf{G}_t = \mathbf{I}_N$, the model belongs to the family of Conditional Correlation (CC-) GARCH models. In this work, we assume the correlation matrix $\mathbf{P}_t$ to change smoothly between two extreme states as in the smooth transition conditional correlation (STCC-) GARCH model of Silvennoinen and Teräsvirta (2005, 2015):

$$\mathbf{P}_t(s_t) = \{1 - G(s_t, \gamma, \mathbf{c})\} \mathbf{P}_1 + G(s_t, \gamma, \mathbf{c}) \mathbf{P}_2 \quad (9)$$

where $\mathbf{P}_1$ and $\mathbf{P}_2$ are positive definite correlation matrices that describe the two extreme states of correlations driven by the transition variable s_t . The extended multivariate multiplicative GARCH model with a correlation matrix defined as (9) shall be called the MTV-STCC-GARCH model. Recently, Silvennoinen and Teräsvirta (2017) derive the asymptotic properties for the MTV-STCC-GARCH model with deterministically time-varying correlations when the transition variable is rescaled time, i.e., $\mathbf{P}_t \equiv \mathbf{P}(t/T)$.

Possible choices for the observable indicator s_t include a function of lagged yields, exogenous variables or calendar time as in Berben and Jansen (2005). Economic theory may provide insight into the appropriate choice of the transition variable. However, if there is uncertainty about which alternative to use as transition variable, testing the constancy of correlations may be a useful tool for selecting a particular transition variable; see Silvennoinen and Teräsvirta (2009). We shall further discuss the choice of this variable in Section 4. The main advantage of the STCC-GARCH model over the conventional

Figure 1: Daily data on 10-year government bond yields for nine Eurozone countries from January 1, 2007 and April 18, 2017. The vertical red lines show the estimated start of the crisis phases and post-crisis period for the periphery countries and the black vertical line corresponds to the Greek deficit revision in October 22, 2009.

Dynamic Conditional Correlation (DCC-) GARCH model of [Engle \(2002\)](#) is that it introduces flexibility by allowing time-variation in correlations driven by an observable transition variable. Details on estimation of the model can be found in the Appendix.

3 Data and preliminary analysis

In order to study the presence of cross-market contagion in the European sovereign debt crisis, we use daily data on 10-year government benchmark bond yields. The sample period extends from January 1, 2007 to April 18, 2017 which amounts to 2684 observations. The data was collected from the Thomson Reuters Datastream and it covers nine Eurozone countries that we group as core (Belgium, Finland, France and Germany) and periphery (Greece, Ireland, Italy, Portugal and Spain). This division has become standard due to the similarity in yields and the debt positions of countries in each group. Core countries also have different levels of risk and liquidity from the peripheral countries.

Figure 1 shows the daily 10-year government bond yields. We observe that after the end of 2009, the yields on the Greek bonds peaked sharply, followed foremost by

Ireland and Portugal. Over time, the diverging behaviour between core and periphery countries gradually disappears, leading to stronger comovements across markets. Yet, the Greek bonds drifts away again around 2015, before moving closer to the other countries' yields. Results from the MTV-TVC-GARCH model (to be further discussed in section 5.1) identify three changes in comovements for periphery countries, represented by the red vertical lines in Figure 1. According to these results, dominant changes in correlations occurred in May 2009, June 2014 and March 2016. We shall discuss these dates in further detail in section 5.1.

To examine bond yields linkages, we adopt the changes in bond yields to eliminate the presence of unit roots in the raw series; see [Campbell and Ammer \(1993\)](#). In order to handle nonstationarity in the mean, we compute the changes in bond yields (in relative terms) as $r_{i,t} = (p_{i,t}/p_{i,t-1} - 1) \times 100$, where $p_{i,t}$ is the yield to maturity at time t for country i . These are approximately equal to the holding period returns for long-term bonds; see [Flannery and James \(1984\)](#) for details. To prevent problems in estimation, the changes in bond yields are truncated such that extremely large positive/negative values are limited to $+/- 5$ times the standard deviation of the series. The truncated changes are depicted in Figure 2. Bond yield changes above or below three times their standard deviation (represented in blue) occur mostly after October 2009. For most series, large changes in yields are the indication of unusually large shocks to sovereign bond yields and high levels of volatility and these are especially noticeable at the end of the sample.

Summary statistics for each series are provided in Table 1. The skewness and kurtosis show that the bond yield changes have a right-skewed and significant fat-tailed distribution. Results of the robust portmanteau $Q(10)$ statistic show linear time-dependence for the Greek, Italian and Portuguese bond yield changes. There is also evidence of time-dependence in the second moment for the series of changes in yields, but no remaining ARCH effects are found on the standardised residuals. To filter out the linear dependence in the conditional mean we fit an AR(2) to the Italian yields, and an AR(1) to the Greek and Portuguese yields. Results are not shown to conserve space, but the estimation results from the standard GARCH model indicate that, except for Ireland, the persistence of

Figure 2: Daily changes in yields on 10-year government bonds after truncation. The horizontal blue lines correspond to ± 3 times the sample standard deviation of the truncated series.

volatility exceeds unity. Given the nonstationary nature of volatility, we test for changes in the unconditional variance component. Test results are not provided for space reasons, but constancy is rejected for all series; for details of the test, see [Amado and Teräsvirta \(2017\)](#). The shape of the deterministic component g_{it} function is specified by the sequential testing proposed by [Amado and Teräsvirta \(2017\)](#). The dynamics of the long-term bond yields volatility by the MTV-GARCH model is displayed in Figure 3. For comparison, the conditional standard deviation from the GARCH model is also plotted. A common pattern is visible from the graphs. There is a clear distinction between core and periphery countries. The long-run volatility of the core countries looks rather flat in the beginning of the sample. Around 2015 starts a more volatile period that continues an upward trajectory until the end of the sample period. With respect to the periphery countries, the unconditional variance shows different patterns, but they have the common feature of showing an increasing trend over time.

Table 1: Descriptive statistics and diagnostic tests for the daily changes in bond yields after truncating the extreme values. The threshold is ± 5 standard deviations above/below the extreme changes in yields. SK. and KR. denote, respectively, the skewness and excess kurtosis. ROB. $Q(10)$ is the corrected portmanteau test statistic for serial correlation up to order 10 in the presence of ARCH effects of [Francq and Zakoïan \(2009\)](#). ARCH(5) is the Engle’s (1982) test for ARCH effects up to order 5. The reported values of the tests are p -values.

	CORE				PERIPHERY				
	BELGIUM	FINLAND	FRANCE	GERMANY	GREECE	IRELAND	ITALY	PORTUGAL	SPAIN
NO. TRUNC.	24	20	23	29	11	21	7	9	10
OBS.	2684	2684	2684	2684	2684	2684	2684	2684	2684
MIN.	−24.44	−52.13	−25.94	−76.48	−14.15	−14.27	−10.24	−10.98	−10.85
MEAN	−0.016	0.025	−0.018	−0.014	0.078	−0.029	−0.008	0.020	−0.014
MAX.	24.44	52.13	25.94	76.48	14.15	14.27	10.24	10.98	10.85
STD.DEV.	4.005	6.789	4.131	11.38	2.437	2.723	1.999	2.102	2.105
SK.	0.831	0.880	0.766	0.468	0.244	0.506	0.461	0.518	0.213
KR.	15.36	31.15	16.94	26.36	8.844	7.945	4.609	4.683	4.106
ROB. $Q(10)$ TEST	0.903	0.496	0.711	0.909	0.016	0.314	0.029	0.011	0.206
ARCH(5) TEST	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000

4 Testing for correlation changes

Testing the adequacy of constant correlations is an important statistical tool because there is empirical evidence that correlations are time-dependent and neglecting variation of parameters leads to invalid asymptotic inference. For model selection, we use the Lagrange Multiplier statistic for testing constancy of correlations proposed in [Silvennoinen and Teräsvirta \(2005, 2015\)](#). For details on the test statistic and analytical expressions for the partial derivatives we refer to [Silvennoinen and Teräsvirta \(2005, 2015\)](#). Failure to reject the null hypothesis can be interpreted that the transition variable is not enough informative about time-variation in the correlation structure. Rejection of the null hypothesis of parameter constancy suggests time-varying correlations driven by an indicator variable or evidence in favour of other types of misspecification.

As discussed by [Silvennoinen and Teräsvirta \(2005\)](#), valuable information for the correlation dynamics can be obtained by studying submodels instead of higher-dimensional models. For this reason, we shall study lower dimensional models of bond yields instead of considering the nine-dimensional case. The choice of the model dimension depends on how far we wish to go into detail about the dynamics of comovements across countries.

Figure 3: Estimated long-run volatility from the MTV-GARCH model (blue curve) and the conditional standard deviation from the GARCH model (black curve) for the nine Eurozone countries.

Therefore, we combine changes in bond yields into three higher-dimensional models comprising of core, periphery, and core and each periphery country. Bivariate test results are also provided for comparison.

To investigate if the comovements of bond yields are linked to the behaviour of observable indicators, we shall use three potential transition variables. First, we use s_t as the calendar time for which we are able to observe long-run movements or dominant trends in the correlations. Results of the tests when time is the transition variable are shown in Table 2. The left panel contains the p -values for the bivariate case of the multiplicative time-varying Constant Conditional Correlation (CCC-) GARCH model of [Bollerslev \(1990\)](#) for core and periphery countries. The strongest rejections occur for the periphery countries and when Greece is included in the model. The right panel contains the p -values for higher dimensional models. This includes the results from the four-variate model across core countries, and the five-variate models for peripheral countries, and between core and each periphery country. The null hypothesis of constant correlations is

Table 3: Results from the test of constant conditional correlations against the alternative of time-varying correlations for the periphery countries. The reported values are p -values. The transition variables are the changes in bond yields for each periphery country (left panel), the lagged VSTOXX index averaged over two weeks (right panel), and the lagged VIX index averaged over two days (right panel).

GIIPS			
GREEK BOND YIELDS	9×10^{-07}		
IRISH BOND YIELDS	2×10^{-11}		
ITALIAN BOND YIELDS	2×10^{-22}	2-W AVL VSTOXX	3×10^{-19}
PORTUGUESE BOND YIELDS	2×10^{-26}	2-D AVL VIX	2×10^{-17}
SPANISH BOND YIELDS	1×10^{-10}		

that comovements in the yields are stronger during volatile periods than during tranquil times; see [Andersen et al. \(2001\)](#). To capture this phenomenon, one option is to consider the general market turbulence as the time-variation indicator in correlations. In that case, the changes in yields, absolute changes in yields and squared changes in yields would be obvious choices. Alternatively, one can use functions of the Chicago Board Options Exchange volatility index (VIX) or the Euro Stoxx 50 volatility index (VSTOXX) to account for uncertainty in the US and European markets, respectively. The tests of constant correlations reject constancy for each model, but the strongest rejections occurred when the transition variable were the lagged 2-week average of VSTOXX and the lagged 2-day average of VIX. These results may be explained by the following. The 2-day average of lagged VIX can be seen as the adjustment for time zone differences between the two markets, where the impact of the US market on the European market is delayed until the next day. The reasoning behind the lagged 2-week average VSTOXX is that it controls for any within week-variations. The test results are presented in the right panel of Table 3. The volatility indexes seem to be informative about the time-variation in correlations, but the market trend measured by time appears to carry more information. These results are in line with those of [Longin and Solnik \(2001\)](#) in which they conclude that the market trend affects international market correlations more than volatility.

5 Empirical results

5.1 Long-run movements in correlations and crisis dating

In this section we investigate long-term comovements across bond markets and characterize the extent of these long-run linkages during the sovereign debt crisis. We begin by estimating the MTV-TVC-GARCH model discussed in subsection 2.2 when time is chosen as the transition variable and we use model selection criteria to choose the best model. The Bayesian information criterion (BIC) of Schwarz (1978) selects three location parameters for the five-variate model among peripheral countries and two location parameters for the five-variate model between each periphery and core countries. Results are not shown due to space limitation, but as expected the model that performs poorly according to information criteria is the multivariate MTV-GARCH model with constant correlations.

The dynamics of the estimated unconditional correlations from the MTV-TVC-GARCH model for the periphery countries is depicted in Figure 4. For comparison, we also plot the estimated short-run dynamic linkages described by the MTV-DCC-GARCH model and the constant correlations obtained from the MTV-CCC-GARCH model. It is interesting to note how the short-run correlations (grey curve) tend to fluctuate around the time-varying unconditional correlations (black curve). We observe a declining trend in the unconditional correlations in the early phase of the crisis, starting in 2009 and reaching its lowest level around 2011, followed by an upward trend in 2014. This increase is offset by another decrease that is particularly noticeable for the pairwise correlations involving Greece. The drop in correlations during the last phase is especially pronounced for the pairs Greece-Italy, Portugal-Greece and Spain-Greece which may be due to the political instability in those countries during that period. These results suggest that the transmission of shocks across markets is far from being immediate. A possible explanation is that investors do not entirely recognise crisis signals and they interpret news as being country-specific. Over time, investors slowly incorporate negative news into prices, which in turn leads to a gradual convergence in sovereign yields, resulting in higher comovements across markets. Our conclusions are consistent to those of Chiang et al. (2007) for the

Asian financial crisis.

We shall use the estimated constant correlations from the MTV-CCC-GARCH model as proxy for expected comovements across markets as it roughly averages the level of correlations. The interdependence threshold in normal times for peripheral countries is represented by the horizontal line (blue colour) in Figure 4. Correlations are generally moderate, ranging from 0.339 to 0.808, with the strongest correlation for the pair Italy-Spain, followed by the combination Portugal-Spain with a correlation of 0.615. It follows that a significant increase in market interactions beyond the expected level of interdependence may be regarded as financial contagion.

The estimated transition parameters of the five-variate model are reported in Table 4. The estimated slope parameter is relatively small ($\hat{\gamma} = 63.15$) yielding a fairly smooth change between the correlation states. The speed and the location parameters determine how level shifts occur in the unconditional correlations. One challenging task when testing for contagion effects is the demarcation of crisis from non-crisis periods. In this work, the identification of the crisis phases will be purely determined from the data and we shall rely on the estimates of the location parameters to distinguish those phases. Table 4 presents the estimated periods. We identify four distinct phases in our sample period. A transition from the pre-crisis phase to the first crisis phase is identified in early May 2009 ($\hat{c}_1 = 0.225$) marked by a decline in correlations a few months before the Greek deficit revision. The next period is identified as the first crisis phase ending in June 2014 ($\hat{c}_2 = 0.724$), a month after Portugal announced its exit from the bailout mechanism. This period includes the most acute phase of the sovereign debt crisis with the bailouts programmes for Greece, Ireland and Portugal, and the rating downgrades of Spain and Italy, further supporting our crisis dating. A second phase of the crisis, characterised by the third Greek bailout package and triggered by the rise of Greek bond yields, ends by mid-March 2016 ($\hat{c}_3 = 0.893$). The last phase, from March 2016 until the end of the sample, is identified as possibly the post-crisis phase in the light of historical events pointing out to signs of recovery.

Next we examine if the unconditional correlations behave differently over time when

Table 4: Estimated transition parameters (standard errors in parentheses) for the MTV-TVC-GARCH model across the periphery countries and crisis dating.

$\hat{\gamma}$	$\hat{c}_k$	BEGINNING DATE	
		18-01-2007	PRE-CRISIS
0.225 (0.006)		07-05-2009	CRISIS PHASE I
63.15 (0.260)	0.724 (0.026)	20-06-2014	CRISIS PHASE II
0.893 (0.016)		15-03-2016	POST-CRISIS

Figure 4: Estimated time-varying (un)conditional correlations for the periphery countries.

Figure 5: Estimated unconditional correlations for core (grey curves) and between core and periphery countries (blue curves). Each panel corresponds to the five-variate MTV-TVC-GARCH model for each periphery and core countries.

core countries are considered in the analysis. Now, the best selected model is when $K_l = 2$ and crisis dating is done as before. Figure 5 shows the long-term correlations between core countries and each periphery country. We observe a downward trend in the long-term correlations mostly around 2009-2012 before rising up about 2014-2016. The only exception is for the pair Germany-Finland whose unconditional correlations increase during the critical phase of the crisis. We find that level shifts in comovements are fairly smooth across core (grey colour) and sharper between core and periphery countries (blue colour). Furthermore, the long-term correlations in the former countries preserved their high levels, contrary to the correlations across the latter countries which became negative at the peak of the crisis. Results also suggest a faster adjustment for Ireland and Italy towards core yield levels. It is interesting to note that, at the end of the sample, other peripheral countries than Ireland and Italy yields have not converged entirely back to pre-crisis levels.

The decline in the long-term correlations may be explained by the flight-to-quality phenomenon from *bad* to *good* bond markets. This concept derives from the flight-to-

quality from stocks to bonds when investors reallocate their portfolio to reduce the risk of loss during turbulent times; see [Baur and Lucey \(2009\)](#) for further details. This idea may also be extended to the bond-bond case, where flight-to-quality occurs when investors move from falling to safer bond markets, causing them to move in opposite directions. We shall thus conclude for the presence of flight-to-quality effects if correlations across markets decline to negative levels. In order to do this, we compute the average weekly correlations for the estimated MTV-TVC-GARCH model in times of distress. Our findings indicate flight-to-quality from Greece to all core countries, from Ireland to Finland, France and Germany, from Italy and Portugal to Finland and Germany, and from Spain to Germany. Therefore, our results indicate that flight-to-quality flows from all peripheral countries are mostly pronounced to the German bond market.

5.2 Effects of shocks on bond yield comovements

There is widely accepted evidence of the asymmetric phenomenon in the correlation dynamics of equities, yet the literature is scarce about this effect for bond comovements. In order to fill this gap, we examine how correlations across periphery countries respond to country-specific shocks. This is done by using the changes in bond yields from each peripheral country as proxy of shocks and studying the time-variation in correlations given this market indicator. This choice is explained by the fact, as discussed in [Section 4](#), that changes in bond yields of peripheral countries play an important role on changes in correlations, albeit weaker than time. By doing this, the model will be able to accommodate, if present, an asymmetric response in correlations to negative shocks.

The best model using the BIC criterion selects two location parameters, i.e., $K_l = 2$. Visual inspection of the estimated transition functions of the MTV-STCC-GARCH model is depicted in [Figure 6](#) where each panel corresponds to the indicator used as transition variable. We observe that transitions in correlations are close to the regime-switching behaviour as the smoothness parameter is fairly abrupt for all models (except the one assuming Irish yield changes as the transition variable). It is evident that for changes in bond yields of the periphery located between $\hat{c}_1$ and $\hat{c}_2$, the logistic function becomes

close to zero and the conditional correlations approach the high extreme state $\mathbf{P}_1$. On the contrary, large changes in yields, positive or negative, result in correlations close to the low extreme state $\mathbf{P}_2$.

An interesting pattern can be perceived from these results. Small absolute shocks or periods of lower uncertainty are associated with higher correlations in bond markets. Conversely, smaller correlations are linked to large absolute shocks or higher uncertainty in these markets. On a different note, we find bond yield comovements to be unaffected by the direction, positive or negative, of shock. In other words, while there is compelling evidence that bond correlations across periphery are strongly affected by the size of shock (small or large), they are not linked to the sign (negative or positive) of innovations from each periphery country. One can therefore expect higher correlations for smaller changes in yields rather than for larger movements in bond yields. A plausible explanation is because during calm periods, even if the market is hit by positive or negative news, investors do not reallocate their investments from high-risk yield into safe-haven bond markets, possibly leading to an increase in bond yield correlations. By contrast, relying on the estimation results, we find no evidence of asymmetric response of bond yield comovements to negative shocks. Thus, contrary to equity markets, the results reveal that bond correlations are not sensitive to the sign of shocks. This conclusion accords with [Cappiello et al. \(2006\)](#) who argue that bond correlations exhibit no leverage effect and therefore its presence is implausible in these markets.

5.3 Bond yield correlations and financial market uncertainty

It is a widespread phenomenon that the correlations between asset returns often increase during periods of turbulence, while in tranquil times the returns are expected to behave more independently. However, it is also of interest to investigate how bond yield correlations respond to changes in market distress. We now turn our attention to bond yield comovements and study how their dynamics is affected by general market turbulence. Recent empirical evidence for the relationship between sovereign yield correlations and market volatility has been provided in [De Santis and Stein \(2015\)](#) and [Xu \(2017\)](#), among

Figure 6: Estimated logistic functions for the five-variate MTV-STCC-GARCH models for the periphery countries as a function of s_t . The transition variable s_t is the change in bond yields for each periphery country (in each panel). The lower and upper regime of correlations are represented, respectively, in blue and red colour.

others.

We shall measure the level of uncertainty by using the VIX and VSTOXX indexes as indicators of expected stock market volatility for the US and the euro area over the next 30 days. These are calculated using the 30-day implied volatility of the S&P 500 and EURO STOXX 50 indexes, respectively. The VIX and VSTOXX are commonly perceived as "investor fear indexes" of future stock market volatility in the US and European market and thus viewed as measures for global and regional market risk aversion, respectively. Therefore, high values of the indexes are generally associated with high levels of volatility and hence to periods of high uncertainty. On the contrary, low values of the indexes are often related to tranquil times or less uncertainty.

We now proceed with the estimation of the MTV-STCC-GARCH model whose correlations are driven by functions of lagged VIX and VSTOXX as discussed in section 4. The correlation estimates of the model using either the lagged 2-week average of VSTOXX or lagged 2-day average of VIX as transition variable can be found in Table 5. The estimated transition functions for both indicator variables are displayed in Figure 7. Results clearly indicate that the bond yield correlations tend to decline following an increase in the European index, which is certainly reflecting a period of increasing regional uncertainty. Correspondingly, bond comovements driven by the European volatility index tend to exhibit a pro-cyclical behavior. This is not surprising as Xu (2017) demonstrated that bond yield correlations are weakly pro-cyclical, as opposed to the countercyclical behavior of equity yield correlations. Our findings are also consistent with Longin and Solnik (2001) who demonstrated that the market trend is a major driver of the increase in correlations, instead of volatility. Furthermore, they showed that high volatility *per se* does not explain the rise in conditional correlations. As regards the effect of VIX on correlations, the results reveal an interesting pattern. There is empirical support of higher global uncertainty being associated with higher conditional correlations in changes in bond yields, but this effect is essentially observed for the pairwise correlations involving either Greece or Portugal. This observation corroborates the countercyclical bond comovements behaviour for each of these countries as they tend to move in the opposite direction as the

Figure 7: Estimated transition functions for the five-variate MTV-STCC-GARCH models for periphery countries as a function of s_t . The transition variables are the lagged VSTOXX averaged over two weeks (upper panel) and the lagged VIX averaged over two days (bottom panel). The lower and upper regime of correlations are represented, respectively, in blue and red colour.

world economic cycle. This behaviour is, however, reversed for the remaining periphery countries. Such effects can be observed in Figure 7. From the results, we may therefore conclude that it is most likely to exist contagion effects from the global financial crisis to the Greek and Portuguese bond markets.

Despite the evidence that both volatility measures carry information about the dynamics of the correlations, a few differences emerge from them. First, the transmission between the extreme states of correlations is abrupt when using the VIX as indicator variable and quite smooth when using its European counterpart. The estimates of the location parameters are 20.25 for the VIX and about 25 for the VSTOXX. Therefore, values of the US and European volatility indexes larger than 20.25 or 25, depending on the index, expect to lead to lower correlations across bond yields (with Greece or Portugal being an exception). The implication of these results is that bond yield comovements in the eurozone are thus expected to react faster to higher levels of uncertainty in the US market than that of the euro area. This is in agreement with the results of [Ehrmann and Fratzscher \(2005\)](#) who concluded that European markets react more strongly to the macroeconomic news about the US economy than to European news.

Table 5: Estimated results for the five-variate MTV-STCC-GARCH model (robust standard errors in parentheses) for periphery countries. The transition variables are the lagged VSTOXX index averaged over two weeks (upper panel) and the lagged VIX index averaged over two days (bottom panel). Each panel shows the estimated correlation matrices $\hat{\mathbf{P}}_1$ (left panel) and $\hat{\mathbf{P}}_2$ (right panel).

2-W AVL VSTOXX								
	GREECE	IRELAND	ITALY	PORTUGAL	GREECE	IRELAND	ITALY	PORTUGAL
IRELAND	0.372 (0.166)				0.304 (0.092)			
ITALY	0.416 (0.121)	0.797 (0.170)			0.428 (0.090)	0.229 (0.424)		
PORTUGAL	0.472 (0.123)	0.607 (0.072)	0.686 (0.073)		0.427 (0.095)	0.373 (0.168)	0.505 (0.145)	
SPAIN	0.468 (0.046)	0.759 (0.133)	0.857 (0.048)	0.737 (0.090)	0.388 (0.112)	0.298 (0.347)	0.757 (0.091)	0.487 (0.175)
$\hat{c} = 24.78$ $\hat{\gamma} = 0.151$ (6.935) (0.218)								
2-D AVL VIX								
	GREECE	IRELAND	ITALY	PORTUGAL	GREECE	IRELAND	ITALY	PORTUGAL
IRELAND	0.299 (0.023)				0.408 (0.030)			
ITALY	0.357 (0.027)	0.573 (0.021)			0.529 (0.030)	0.441 (0.028)		
PORTUGAL	0.396 (0.026)	0.481 (0.027)	0.579 (0.024)		0.540 (0.031)	0.513 (0.029)	0.631 (0.031)	
SPAIN	0.388 (0.025)	0.568 (0.019)	0.818 (0.010)	0.609 (0.023)	0.495 (0.034)	0.484 (0.030)	0.792 (0.015)	0.625 (0.031)
$\hat{c} = 20.25$ $\hat{\gamma} = 100.0$ (0.028) (–)								

5.4 Testing for financial contagion

In this section we use the correlation-based statistical test for contagion of [Forbes and Rigobon \(2002\)](#) adjusted to our approach. As discussed before, we assume interdependence measured by the long-term level of comovements across markets, whereas contagion is identified as a significant increase in cross-market linkages after a shock. We interpret the correlations across markets in tranquil periods as the long-run equilibrium correlations, from where they can fluctuate in the short-run during times of distress. Financial contagion will be thus related to this excess of short-run comovements from its long-term level during periods of crisis. In what follows, the long-run correlations shall be measured by the estimated constant conditional correlations for the full observation period.

Let $\rho_{ij,ccc}$ be the long-run level of correlations proxied by the constant conditional correlation between countries i and j for the non-crisis period, and $\rho_{ij,n,stcc}$ be the time-varying conditional correlation from the MTV-STCC-GARCH model for the crisis period n adjusting for long-run movements in the volatility. In the case of deterministically time-varying correlations, the notation will be changed to $\rho_{ij,n,tvc}$. It follows that the pair of hypotheses for testing the null hypothesis of interdependence against the alternative of contagion are (suppressing subscripts for notational convenience):

$$H_0 : \bar{\rho}_{stcc} = \rho_{ccc}$$

$$H_1 : \bar{\rho}_{stcc} > \rho_{ccc}$$

where $\bar{\rho}_{stcc} = E(\rho_{n,stcc})$ is the expected value of $\rho_{n,stcc}$ over the crisis period n . After the crisis phases have been identified (see section 5.1) and the correlations estimated for the crisis and non-crisis periods, the test statistic can be easily computed in a straightforward fashion as a standard t -test.

In their testing procedure, [Forbes and Rigobon \(2002\)](#) define the non-crisis period as the full observation period. Their test statistic is based on the underlying assumption of independence, which becomes inappropriate when using overlapping data due to the conservative property of the test. The solution lies in correcting the asymptotic variance

of the test statistic to improve the asymptotic approximation to the normal distribution. Under the null hypothesis of no contagion, the adjusted test statistic is given by:

$$\text{FR}_{\text{adj}} = \frac{z(\hat{\rho}_{n,stcc}) - z(\hat{\rho}_{ccc})}{\sqrt{1/(T_{stcc} - 3) - 1/(T_{ccc} - 3)}} \xrightarrow{d} N(0, 1), \quad (10)$$

where $\xrightarrow{d}$ denotes convergence in distribution and $z(\hat{\rho}) = \frac{1}{2} \ln \frac{1+\hat{\rho}}{1-\hat{\rho}}$ denotes the Fisher transformation of the estimated correlation coefficient $\hat{\rho}$. T_{stcc} and T_{ccc} denote the number of observations during the crisis period and the full observation period, respectively. The test statistic is based on the assumption that two samples are drawn from two independent bivariate normal distributions with equal correlation coefficients. However, [Kocherlakota and Singh \(1982\)](#) show that the Fisher transformation of the correlation coefficient is fairly robust to deviations from normality. As the sample counterpart of $\bar{\rho}_{stcc}$, we use $\hat{\rho}_{n,stcc}$ which is defined as the sample mean of the estimated correlations from the MTV-STCC-GARCH model over the crisis period n . The estimate of the long-term level of correlations in the full sample period is given by $\hat{\rho}_{ccc}$. In order to compute the test statistic, besides estimating the level of constant correlations, we need to look at the estimated time-varying correlations beyond the long-run level of interdependence in the crisis period and compute their average thereafter.

It may be useful to examine if unspecified changes affecting the overall level of correlations leads to contagion effects. We thus begin by testing for contagion when time is selected as the transition variable. As the crisis period, we select the second phase of the crisis because the long-term level of correlations increase during that period. The test results from the correlation-based test across the periphery countries using time as the indicator variable are reported in Table 6. Our test results suggest that there is evidence of contagion either from or to Greece, Italy, Spain and Portugal (with Italy-Spain being the exception). Interestingly, the rejection of the null hypothesis mostly occurs when either Greece or Portugal are involved in the model. Our results fail to reject the null hypothesis of interdependence either from or to Ireland, Italy and Spain, which is not surprising since the constancy correlation tests failed to reject the null for these countries in the bivariate

Table 6: Results from the correlation-based tests of contagion within the periphery countries when the transition variable is time. The coefficients $\hat{\rho}_{ccc}$ and $\hat{\rho}_{2,tvc}$ denote the estimated correlations from the MTV-CCC-GARCH model and the MTV-TVC-GARCH model above the interdependence threshold averaged over the second phase of the crisis, respectively. "C" and "I" denote, respectively, cross-market contagion and interdependence at the 5% significance level.

	$\hat{\rho}_{ccc}$	$\hat{\rho}_{2,tvc}$	P -VALUE	
GREECE↔IRELAND	0.340	0.391	0.085	I
GREECE↔ITALY	0.422	0.497	0.013	C
GREECE↔PORTUGAL	0.450	0.516	0.023	C
GREECE↔SPAIN	0.429	0.498	0.020	C
IRELAND↔ITALY	0.525	0.558	0.134	I
IRELAND↔PORTUGAL	0.493	0.523	0.168	I
IRELAND↔SPAIN	0.537	0.572	0.125	I
ITALY↔PORTUGAL	0.598	0.660	0.009	C
ITALY↔SPAIN	0.808	0.827	0.090	I
PORTUGAL↔SPAIN	0.615	0.673	0.010	C

case. Therefore, focussing on a shorter period of crisis, and not necessarily in the full crisis period, we find evidence of financial contagion across peripheral countries. This accords with the findings of [Beirne and Fratzscher \(2013\)](#) who found regional contagion to be fairly trivial during the most acute phase of the European sovereign debt crisis.

We next examine the strength of market interactions across core and each periphery country. As before, we estimate the time-varying correlations whose dynamics is driven by time. Results of the tests are shown in Table 7. The tests strongly reject the hypothesis of interdependence and thus supporting for the presence of contagion effects across core and periphery countries. Interestingly, the test results within core lead in general to higher p -values. To save space, these results are not shown. Opposite conclusions can be drawn when Belgium is involved. We find stronger contagious linkages for the combinations Belgium-France and Belgium-Germany, implying there is a clear evidence of contagion effects among these pairs. However, we fail to reject the constancy of correlations for the pair Belgium-Germany and therefore the evidence of contagion for this pair may be seen as spurious. To summarize, when time is selected as the transition variable, we find

Table 7: Results from the correlation-based tests of contagion between core countries and each periphery country when the transition variable is time. The coefficients $\hat{\rho}_{ccc}$ and $\bar{\hat{\rho}}_{2,tvc}$ denote the estimated correlations from the MTV-CCC-GARCH model and the MTV-TVC-GARCH model above the interdependence threshold averaged over the second phase of the crisis, respectively. "C" and "I" denote, respectively, cross-market contagion and interdependence at the 5% significance level.

	$\hat{\rho}_{ccc}$	$\bar{\hat{\rho}}_{2,tvc}$	P-VALUE			$\hat{\rho}_{ccc}$	$\bar{\hat{\rho}}_{2,tvc}$	P-VALUE	
IRELAND↔BELGIUM	0.478	0.711	0.000	C	ITALY↔BELGIUM	0.557	0.623	0.000	C
IRELAND↔FINLAND	0.323	0.584	0.000	C	ITALY↔FINLAND	0.273	0.444	0.000	C
IRELAND↔FRANCE	0.394	0.676	0.000	C	ITALY↔FRANCE	0.488	0.643	0.000	C
IRELAND↔GERMANY	0.313	0.626	0.000	C	ITALY↔GERMANY	0.228	0.416	0.000	C
PORTUGAL↔BELGIUM	0.387	0.608	0.000	C	SPAIN↔BELGIUM	0.560	0.717	0.000	C
PORTUGAL↔FINLAND	0.205	0.399	0.003	C	SPAIN↔FINLAND	0.293	0.474	0.000	C
PORTUGAL↔FRANCE	0.335	0.579	0.000	C	SPAIN↔FRANCE	0.482	0.691	0.000	C
PORTUGAL↔GERMANY	0.158	0.419	0.000	C	SPAIN↔GERMANY	0.229	0.479	0.000	C
GREECE↔BELGIUM	0.248	0.409	0.000	C					
GREECE↔FINLAND	0.093	0.248	0.001	C					
GREECE↔FRANCE	0.174	0.371	0.000	C					
GREECE↔GERMANY	0.040	0.222	0.000	C					

strong evidence of shift contagion within the periphery countries, mostly either from or to Greece and Portugal, and between core and periphery countries following the more severe period of the crisis.

If one wishes to infer about the direction of the spillover effects, using time as the indicator variable will not be a suitable choice. Instead, by selecting the changes in bond yields of each periphery country as transition variable, we are able to identify the source of contagion from which shocks emanate. Two remarks are in order. First, using the changes in yields of periphery as the market indicator, the correlations tend to be higher during the first phase of the crisis. Thus, we shall define the unstable period as the first phase of the crisis. Second, before computing the correlation level for the crisis period, we consider the weekly average of the time-varying correlations to smooth out high-frequency noise. The test results can be found in Table 8. The results reveal either unidirectional or bidirectional contagion effects between countries. For instance, there is evidence of unidirectional contagion from the Portuguese bond market to the Italian during the first phase of the crisis, but not the other way around. In fact, we find no significant increase in

Table 8: Results from the correlation-based tests of contagion between the periphery countries using as transition variable the changes in bond yields of the source country (represented by the leftmost country) averaged over one week. The coefficients $\hat{\rho}_{ccc}$ and $\hat{\rho}_{1,stcc}$ denote the estimated correlations from the MTV-CCC-GARCH model and the MTV-STCC-GARCH model above the interdependence threshold averaged over the first phase of the crisis, respectively. "C" and "I" denote, respectively, cross-market contagion and interdependence at the 5% significance level.

	$\hat{\rho}_{ccc}$	$\hat{\rho}_{1,stcc}$	P-VALUE			$\hat{\rho}_{ccc}$	$\hat{\rho}_{1,stcc}$	P-VALUE	
GREECE→IRELAND	0.340	0.411	0.097	I	IRELAND→GREECE	0.340	0.441	0.023	C
GREECE→ITALY	0.422	0.545	0.006	C	IRELAND→ITALY	0.525	0.550	0.274	I
GREECE→PORTUGAL	0.450	0.538	0.036	C	IRELAND→PORTUGAL	0.493	0.542	0.131	I
GREECE→SPAIN	0.429	0.542	0.011	C	IRELAND→SPAIN	0.537	0.570	0.219	I
ITALY→GREECE	0.422	0.547	0.004	C	PORTUGAL→GREECE	0.450	0.541	0.029	C
ITALY→IRELAND	0.525	0.569	0.147	I	PORTUGAL→IRELAND	0.493	0.539	0.157	I
ITALY→PORTUGAL	0.598	0.652	0.095	I	PORTUGAL→ITALY	0.598	0.677	0.017	C
ITALY→SPAIN	0.808	0.835	0.110	I	PORTUGAL→SPAIN	0.615	0.692	0.017	C
SPAIN→GREECE	0.429	0.532	0.013	C					
SPAIN→IRELAND	0.537	0.579	0.177	I					
SPAIN→ITALY	0.808	0.836	0.096	I					
SPAIN→PORTUGAL	0.615	0.667	0.087	I					

financial linkages between Italy and Portugal when the Italian yield changes are selected as the transition variable as opposed to when we use the changes in Portuguese yields. Surprisingly, the results suggest an increase in comovements from the Irish bond market to the Greek, but not from the reverse direction. Another interesting finding is that there is empirical evidence of bidirectional contagion effects between Greece and the remaining periphery countries (Ireland being an exception).

If the interest lies in finding out whether general market turbulence plays a role on contagion, one may use regional and global volatility indexes as drivers of the correlation dynamics. The tests of contagion when choosing these indicators are presented in Table 9. Our results indicate contagion effects for the pairs Ireland-Italy and Portugal-Spain during the first phase of the crisis for low values of VSTOXX. Conversely, higher levels of the regional stock market volatility do not seem to drive contagion. When it comes to global volatility, we find contagion effects for all pairwise correlations involving Greece during the first phase of the crisis. Therefore, cross-country linkages between Greece and other

peripheral countries are strengthened when uncertainty is persistently high in the global financial market. An interesting finding can be perceived from the results. The correlations between Greece and other periphery countries appear to be strongly affected by global financial market volatility, whereas other pairwise correlations are mainly influenced by the euro area bond market. Our results corroborate the findings of [Broto and Pérez-Quirós \(2015\)](#) and [Mink and de Haan \(2013\)](#) who found Greece, Portugal and Ireland to be the major sources of contagion. Another interesting result, also consistent with ours, is that the size of a shock is not proportional to its capacity for spreading and leading contagion. They argue that, in fact, Portugal showed smaller shocks than Greece and yet it was the main driver of contagion.

The findings discussed above can be explained by the alternative choices for the transition variable. When using the calendar time, the modeller is interested in identifying level shifts in the unconditional correlations and therefore how the overall level of correlations is changing over time. Thus, when choosing time as driver of the correlation dynamics, any significant increase in the bond yield comovements may be regarded as long-run contagion. Because it seems to occur beyond what is explained by country-specific and global financial indicators, the long-run contagion effect is closely related to the concept of pure contagion. For more details about this type of contagion see [Giordano et al. \(2013\)](#). Instead, by selecting a financial indicator, the correlations are expected to update quite frequently. When a significant increase in cross-market linkages occurs in such erratic behaviour, this may be perceived as short-run contagion. Such contagion effect is closely related to the wake-up-call definition and we find this form of contagion to prevail mostly during the first-phase of the crisis. Wake-up-call contagion occurs when additional information about a crisis in one market prompts investors to reassess the default risk of other markets with similar structural problems. It is thus strongly related to country-specific factors. When using the indicator of global market uncertainty, our findings support Greece as the transmission channel of shocks from the global financial crisis to the sovereign debt crisis. The above results suggest two variants for the tests of contagion. Depending on the selection of the indicator variable, the tests of contagion will be testing the presence

Table 9: Results from the correlation-based tests of contagion for the periphery countries using as transition variable the lagged VSTOXX index averaged over two weeks and the lagged VIX index averaged over two days. The coefficients $\hat{\rho}_{ccc}$ and $\bar{\hat{\rho}}_{1,stcc}$ denote the estimated correlations from the MTV-CCC-GARCH model and the MTV-STCC-GARCH model above the interdependence threshold averaged over the first phase of the crisis, respectively. "C" and "I" denote, respectively, cross-market contagion and interdependence at the 5% significance level.

	$\hat{\rho}_{ccc}$	2-W AVG VSTOXX			2-D AVG VIX			
		$\bar{\hat{\rho}}_{1,stcc}$	P-VALUE		$\bar{\hat{\rho}}_{1,stcc}$	P-VALUE		
GREECE↔IRELAND	0.340	0.350	0.357	I	0.408	0.025	C	
GREECE↔ITALY	0.422	0.424	0.474	I	0.529	0.000	C	
GREECE↔PORTUGAL	0.450	0.457	0.393	I	0.539	0.002	C	
GREECE↔SPAIN	0.429	0.441	0.312	I	0.495	0.019	C	
IRELAND↔ITALY	0.525	0.609	0.000	C	0.573	0.008	C	
IRELAND↔PORTUGAL	0.493	0.528	0.059	I	0.513	0.252	I	
IRELAND↔SPAIN	0.537	0.606	0.001	I	0.568	0.059	I	
ITALY↔PORTUGAL	0.598	0.625	0.084	I	0.630	0.103	I	
ITALY↔SPAIN	0.808	0.823	0.075	I	0.818	0.165	I	
PORTUGAL↔SPAIN	0.615	0.653	0.019	C	0.625	0.350	I	

of either long-run or short-run contagion. The choice of either one will thus depend on the problem at hand.

6 Conclusions

In this paper, we study the presence and extent of contagion during the sovereign debt crisis for nine Eurozone countries. We address this problem by testing for financial contagion using a correlation-based analysis relying on the multiplicative time-varying STCC-GARCH model. The new model extends the multiplicative time-varying GARCH model of [Amado and Teräsvirta \(2013\)](#) to the multidimensional case where the time-variation in the conditional correlations is driven by time and observable financial indicators. This approach has the advantage of adjusting the correlations to long-term and short-term time-varying volatility, and therefore avoiding the bias in cross-market correlations. Besides, when time is selected as the indicator, the identification of the crisis phases can be determined endogenously by the model and not pre-defined by the modeller.

The new model is applied to nine daily data on 10-year government bond yields using

time and financial variables to control the changes in correlations. We find a smooth decline in the long-term trend in correlations between core and periphery, which may be explained by the flight-to-quality phenomenon from *bad* to *good* bond markets, when investors move their portfolio from falling to safer bond markets. When the transition variable is defined as a function of idiosyncratic shocks from peripheral markets, the transmission channel is viewed as country-specific. It is found that bond correlations across periphery are strongly affected by the size of shock (small or large), but they are not sensitive to the sign of shocks (negative or positive). When changes in conditional correlations are controlled by a regional market turbulence indicator, bond yield comovements tend to exhibit a pro-cyclical behavior as opposed to the countercyclical behavior of equity return correlations. There is, however, empirical support of higher global uncertainty being associated with higher conditional correlations in bond yields, but this effect is essentially observed for the pairwise correlations involving either Greece or Portugal.

Finally, our results also suggest strong evidence of long-run contagion effects within the periphery countries, mostly either from or to Greece and Portugal during the second phase of the crisis. With respect to the presence of short-run contagion effects, these are mainly observed around 2009-2014. We observe that short-term contagion is essentially driven by country-specific shocks from peripheral countries and higher levels of global stock market volatility. On the contrary, regional stock market turbulence does not seem to play a role on financial contagion.

Appendix: Estimation of parameters

Assuming joint conditional normality of the errors, $\varepsilon_t | \mathcal{F}_{t-1} \sim N(\mathbf{0}, \mathbf{H}_t)$, the parameters of the MTV-STCC-GARCH model can be estimated by maximum likelihood (ML). Let $\boldsymbol{\theta} = (\boldsymbol{\theta}'_g, \boldsymbol{\theta}'_h, \boldsymbol{\theta}'_\rho)'$ be the vector of all parameters of the model, where $\boldsymbol{\theta}_g = (\boldsymbol{\theta}'_{g1}, \dots, \boldsymbol{\theta}'_{gN})'$ is the parameter vector of g_{it} , $\boldsymbol{\theta}_h = (\boldsymbol{\theta}'_{h1}, \dots, \boldsymbol{\theta}'_{hN})'$ is the parameter vector of h_{it} , $i = 1, \dots, N$, and $\boldsymbol{\theta}_\rho$ contains the parameters of the correlation matrix $\mathbf{P}_t$. For notational simplicity, we use $\mathbf{S}_t = \mathbf{S}_t(\boldsymbol{\theta}_g, \boldsymbol{\theta}_h)$, $\mathbf{G}_t = \mathbf{G}_t(\boldsymbol{\theta}_g)$, and $\mathbf{P}_t = \mathbf{P}_t(\boldsymbol{\theta}_\rho)$.

The log-likelihood function for each observation t can be expressed as

$$\begin{aligned}
\ell_t(\boldsymbol{\theta}) &= -(N/2) \ln(2\pi) - (1/2) \ln |\mathbf{S}_t \mathbf{G}_t \mathbf{P}_t \mathbf{G}_t \mathbf{S}_t| - (1/2) \boldsymbol{\varepsilon}_t' \mathbf{S}_t^{-1} \mathbf{G}_t^{-1} \mathbf{P}_t^{-1} \mathbf{G}_t^{-1} \mathbf{S}_t^{-1} \boldsymbol{\varepsilon}_t \\
&= -(N/2) \ln(2\pi) - \ln |\mathbf{G}_t| - (1/2) \tilde{\boldsymbol{\varepsilon}}_t' \mathbf{G}_t^{-2} \tilde{\boldsymbol{\varepsilon}}_t - \ln |\mathbf{S}_t| - (1/2) \boldsymbol{\phi}_t' \mathbf{S}_t^{-2} \boldsymbol{\phi}_t \\
&\quad - (1/2) \ln |\mathbf{P}_t| - (1/2) \mathbf{z}_t' \mathbf{P}_t^{-1} \mathbf{z}_t + \mathbf{z}_t' \mathbf{z}_t
\end{aligned} \tag{11}$$

where $\tilde{\boldsymbol{\varepsilon}}_t = \mathbf{S}_t^{-1} \boldsymbol{\varepsilon}_t$, $\boldsymbol{\phi}_t = \mathbf{G}_t^{-1} \boldsymbol{\varepsilon}_t$, and $\mathbf{z}_t = \mathbf{G}_t^{-1} \mathbf{S}_t^{-1} \boldsymbol{\varepsilon}_t$. Maximising $\sum_{t=1}^T \ell_t(\boldsymbol{\theta})$ over the parameters of the model yields the maximum likelihood estimator $\hat{\boldsymbol{\theta}}_T$. Maximising the joint log-likelihood function with respect to all parameters is numerically very difficult, usually converging to local maxima and leading to computational problems in the standard errors. To facilitate parameter estimation, we use the fact that the log-likelihood (11) can be decomposed (ignoring the constant) as the sum of an unconditional and conditional volatility part, and a correlation part:

$$\ell_t(\boldsymbol{\theta}) = \ell_t^{UV}(\boldsymbol{\theta}_g) + \ell_t^{CV}(\boldsymbol{\theta}_g, \boldsymbol{\theta}_h) + \ell_t^{CC}(\boldsymbol{\theta}_g, \boldsymbol{\theta}_h, \boldsymbol{\theta}_\rho)$$

and use the two-step approach as suggested by Engle (2002) for estimating the parameters.

The unconditional variance term is

$$\ell_t^{UV}(\boldsymbol{\theta}_g) = -(1/2) \sum_{i=1}^N \{ \ln g_{it}(\boldsymbol{\theta}_{gi}) + \tilde{\varepsilon}_{it}^2 / g_{it}(\boldsymbol{\theta}_{gi}) \} \tag{12}$$

with $\tilde{\varepsilon}_{it} = \varepsilon_{it} / h_{it}^{1/2}(\boldsymbol{\theta}_{gi}, \boldsymbol{\theta}_{hi})$, $i = 1, \dots, N$, and the conditional volatility component is

$$\ell_t^{CV}(\boldsymbol{\theta}_g, \boldsymbol{\theta}_h) = -(1/2) \sum_{i=1}^N \{ \ln h_{it}(\boldsymbol{\theta}_{gi}, \boldsymbol{\theta}_{hi}) + \phi_{it}^2 / h_{it}(\boldsymbol{\theta}_{gi}, \boldsymbol{\theta}_{hi}) \} \tag{13}$$

where $\phi_{it} = \varepsilon_{it} / g_{it}^{1/2}(\boldsymbol{\theta}_{gi})$, for each $i = 1, \dots, N$. In the second step, the correlation parameters are estimated conditionally on the volatility parameters estimated in the first step by maximising the correlation component:

$$\ell_t^{CC}(\hat{\boldsymbol{\theta}}_g, \hat{\boldsymbol{\theta}}_h, \boldsymbol{\theta}_\rho) = -(1/2) \{ \ln |\mathbf{P}_t(\boldsymbol{\theta}_\rho)| + \mathbf{z}_t' \mathbf{P}_t^{-1}(\boldsymbol{\theta}_\rho) \mathbf{z}_t - 2 \mathbf{z}_t' \mathbf{z}_t \}. \tag{14}$$

where $\mathbf{z}_t = (z_{1t}, \dots, z_{Nt})'$ and $z_{it} = \varepsilon_{it} / (h_{it}^{1/2}(\boldsymbol{\theta}_{gi}, \boldsymbol{\theta}_{hi}) g_{it}^{1/2}(\boldsymbol{\theta}_{gi}))$, for each $i = 1, \dots, N$. Maximum likelihood estimates of the variance equations are obtained by splitting the maximisation problem into (12) and (13) and iterate between them until convergence. This method is called maximisation by parts by Song et al. (2005). Amado and Teräsvirta (2013) applied it to the estimation of the univariate MTV-GARCH model and proved consistency and asymptotic normality for the ML estimator. Under regularity conditions, consistency on the first step will ensure consistent estimators on the second step.

Our scheme differs from that of Silvennoinen and Teräsvirta (2017) who generalise maximisation by parts to the estimation of the multivariate MTV-GARCH model with deterministically time-varying correlations. Under standard regularity conditions, they established consistency and asymptotic normality of the ML estimator of the MTV-TVC-GARCH model. Compared to the two-step estimates, parameter estimators of their maximisation algorithm are fully efficient. Asymptotic properties of the ML estimator when the transition variable is stochastic are not yet known and deriving the asymptotic properties is beyond the scope of this paper.

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