



# Mapping the Pressure-dependent Day–Night Temperature Contrast of a Strongly Irradiated Atmosphere with HST Spectroscopic Phase Curve

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## Abstract

Many brown dwarfs are on ultrashort-period and tidally locked orbits around white dwarf hosts. Because of these small orbital separations, the brown dwarfs are irradiated at levels similar to hot Jupiters. Yet, they are easier to observe than hot Jupiters because white dwarfs are fainter than main-sequence stars at near-infrared wavelengths. Irradiated brown dwarfs are, therefore, ideal hot Jupiter analogs for studying the atmospheric response under strong irradiation and fast rotation. We present the 1.1–1.67  $\mu\text{m}$  spectroscopic phase curve of the irradiated brown dwarf (SDSS1411-B) in the SDSS J141126.20 + 200911.1 brown dwarf–white dwarf binary with the near-infrared G141 grism of the Hubble Space Telescope Wide Field Camera 3. SDSS1411-B is a 50  $M_{\text{Jup}}$  brown dwarf with an irradiation temperature of 1300 K and has an orbital period of 2.02864 hr. Our best-fit model suggests a phase-curve amplitude of 1.4% and places an upper limit of 11° for the phase offset from the secondary eclipse. After fitting the white dwarf spectrum, we extract the phase-resolved brown dwarf emission spectra. We report a highly wavelength-dependent day–night spectral variation, with a water-band flux variation of about  $360\% \pm 70\%$  and a comparatively small  $J$ -band flux variation of  $37\% \pm 2\%$ . By combining the atmospheric modeling results and the day–night brightness temperature variations, we derive a pressure-dependent temperature contrast. We discuss the difference in the spectral features of SDSS1411-B and hot Jupiter WASP-43b, as well as the lower-than-predicted day–night temperature contrast of J4111-BD. Our study provides the high-precision observational constraints on the atmospheric structures of an irradiated brown dwarf at different orbital phases.

*Unified Astronomy Thesaurus concepts:* Brown dwarfs (185); Exoplanet atmospheres (487); Hot Jupiters (753); White dwarf stars (1799)

## 1. Introduction

State-of-the-art phase-curve observations of hot Jupiters (e.g., Cowan et al. 2012; Knutson et al. 2012; Arcangeli et al. 2019) find extreme temperature contrasts between dayside and nightside atmospheres that can exceed a few hundred kelvin. Such drastic day–night temperature contrasts in these strongly irradiated atmospheres drive a wealth of atmospheric waves, jets, and turbulence that affect the atmospheric composition and structure (e.g., Showman & Guillot 2002). The exciting observations of strongly irradiated atmospheres motivate a series of theoretical studies to understand the relevant physical and chemical atmospheric processes, including the radiative cooling and advection (e.g., Showman & Guillot 2002), ohmic dissipation (e.g., Perna et al. 2010), nonequilibrium chemistry (e.g., Agúndez et al. 2014b), nonhomogeneous cloud formation and distribution (e.g., Parmentier et al. 2016; Powell et al. 2018), and hydrogen dissociation and recombination effects (Bell & Cowan 2018; Komacek & Tan 2018; Tan & Showman 2019;

see Heng & Showman 2015; Parmentier & Crossfield 2018; Showman et al. 2020; Fortney et al. 2021, for reviews). Despite the significant progress made on both the observational and modeling fronts on understanding the strongly irradiated atmospheres, many fundamental questions remained unanswered: What are the dominating physical mechanisms in redistributing irradiation energy at different rotation rates, temperatures, and altitudes? How do the clouds and atmospheric chemistry couple to global atmospheric circulation?

Time-series spectroscopy is one of the most powerful methods for constraining the atmospheric structure and tackling those fundamental questions. By observing the emission at different orbital phases, we can study the hemispherically integrated spectra at different local times, or longitudes, of the irradiated atmosphere of a tidally locked planet. The light-curve profile of the spectroscopic phase curve constrains the day–night temperature contrast and possible atmospheric dynamics through comparisons to three-dimensional global circulation model results. Furthermore, the wavelength dependence in the spectroscopic phase curve is a proxy of atmospheric properties at different altitudes because optical depth of an atmosphere is wavelength dependent. Therefore, spectroscopic phase curves have the potential to provide key insights into the variations of atmospheric structure at different longitudes and altitudes.

It is challenging, however, to obtain high-precision spectroscopic phase curves for hot Jupiters because of the bright host

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stars. Almost all hot Jupiter phase curves are in photometric mode collected by Spitzer/IRAC, with a few exceptions having been observed by the Hubble Space Telescope (HST) spectroscopic mode (e.g., Stevenson et al. 2014; Arcangeli et al. 2019). Interestingly, the strong irradiation level experienced by hot Jupiters can also be found in a rare class of objects—brown dwarf–white dwarf systems with ultrashort orbital periods of only a few hours (e.g., Casewell et al. 2012; Beuermann et al. 2013; Parsons et al. 2017; Casewell et al. 2020a, 2020b). Because of the Earth-sized white dwarf radius and the white dwarf spectrum, which often peaks at UV wavelengths, the near-infrared flux ratio of brown dwarf over white dwarf is higher than that of a hot Jupiter over its main-sequence host star. Therefore, the strongly irradiated brown dwarf in a brown dwarf–white dwarf system is an easier target than hot Jupiters for obtaining a high-precision spectroscopic phase curve and is an excellent hot Jupiter analog.

In addition to being hot Jupiter analogs, strongly irradiated brown dwarfs are ideal objects for studying the atmospheric dynamics in an atmosphere with similarly strong internal and external energy budgets (Showman 2016). Advanced global atmospheric circulation simulations of brown dwarfs orbiting white dwarfs (Lee et al. 2020; Tan & Showman 2020) suggest that the rapid rotation of a timescale of a few hours causes a narrow equatorial jet, alternating eastward and westward zonal flows in off-equatorial regions, and large day–night temperature contrasts in the irradiated brown dwarf atmospheres. The simulational results also indicate that the phase offset from the secondary eclipse<sup>12</sup> is pressure dependent (see Figure 10 in Tan & Showman 2020). In addition to the atmospheric dynamic studies, the 1D atmospheric radiative transfer modeling of Lothringer & Casewell (2020) finds that thermal inversion due to strong UV heating could explain the atomic emission lines seen in some of the hottest irradiated brown dwarf atmospheres (Longstaff et al. 2017). These models illustrate the rich and complex atmospheric dynamics and structure in the irradiated atmospheres.

To address the gap in our knowledge of the rapidly rotating irradiated atmosphere, we launched the observing campaign *Dancing with the Dwarfs* (ID: 15947; P.I: Dániel Apai). In this campaign, we use the HST Wide Field Camera 3 (WFC3)/G141 grism to obtain the spectroscopic phase curves of six irradiated brown dwarfs, which are SDSS J141126.20 + 200911.1, GSC2.3-SBBO006229, SDSS J155720.78 + 091624.7, BPS CS 29504–0036, LSPM J0135 + 1445, GD 1400, and SDSS J155720.78 + 091624.7. These irradiated brown dwarfs have equilibrium temperatures ranging from around 600 to 4000 K. Here we present the results of the first object observed in this campaign, the irradiated brown dwarf in the SDSS J141126.20 + 200911.1 binary system.

## 2. Brown Dwarf–White Dwarf Binary System SDSS J141126.20 + 200911.1

SDSS J141126.20 + 200911.1 (hereafter SDSS1411) is one of only three known eclipsing detached post-common-envelope white dwarf–brown dwarf binaries. It was initially identified by Beuermann et al. (2013) in the Catalina Sky Survey and was further characterized by Littlefair et al. (2014) and Casewell et al. (2018). The white dwarf primary is a 13,000 K hydrogen-

rich white dwarf with a mass of  $0.53 M_{\odot}$ . The binary has likely been in this configuration for the  $260 \pm 20$  Myr cooling time of the white dwarf, although the space motion of the binary suggests that it is a thin-disk member with a total system age of at least 3 Gyr. The brown dwarf secondary SDSS1411-B is likely tidally locked<sup>13</sup> in its 121.73-minute orbit and has a mass of  $50 M_{\text{Jup}}$  and a radius of  $0.70 R_{\text{Jup}}$  (Littlefair et al. 2014). The mass and radius of SDSS1411-B are consistent with the brown dwarf evolutionary models (Baraffe et al. 2003) at the system age and indicate that the brown dwarf is not inflated. At an orbital distance of 0.003 au, the irradiation temperature (assuming global redistribution of irradiation energy, zero albedo, and zero internal energy) of SDSS1411-B is about 1300 K. This brown dwarf mass and radius suggest a spectral type of T5, while the lack of detected secondary eclipse and  $K_s$ -band excess suggests a spectral type of L7–T1. Casewell et al. (2018) used the infrared imager Hawk-I (Kissler-Patig et al. 2008) of the Very Large Telescope to obtain the partial  $J$ -band and full  $H$ - and  $K_s$ -band phase curves of SDSS1411-B. They determined a dayside–nightside temperature difference of  $\sim 200$  K based on the  $H$ -band phase curve. By comparing the measured  $H$ - and  $K_s$ -band brightness temperatures to atmospheric models (Marley & McKay 1999; Marley et al. 2002; Fortney et al. 2005), they found a likely brightness temperature for the nightside of 1300 K, considerably warmer than would be expected by a T dwarf, particularly considering the high fraction of heat absorbed by the brown dwarf ( $\sim 80\%$  in the  $K_s$  band).

The ground-based broadband photometric phase curves of SDSS1411-B provide important constraints on the phase-curve amplitudes, yet they contain limited information on the possible dayside and nightside atmospheric structures. Resolved molecular features like water and methane absorptions from time-series spectroscopy are essential for constraining the temperature–pressure profile of the dayside and nightside atmospheres. By simultaneously probing different atmospheric depths with high-precision HST spectroscopic phase curves, our main goal is to answer the following question: “How does heat redistribution vary across different pressures in the rapidly rotating irradiated atmosphere of SDSS1411-B?”

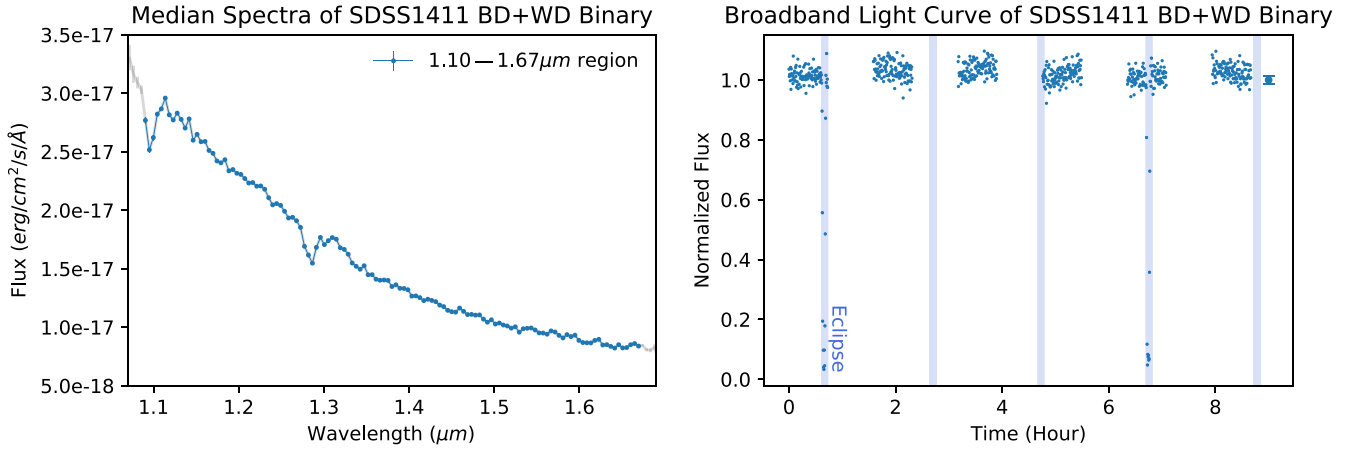
We structure the paper by first describing the data reduction of HST observational data in Section 3. Based on the reduced time-series spectra, we analyze the light-curve profile in Section 4 and the spectral components in Section 5. We adopt a forward-modeling approach to model the irradiated atmosphere and interpret the observed spectra in Section 6. Finally, we discuss the implications of our results and compare the spectra of the irradiated brown dwarf with those of hot Jupiters and isolated brown dwarfs in Section 7.

## 3. Data Reduction

We observed SDSS1411 in six consecutive HST orbits with the WFC3/IR/G141 grism on 2020 January 4 in the HST program GO-15947 (PI: Apai). In each HST orbit we obtained two to three F127M direct images for wavelength calibration and eight G141 Multiaccum exposures. Each Multiaccum exposure spans 313 s and consists of 15 readouts. Given the short orbital period of the target system, we aimed to retain the highest possible time resolution in our analysis. Therefore, we performed the data reduction starting from the *\_ima* files,

<sup>12</sup> We follow the nomenclature of exoplanet community here even though the brown dwarf’s emission is not fully obscured by the white dwarf at orbital phase of 0.5 (see also Figure 3).

<sup>13</sup> The tidal synchronization timescale is estimated to be around 10 Myr based on Equation (1) in Guillot et al. (1996) and an assumed tidal dissipation factor of  $10^5$ .



**Figure 1.** Left panel: the median spectra of the white dwarf–brown dwarf system. The blue line highlights the spectra from 1.1 to 1.67  $\mu\text{m}$ . The two hydrogen absorption regions of white dwarfs are 1.09–1.11  $\mu\text{m}$  and 1.27–1.32  $\mu\text{m}$ . Right panel: the six-orbit 1.1–1.67  $\mu\text{m}$  integrated broadband light curve. The two white dwarf eclipse events occur at the first and fifth HST orbits. The error bar at  $t = 9$  hr shows the representative flux uncertainties of 1.4% for a single photometric point. The shaded blue regions indicate the expected eclipse events with a period of 121.72 minutes.

which store every single detector readout. The *\_ima* files are products of the standard *calwfc3* pipeline, which removes dark current, corrects the bias, subtracts zero-read signals, calibrates the detector nonlinearity, flags bad pixels, and estimates electron count uncertainty. In each *\_ima* file, the recorded count rates and uncertainties are cumulative averages, with the zeroth readout as the reference point. We calculated the difference in counts and the corresponding uncertainty between two adjacent readouts, obtaining—in each exposure—14 22.35 s independent differential frames. In total, there are 672 frames over the six HST orbits.

We masked all pixels flagged for bad data quality (DQ), except those that were only flagged with cosmic-ray hits. These pixels were instead reprocessed via our own cosmic-ray detection algorithm. In our algorithm, we identified cosmic-ray impacted pixels based on the change in count rate, which is measured by the difference in electron counts between two successive frames. We find that a threshold of five times the photometric uncertainty can separate most of the drastic changes in count rates due to cosmic-ray events from those that are due to the white dwarf–brown dwarf eclipse event (the fastest change in the system’s intensity due to a physical process, i.e.,  $\sim 2$  minutes). We verified the results by visually inspecting the maximum electron count and the number of detected cosmic-ray events of each pixel in and out of the eclipse event.

We removed the sky component by least  $\chi^2$  fitting a scaled master sky image (Kümmel et al. 2011) and subtracted it from the science images. Based on the fitted centroid positions of SDSS1411 in our direct images, we calculated and applied the field-dependent flat-field correction. After the sky removal and flat-fielding, we interpolated the masked pixels from unmasked pixels within the same row. We then corrected the HST ramp effect by using the RECTE ramp-correction method as described in Lew et al. (2020a), which solves the intrinsic incoming count rate by minimizing the difference in count rates between the RECTE model prediction (Zhou et al. 2017) and the observations.

### 3.1. Spectral Extraction

Because the standard spectral extraction pipeline aXe (Kümmel et al. 2009) does not directly work with the *\_ima.fits* files, we developed our own spectral extraction procedure that follows the method described in the aXe manual. In

addition, we included the optimal spectral extraction algorithm (Horne 1986) in our pipeline, as described below.

First, based on the SDSS1411 position on the direct images and the position-dependent wavelength solution by Kuntschner et al. (2009), we constructed a wavelength solution for the spectral traces in the G141 images. Afterward, we converted count-per-pixel units into count-per-wavelength units by considering a weighting function, which calculates the fractional area of pixels projected to wavelength solutions in the cross-dispersion direction (see Appendix B). We also used the median-averaged spectra over six HST orbits as the two-dimensional spectral dispersion profile to extract the spectra with the optimal extraction method (Horne 1986). We use an aperture size of 8 pixels in the cross-dispersion direction for the spectral extraction. We converted the electron counts to flux densities by dividing them by the sensitivity curve,<sup>14</sup> considering the wavelength resolution and the exposure time. Finally, to correct the wavelength-dependent flux loss due to the finite aperture of 8 pixels, we performed an aperture correction using an interpolated table based on Kuntschner et al. (2011).

## 4. Light-curve Analysis

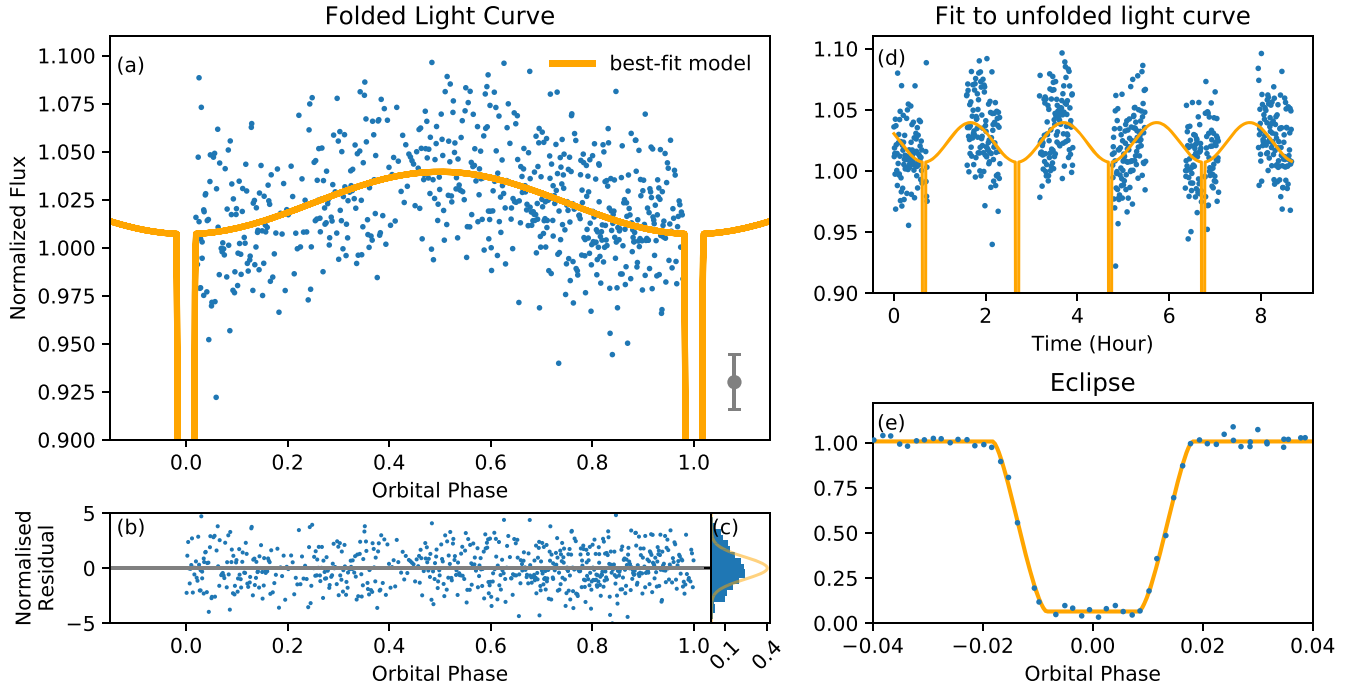
Figure 1 provides an overview of the reduced white dwarf and brown dwarf combined spectra and light curve. The spectra show the Pa $\beta$  and Pa $\gamma$  hydrogen absorption features of the white dwarf spectrum at around 1.095 and 1.284  $\mu\text{m}$ . We detect two primary-eclipse (occultation of white dwarf emission by brown dwarf) events in the six HST-orbit observations.

### 4.1. Day–Night Contrast and Mid-eclipse Time

We integrate the spectra from 1.15 to 1.67  $\mu\text{m}$  to create a synthetic broadband white light curve. We normalize the white light curve with the mean of the light curve. We construct a simple model to fit the normalized light curve:

$$\text{Model}(t) = M_{\text{eclipse}}(t, P, i, t_0, r_p/r_s, a, u) \times c_{\text{WD}} + A \sin\left[\frac{2\pi(t - t_0)}{P} + \phi_{\text{sine}}\right] + c_{\text{night}},$$

<sup>14</sup> <https://www.stsci.edu/hst/instrumentation/wfc3/documentation/grism-resources/wfc3-g141-calibrations>



**Figure 2.** (a) The folded light curve with the fitted period of 2.02862 hr. The primary-eclipse part of the phase-folded light curve is plotted separately in panel (e). (b) The residuals of the model fit to the light curve. The residuals are normalized by the photometric uncertainty. (c) The histogram of all the residuals. The orange line shows a normal distribution with one standard deviation. (d) The best-fit model and the light curve plotted in units of time on the  $x$ -axis. (e) A zoom-in plot of the model fit to the light curve in the eclipse region.

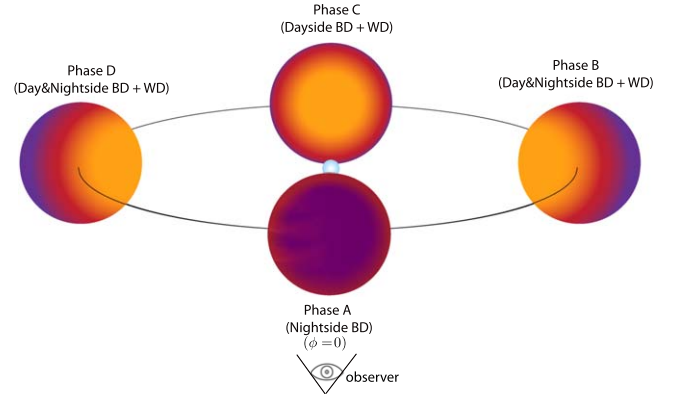
**Table 1**  
Light-curve Fitting Results

Parameter	Least $\chi^2$	MCMC
Orbital period $P$ (hr)	2.02864	$2.02863 \pm 0.00006$
Radius ratio $r_{\text{BD}}/r_{\text{WD}}$	4.6	$3.6^{+1.5}_{-0.8}$
Inclination $i$ (deg)	86	$87^{+2}_{-2}$
Mid-eclipse time $t_0$ (hr)	0.65388	$0.6539 \pm 0.0001$
Semimajor-axis ratio $a/r_{\text{WD}}$	43	$37^{+7}_{-4}$
Limb-darkening coefficient	0.0	$0.3 \pm 0.2$
Flux constant $c_{\text{WD}}$	0.943	$0.943 \pm 0.004$
$A_{\text{sine}}$	0.0162	$0.0160 \pm 0.0008$
$c_{\text{sine}}$	0.081	$0.080 \pm 0.004$
$\phi_{\text{sine}}$	$1.50\pi$	$(1.50 \pm 0.02)\pi$

**Note.** The second column shows the best-fit model parameters from a least  $\chi^2$  method. The third column shows the median values and  $1\sigma$  uncertainties (16th and 84th percentiles) of the marginalized posterior distributions of model parameters with the MCMC method. The semimajor-axis ratio, inclination, and radius ratio are correlated.

where  $M_{\text{eclipse}}$  represents the eclipse model calculated with the *Batman* package (Kreidberg 2015). There are six parameters in  $M_{\text{eclipse}}$ —orbital period  $P$ , mid-eclipse time  $t_0$ , inclination  $i$ , the ratio of the brown dwarf radius over the white dwarf radius  $r_p/r_s$ , the orbital semimajor axis  $a$ , and a linear limb-darkening coefficient  $u$ . The modeled white dwarf flux contribution equals  $M_{\text{eclipse}}$  multiplied by the time-averaged broadband white dwarf flux  $c_{\text{wd}}$ . The sinusoidal term and the constant  $c_{\text{sine}}$  term represent the orbital-phase-modulated brown dwarf’s emission.  $\phi_{\text{sine}}$  is defined as the phase offset of the primary-eclipse time from the zero-point of the sine wave.

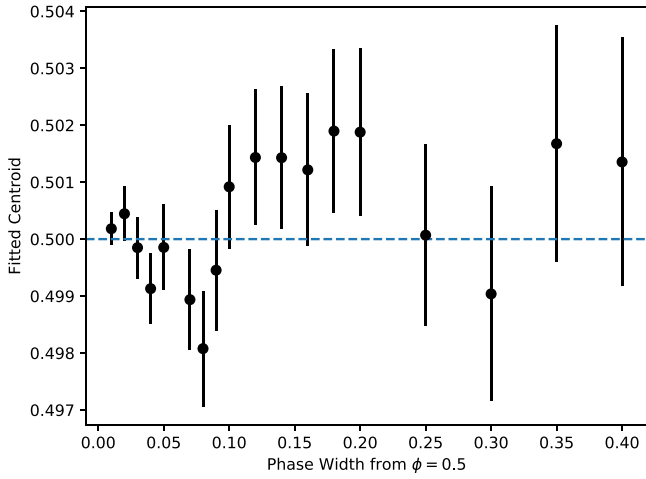
We plot the best-fit light-curve model with the least  $\chi^2$  method in Figure 2 with fitted parameters in Table 1. The fitted



**Figure 3.** An illustration of the white dwarf–brown dwarf system at different phases. We define Phase A ( $\phi = 0$ ) as the primary-eclipse phase and Phase C ( $\phi = 0.5$ ) as the secondary-eclipse phase. The white dwarf emission is completely blocked by the brown dwarf, so only the brown dwarf nightside (midnight) emission is observed during the primary eclipse. Because the brown dwarf radius is at least 3.5 times larger than that of the white dwarf, the brown dwarf’s emission is at best only partially obscured during the secondary eclipse.

reduced  $\chi^2$  is 3.1. The histogram of the residuals normalized by photometric uncertainties in panel (c) has a standard deviation of 1.76. Compared to spectra extracted with uniform aperture, the optimal extraction method lowers the averaged photometric uncertainty from 4% to 1.8% and gives a similar median ( $-0.001$ ) and standard deviation (0.025) of the residuals of light-curve fitting. We cannot reject the null hypothesis (i.e., normal distribution) based on the Shapiro–Wilk normality test of the residual with a  $p$ -value of 0.87. Therefore, we argue that the sinusoid model is a good approximation to the light curve out of eclipse.





**Figure 4.** The calculated centroids with partial light curves with phase coverage around the secondary eclipse ( $\phi = 0.5$ ). The centroid of a light curve that peaks after secondary eclipse has a value above 0.5 and vice versa. The derived centroids depend on the phase coverage of the partial light curves, so we find no convincing evidence of phase offset based on our data set.

We use the Markov Chain Monte Carlo (MCMC) method with *emcee* (Foreman-Mackey et al. 2013) to sample the posterior distributions of the fitted model parameters. We set up the MCMC chain with 400 walkers for 400,000 steps. We listed the uniform priors of parameters in Appendix C. We find that the fitted radius ratio, semimajor axis, and inclination are correlated; the fitted eclipse baseline and sinusoidal baseline are correlated too. The autocorrelation timescales of all parameters are less than 0.3% of the total steps and thus are well converged. We listed the 15th, 50th, and 85th percentiles of the posterior distributions of the model parameters in Table 1.

Based on the marginalized posterior distribution of  $c_{WD}$  and  $c_{sine}$ , the mean broadband flux of the white dwarf is about  $0.94/0.08 \sim 12$  times higher than the brown dwarf’s time-averaged emission. If we assume that the amplitude of the light curve solely originates from the brown dwarf’s emission variation, then the intrinsic brown dwarf variability amplitude is about 19%, equivalent to a 38% peak-to-trough flux variation. Assuming that the photosphere radii of the dayside and nightside of the SDSS1411-B atmosphere are identical,<sup>15</sup> then the 38% broadband flux variation corresponds to a day–night temperature variation of about 8%.

Based on the marginalized posterior distribution of the phase of the sinusoid, the phase of mid-eclipse is  $(1.50 \pm 0.02)\pi$ . The fitted sinusoidal phase suggests that the mid-eclipse occurs at the trough of the fitted sinusoid. The fitted orbital period of  $2.02863 \pm 0.00008$  hr, or  $121.718 \pm 0.005$  minutes, is within  $2\sigma$  of the reported period of 121.73 minutes in Beuermann et al. (2013).

#### 4.2. Phase Offset from the Secondary-eclipse Phase

The fitted phase of the mid-eclipse time suggests no significant phase shift between the mid-eclipse time and the trough of the

fitted sinusoid. By fitting the full orbital phase light curve, our light-curve model is less sensitive to the potential phase offset between the expected secondary-eclipse phase (orbital phase of 0.5; see also Figure 3) and the peak of the light curve. Therefore, we use a nonparametric method to examine whether there is any phase offset from the secondary eclipse. We calculate the centroids of partial light curves with different phase coverages. We estimate the centroid uncertainty by adding photometric noise to the partial light curve and repeat the calculation 10,000 times. We use the 16th and 85th percentiles of the 10,000 centroid samples as our centroid uncertainties for the partial light curves. In Figure 4, our results suggest that the calculated centroids depend on the phase coverages of the partial light curves. The fitted centroids are well within the uncertainty of the fitted eclipse phase ( $\sigma_{\phi_{sine}} = 0.02\pi = 0.01$  orbital phase; see Table 1). Therefore, we conclude that we find no evidence of phase offset from the secondary eclipse that exceeds a  $3\sigma$  limit of 0.03 orbital phase. The nearly zero phase offset suggests that the observed hemisphere appears to be the hottest at the secondary eclipse, or local noon time. This suggests that the radiative cooling timescale of the near-infrared photosphere is shorter than the horizontal advection timescale. Alternatively, the spatial scale of the circulation patterns could be too small to affect the phase offset.

We also fit the single sinusoidal model to the  $J'$ -band, water-band, and  $H'$ -band light curves. We conclude that no significant phase offsets (less than 3% of orbital phase) are detected between the three light curves and the white light curve.

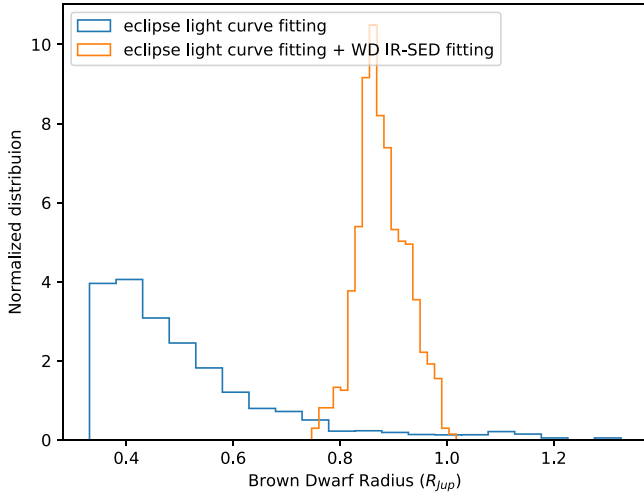
#### 4.3. Brown Dwarf Radius

Our eclipse light curve alone does not uniquely constrain the brown dwarf radius because of the strong degeneracy between inclination, white dwarf–brown dwarf radius ratio, and semimajor axis. We utilize multiple independent measurement methods to further constrain the brown dwarf radius. The absolute white dwarf radius is  $0.0130 \pm 0.0003 R_{\odot}$  based on near-infrared spectral fitting from Section 5.1. Given the absolute white dwarf radius and the estimated SDSS1411 system mass of  $0.58 \pm 0.03 M_{\odot}$  that is derived from the white dwarf evolutionary models and the semiamplitude of radial velocity measurements in Littlefair et al. (2014), we constrain the semimajor axis over white dwarf radius ratio to be  $a/r_{WD} = 52 \pm 2$ . By sampling the posterior distribution of light-curve fitting that satisfies the semimajor-axis constraints, we plot the updated marginalized posterior distribution of brown dwarf radius in Figure 5. The 16th, 50th, and 84th percentiles of the brown dwarf radius distribution are  $0.84R_{Jup}$ ,  $0.87R_{Jup}$ , and  $0.93R_{Jup}$ , respectively. Our derived brown dwarf radius values are higher than that in Littlefair et al. (2014) by  $\sim 2\sigma$  mainly because we adopt a closer distance (177 pc vs. 190 pc). Since the common-envelope evolution history and the tidal interaction in the SDSS1411 system, it is possible that the radius and the mass of SDSS1411-B could be different from those predicted by evolutionary models at a given age. We find that the updated brown dwarf radius of  $0.87R_{Jup} \pm 0.02R_{Jup}$  is consistent with the  $0.854R_{Jup}$ – $0.807R_{Jup}$  at ages of 3–10 Gyr, respectively, predicted by brown dwarf evolutionary models Sonora V2.0 (Marley et al. 2021) for  $50M_{Jup}$ .

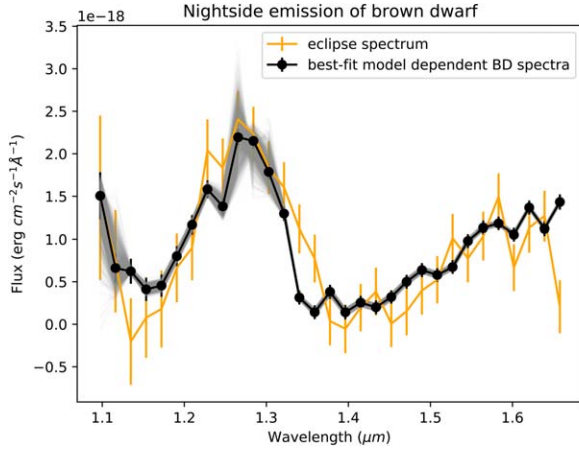
### 5. Spectral Analysis

Before we can study the dayside and nightside spectra of the irradiated brown dwarf atmosphere, we need to separate out the

<sup>15</sup> The light-curve fitting results of the  $g$ -band primary eclipse in Littlefair et al. (2014) find no detection of reflection from SDSS1411-B and see no evidence of Roche lobe distortion. We used the ROCHE software, which is part of the LCURVE model (Copperwheat et al. 2010), to estimate the Roche distortion due to tidal force and rotation. Based on the given mass ratio (0.1), orbital separation (0.003 au), and brown dwarf radius ( $0.7R_{Jup}$ ), the modeled distortion for SDSS1411-B is around 0.67%. The model calculation is the same as that in Casewell et al. (2020b).



**Figure 5.** The comparison of marginalized brown dwarf radius posterior distribution based on the MCMC eclipse light-curve fitting results and that with the additional constraint from white dwarf evolutionary models, radial velocity semiamplitudes, and white dwarf near-infrared spectral fitting.



**Figure 6.** The binned averaged nightside spectra (black line), which are observed just before or after the primary eclipse, show less scatters between spectral points and is similar to the SDSS1411-B spectrum during eclipse (orange line). The gray lines show the potential bias of the averaged nightside spectrum due to uncertainty of white dwarf temperature, gravity, and wavelength calibration sampled by the Monte Carlo method.

white dwarf spectrum from the spatially unresolved white dwarf and brown dwarf combined spectra. We assume that there are three stationary components and one time-dependent component in the spectroscopic phase curves: the white dwarf spectrum  $F_{WD}$ , the brown dwarf dayside spectrum  $F_{dayBD}$ , the brown dwarf nightside spectrum  $F_{nightBD}$ , and the dayside area fraction  $A(\phi)$  as a function of orbital phase  $\phi$ :

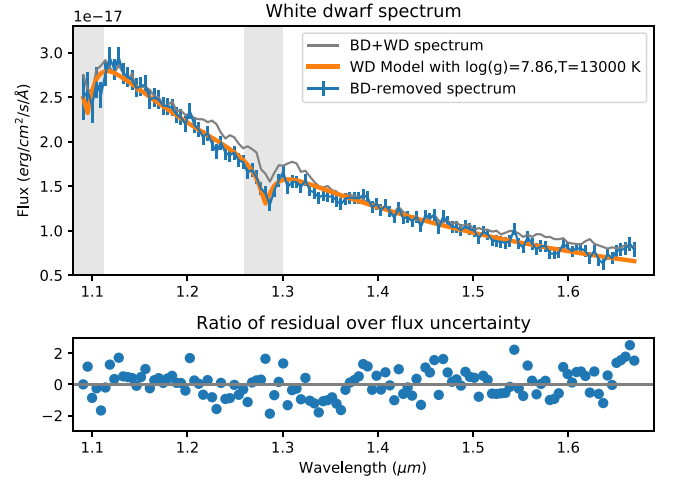
$$F_{total} = F_{WD} + F_{nightBD} + [1 - A(\phi)] \times (F_{dayBD} - F_{nightBD})$$

where  $\phi = [0, 1)$ .

In Section 4 we already solved for the wavelength-averaged  $A(\phi)$ . In the following subsections, we derive each spectral component based on the model.

### 5.1. Extracting White Dwarf Spectrum and Brown Dwarf Nightside Emission

When the white dwarf is eclipsed by the brown dwarf at  $\phi = 0$ , the observed flux ( $F_{eclipseBD}$ ) is equal to the brown



**Figure 7.** The blue line shows the cleaned white dwarf spectrum after removal of the brown dwarf eclipse spectrum. The orange line shows the binned white dwarf model spectrum. The gray shaded regions highlight the absorption lines in the white dwarf spectrum.

dwarf's nightside emission. In Figure 6, we plot the brown dwarf's emission during the eclipse. We report  $11\sigma$  and  $7\sigma$  level detections in the  $1.2\text{--}1.3\ \mu\text{m}$  and  $1.5\text{--}1.6\ \mu\text{m}$  regions, respectively.

We obtained a nightside spectrum with a higher signal-to-noise ratio than that of the eclipse spectrum by leveraging our understanding of the white dwarf spectrum. We apply a model-driven approach to separate the nightside emission from the white dwarf spectrum during the night phase, which is defined as the phase intervals before and after the eclipse event ( $\phi = 0.90\text{--}0.98$  and  $0.02\text{--}0.07$ ). During the night phase, the observed spectra are assumed to be

$$\phi_{\text{nightBD}} = [0.9 - 0.98, 0.02 - 0.10];$$

$$\phi_{\text{eclipseBD}} = [0.992 - 1, 0 - 0.008]$$

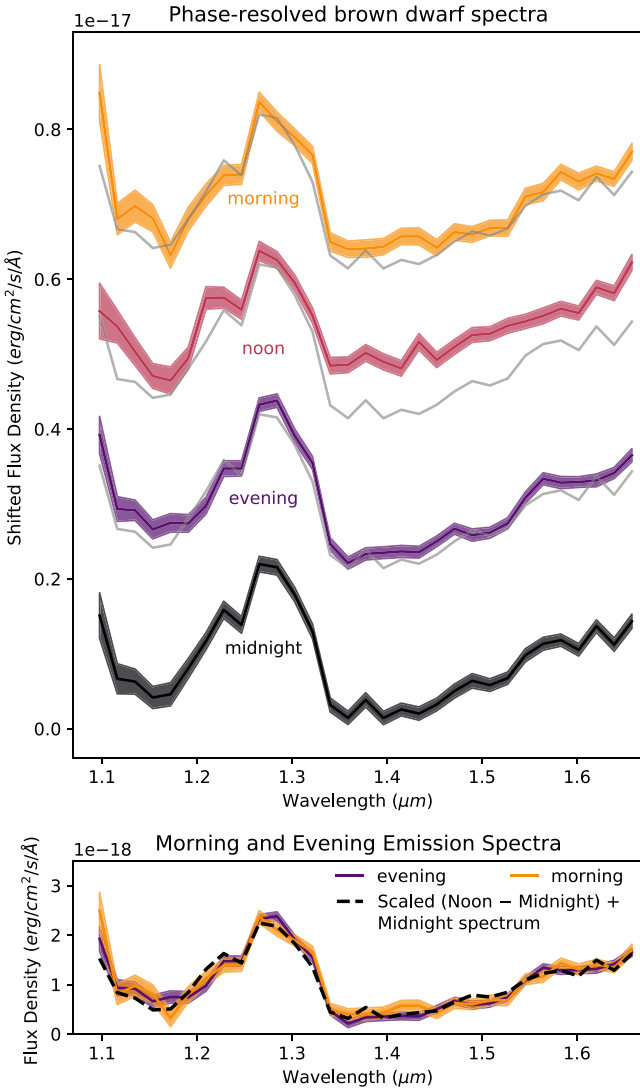
$$F_{\text{nightphase}} = F_{WD} + F_{\text{nightBD}} \quad (1)$$

$$\text{If } F_{\text{nightBD}} \approx F_{\text{eclipseBD}},$$

$$F_{WD} \approx F_{\text{nightphase}} - F_{\text{eclipseBD}}. \quad (2)$$

In this approach, we assume that the brown dwarf's emission remains unchanged throughout the night phase and approximate the brown dwarf's spectrum at night phase with the eclipse spectrum. We also assume a constant (phase-independent) white dwarf emission. Therefore, we can extract the white dwarf spectrum by subtracting the approximated brown dwarf's night-phase spectrum from the combined spectrum (see Equation (2)).

We adopt the best-fit white dwarf model parameters ( $\log(g) = 7.86 \pm 0.07$ ,  $T = 13,000 \pm 300$  K) reported in Littlefair et al. (2014). We linearly interpolate the white dwarf model spectra grid of Koester (2010) to obtain the white dwarf model spectrum with  $\log(g) = 7.86$  and  $T = 13,000$  K. We then obtain the best-fit white dwarf model spectrum by fitting the white dwarf model spectrum to the white dwarf spectrum approximated from Equation (2). The only free variable in the spectral fitting is the scaling factor,  $r_{WD}^2/d^2$ , where  $r_{WD}$  is the white dwarf radius and  $d$  is the distance of the SDSS1411 system. We plot the white dwarf model fitting results in Figure 7. We note that the center of  $\text{Pa}\beta$  and  $\text{Pa}\gamma$  absorptions in the observed spectra is off by 1 pixel ( $0.0046\ \mu\text{m}$ ) from that of the model spectra, which is likely caused by imperfect absolute wavelength calibration. Our



**Figure 8.** Top panel: the binned spectra at morning, noon, evening, and night orbital phases. The gray line represents the nightside spectrum. Bottom panel: comparison of the evening and morning spectra shows similar spectral features across 1.1–1.67  $\mu\text{m}$ . The scaled day–night spectral difference (dashed line) also matches well to the evening and morning spectra, showing that the evening and morning spectra can be reproduced by a linear combination of the dayside and nightside spectra.

subsequent analysis focuses on the broadband features, so the slight deviation does not affect our results. At a Gaia DR2 distance of  $177 \pm 5$  pc, the fitted scaling factor indicates a white dwarf radius of  $0.0130 \pm 0.0003 R_{\odot}$ .

Based on the best-fit white dwarf model spectrum, we then derive the brown dwarf’s nightside spectrum as shown by the following equation:

$$F_{\text{nightBD}} = F_{\text{nightphase}} - (r/d)^2 F_{\text{modelWD}}. \quad (3)$$

Because the phase coverage of spectra observed during the night phase ( $\Delta\phi = 0.16$ ) is wider than that during the eclipse phase ( $\Delta\phi = 0.016$ ), the averaged night-phase spectrum has a much higher signal-to-noise ratio than the eclipse spectrum, as shown in Figure 6.

The accuracy of the model-dependent night-phase spectrum depends on the accuracy of white dwarf temperature and gravity and that of the wavelength calibration of the HST data.

To investigate the potential systematic uncertainties in our results, we use a Monte Carlo method to sample three one-dimensional normal distributions of temperature, gravity, and wavelength offset. We adopt the uncertainties ( $\sigma_T = 300$  K,  $\sigma_{\log(g)} = 0.07$ ) reported in Littlefair et al. (2014) as the standard deviations of the normal distributions of temperature and gravity. We conservatively estimate the uncertainty in the wavelength calibration to be half the pixel resolution, or 23 Å. Based on the 1000 white dwarf model spectra that were derived from the three normal distributions of temperature, gravity, and potential wavelength offset, we fit each model to the observed white dwarf spectrum (Equation (2)) with the least  $\chi^2$  method. The scaling factor is the only free parameter in the fitting process. In Figure 6, we plot the derived brown dwarf night-phase spectral component after subtracting off the fitted white dwarf model spectra from the observed night-phase spectra. We show that, except at wavelengths where white dwarf model spectra show strong hydrogen absorption lines (1.25–1.30  $\mu\text{m}$  and 1.09–1.11  $\mu\text{m}$ ), the model-dependent night-phase spectrum of the brown dwarf is robust against the white dwarf temperature, white dwarf gravity, and the HST wavelength calibration uncertainties.

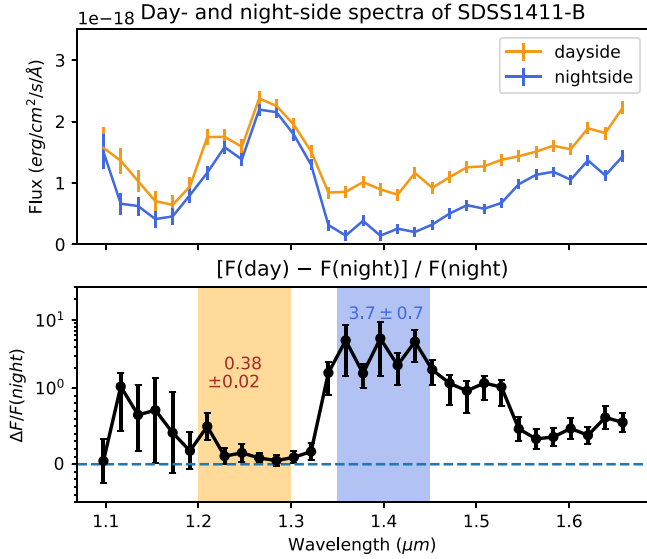
## 5.2. Phase-resolved Spectra and Day–Night Spectral Variation

After fitting and subtracting the phase-independent white dwarf spectral component, we plot the derived phase-averaged brown dwarf spectra over the midnight ( $\phi = 0.90$ – $0.98$  and  $0.02$ – $0.10$ ), evening ( $\phi = 0.17$ – $0.33$ ), noon ( $\phi = 0.42$ – $0.58$ ), and morning ( $\phi = 0.67$ – $0.83$ ) orbital phases in Figure 8. We test whether the evening and morning spectra are a linear combination of dayside (noon) and nightside (midnight) spectral components. We fit a scale factor  $k$  to the composite spectra made of dayside and nightside spectra to the observed evening and morning spectra as shown by the cost function equation below:

$$C = [k \times (F_{\text{day}} - F_{\text{night}}) + F_{\text{night}}] - F_{\text{evening(or } F_{\text{morning}})}. \quad (4)$$

Our least-squares fitting that minimizes the cost function  $C$  over observational uncertainties gives reduced  $\chi^2$  of 0.98 and 0.88. The close-to-unity reduced  $\chi^2$  suggest that both evening and morning spectra can be well approximated by a linear combination of dayside and nightside spectra. We also perform a simple check on the spectral difference between evening and morning spectra. We find that the maximum absolute spectral difference between the two spectra is about  $2\sigma$  and the median value of the absolute spectral difference across different wavelengths is about  $0.5\sigma$ , where  $\sigma$  is the propagated observational uncertainties. In conclusion, we do not find significant differences between the evening and morning spectra. In our following analysis, we focus on analyzing the day(noon)–night(midnight) spectral variations.

In the top panel of Figure 9, we plot the extracted brown dwarf dayside and nightside spectrum. We find that the water-band flux in the dayside spectrum is almost twice as high as in the nightside spectrum. In the bottom panel of Figure 9, we plot the day–night spectral variations relative to the nightside spectrum. We find that one of the key features in the relative spectral variation is the relatively low flux difference in the  $J'$  band (1.2–1.3  $\mu\text{m}$ ). The binned  $J'$ -band flux difference is  $38\% \pm 2\%$ , while the binned water-band flux difference is  $370\% \pm 70\%$ .



**Figure 9.** Top panel: the binned dayside and nightside spectra of SDSS1411-B. The water-band flux of the dayside spectrum is almost two times higher than that of nightside spectrum. Bottom panel: the relative spectral variation between the dayside and nightside spectra. The spectral variation is almost 10 times larger in the water band than in the  $J'$  band. To show order-of-magnitude variations with uncertainty ranges that include negative values, we use the “symlog” y-axis scale, which is in linear scale below unity and in log scale above unity.

### 5.3. Brightness Temperature Variation

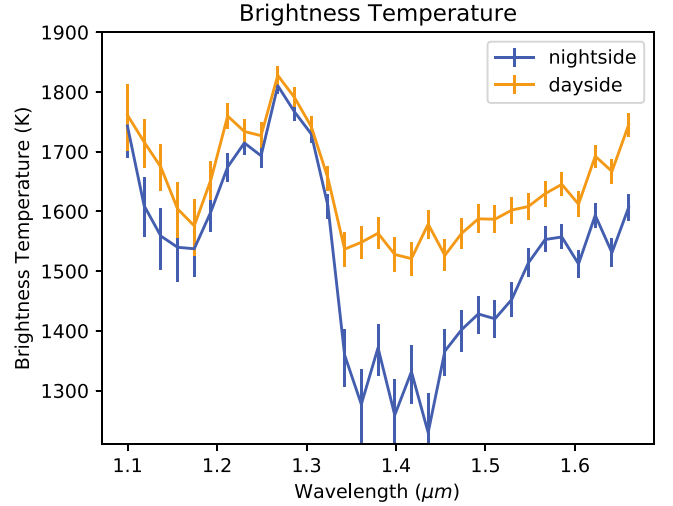
Brightness temperature is the temperature at which a blackbody emits the same amount of specific intensity as the observed value. In an atmosphere where the temperature monotonically decreases with lower pressure, a hotter brightness temperature indicates that the flux emits from a higher pressure. Based on the assumption of the monotonic relationship between temperature and pressure, brightness temperature is then a useful proxy to compare the pressure regions that different wavelengths probe.

After converting flux densities to brightness temperatures with the Planck equation and the derived brown dwarf radius in Section 4.3, in Figure 10 we plot the brightness temperatures as a function of wavelengths for the dayside and nightside spectra. Based on Figure 10, we conclude that the high-altitude atmosphere—which emits the bulk of the water-band flux—experiences a larger change in temperature than the low-altitude atmosphere that the  $J$ -band flux probes. The conclusion that lower-altitude atmosphere has lower change in temperature variation is also consistent with the reported broadband photometric phase-curve observation by Casewell et al. (2018). Casewell et al. (2018) reported that the brightness temperature variations ( $360 \pm 80$  K) in the  $K_s$  band are higher than those ( $93 \pm 12$  K) in the  $H$  bands.

## 6. Modeling Day–Night Spectral Variations

### 6.1. Description of Models

To study the difference in atmospheric structure between the dayside and nightside atmosphere, we model the irradiated SDSS1411-B atmosphere with one-dimensional cloudless atmospheric models. The models are based on McKay et al. (1989), Marley & McKay (1999), and Mayorga et al. (2019), with a wavelength grid ranging from 0.3 to 200  $\mu\text{m}$ . The models assume a surface gravity of  $\log(g) = 4.4$ , solar



**Figure 10.** The brightness temperatures of the dayside and nightside spectra. The brightness temperatures are binned with a bin size of 0.014  $\mu\text{m}$ . The brightness temperatures are higher in the  $J'$  band than in the water bands.

metallicity, and chemical-equilibrium abundances. The models properly account for the scattering and deposition of incident flux such that the irradiated atmospheres have nonzero albedo values. The modeled dayside atmosphere is irradiated by a 13,000 K white dwarf at 0.003 au (Littlefair et al. 2014). The shortest wavelength bin of our models is around 0.3  $\mu\text{m}$ . To include the irradiation flux at wavelengths shorter than 0.3  $\mu\text{m}$ , we increase the irradiation flux at the 0.3  $\mu\text{m}$  bin such that it is equivalent to the sum of the white dwarf irradiation flux at  $\lambda < 0.3 \mu\text{m}$ , which is about 60% of bolometric luminosity. This approximate treatment is necessitated by a lack of appropriate UV opacities required for the models.

Further, we assume that the nightside  $T$ – $P$  profile has an identical interior temperature ( $T(P = 100 \text{ bar})$ ) to that of the dayside. The modeled brown dwarf atmospheres therefore have nonzero internal energy. Because our nonirradiated model is designed to converge to a specified effective temperature, we construct two models whose effective temperatures are slightly lower and higher than that of the dayside model. We then linearly interpolate the two  $T$ – $P$  profiles ( $T_{\text{night1}}(p)$  and  $T_{\text{night2}}(p)$ ) so that the interpolated  $T$ – $P$  profile shares the same temperature with the dayside model at the pressure of 100 bars. In the linear interpolation, we calculate the averaged temperature difference at  $P > 90$  bars between the nightside  $T$ – $P$  profiles and the dayside  $T$ – $P$  profile:

at  $P > 90$  bars,

$$\Delta T_1 = |\text{mean}(T_{\text{day}}(p) - T_{\text{night1}}(p))| \quad (5)$$

$$\Delta T_2 = |\text{mean}(T_{\text{day}}(p) - T_{\text{night2}}(p))|. \quad (6)$$

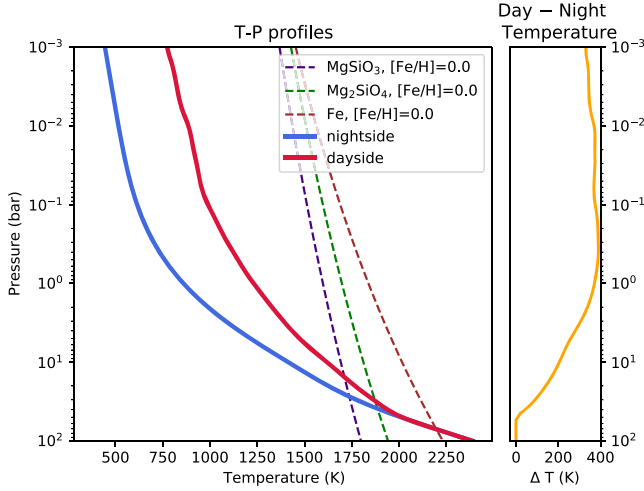
We then assign a relative weighting for the two nightside  $T$ – $P$  profiles based on the temperature differences at the high-pressure region for the linear temperature interpolation over isobars and obtain the interpolated nightside  $T$ – $P$  profile ( $T_{\text{newnight}}(p)$ ):

$$W = \Delta T_1 + \Delta T_2, \quad (7)$$

$$T_{\text{newnight}}(p) = T_{\text{night1}}(p) \times \frac{\Delta T_2}{W} + T_{\text{night2}}(p) \times \frac{\Delta T_1}{W}. \quad (8)$$

We use the PICASO model (Batalha et al. 2019) to calculate the outgoing emission based on the interpolated nightside  $T$ – $P$





**Figure 11.** Left panel: the  $T$ - $P$  profiles of nightside (solid blue line) and dayside (solid red line) models. The purple, green, and red dashed lines show the condensation curves of  $\text{MgSiO}_3$ ,  $\text{Mg}_2\text{SiO}_4$ , and  $\text{Fe}$ , respectively, from Visscher et al. (2010). The RCBs of nightside and dayside models are at around 30–60 bars. Right panel: the day–night temperature difference.

profile. We plot the modeled dayside and nightside temperature–pressure profiles in Figure 11.

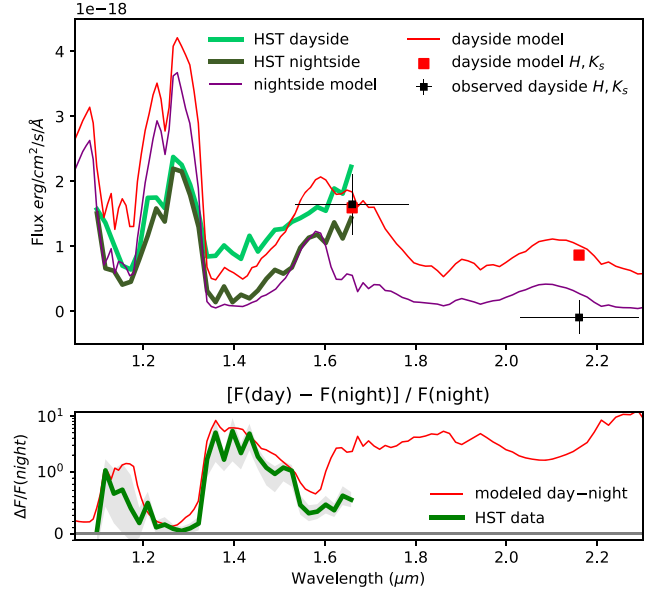
### 6.2. Spectral Modeling Results

In Figure 12, we plot the modeled dayside and nightside spectra and the day–night spectral variation. In addition to the HST WFC3/G141 spectra, we also compare our models with the ground-based  $H$ - and  $K_s$ -band photometry (black squares) from Casewell et al. (2018). Based on the reported SDSS1411 WD+BD system magnitudes in Casewell et al. (2018), in Section 5.1 we subtract the best-fit white dwarf model flux contribution to derive the brown dwarf dayside  $H$ - and  $K_s$ -band flux. We find that the dayside and nightside atmospheric model spectra qualitatively reproduce the main spectral features, including the water-band absorption at 1.15 and 1.45  $\mu\text{m}$  and the potassium line (K I) absorption at around 1.27  $\mu\text{m}$ . Both the dayside and nightside models overestimate the  $J$ -band flux and underestimate the 1.4–1.67  $\mu\text{m}$  flux. The ground-based  $H$ -band flux is consistent with the dayside-model flux within  $1\sigma$ ; the dayside-model  $K_s$ -band flux is about  $4\sigma$  higher than the observed value, even though the discrepancy is sensitive to the derived white dwarf flux contribution (see Section 5.1) and the  $K_s$ -band absolute flux calibration. The deviations between the data and our forward-model-based spectral fits suggest that our understanding of the atmospheric processes and line lists is incomplete for irradiated atmospheres. For example, absorption by strong UV transitions could heat up the pressure region probed by water- and  $H$ -band flux and, therefore, increase the emission at these wavelengths. Furthermore, including cloud opacity could lower the modeled  $J$ -band flux and provide a better fit to the observed value. We discuss further the impact of potential clouds in Section 7.4.

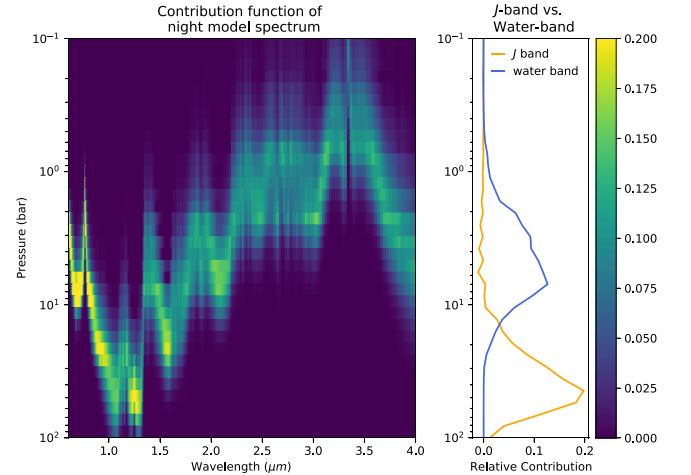
### 6.3. Pressure-dependent Temperature Contrast

Constraining the pressures from which the fluxes at different wavelengths are emitted is essential for mapping the observed spectral variation to the day–night temperature contrast as a function of pressure. We calculate the contribution function of the nightside model to measure the relative flux contribution to

Model spectra of dayside and nightside cloudless atmospheres

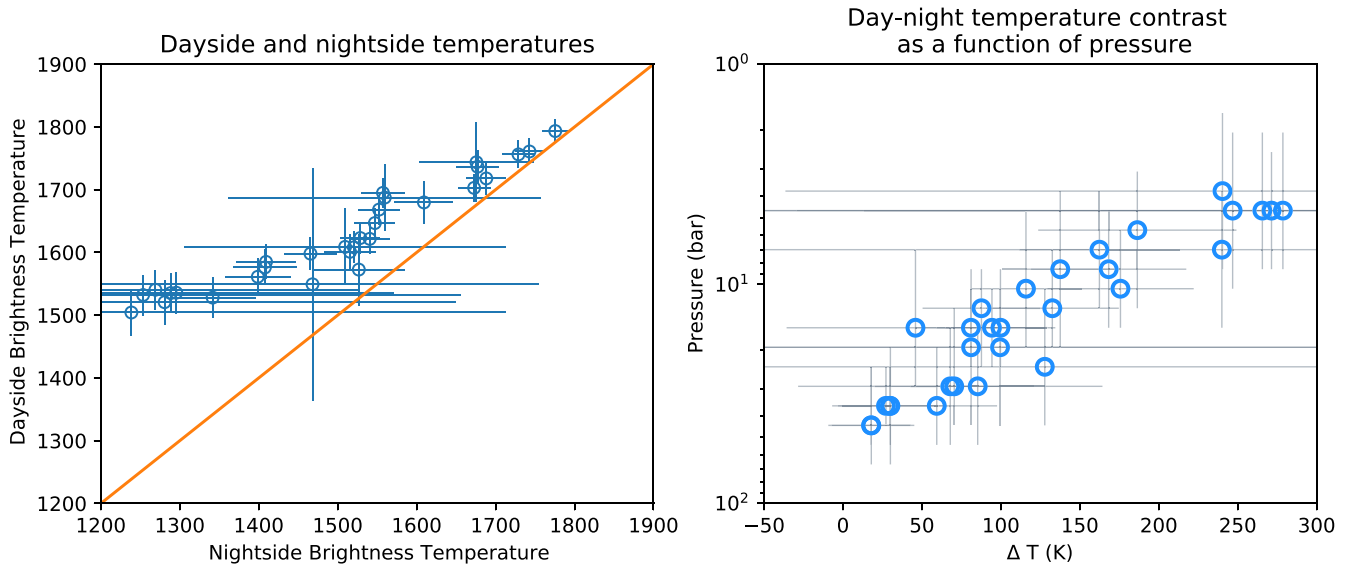


**Figure 12.** Top panel: the nightside (purple line) and dayside (red line) model spectra qualitatively reproduce the spectral shape of the observed nightside (dark-green line) and dayside spectra (light-green line). We plot the ground-based  $H$ - and  $K_s$ -band photometry from Casewell et al. (2018) as black squares at 1.66 and 2.16  $\mu\text{m}$ , respectively. The modeled dayside  $H$ -band flux (red square) is consistent with observed values, while the modeled  $K_s$ -band flux (red square) is higher than the observed value. See text for the discussion of the difference between modeled and observed spectra. Bottom panel: the modeled day–night spectral variation shows that the flux variation is about an order of magnitude higher in the water-band region than that in the  $J$ -band region, matching the observed wavelength dependence in day–night spectral variation.



**Figure 13.** Left panel: the contribution function of the nightside model. The colors represent the relative contribution per pressure layer to the emission. Right panel: the peak of the  $J$ -band and water-band contribution function of the nightside spectrum is at  $\sim 20$ –80 bars and 2–20 bars, respectively.

the top-of-atmosphere emission at each wavelength bin across different pressures. To calculate the contribution function, we perturb the nightside  $T$ - $P$  profile by increasing the temperature in each pressure layer by 100 K and calculate the change in the top-of-atmosphere emission. At each wavelength bin, we divide the emission change due to the temperature perturbation of each layer by the total emission change to obtain the relative flux contribution per layer. In Figure 13 we plot the



**Figure 14.** Left panel: the nightside and dayside brightness temperatures are less different at higher nightside brightness temperatures. The orange  $y = x$  line portrays equal dayside and nightside temperatures. Right panel: the measured day–night brightness temperature contrast as a function of nightside pressures suggests that day–night temperature contrast increases with lower pressure.

contribution function for the nightside model spectrum. The contribution function suggests that  $J'$ -band and water-band emission originates from around regions of 20–80 bars and 2–20 bars, respectively.

With the calculated contribution function and the measured day–night brightness temperature contrast in Section 5.3, we illustrate the pressure-dependent day–night temperature contrast in Figure 14. As shown in the right panel of Figure 14, the day–night temperature contrast increases with lower pressure. We can qualitatively explain the trend in the pressure-dependent temperature contrast with cooling and advection timescales. The radiative cooling timescale decreases with higher pressure (e.g., Showman & Guillot 2002). Assuming that the advection timescale of atmospheric jets is roughly the same in the range of 1–50 bars (see, e.g., Figure 5 in Tan & Showman 2020 and Figure 4 in Lee et al. 2020), the ratio of radiative cooling over advection timescale decreases with lower pressure. Therefore, the dayside atmosphere at a lower pressure cools faster, so the day–night temperature contrast is higher at lower pressure. Besides the advection and cooling processes, convection could also play an important role in explaining the similar dayside and nightside temperatures, or low day–night temperature contrasts, at high-pressure regions. Our atmospheric models indicate that the radiative–convective boundary (RCB) is at around 30–60 bars. The interiors of brown dwarfs should be fully convective, and the interior specific entropy is expected to be homogenized. At atmospheric layers deeper than the RCB, convection is expected to drive the profiles toward having the same specific entropy as the interior. Therefore, the dayside and nightside flux that originates below the RCB could be similar to each other because of convection. Our results demonstrate the observational constraints on the pressure-dependent day–night temperature differences that extend to the high-pressure region ( $P > 20$  bars) of the irradiated atmosphere.

#### 6.4. Temperature Gradient

In Figure 15, we plot the observed brightness temperature over the inferred pressure based on the calculated contribution functions in Section 6.3. We emphasize that the inferred

pressures are model dependent while the brightness temperatures are derived from the observed flux densities. We also plot the adiabat profile assuming that the temperature gradient follows the adiabat gradient derived by Parmentier et al. (2015) based on the fit to the equation of state of substellar objects at high-pressure regions (Saumon et al. 1995):

$$\nabla_{\text{ad}} \approx 0.32 - 0.1 \left( \frac{T}{3000 \text{ K}} \right). \quad (9)$$

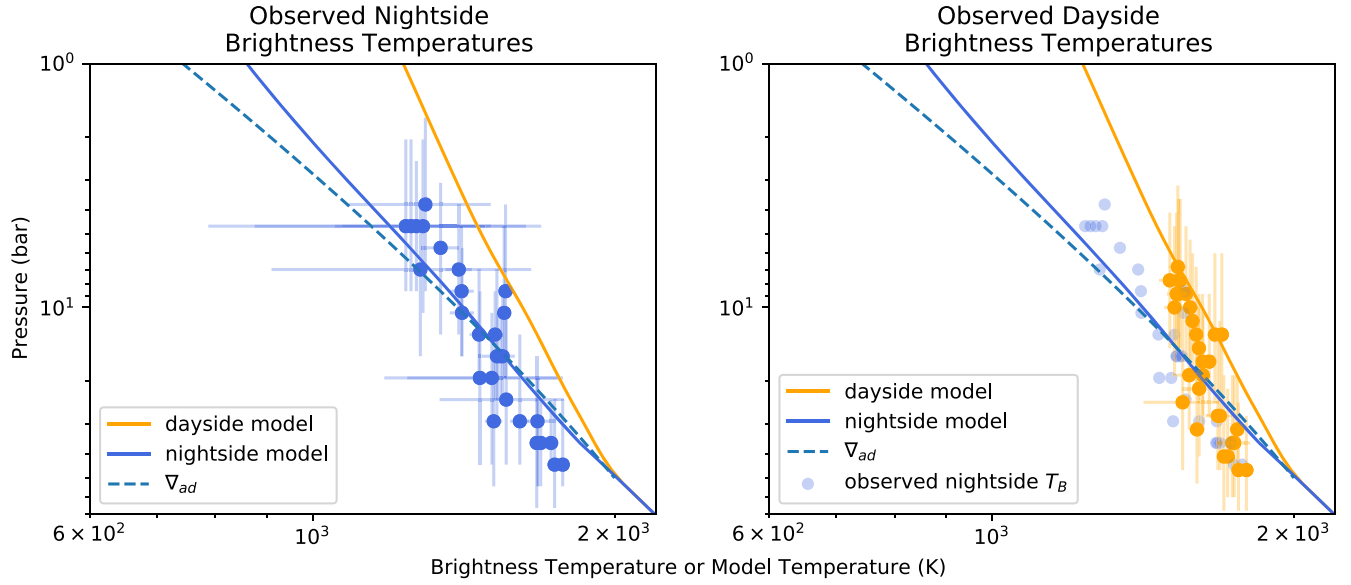
We integrate the temperature gradient with a boundary condition such that the adiabatic profile shares the same temperature at high pressures ( $\sim 50$  bars) with that of both the dayside and nightside models. Both dayside and nightside brightness temperatures show a shallower temperature gradient than that of the adiabat (i.e., temperature decreases less with lower pressure than that of an adiabatic profile or  $|d \log T / d \log P| < |\nabla_{\text{ad}}|$ ), although the uncertainties are large. In the right panel of Figure 15, the dayside atmosphere has a shallower temperature gradient than that of the nightside atmosphere.

The thermal profile in irradiated objects is determined by the competition between the bottom heating via the internal flux and the top heating from the stellar light. When the received stellar irradiation is larger than the internal flux, it stabilizes the atmosphere against convection and reduces the thermal gradient. The effect happens mainly on the dayside, where the stellar heat is deposited, but it also happens on the nightside because of the advection of heat from dayside to nightside. Because this heat advection is not perfectly efficient, the nightside profile is closer to the adiabatic gradient than the dayside atmosphere.

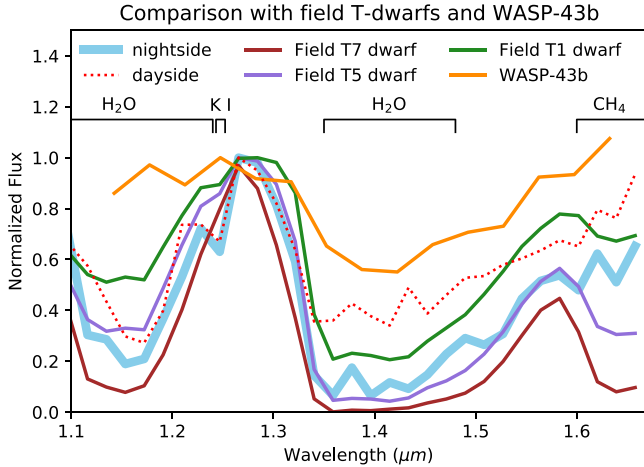
## 7. Discussion

### 7.1. Comparison of Spectra and Color Variations to Those in Isolated Brown Dwarfs

How does the redistribution of irradiation energy from the dayside to the nightside affect the nightside emission spectra of the irradiated brown dwarf SDSS1411-B? In Figure 16, we compare the spectra of a field T1 dwarf (2MASS J10393137



**Figure 15.** Left panel: the observed nightside brightness temperatures at different inferred pressures, which are derived from the contribution function of the nightside model, are plotted as blue points. The solid blue and orange lines show the modeled dayside and nightside temperature–pressure profile. The blue dashed line shows an adiabat profile that shares the same interior temperature at 30 bars with the model. Right panel: observed dayside brightness temperatures over different inferred pressures, which are derived from the contribution function of the dayside model, are plotted in orange points. The solid and dashed lines are the same as those in the left panel.



**Figure 16.** Comparison of the binned dayside (dotted red line) and nightside (solid blue line) SDSS1411-B spectra with field T dwarfs and WASP-43 b spectra. The SDSS1411-B nightside spectrum (thick light-blue line) shows a similar water-band absorption depth to the field T5 dwarf (solid purple line) and the lack of a strong methane absorption feature at 1.65 μm, which is prevalent among T dwarf spectra. The higher gravity and the steeper temperature gradient of SDSS1411-B cause the deeper water-band absorption compared to that of the nightside spectrum of hot Jupiter WASP-43 b (solid orange line). We also plot the spectra of field T1 and T7 dwarfs in solid green and maroon lines, respectively, for reference.

+3256263; Buenzli et al. 2014; Manjavacas et al. 2019), field T5 dwarf (2MASS J00001354+2554180; Buenzli et al. 2014; Manjavacas et al. 2019), and field T7 dwarf (2MASS J1553022+153236; Burgasser et al. 2010) with those of SDSS1411-B, which are normalized by the flux at around 1.27 μm. SDSS1411-B nightside emission spectra show a similar water-band absorption depth to that of the field T5 dwarf, which has an effective temperature of around 1000 K (Filippazzo et al. 2015). However, we notice the lack of methane absorption feature in the nightside emission spectra at around 1.6–1.67 μm, which is prominent in the spectra of T

dwarfs. We speculate that the shallower methane absorption feature in the nightside emission spectra is likely because SDSS1411-B is hotter than field T dwarfs in the low-pressure region probed by *H*-band flux, which is approximately 10 bars as indicated by our contribution function in Figure 13. It is also possible that the global atmospheric circulation drives the methane abundance out of chemical equilibrium, a process that has been studied for hot Jupiter atmospheres (e.g., Cooper & Showman 2006; Agúndez et al. 2014a; Steinrueck et al. 2019; Drummond et al. 2020). Finally, photochemical processes could destroy CH<sub>4</sub> in the dayside atmosphere (Zahnle & Marley 2014). Further studies into how the atmospheric circulation in such atmospheres affects horizontal and vertical quenching are needed to fully understand the impact of atmospheric dynamics on molecular abundances.

The observed color variations of SDSS1411-B are mainly driven by the orbital-phase-dependent irradiation and atmospheric circulation. In contrast, the observed color variations of isolated brown dwarfs are likely driven by the heterogeneous clouds in their atmosphere. In Figure 17, we compare the Two Micron All Sky Survey (2MASS) *J*–*H* color variations of SDSS1411-B with those of 12 isolated L to T dwarfs, as reported in Lew et al. (2020b). The plot is the same as Figure 6 in Lew et al. (2020b), with the addition of SDSS1411-B colors at four orbital phases (i.e., the four spectra in Figure 8). All plotted objects are observed under the HST/WFC3/G141 mode. Each colored data point represents the approximated *J*–*H* colors and absolute magnitudes *M<sub>J</sub>* averaged over one HST orbit of each isolated brown dwarf. The solid lines indicate, for each object, the linear extrapolation for its Δ*J* versus Δ(*J*–*H*) trend. Because the WFC3/G141 spectra do not fully cover the 2MASS *H* band, we derive the 2MASS *H* magnitude of SDSS1411-B with the white dwarf–brown dwarf *H*-band magnitude (17.80 ± 0.04) from Casewell et al. (2018) and the best-fit white dwarf model in Section 5.1. We subtract the *H*-band magnitude of 17.99 of the best-fit white dwarf model from 17.80 to obtain the brown dwarf *H*-band

magnitude of  $19.6 \pm 0.4$ . Finally, we also assume that the  $H$ -band magnitude variations are the same as those in the partial  $H$ -band coverage of the WFC3/G141 spectra.

Based on Figure 17, it is clear that no strong color variations are found among the L and T dwarf atmospheres, as concluded in Lew et al. (2020b). In contrast, we observe strong  $J-H$  color changes (compared to its  $J$ -band brightness variation) for SDSS1411-B. The comparison of color-magnitude variations between SDSS1411-B and isolated brown dwarfs demonstrates the impact of different atmospheric processes on the near-IR colors in brown dwarf atmospheres.

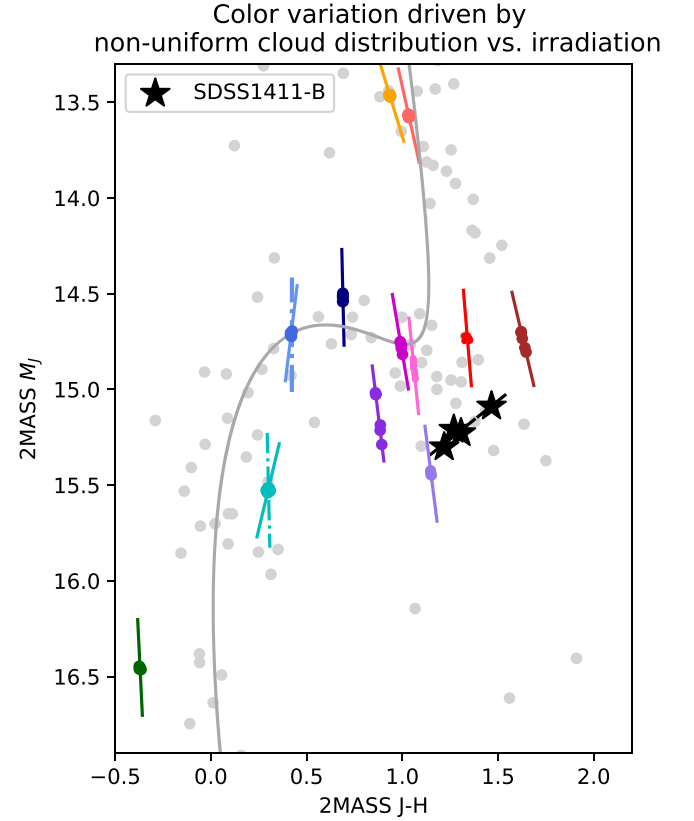
### 7.2. Comparison to Hot Jupiter WASP-43b

SDSS1411-B shares a similar irradiation temperature ( $T_{\text{irr}} \sim 1300$  K with zero albedo) to many hot Jupiters but has a higher mass and internal energy budget. In Figure 16, we compare the spectral features of SDSS1411-B to those of hot Jupiter WASP-43 b (Stevenson et al. 2014), which has an equilibrium temperature of around 1440 K (Blecic et al. 2014) and is one of the few hot Jupiters with a measured spectroscopic phase curve. A key difference in the nightside emission spectra between the two strongly irradiated atmospheres is the water-band feature—SDSS1411-B has a much deeper water-band absorption than WASP-43 b.

We attribute the difference in the water-band flux between SDSS1411-B and WASP-43 b to the difference in their interior energy and gravity. Brown dwarf evolutionary model Sonora (Marley et al. 2018) estimates an effective temperature of around 900 K for an isolated brown dwarf that shares the same mass ( $50M_{\text{Jup}}$ ) and age ( $>3$  Gyr) with SDSS1411-B. In contrast, typical gas giant planets with an age of a few Gyr like Jupiter are often assumed to have an intrinsic temperature, which is the effective temperature in the absence of irradiation, of around 100–250 K (Fortney et al. 2008).

The interior energy is important for the emission spectral feature because it affects the RCB and the corresponding temperature gradient. At the same gravity, an atmosphere with a higher interior energy has an RCB at a lower pressure. With a lower RCB pressure, the adiabatic temperature gradient in the convection zone, which is steeper than the temperature gradient in the radiative zone, extends to a lower pressure. Flux that originated from the part of the atmosphere with the steeper temperature gradient manifests a stronger spectral feature such as water-band absorption. Therefore, the higher internal energy of SDSS1411-B than WASP-43b leads to a lower RCB pressure and thus shows stronger emission spectral features, including the water-band absorption.

In addition to the interior energy, the gravity is important to understand the spectral feature difference because gravity affects the photospheric pressure. SDSS1411-B ( $M \sim 50M_{\text{Jup}}$ ) is about 25 times more massive than WASP-43 b ( $\sim 2M_{\text{Jup}}$ ), with a similar radius. The photospheric pressure  $P$  at  $\tau = 1$  is proportional to the gravity  $g$ , i.e.,  $P(\tau = 1) \propto g$ . With the higher gravity, the near-infrared emission probes a higher pressure that is closer to or deeper into the convection zone. As mentioned earlier, the temperature gradient is steeper in the convection zone than in the radiative zone. The likely steeper temperature gradient, combined with the higher photospheric pressure, results in a deeper water-band absorption in the atmosphere of SDSS1411-B than in WASP-43 b. We note that the effects of pressure broadening should also increase with a higher photospheric pressure. Pressure broadening typically weakens



**Figure 17.** The isolated brown dwarfs, plotted as colored circles, manifest weak color variations in rotational modulations (Lew et al. 2020b); SDSS1411-B, plotted as black stars, shows significant change in  $J-H$  colors as the irradiation varies across the night (faintest  $M_J$ ), morning, evening, and noon (brightest  $M_J$ ) orbital phases. The colored solid lines are the fitted straight lines to the color-magnitude variations of each objects. The dashed-dotted lines show the semimajor axis of the fitted ellipses to the color-magnitude variations of two T dwarfs, GU Piscium b and 2MASS J22282889-431026. The gray circles show the  $J-H$  colors and  $J$ -band magnitudes of field L and T dwarfs based on the catalog managed by Dupuy & Liu (2012). The gray curve shows the evolution from L (upper right) to T spectral type (lower left).

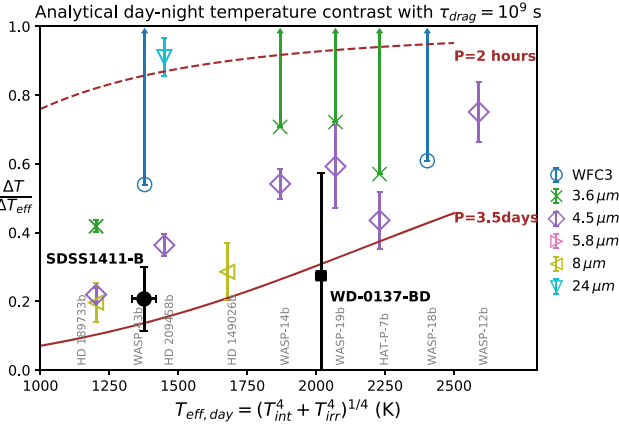
spectral features and thus partially cancels out the impact of a high internal energy flux and a high photospheric pressure, which would both work to strengthen the spectral features, such as the water-band absorption feature we discuss here.

Besides the difference in interior energy and gravity, the irradiation luminosity of WASP-43 b is about 1.5 times higher than that of SDSS1411-B. The striking difference in the host star effective temperature (4400 K vs. 13,000 K) means that the majority of stellar flux received by WASP-43 b is in the optical wavelength range, and thus the subsequent heating of atmosphere depends on the optical opacities. In contrast, SDSS1411-B mainly receives irradiation flux at UV wavelengths, so UV opacity becomes critical for atmospheric heating. Spectral or photometric observations of SDSS1411-B at longer wavelengths that probe low pressure are vital for studying the  $T-P$  profile and atmospheric composition under strong UV irradiation.

### 7.3. Day–Night Temperature Contrast, the Nearly Zero Phase Offset, and Implications for Atmospheric Dynamics

Atmospheric circulation models (e.g., see Lee et al. 2020; Tan & Showman 2020; Showman et al. 2020) for a rapidly rotating atmosphere under strong irradiation predict a large





**Figure 18.** The analytical estimate of day–night temperature contrast ratio with rotational periods of 2 hr (dashed brown line) and 3.5 days (solid brown line) with a fixed drag timescale of  $10^9$  s. The temperature contrast ratio of SDSS1411-B, shown as a filled black circle, is lower than the analytical estimate with a period of 2 hr. The analytical temperature contrast ratio with the  $10^9$  s drag timescale is a lower limit because the temperature contrast ratio increases with shorter drag timescale. The colored points show the observed day–night temperature contrast ratio of hot Jupiters listed in Table 2 in Komacek & Showman (2016), including HD 189733b (Knutson et al. 2009, 2012), WASP-43b (Stevenson et al. 2014), HD 209458b (Crossfield et al. 2012; Zellem et al. 2014), HD 149026b (Knutson et al. 2009), WASP-14b (Wong et al. 2015), WASP-19b (Wong et al. 2016), HAT-P-7b (Wong et al. 2016), WASP-18b (Arcangeli et al. 2019), and WASP-12b (Cowan et al. 2012). The temperature contrast ratios of hot Jupiters observed at different wavelengths are plotted in different colors and markers. The observed temperature contrast ratio of WD-0137-BD (Lothringer & Casewell 2020), which is another irradiated brown dwarf, is plotted as a black square.

fractional day–night temperature contrast ratio, which is the ratio of the temperature contrast with irradiational heat redistribution over the radiative-equilibrium temperature contrast (see Figure 6 in Komacek & Showman 2016 and Equation (10)), and a small phase offset. Below we discuss the measured values of SDSS1411-B and place them in the context of close-in gas giants, including hot Jupiters.

Assuming no heat redistribution, the dayside radiative-equilibrium temperature ( $T_{\text{eff,day}}$ ) is determined by both stellar irradiation and internal heat flux (which, in turn, is characterized by the intrinsic temperature  $T_{\text{int}}$ , which is equal to the effective temperature of an isolated brown dwarf). In contrast, the nightside is purely set by the internal heat:

$$\begin{aligned} T_{\text{eff,day}} &= (T_{\text{int}}^4 + T_{\text{irr}}^4)^{1/4}, \\ T_{\text{eff,night}} &= T_{\text{int}}, \\ \Delta T_{\text{eff}} &= T_{\text{eff,day}} - T_{\text{eff,night}}, \end{aligned} \quad (10)$$

where  $T_{\text{irr}}$  is the dayside equilibrium temperature with zero albedo, global heat redistribution, and negligible interior energy budget and  $\Delta T_{\text{eff}}$  is the radiative-equilibrium temperature contrast. We estimate the intrinsic temperature  $T_{\text{int}}$  of SDSS1411-B to be around  $900 \pm 200$  K based on the Sonora brown dwarf evolutionary model, which does not include irradiation, for a  $50M_{\text{Jup}}$  object with an age of 3–10 Gyr. We note that the preceding common-envelope evolutionary phase interaction between the brown dwarf and the white dwarf progenitor makes the deduction of the main-sequence mass of the star, and hence its main-sequence lifetime (and thus the

evolutionary age of the brown dwarf), uncertain (see, e.g., Geier et al. 2011). Any potential mass accretion or loss of the brown dwarf during the AGB/RGB phase of the star would add to this uncertainty (see, e.g., Lagos et al. 2021; Villaver et al. 2007). We adopt a surface gravity of  $2500 \text{ ms}^{-2}$  for the analytical model. We integrate the  $1.1\text{--}1.7 \mu\text{m}$  spectra and calculate the WFC3 band-averaged day–night brightness temperature difference of SDSS1411-B.

The ratio between the measured day–night temperature difference and the estimated radiative-equilibrium difference is shown in Figure 18, along with measurements of hot Jupiters as a function of equilibrium temperature. Theoretical predictions using the theory of Komacek & Showman (2016) with two planetary rotation periods (2 hr and 3.5 days) and a negligible drag ( $\tau_{\text{drag}} = 10^9$  s) are plotted as curves for comparisons. As shown in Figure 18, the expected fractional temperature contrast ratio increases significantly with shorter rotational period (i.e., the dashed vs. solid brown lines) given the same equilibrium temperature. The measured value of SDSS1411-B is among those of hot Jupiters at nearby equilibrium temperatures that have a wide scatter. The measured temperature contrast ratio of SDSS1411-B is much lower than the analytical estimate at a rotation period of 2 hr.

Two factors may contribute to this discrepancy. First, the wavelength range in our study generally probes a deep atmosphere where the brightness temperature greatly exceeds  $T_{\text{int}}$ . For example, the brightness temperature at the WFC3 bandpass ranges from 1000 K to over 1800 K with an average of  $\sim 1400$  K based on the Sonora cloud-free models (Marley et al. 2018) with  $T_{\text{int}} = T_{\text{eff}} = 900$  K and  $g = 1780 \text{ ms}^{-2}$ . This likely shifts the intrinsic temperature “seen” by our measurements considerably higher than the assumed  $T_{\text{int}}$  based on the evolution models. With a higher “ $T_{\text{int}}$ ” in Equation (10) for our wavelength range, the inferred fractional day–night temperature contrast ratio can move closer to the theoretical expectation. Second, some processes may help to increase day–night heat transport and lower the expectation shown in Figure 18. For example, if the latitudinal width of the standing waves and equatorial jet is larger than we expected, this could help to increase the day-to-night heat transport. One possible cause may be the increase of effective static stability of the atmosphere due to a strong dayside thermal inversion in the upper atmosphere (not probed by our HST observations; Lothringer & Casewell 2020). The lack of phase offset with respect to the expected secondary-eclipse phase (see Figure 4) is consistent with the lack of a pronounced equatorial and/or zonal wind pattern in Tan & Showman (2020) and Lee et al. (2020). Further, the negligible phase offsets across multiple bands in Section 4.2 hint that the horizontal thermal structure could be similar across a wide pressure range.

#### 7.4. Clouds

Based on the  $T$ – $P$  profiles and condensation curves of common cloud species plotted in Figure 11, it is possible that clouds form at the near-infrared photosphere pressures of the dayside and nightside hemispheres. While we defer the exploration of possible cloud structure to future studies, we herein provide a brief qualitative discussion of the potential impact of cloud formation in the irradiated brown dwarf atmosphere.

Given the same effective temperature, gravity, and irradiation, a cloudy atmosphere's model spectrum is fainter in the  $J$  band and has weaker spectral features in comparison with a cloudless model spectrum. With the addition of cloud opacity, the photospheric pressure, particularly that in the  $J$  band in Section 6.3, shifts to a lower pressure. While the absolute photospheric pressure could shift in the presence of clouds, the relative pressure probed at different wavelengths should remain roughly the same. Therefore, we argue that the presented trend of higher temperature contrast with lower pressure shown in Figure 14 remains valid in the cloudy atmosphere scenario. The estimated temperature gradient (Figure 15) could be steeper in a cloudy atmosphere because cloud opacity limits the pressure range probed by the HST observation.

We can also qualitatively discuss the potential cloud coverage difference between the dayside and nightside atmospheres. Cloud modeling studies for hot Jupiter atmospheres with equilibrium temperatures near 1400 K (see Figure 19 in Parmentier et al. 2021) show that the  $J$ -band brightness temperature difference between a fully cloudy nightside and cloudless dayside could be on the order of several hundred kelvin. We argue that the observed small ( $\sim 10\%$ ) day–night  $J$ -band brightness temperature variations (Figure 10), which are sensitive to cloud opacity, hint that it is unlikely that there is a drastic change in cloud coverage, such as a fully cloud-free to cloudy transition, between the dayside and nightside atmospheres. Meanwhile, global cloudless atmospheric circulation studies (e.g., Lee et al. 2020; Tan & Showman 2020) of rapidly rotating irradiated atmospheres suggest a strong latitudinal-dependent temperature profile because of the fast rotation. Further studies on the vertical mixing, latitudinal and longitudinal variations of  $T$ – $P$  profiles, and the corresponding cloud structure are important to interpret the disk-integrated emission spectra of a cloudy atmosphere with rapid rotation.

## 8. Conclusions

We present the first time-resolved spectrophotometry of the white dwarf–brown dwarf close binary system SDSS J141126.20 + 200911.1, observed by the HST WFC3's G141 near-infrared grism. Our data baseline covers 8.666 hr, or around 4.3 orbits of the system. Our high-precision data provide the first complete orbital-phase-resolved spectroscopy of a highly irradiated brown dwarf and, as such, open a new window on yet-unexplored types of atmospheres. The key findings of our study are as follows:

1. The broadband (1.15–1.67  $\mu\text{m}$ ) white light curve, which includes flux from the white dwarf and the brown dwarf of the SDSS1411 system, varies by around 2.8% from trough to peak over an orbital period of 2.0287 hr. The best-fit light-curve model results show that the white dwarf broadband emission is about 12 times brighter than the time-averaged brown dwarf's emission. If only the brown dwarf's emission varies across orbital phases while the white dwarf emission remains constant, the observed 2.8% variability amplitude of the white dwarf–brown dwarf light curve implies that the brown dwarf broadband emission varies by around 38% from the nightside to the dayside phase.

2. A single sinusoidal fit to the light curve indicates that the phase offset, if any, is less than a  $3\sigma$  upper limit of  $11^\circ$  from the center of the secondary-eclipse phase.
3. We directly detect the nightside spectrum of SDSS1411-B during the eclipse of the white dwarf. We report a  $J'$ -band (1.2–1.3  $\mu\text{m}$ ) detection at the  $11\sigma$  level and an  $H'$ -band (1.5–1.6  $\mu\text{m}$ ) detection at the  $7\sigma$  level.
4. We extract the brown dwarf spectra at morning, noon, evening, and night phases. The flux variation between the dayside and nightside hemispheres of SDSS1411-B in the water band (1.35–1.45  $\mu\text{m}$ ) is  $370\% \pm 70\%$ , which is about 10 times higher than the  $38\% \pm 2\%$  variation observed in the  $J'$  band.
5. Our atmospheric model spectrum reproduces the overall spectral feature of the observed nightside spectrum. Based on the nightside atmospheric model, the  $J'$ -band emission emerges from the region of 20–80 bars. Based on the estimated  $J'$ -band photosphere pressures, we interpret that the day–night temperature contrast extends down to at least 20 bars and causes the observed  $J'$ -band flux variation.
6. Based on the day–night brightness temperature difference and nightside atmosphere model, we calculate the pressure-dependent day–night temperature contrast. We show that the temperature contrast increases with lower pressure in the pressure range of 2–80 bars that is probed by the HST 1.1–1.7  $\mu\text{m}$  observation. The derived temperature gradient based on the brightness temperatures and inferred pressures suggests that the dayside atmosphere has a shallower temperature gradient (closer to an isothermal-like profile) than the nightside atmosphere.
7. We show that the spectra of SDSS1411-B and of isolated T dwarfs manifest different spectral features. The color–magnitude variations of SDSS1411-B, which are driven by the varying irradiances, are also distinct from those of many isolated, rotating L and T dwarfs (driven by nonuniform cloud distributions). Our comparative study of spectra and color variations between irradiated brown dwarfs and isolated field dwarfs illustrates the impact of irradiation on brown dwarf atmosphere.
8. The comparison between SDSS1411-B and WASP-43 b nightside spectra demonstrates that a higher gravity and a higher internal heat flux lead to a stronger water-absorption feature.
9. We find that the observed day–night temperature contrast of SDSS1411-B is lower than the analytical estimate of Komacek & Showman (2016). We interpret that this could be caused by the fact that 1.1–1.67  $\mu\text{m}$  emission spectra probe atmospheric regions that are hotter than the  $T_{\text{int}}$  and/or a more effective day–night heat transport.

Our observations successfully demonstrate that high-precision, orbital-phase-resolved spectrophotometry of highly irradiated brown dwarfs is possible with the HST. Our analysis shows the potential for characterizing these atmospheres, the yet-unexplored link between nonirradiated brown dwarfs and highly irradiated hot Jupiters. Analysis of our observations provides some constraints on atmospheric circulation and the pressure–temperature profiles of irradiated brown dwarfs.

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*Software:* Astropy (Astropy Collaboration et al. 2013), Numpy (Harris et al. 2020), Matplotlib (Hunter 2007), Scipy (Virtanen et al. 2020), Batman (Kreidberg 2015).

### Authors’ Contributions

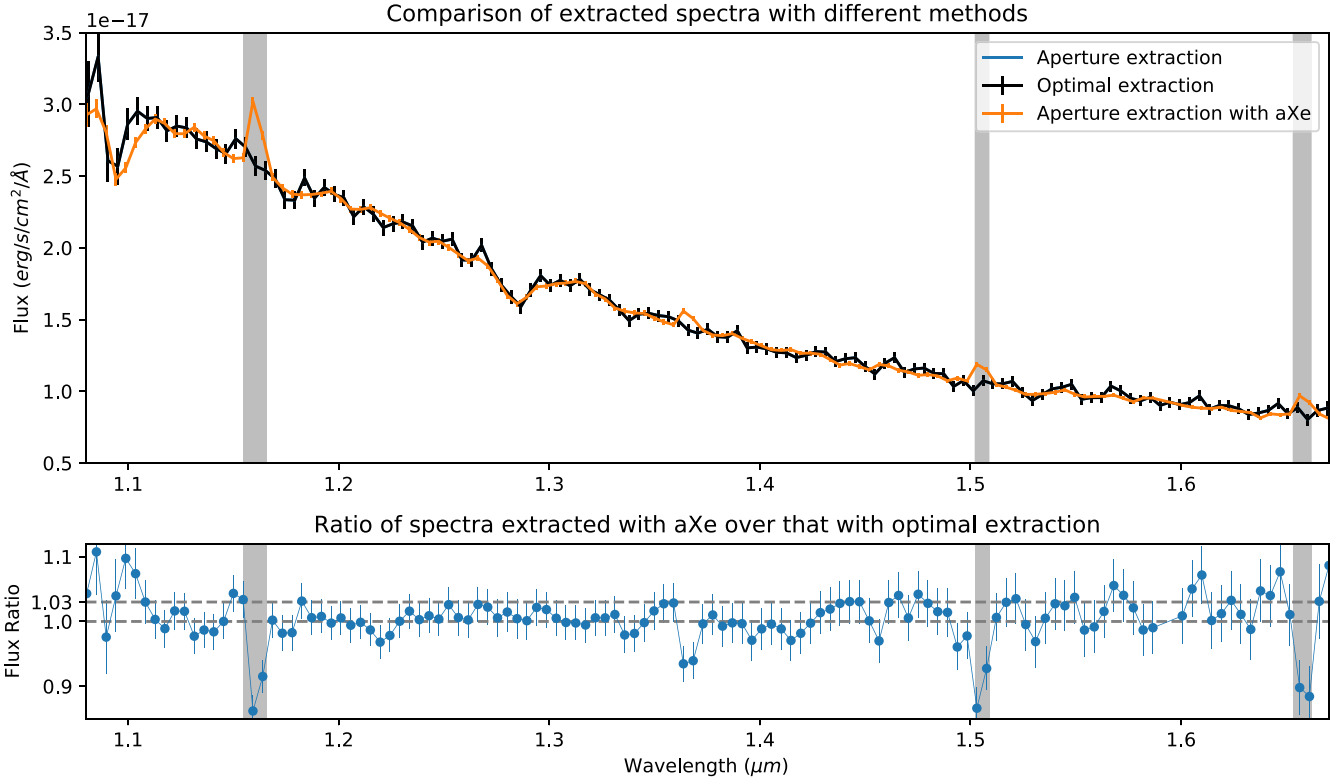
B.W.P.L. reduced the data, performed the time-series and spectral analysis, and led the writing of the manuscript. D.A., M.M., S.X., and Y.Z. prepared the observing proposal.

S.C. provided the summary of the target properties. M.M. and L.M. simulated the atmospheric model spectra. X.T., V.P., L.M., and M.M. aided in interpreting the atmospheric structure and circulation. All authors contributed to the manuscript preparation.

## Appendix A

### Validation of Spectra Extracted with the New Pipeline

We conduct several tests to benchmark our extracted spectra. We confirm that the spectra extracted with the optimal extraction method are consistent with apertures of 3, 4, and 5 pixels. The median differences in the flux density between two spectra extracted with different apertures are less than 0.6%, which is about five times lower than the averaged observed uncertainty of 3%. We then compare the spectra that are extracted with the new pipeline and those with the standard aXe pipeline that have been used in many studies (e.g., Buenzli et al. 2012; Apai et al. 2013; Yang et al. 2015; Lew et al. 2016; Manjavacas et al. 2018; Zhou et al. 2018; as shown in Figure 19). We compare the median spectra in the second HST-orbit observation that is free from the eclipse event because an unresolved eclipse event in the standard pipeline will skew the median values of spectra. We notice that the hydrogen Paschen absorption line at  $1.09\ \mu\text{m}$  is off by around 10% between the spectra extracted with aXe and with our own pipeline. We interpret that the deviation is likely caused by the imperfect wavelength calibration. Overall, our comparison suggests that our pipeline produces similar reduced spectra to those by the standard aXe pipeline.



**Figure 19.** Comparison of median spectra with different spectral extraction methods illustrates that the three spectra extracted with different methods are consistent with each other within  $\sim 3\%$  levels for a wavelength range of  $1.1\text{--}1.67\ \mu\text{m}$ . The uniform and optimal extraction methods do not change the median spectra but do change the standard deviation of the light curve. The bottom panel shows the ratio of spectra extracted with the self-developed pipeline and with the standard aXe pipeline. Visual inspection of the images confirms that the three gray shaded regions of the spectra extracted with the aXe pipeline are affected by cosmic-ray or bad pixels.



## Appendix B

### Conversion from Counts per Pixel to Counts per Wavelength

As mentioned in Section 3, we convert the counts per pixel to counts per wavelength with a weighting function. The weighting function comprises two components,  $A_1$  and  $A_2$ .  $A_1$  projects each pixel to the wavelength solution in the cross-dispersion direction and calculates the fractional pixel area that falls in the bins of the solution.  $A_1(i, j) = 1$  means that the entire area of pixel  $i$  falls into the wavelength bin  $j$  in the cross-dispersion direction.  $A_2$  assigns weights to pixels that are within a specified aperture width from the spectral trace. The value of  $A_2(i)$  ranges from zero to unity. A unity value of  $A_2(i)$  means that the pixel  $i$  is at a distance less than or equal to the aperture width from the spectral trace. The weighting function  $W(i, j)$  of pixel  $i$  at wavelength  $j$  thus equals  $W$

$(i, j) = A_1(i, j) \times A_2(i)$ . We verify that the calculation result of the weighting function by examining the total weight of each pixel  $i$  over all wavelength bins is equal to unity and the total weight of each wavelength bin  $j$  over all the pixels is equal to two times the aperture width. With the weighting function, we sum the weighted electron count over all pixels as count per wavelength bin  $C(j) = \sum_{i=1}^N W(i, j) \times C(i)$ , where  $C(i)$  is the count rate of pixel  $i$  and  $C(j)$  is the count rate of wavelength bin  $j$ .

## Appendix C

### The Priors and Posterior Distribution of MCMC Sampling Results

Table 2 shows the uniform priors of the MCMC method used in the light-curve modeling in Section 4.1; Figure 20

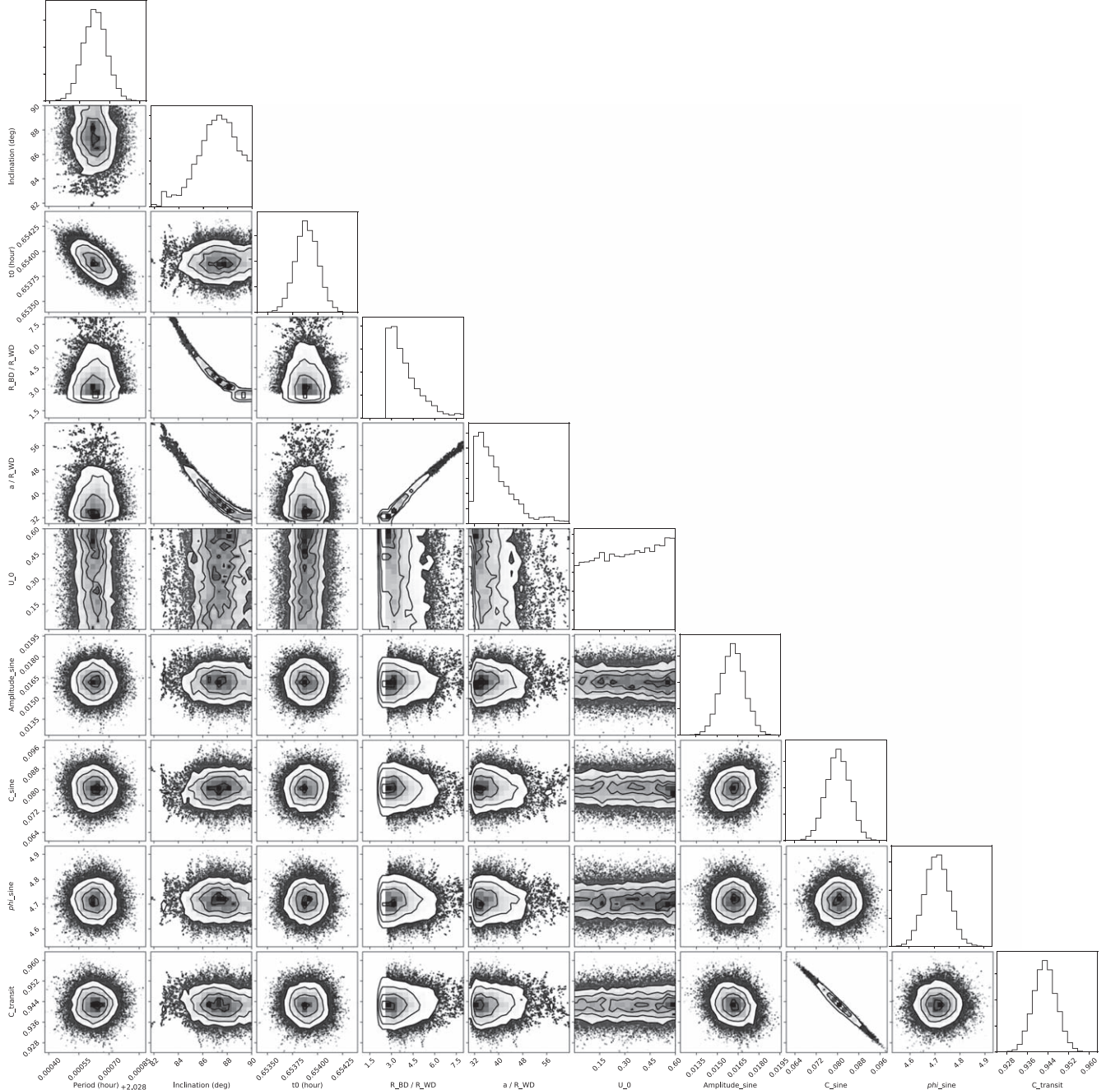


Figure 20. The posterior distribution of the light-curve model parameters with the MCMC method.












**Table 2**

The Uniform Priors of the Light-curve Model Parameters in the MCMC Method

Parameter	Prior Range
Orbital period $P$ (hr)	$[2.0288^{+0.99}_{-0.99}, 2.0288^{+1.01}_{-1.01}]$
Radius ratio $r_{\text{BD}}/r_{\text{WD}}$	$[1, \frac{1.4R_{\text{Jup}}}{0.012R_{\odot}} = 14]$
Inclination $i$ (deg)	$[80, 90]$
Mid-eclipse time $t_0$ (hr)	$[0.63, 0.68]$
Semimajor-axis ratio $a/r_{\text{WD}}$	$[30, 70]$
Limb-darkening coefficient	$[0, 0.6]$
Flux constant $c_{\text{WD}}$	$[0.8, 1]$
$A_{\text{sine}}$	$[0, 0.1]$
$C_{\text{sine}}$	$[0, 0.2]$
$\phi_{\text{sine}}$	$[10^{-5}, 2]\pi$

shows the posterior distribution of the MCMC modeling results.

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